

# Error Performance of Information Decoder for SWIPT With Integrated Receiver

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# Abbreviations

- SWIPT - Simultaneous Wireless Information and Power Transfer
- EH - Energy Harvester
- ID - Information Decoder
- QD - Quadratic Detector
- ED - Envelope Detector
- RX - Separated Receiver
- IoT - Internet of Things
- IIE-RX - Integrated Information and Energy Receiver
- SISO - Single-Input Single-Output
- ASK - Amplitude Shift Keying
- BER - Bit Error Rate
- ADC - Analog to Digital Converter

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# Abstract

- SWIPT can be realized by means of Integrated Receiver, where both the EH and ID operate on rectified received signal.
- Researchers investigate the effect of the non-linearity of rectifier on the error performance of the information decoder when transmitting over a Nakagami-m fading channel.
- Demonstrated through analysis and simulation, that, the low-noise error performance strongly depends on the small-signal behaviour of the rectifier.
- Approximating the rectifier by a quadratic detector yields accurate bit error rate results, whereas an over-optimistic error performance is obtained when applying the envelope detector approximation.

# Introduction

- SWIPT is a promising technique for powering energy-limited information-processing devices, which are commonly used in the IoT.
- Recently, a new type of RX was proposed, namely IIE-RX, which rectifies the incoming signal, and subsequently splits the rectifier output current between the EH and ID circuits.
- Authors investigate the error performance of the ID in the IIE-RX, using biased ASK on a SISO Nakagami-m block-fading channel, with the receiver knowing the distorted ASK constellation at the rectifier output.
- The main contribution is the derivation of an analytical expression for the BER of the Maximum Likelihood(ML) detector in the low-noise regime.

# SWIPT with Integrated ID and EH Receiver

- Considering a single-antenna TX sending symbols  $a(k)$  from a normalized constellation (i.e,  $E[|a(k)|^2] = 1$ ) over a flat Nakagami-m block-fading channel to a single-antenna IIE-RX.
- As discussed, the IIE-RX rectifies the input signal and then splits up the output current between ID and EH.

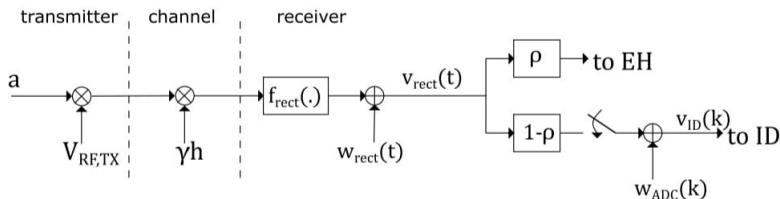


Figure: Block diagram of the Model for the IIE-RX

Symbols used in the above figure are as described,

TABLE I  
SYMBOL DESCRIPTION TABLE

$V_{\text{RF,TX}}$	TX rms voltage	$\rho$	current splitting factor
$V_{\text{RF}}$	RX rms voltage	$f_{\text{rect}}$	rectifier characteristic
$v_{\text{ID}}$	voltage at ID	$w_{\text{rect}}$	rectifier noise
$P_{\text{EH}}$	harvested power	$w_{\text{ADC}}$	quantization noise
$v_{\text{rect}}$	rectifier output	$w_{\text{ID}}$	total noise at ID
$\gamma h$	channel gain	$\mathcal{A}_M$	$M$ -ASK constellation

- During the  $k$ th symbol interval  $(kT, kT + T)$ , an RF voltage  $v_{RF,TX}(t)$  is applied to the TX antenna, with,

$$v_{RF,TX}(t) = \sqrt{2}|a(k)|V_{RF,TX}\cos(2\pi f_c t + \angle a(k)) \quad (1)$$

where  $|a(k)|$  and  $\angle a(k)$  denote the magnitude and phase of  $a(k)$ ; the rms value of  $v_{RF,TX}(t)$  in this interval equals  $|a(k)|V_{RF,TX}$ , making  $V_{RF,TX}$  the long-term rms value.

- $\gamma h$  is the channel gain, such that  $-20\log(\gamma)$  denotes pathloss(in dB) and  $h$  is normalized fading gain.
- Assuming,  $h = |h|e^{j\angle h}$  is constant over a block of  $K$  symbol intervals;  $|h|$  has a Nakagami-m distribution with  $E|h^2| = 1$  and  $\angle h \in [0, 2\pi)$ , (1) can be written as,

$$v_{RF,TX}(t) = \sqrt{2}V_{RF}|h||a(k)|\cos(2\pi f_c t + \theta(k)) \quad (2)$$

where,  $V_{RF} = \gamma V_{RF,TX}$  and  $\theta(k) = \angle a(k) + \angle h$ .



- The corresponding rectifier output signal  $v_{rect}(t)$  is decomposed as ,

$$v_{rect}(t) = f_{rect}(|h||a(k)|V_{RF}) + w_{rect}(t) \quad (3)$$

- The function  $f_{rect}(A)$  is referred to as the rectifier characteristic, which expresses the rms value  $A$  of a sinusoidal input signal.
- Considering the simple rectifier circuit from Fig.,

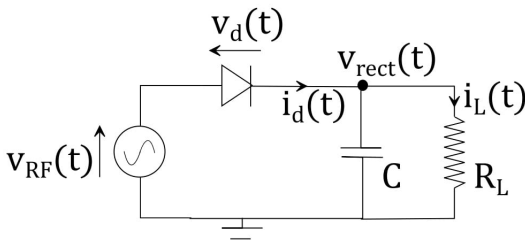


Figure: Simple Rectifier Circuit

- Here, resistive load  $R_L$  in Fig. 2 represents the parallel connection of the EH part (load  $\frac{R_L}{\rho}$ ) and the ID part (load  $\frac{R_L}{1-\rho}$ ) of the receiver, which draw currents  $\rho \frac{V_{rect}}{R_L}$  and  $(1-\rho) \frac{V_{rect}}{R_L}$ , respectively.
- The current drawn by the ID part is fed to a sampler and ADC, which results in the voltage  $v_{ID}(k)$ ,

$$v_{ID}(k) = (1-\rho)f_{rect}(|h||a(k)|V_{RF}) + w_{ID}(k) \quad (4)$$

where,  $w_{ID}(k) = (1-\rho)w_{rect}(kT) + w_{ADC}(k)$ , (4) suggests that  $v_{ID}(k)$  doesn't depend on the phase of data symbol  $a(k)$ .

# Rectifier Characteristic

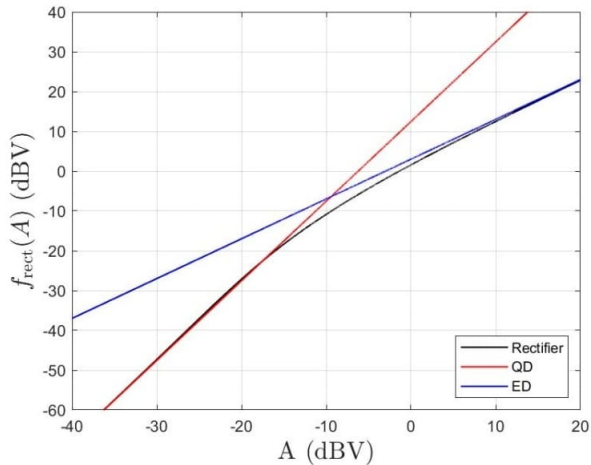
- We determine the characteristic  $f_{rect}(A)$  of the rectifier from above fig. by solving the differential equation,

$$C \frac{dv_{rect}}{dt} + \frac{v_{rect}}{R_L} = I_s \cdot (e^{\frac{1}{nV_{th}}} - 1) \quad (5)$$

where  $V_{th}$  is thermal voltage and the diode is characterized by the reverse saturation current  $I_s$  and ideality factor  $n$ .

- On solving using proper assumptions, we get,

$$f_{rect}(A) = \frac{1}{2} \left( \frac{1}{R_L I_s} + \frac{1}{nV_{th}} \right)^{-1} \cdot \left( \frac{A}{nV_{th}} \right)^2 \quad (6)$$



**Figure:** Rectifier Characteristics showing DC output voltage versus rms input voltage.

# BER Analysis

- Considering the transmission of uncoded symbols from biased  $M$ -ASK constellation  $A_M$ .
- This constellation gets distorted by the rectifier: the signal component in  $v_{ID}(k)$  corresponding to  $a(k) = \alpha_\ell$  is denoted as,

$$S_\ell = (1 - \rho)f_{rect}(|h|\alpha_\ell VRF) \quad (7)$$

- For given  $|h|$ , the BER is given by,

$$BER = \frac{1}{M \log_2 M} \sum_{i,j=0}^{M-1} n_{i,j} P_{i,j} \quad (8)$$

where  $n_{i,j}$  is the number of bits in which  $\alpha_i$  and  $\alpha_j$  differ and  $P_{i,j}$  is the probability that  $\alpha_i$  is detected when  $\alpha_j$  is transmitted.

- After performing extensive calculation, it is obtained that,

$$BER_{avg} = C_{A_M}(m, \beta) \cdot \left( \frac{\sigma_{ID}^{2/\beta}}{V_{RF}^2} \right)^m \quad (9)$$

where  $m$  is the Nakagami parameter,  $\beta$  is the variable which tells whether the detector is ED( $\beta = 1$ ) or QD( $\beta = 2$ ) and,

$$C_{A_M}(m, \beta) = \frac{1}{M \log_2 M} \cdot \sum_{i,j=0}^{M-1} n_{i,j} D(m, \beta, i, j) \quad (10)$$

- From (9), we can say, for small  $\sigma_{ID}$ ,

$$BER_{avg} \propto \left( \frac{\sigma_{ID}^{2/\beta}}{V_{RF}^2} \right)^m \quad (11)$$

this indicates a performance advantage of ED over the rectifier for small  $\sigma_{ID}$ .

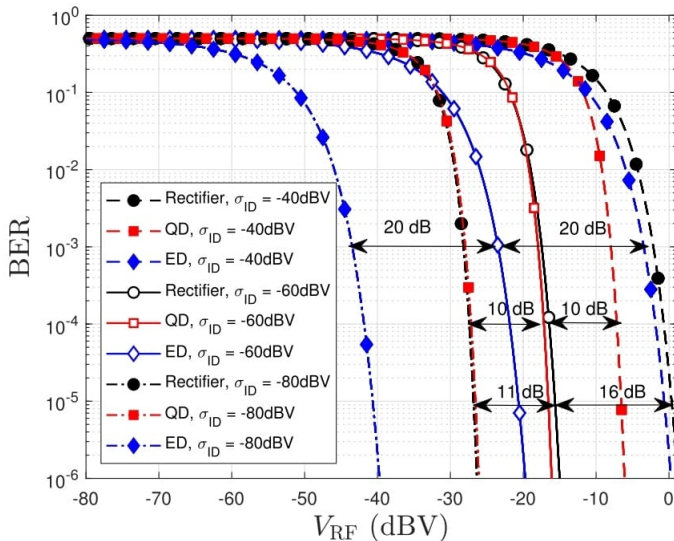


Figure: Conditional BER ( $|h| = 1$ ) versus  $V_{RF}$  (2-ASK).

# Conclusion

- It is investigated the BER of the ID for SWIPT with an IIE-RX, for the uncoded transmission of biased ASK on a Nakagami-m fading channel, and presented an analytical expression for the resulting BER in the small-noise regime.
- The characteristics of the rectifier and the QD differ considerably for larger input signals, but their small-noise BER curves nearly coincide.
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*Thank You*