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YOUR TITLE SMALL CAPS

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par

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33 En français ici. La typographie française s'applique avec des espaces avant et après cer-
34 taines ponctuations, Ah oui ? Test : oui ! Trop cool. La césure des mots se fera aussi selon
35 les règles françaises.

36 **Mots-clefs :** Mot clef 1, 2, ...

ABSTRACT

38 In english here.

39 **Mots-clefs :** Keyword 1, 2, ...

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76

CHAPITRE 1

77

INTRODUCTION GÉNÉRALE

78 Qwerty (Goudriaan, [1986](#); Clark, [2003](#)), Test if punctuation is following english rules! Ah
79 yes? Ok no space...

80 **1.1 Sec1**

81 Lalala

82 **1.1.1 Sec 1.1**

83 Lalalala (Hutchinson, [1957](#), and also the beatles)

A great chapter about biology

86 **2.1 Introduction**

87 A common, although rarely tested, assumption in ecology is that a species is more likely
 88 to be found where it performs the best. In other words, species probability of occurrence
 89 across its range should be positively correlated to the per capita intrinsic growth rate
 90 (McGill, 2012). This hypothesis stems from the interpretation of Hutchinsonian niche
 91 theory (Hutchinson, 1957; Maguire, 1973), which poses that species are limited to loc-
 92 ations where the environmental conditions (*i.e.*, any property outside of the considered
 93 organisms) allow a population to persist. At the core of species distribution models, this
 94 hypothesis is used to identify the climatic variables that are constraining species ranges,
 95 and their projection in the future allows to forecast potential range shifts.

96 This theory, in its more concise formulation, relates the population growth rate r to the
 97 species' niche: the hypervolume in the environmental factors space is the set such that
 98 $r \geq 0$ (Holt, 2009; Godsoe, Jankowski, Holt, & Gravel, 2017). Formally, let $r_i(\mathbf{E}, \mathbf{R})$ be
 99 the growth rate of a focal species i when rare, namely the intrinsic growth rate for a given
 100 environment \mathbf{E} and amount of resources \mathbf{R} . The equation

$$r_i(\mathbf{E}, \mathbf{R}) \geq 0,$$

101 specifies that the fundamental niche corresponds to the locations where \mathbf{E} and \mathbf{R} allow
 102 positive growth.

103 2.2 References

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115

CHAPITRE 3

116

A great chapter

117 (Goudriaan, [1986](#); Strigul, Pristinski, Purves, Dushoff, & Pacala, [2008](#); Lucas, [2020](#))

118 3.1 References

- 119 Goudriaan, J. (1986). Boxcartain methods for modelling of ageing, development, delays
120 and dispersion. In J. Metz & O. Diekmann (Eds.), *The dynamics of physiologically*
121 *structured populations* (pp. 453–473).
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126 *gical Monographs*, ecm.1422.

127

CHAPITRE 4

128

Examples of nomenclature commands

129 In this section we adapt EBT to spatial PSPMs, with the space Γ discretised such that
130 $\Gamma = \bigcup_k \gamma_k$. The growth speed of trees is G . Actually, I changed my mind and now G
131 stands for the Galapagos Islands.

132

CHAPITRE 5

133

DISCUSSION GÉNÉRALE ET CONCLUSION

134 Qwerty

135 **5.1 Sec1**

136 Lalala

137 **5.1.1 Sec 1.1**

138 Lalalala (McDowell et al., [2020](#))

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ANNEXE A

Article 1

A.1 Derivation of the net reproduction rate R_0 and some of its properties

In this appendix, we derive the net reproduction rate $R_0(x, s^*)$ for a given location x and a canopy height s^* . Finally, we prove that $R_0(x, s^*)$ is a decreasing function of s^* which allows us to make our interpretation in the results section. We suppose that the dispersal kernel \mathcal{K} is a Dirac, in other words, seeds emitted from x remain in their source patch x .

A.1.1 Derivation of R_0

We use the method of characteristics in equation (??). This method is commonly used in transport equations, like (??) describing the advection of trees at a non-constant speed G along the size axis. Characteristics allow us to follow individuals through their life, *i.e.*, they represent the trajectories of individuals in the time-size plan (fig. A.1.1 for an example). Our transport equation requires an initial population at time $t = 0$ that we denote by $\phi(s)$. It is the density of trees of size s at the beginning.

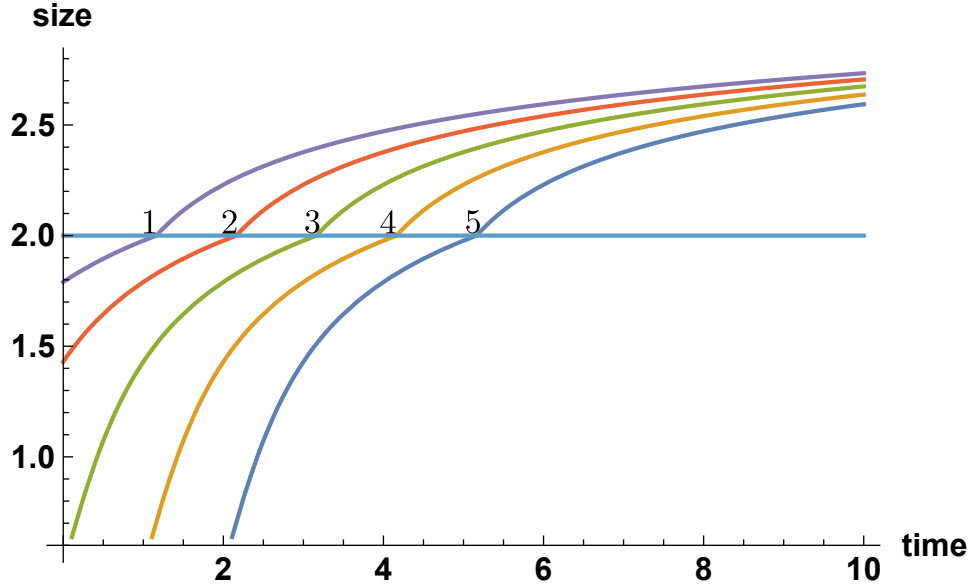


Figure A.1.1: Characteristics for a constant competition $s_c^* = 2$, a climatic constant $\xi_{x,i} = 1$, and for coefficients $\beta_0 = \ln(3)$, $\beta_1 = 1$ and $\beta_2 = -1$. These curves are parameterised by θ and allow us to follow a cohort with relative time θ

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 169 Models. In S. Tuljapurkar & H. Caswell (Eds.), *Structured-population models in*
 170 *marine, terrestrial, and freshwater systems* (Chap. 5, pp. 119–204).
 171 Purves, D. W., Lichstein, J. W., Strigul, N., & Pacala, S. W. (2008). Predicting and
 172 understanding forest dynamics using a simple tractable model. *Proceedings of the*
 173 *National Academy of Sciences of the United States of America*, 105(44), 17018–22.

174 A.2 Proofs of the relations between Purves (2009) and our study

175 In this section, we first provide the assumptions concerning the demography in Drew W
 176 Purves (2009), and match our notations with Drew W Purves’s article in the table A.1.
 177 Finally, we derive Drew W Purves (2009)’s formulæ from our R_0 equation (??).

Table A.1: Link between our notations and Drew W Purves (2009)’s notations. Note that Drew W Purves uses the flat-top version of the perfect-plasticity approximation, which implies the fecundity function to be proportional to the trunk area.

	Meaning	Our notation	Drew W Purves (2009)
	Species index	j , but mostly dropped	j
	Space	x	R (not to be confound with R_0)
	Time	t	τ
	Threshold diameter	s^*, s_c^*	D^*
	Net reprod. rate	$R_0(x, s_c^*)$	$R_{0,j,R}$
	Indiv. growth rate overstorey	$G(s, s^*, x), s \geq s^*$	$G_{L,j,R}$
	Indiv. growth rate understorey	$G(s, s^*, x), s < s^*$	$G_{D,j,R}$
	Mortality rate overstorey	$\mu(s, s^*, x), s \geq s^*$	$\mu_{L,j,R} = 1/\rho_{L,j,R}$
	Mortality rate understorey	$\mu(s, s^*, x), s < s^*$	$\mu_{D,j,R} = 1/\rho_{D,j,R}$
	Fecundity function	$\mathcal{F}\mathcal{A}(s, s^*)$	$F_{j,R}^{\text{capita}} \pi s^2/4$

References

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- Purves, D. W. [Drew W]. (2009). The demography of range boundaries versus range cores in eastern US tree species. *Proceedings. Biological sciences / The Royal Society*, 276(1661), 1477–1484.

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ANNEXE B

187

Article 2

