

MCSC6280: Particle Based Modeling and Simulation

Assignment 1

September 18, 2015

Important Notes

- do your own work
- please submit your material as a single archive file (e.g. *.zip)
- the title of the archive file you submit must contain your last name and the assignment number
- for each question I indicate what material must be submitted; although not explicitly stated, **you must also include a discussion of the results!** (ie, does the result make sense? why or why not?)

1. Inverse transform sampling

a) Write a program to generate random numbers from the following distribution using the inverse transform sampling method:

$$\rho(x) = \sin(x) \quad [0, \pi] \quad (1)$$

b) Make a plot of the distribution of the random numbers produced from your program. You should generate enough random numbers to verify the distribution.

TO BE SUBMITTED:

- your program
- your data file containing the random numbers
- your plot of the distribution of random numbers that includes the original distribution for verification

2. Central Limit Theorem

a) select a non-Gaussian distribution with a zero mean and a standard deviation of one (you can use any distribution you like - but not a Gaussian!)

b) write a program to generate $N_{samples}$ from the distribution and calculate the average and repeat this N times

(you can use any of the methods we discussed in class to generate the random numbers according to the distribution you chose)

c) plot the distribution of the averages; include the normal distribution for verification

TO BE SUBMITTED:

- details of your original distribution
- your program
- your data file containing the averages
- your plot of the distribution including the normal distribution for verification

3. Ideal Gas

a) Write a program to simulate an ideal gas in three dimensions.

b) calculate the pressure on the walls of the system for a minimum of three different sizes

(note that you will want L to be smaller than the 2D case we looked at in class to ensure you simulate a sufficient number of collisions)

c) plot P vs. V ; include the ideal gas law for verification

TO BE SUBMITTED:

- your program
- your data file containing the data you used to verify the ideal gas law
- your plot of the P vs. V including the ideal gas law for verification