

# 0

# Python Introduction

## Installation

For this class we will use Python3 (version 3.7.3) and the following libraries:

- **Numpy**: a package for scientific computing.
- **Scipy**: another package for scientific computing.
- **Sympy**: library for symbolic mathematics.
- **Matplotlib**: library for plotting.
- **pycodestyle**: a tool to check your Python code against some of the style conventions.

## Windows and Mac OS installation

First you need to install Python 3 (the current stable version is 3.7.3). You can download it from the [Python Official Website](#). **Be careful to download the 64-bit version of Python.**

Then you can use pip to install the libraries:

```
$ pip install numpy scipy sympy matplotlib pycodestyle
```

## Linux (Ubuntu installation)

```
$ sudo apt-get install python3-dev python3-numpy python3-matplotlib \  
python3-scipy python3-sympy python3-pycodestyle
```

## Basic commands

Here are some basic commands that you should know. You can also look at the [Linux Command Cheatsheet](#) that contains a more exhaustive list for Mac OS and Linux.

| Windows | Linux/Mac OS |   |
|---------|--------------|---|
| attrib  | chown/chmod  | Sets ownership on files and directories   |
| cd      | cd           | Change directory                          |
| cd      | pwd          | Prints the current directory              |
| copy    | cp           | Copy                                      |
| del     | rm           | Delete                                    |
| deltree | rm -r        | Recursively deletes entire directory tree |
| dir     | ls           | Prints folders and files in the directory |
| edit    | vi           | Edit a file                               |
| mkdir   | mkdir        | Create a directory                        |
| move    | mv           | Move a file                               |
| xcopy   | cp -R        | Recursively copy a directory tree         |

# Numpy

## Array

The basic object in NumPy is the array, which is conceptually similar to a matrix. The NumPy array class is called ndarray (for “n-dimensional array”). The simplest way to explicitly create a 1-D ndarray is to define a list, then cast that list as an ndarray with NumPy’s array() function.

```
>>> import numpy as np
# Create a 1-D array by passing a list into NumPy's array() function.
>>> np.array([8, 4, 6, 0, 2])
array([8, 4, 6, 0, 2])
# The string representation has no commas or an array() label.
>>> print(np.array([1, 3, 5, 7, 9]))
[1 3 5 7 9]
```

The type of the resulting array is deduced from the type of the elements in the sequences.

```
>>> import numpy as np
>>> a = np.array([2,3,4])
>>> a
array([2, 3, 4])
>>> a.dtype
dtype('int64')
>>> b = np.array([1.2, 3.5, 5.1])
>>> b.dtype
dtype('float64')
```

You can also specify the type of the elements in a array.

```
>>> import numpy as np
>>> a = np.array([2,3,4], 'd')
>>> a
array([ 2.,  3.,  4.])
>>> a.dtype
dtype('float64')
>>> b = np.array([1.2, 3.5, 5.1], 'i')
>>> b
array([1, 3, 5], dtype=int32)
>>> b.dtype
dtype('int32')
```

## Addition/substraction of Arrays

NumPy arrays behave differently with respect to the binary arithmetic operators + and \* than Python lists do. For lists, + concatenates two lists and \* replicates a list by a scalar amount (strings also behave this

way).

```
# Addition concatenates lists together.
>>> [1, 2, 3] + [4, 5, 6]
[1, 2, 3, 4, 5, 6]
# Multiplication concatenates a list with itself a given number of times.
>>> [1, 2, 3] * 4
[1, 2, 3, 1, 2, 3, 1, 2, 3, 1, 2, 3]
```

NumPy arrays act like mathematical vectors and matrices: + and \* perform component-wise addition or multiplication.

```
>>> x, y = np.array([1, 2, 3]), np.array([4, 5, 6])
# Addition or multiplication by a scalar acts on each element of the array.
>>> x + 10
# Add 10 to each entry of x.
array([11, 12, 13])
>>> x * 4
# Multiply each entry of x by 4.
array([ 4, 8, 12])
# Add two arrays together (component-wise).
>>> x + y
array([5, 7, 9])
# Multiply two arrays together (component-wise).
>>> x * y
array([ 4, 10, 18])
```

## Sequences

To create sequences of numbers, NumPy provides a function analogous to range that returns arrays instead of lists.

```
>>> np.arange( 10, 30, 5 )
array([10, 15, 20, 25])
>>> np.arange( 0, 2, 0.3 ) # it accepts float arguments
array([ 0. , 0.3, 0.6, 0.9, 1.2, 1.5, 1.8])
```

When arange is used with floating point arguments, it is generally not possible to predict the number of elements obtained, due to the finite floating point precision. For this reason, it is usually better to use the function linspace that receives as an argument the number of elements that we want, instead of the step:

```
>>> from numpy import pi
>>> np.linspace( 0, 2, 9 )           # 9 numbers from 0 to 2
array([ 0.   ,  0.25,  0.5  ,  0.75,  1.   ,  1.25,  1.5  ,  1.75,  2.   ])
>>> x = np.linspace( 0, 2*pi, 100 )  # useful to evaluate function
>>> f = np.sin(x)
```

Two other useful commands are **numpy.ones** and **numpy.zeros**.

```
>>> import numpy as np
>>> z = np.zeros(10,'d')
>>> print(z)
[ 0.  0.  0.  0.  0.  0.  0.  0.  0.  0.]
>>> w = np.ones(10,'d')
>>> print(w)
[ 1.  1.  1.  1.  1.  1.  1.  1.  1.  1.]
```

## Indexing

Indexing for a 1-D NumPy array uses the slicing syntax `x[start:stop:step]`. If there is no colon, a single entry of that dimension is accessed. With a colon, a range of values is accessed.

```
# Make an array of the integers from 0 to 10 (exclusive).
>>> x = np.arange(10)
>>> x
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
# Access elements of the array with slicing syntax.
>>> x[3]
# The element at index 3.
3
>>> x[:3]
# Everything up to index 3 (exclusive).
array([0, 1, 2])
>>> x[3:]
# Everything from index 3 on.
array([3, 4, 5, 6, 7, 8, 9])
>>> x[3:8]
# The elements from index 3 to 8.
array([3, 4, 5, 6, 7])
```

So-called fancy indexing is a second way to access or change the elements of an array. Instead of using slicing syntax, provide either an array of indices or an array of boolean values (called a mask ) to extract specific elements.

```

>>> x = np.arange(0, 50, 10)
>>> x
array([ 0, 10, 20, 30, 40])
# The integers from 0 to 50 by tens.
# An array of integers extracts the entries of 'x' at the given indices.
>>> index = np.array([3, 1, 4])
# Get the 3rd, 1st, and 4th elements.
>>> x[index]
# Same as np.array([x[i] for i in index]).
array([30, 10, 40])
# A boolean array extracts the elements of 'x' at the same places as 'True'.
>>> mask = np.array([True, False, False, True, False])
>>> x[mask]
# Get the 0th and 3rd entries.
array([ 0, 30])

```

Fancy indexing is especially useful for extracting or changing the values of an array that meet some sort of criterion. Use comparison operators like `<` and `==` to create masks.

```

>>> y = np.arange(10, 20, 2)
>>> y
array([10, 12, 14, 16, 18])
# Every other integers from 10 to 20.
# Extract the values of 'y' larger than 15.
>>> mask = y > 15
# Same as np.array([i > 15 for i in y]).
>>> mask
array([False, False, False, True, True], dtype=bool)
>>> y[mask]
# Same as y[y > 15]
array([16, 18])
# Change the values of 'y' that are larger than 15 to 100.
>>> y[mask] = 100
>>> print(y)
[10 12 14 100 100]

```

## Matplotlib

Matplotlib is a collection of command style functions that make matplotlib work like MATLAB. Each pyplot function makes some change to a figure: e.g., creates a figure, creates a plotting area in a figure, plots some lines in a plotting area, decorates the plot with labels, etc.

Generating visualizations with pyplot is very quick:

```
import matplotlib.pyplot as plt
plt.plot([1, 2, 3, 4])
plt.ylabel('some numbers')
plt.show()
```

If matplotlib were limited to working with lists, it would be fairly useless for numeric processing. Generally, you will use numpy arrays. In fact, all sequences are converted to numpy arrays internally. The example below illustrates a plotting several lines with different format styles in one command using arrays.

```
import numpy as np

# evenly sampled time at 200ms intervals
t = np.arange(0., 5., 0.2)

# red dashes, blue squares and green triangles
plt.plot(t, np.sin(t), 'r--', t, t**2, 'bs', t, t**3, 'g^')
plt.show()
```

Last example shows how to save the figure:

```
def f(t):
    return np.exp(-t) * np.cos(2*np.pi*t)

# evenly 100 sampled times
t = np.linspace(0.0, 5.0, 100)

plt.figure(1)
plt.plot(t, f(t), 'k')
plt.savefig('figure.eps')      # save the figure
plt.show()                    # plot the figure
```

## Sympy

SymPy is Python's library for doing symbolic algebra and calculus. It is typically imported with `import sympy` as `sy`, and symbolic variables are usually defined using `sy.symbols()`.

```

>>> import sympy as sy
>>> x0 = sy.symbols('x0')
# Define a single variable.
# Define multiple symbolic variables simultaneously.
>>> x2, x3 = sy.symbols('x2, x3')
# Separate symbols by commas,
>>> m, a = sy.symbols('mass acceleration') # by spaces,
>>> x, y, z = sy.symbols('x:z')
# or by colons.
>>> x4, x5, x6 = sy.symbols('x4:7')
# Combine symbolic variables to form expressions.
>>> expr = x**2 + x*y + 3*x*y + 4*y**3
>>> force = m * a
>>> print(expr, force, sep='\n')
x**2 + 4*x*y + 4*y**3
acceleration*mass

```

Every SymPy expression has a `subs()` method that substitutes one variable for another. The result is usually still a symbolic expression, even if a numerical value is used in the substitution. The `evalf()` method actually evaluates the expression numerically after all symbolic variables have been assigned a value. Both of these methods can accept a dictionary to reassign multiple symbols simultaneously.

```

>>> import sympy as sy
>>> x,y = sy.symbols('x y')
>>> expr = sy.expand((x + y)**3)
>>> print(expr)
x**3 + 3*x**2*y + 3*x*y**2 + y**3
# Replace the symbolic variable y with the expression 2x.
>>> expr.subs(y, 2*x)
27*x**3
# Replace x with pi and y with 1.
>>> new_expr = expr.subs({x:sy.pi, y:1})
>>> print(new_expr)
1 + 3*pi + 3*pi**2 + pi**3
>>> new_expr.evalf()
# Numerically evaluate the expression.
71.0398678443373
# Evaluate the expression by providing values for each variable.
>>> expr.evalf(subs={x:1, y:2})
27.0000000000000

```

These operations are good for evaluating an expression at a single point, but it is typically more useful to turn the expression into a reusable numerical function. To this end, `sy.lambdify()` takes in a symbolic variable (or list of variables) and an expression, then returns a callable function that corresponds to the expression.



```

# Turn the expression sin(x)^2 into a function with x as the variable.
>>> f = sy.lambdify(x, sy.sin(x)**2)
>>> print(f(0), f(np.pi/2), f(np.pi), sep=' ')
0.0 1.0 1.4997597826618576e-32
# Lambdify a function of several variables.
>>> f = sy.lambdify((x,y), sy.sin(x)**2 + sy.cos(y)**2)
>>> print(f(0,1), f(1,0), f(np.pi, np.pi), sep=' ')
0.2919265817264289 1.708073418273571 1.0

```

By default, `sy.lambdify()` uses the `math` module to convert an expression to a function. This allows the resulting function to act element-wise on NumPy arrays, not just on single data points.

```

>>> f = sy.lambdify(x, 2*sy.sin(2*x), "numpy")
>>> f(np.linspace(0, 2*np.pi, 9))
# Evaluate f() at many points.
array([ 0.00000000e+00,
 2.00000000e+00,
 2.44929360e-16,
-2.00000000e+00, -4.89858720e-16,
 2.00000000e+00,
 7.34788079e-16, -2.00000000e+00, -9.79717439e-16])

```

To take derivatives, use the `diff` function.

```

>>> sy.diff(sy.cos(x), x)
-sin(x)
>>> f = sy.exp(x)*x
>>> sy.diff(f,x)
x*exp(x) + exp(x)

```

## Pycodestyle

To make sure your code looks good:

```
$ pycodestyle pythron_script.py
```

## Exercises

**Exercise 1:** Clone your Lab 9 repository

**Exercise 2:** Write a function that accepts a single array as input. Make a copy of the array, then use fancy indexing to set all negative entries of the copy to 0. Return the copy.

**Exercise 3:** Plot the  $x^2 - 3$  on the interval  $[-1, 10]$ .

**Exercise 4:** Compute the antiderivative of  $\frac{x}{x^2 + 2x + 1}$ .

**Exercise 5:** Plot the derivative of  $\frac{x}{x^2 + 2x + 1}$  on the interval  $[0, 1]$ .

**Exercise 6:** Write a README.md, a report.pdf, and push your changes to your GitHub repository for Lab 0.