Basic Neural Networks

OCTOBER 18, 2017 — WORKSHOP #1



Intro

We want to generate a prediction from some input

Output should give some probability of all our expected outputs

Network should give highest probability to correct class most of the time



Forward Pass



FORWARD PASS

Fully-Connected Layers

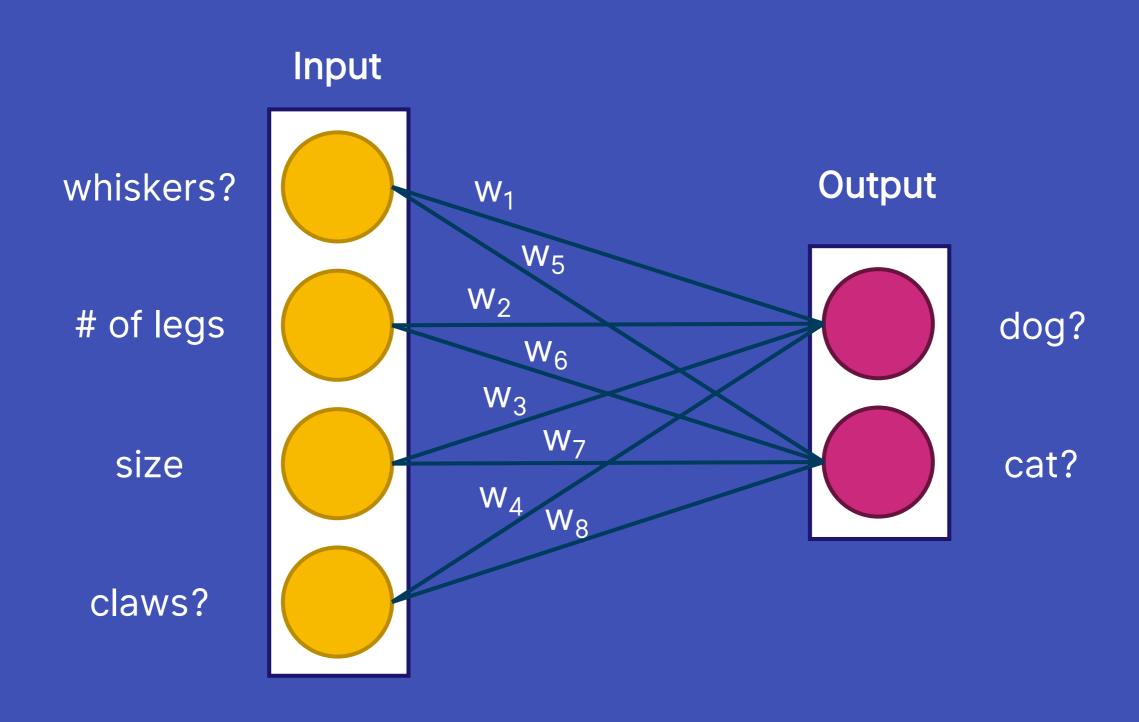
Fully-connected layers are computations where every input neuron is connected to every output neuron

We transform the input by using weights to transform it into the output

The output will have a different shape than the input

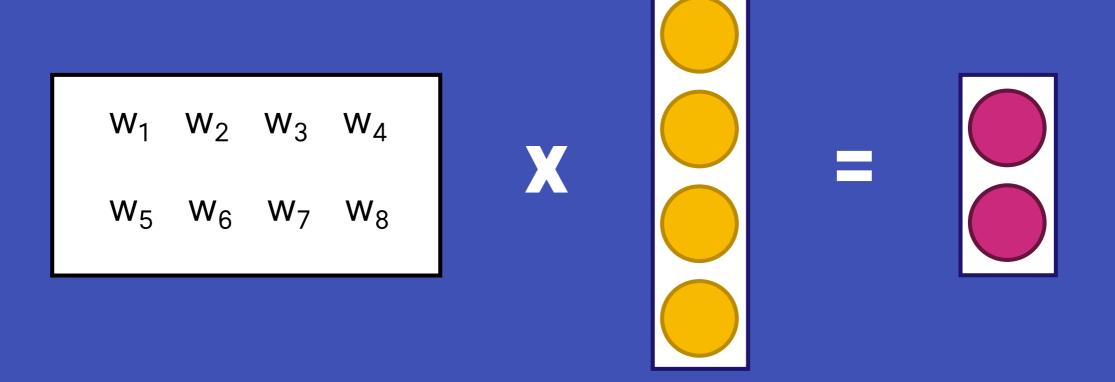


Fully-Connected Network





FC Net as Matrix-Vec Mult





FORWARD PASS

Probability Distribution

The output of our network is arbitrarily scaled

We want to turn the arbitrary scale into a proper probability distribution

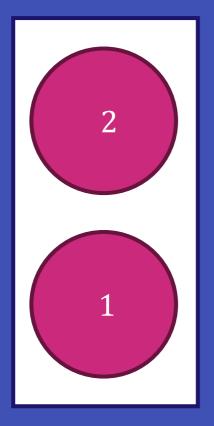
We do so by using the softmax calculation:

$$p_i = \frac{e^{o_i}}{\sum_j e^{o_j}}$$

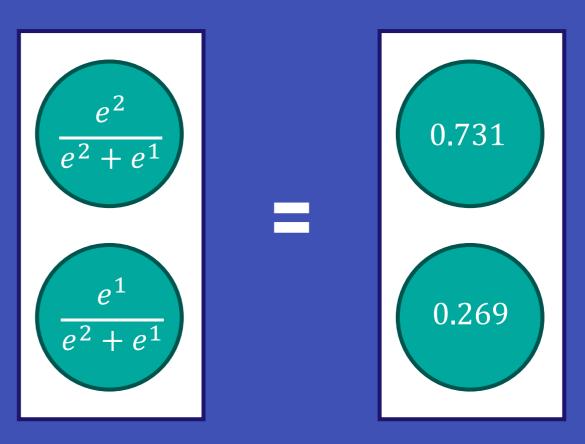


Softmax Layer

Output



Softmax



FORWARD PASS

Loss Value

The network needs an "objective" to work towards—being accurate

We use the targets to figure out how "incorrect" the network was

The loss metric we use is cross-entropy loss:

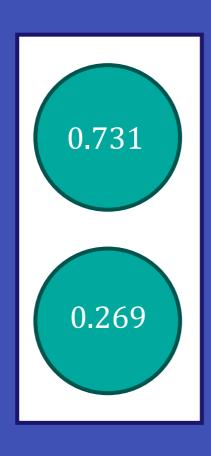
$$L = -\log(p_c)$$



Softmax Layer

Softmax

Loss



$$L = -log(0.731) = 0.313$$

FORWARD PASS

Data Splitting

We are interested in how our model does on unseen data above all

We can split data into training and test—but if we optimize on test, test becomes "indirectly" seen

Instead, we split into train, validation, and test; we run test only once



EXERCISE

Code Up the Forward Pass

Split the dataset into train, validation, and test

Initialize the parameters to random

Create the linear and softmax cross-entropy layers



Backward Pass



Backpropagation

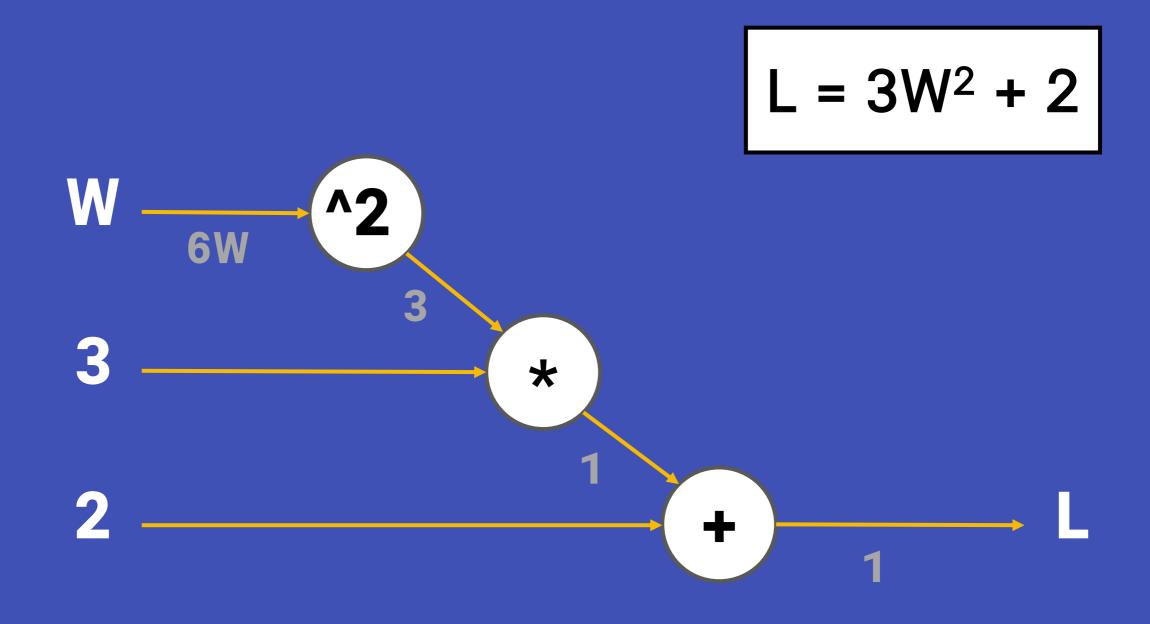
Each computation is represented as a node in a computational graph

Gradients are computed at each node of the graph

Chain rule is applied recursively to get total gradients on each weight

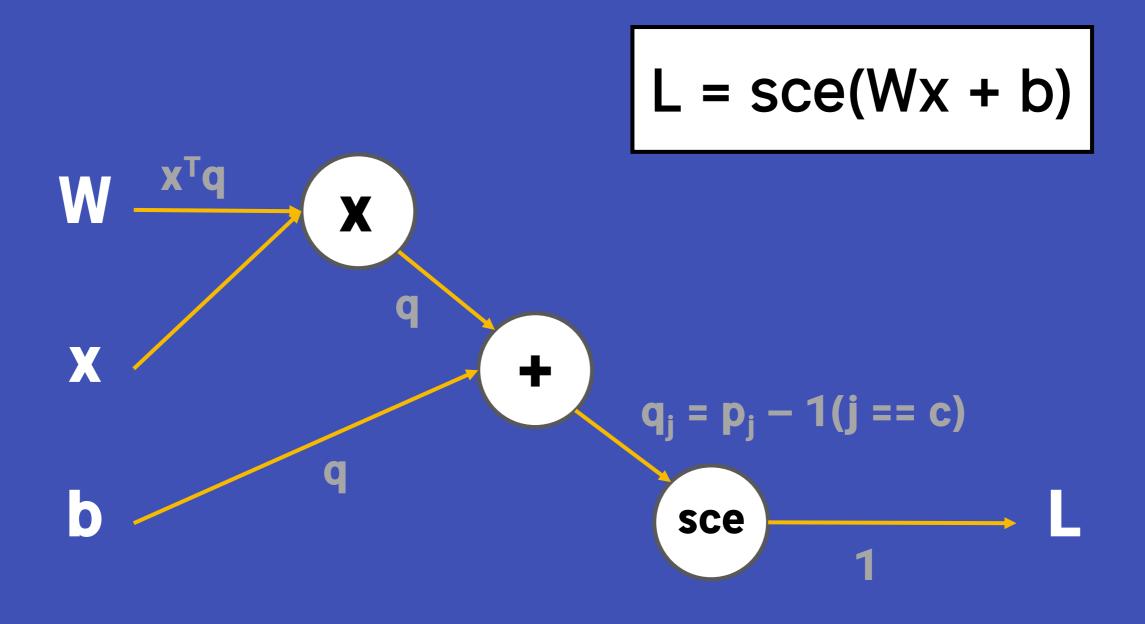


Simple Backprop





Multidimensional Backprop





EXERCISE

Code Up the Backward Pass

Create the backward pass through the linear layer

Create the backward pass through the softmax cross-entropy layer



Training



TRAINING

Weight Update

Once we find gradients, we must change each weight in that direction

We can use a update rules to accomplish this; the simplest is SGD:

$$W_i := W_i - \alpha \left(\frac{\partial L}{\partial W_i} \right)$$



TRAINING

Training Iterations

Each time we move the weights in the direction of the negative gradient, we get closer to a good value for the weights

We want to do this many times until we arrive at good weight values (i.e. converge)

We also want to periodically check the network's accuracy on the training and validation sets



EXERCISE

Code Up the Training Regime

Code the training iteration loop

Implement SGD weight updates

Periodically log the training and validation losses



Conclusion

