Hetrogeneous Multiconstraint Application Partitioner (HMAP)

Servesh Muralidharan[†], Aravind Vasudevan[†], Avinash Malik[§] and David Gregg[†]

†School of Computer Science and Statistics, Trinity College Dublin, Dublin 2, Ireland

Email: muralis@scss.tcd.ie, vasudeva@scss.tcd.ie, David.Gregg.cs.tcd.ie

§IBM Research - Ireland

Email: avinmali@ie.ibm.com

Abstract-In this article we propose a novel framework -Hetrogeneous Multiconstraint Application Partitioner (HMAP) for exploiting parallelism on heterogeneous High Performance Computing (HPC) architectures. Given an hetrogeneous HPC cluster with varying compute units, communication constraints and topology, HMAP framework can be utilized for partitioning applications exhibiting task and data parallelism resulting in increased performance. The challenge lies in the fact that heterogeneous compute clusters consist of processing elements exhibiting different compute speeds, vector lengths, and communication bandwidths, which all need to be considered when partitioning the application and associated data. We tackle this problem using a staged graph partitioning approach. HMAP framework finishes within seconds even for architectures with 100's of processing elements, which makes our algorithm suitable for exploring parallelism potential.

Keywords-Graph partitioning, vectorization, data parallelism, heterogeneous architectures, clusters.

I. INTRODUCTION

High Performance Computing (HPC) clusters increasingly consist of large numbers of heterogeneous processing elements such as CPUs, graphics processing units (GPUs), field programmable gate arrays (FPGAs), low-power processors intended for digital signal processing (DSP), etc. By combining heterogeneous processing units it may be possible to divide the work so that different types of computation in the application are run on different types of units. This can result in significant speed-ups, lower hardware costs and/or reduced power consumption by the HPC system. For example, if a computation contains the right patterns of data parallelism it may run dozens or even hundreds of times faster on a GPU than on a CPU that has similar cost and power consumption. On the other hand, computations with less data parallelism and more complex control flow may run faster on CPUs. Matching the type of computation to the processor can yield significant benefits.

Although the potential of heterogeneous computing is great, exploiting that potential is more difficult. Given a parallel application, it is difficult to map the available parallelism onto the hardware. For example, how does one decide which parallel filters should run on which type of execution unit? Given a system with dozens or hundreds of CPUs, GPUs and other units, how does one divide the work between them? There are several conflicting factors. For

example, one wants to allocate filters to the type of execution unit that will execute it most efficiently. On the other hand, one wants to achieve a good load balance by dividing the work evenly across the units. We want to allocate the filters to reduce communication costs while at the same time taking account of all the other factors.

In this paper we consider the problem of mapping graphs of parallel tasks to heterogeneous HPC computing systems. This problem has been studied extensively for homogeneous architectures where all processing elements are the same. Although the homogeneous case is NP-hard [1], several heuristic solutions have been found that work well in practice. However, extending these solutions to the heterogeneous case is difficult for two reasons.

In the heterogeneous case some processing elements are more powerful than others, so achieving a good load balance usually involves distributing the work unevenly.

A second reason why it can be difficult to extend algorithms for homogeneous architectures to the heterogeneous hardware relates to the strengths and weaknesses of different types of processors. When considering heterogeneous architectures, it is tempting to think of some processing elements simply being more powerful than others. A GPU is not simply a more powerful CPU. In fact, some types of computation run better on CPUs and some on GPUs. For a mapping algorithm to work well, it needs to take account of the strengths and weaknesses of different types of processing elements. In this paper we present an approach to mapping parallel tasks to heterogeneous architectures that addresses both of these concerns.

Our **main contributions** are as follows:

- We present a novel approach to characterizing the type of processing elements based on their level of vector parallelism which allows us to distinguish the suitability of different types of units to different filters.
- We provide a novel algorithm for mapping task and data parallelism to heterogeneous architectures based on hierarchical graph partitioning.
- In addition to mapping filters to processing elements, our framework also allocates the data stores being used by the different filters.

The rest of this paper is organized as follows. We first provide a motivating example in Section II formalizes the problem statement and defines the objective function. Next, in Section III, we provide a detailed description of our framework. Section IV gives the quantitative comparisons of our approach against other approaches. Section V describes the related work and positions our approach in comparison to these works. Finally, we conclude in Section VI.

II. PRELIMINARIES

We now present a formal description of the problem along with the notations used.

A. Execution model

In this paper we consider the streaming [2] model of computation. Streaming is a popular model for programs such as image and signal processing, financial applications, networking, telecommunications, etc.

In the streaming model statements (also called filters/actors/tasks or kernels) execute iteratively, processing the incoming tokens of data. Consider the Jacobi example and its filter graph in Figure 1. The Jacobi algorithm is used in fluid dynamics and heat transfer problems. We consider every statement (marked 1 to 4) in this example to be a filter that can be run in a software pipelined [3] manner on a given architecture. An *example* execution trace of the Jacobi example is shown in Table I for some arbitrary value of computation and communication latency of statements.

P0	10	2_{0}	11		2_1	12
P1		$_{3_0}$	4_0	4_0	3_1	4_1

Table I: Example execution trace of the Jacobi kernel

In a software pipelined model, the different iterations of the filters are run in parallel, e.g., $\mathbf{1}_0$ is the $\mathbf{1}^{st}$ iteration of statement 1 in the Jacobi example, while $\mathbf{1}_1$ is the second iteration and so on and so forth. The latency of the application (termed makespan) is the period, which iterates continuously (shown within the double lined columns in Table I). In such a model, the resource allocation (rather than dependencies) determines the application latency, especially without back-edges in the filter graph (as is the case with our model). In Table I, the resource allocation on processing element P1 determines the application latency, because that is the maximum of the two allocation latencies.

B. Notations

We refer to our application graph, as a *Synchronous DataFlow* (SDF) graph defined formally as a weighted directed graph: $G_t(V_t, E_t)$, where V_t is the set of all filters in the application graph and E_t represents the communication buffers between these filters. The system resources are represented by a weighted undirected graph $G_r(V_r, E_r)$ where V_r represents a set of processing elements (PEs) which can have different processing capabilities and E_r represent the communication links between these PEs with differing latencies and bandwidths.

C. Problem Definition

Given a graph $G_t(V_t, E_t)$, each vertex in the filter graph, $t_i \in V_t$ has a set of associated requirements represented by T^i_j where $j=0...n_t$ with n_t being the number of requirements. These requirements represent the computational requirements of the filter. Namely, T^i_0 represents the scalar requirements, while T^i_1 represents the vector requirements.

The communication edges are decorated with $e^c \in E_t$, which denotes the data the filter requires for processing.

Each resource node $r_i \in V_r$ has a number of computational capabilities, represented by R^i_j where $j=0...n_r$. In our formulation $n_t=n_r$. For each node, capability: R^i_0 represents the frequency of the PE or how many scalar instructions the PE can perform in one second (the *Million Instructions Per Second* (MIPS) count). Capability: R^i_1 denotes the maximum number of parallel vector operations it can perform (the vector length). Each edge $e \in E_r$ has a weight which represents the bandwidth between two PEs r_i and r_i which is denoted by E^c .

The problem at hand is to effectively map the filter graph G_t onto given resource graph G_r . This problem is known to be NP-Hard [1].

Given some filter $t_i \in V_t$ mapped to some resource $r_j \in V_r$, the latency for that node is computed by Equation (1). In this formulation for some filter t_i being mapped onto some resource r_j , we first calculate the number of vectorized instructions that can be executed in parallel (by dividing the required vector length by the vector capacity of r_j represented by R_1^j). We then multiply this number by the number of iterative (non-vectorized) instructions required to get the total number of instructions to be performed by that filter-graph node. Once we have this number we calculate latency of execution of this filter-graph node t_i on this resource r_j by dividing it with the MIPS value of the resource denoted by R_0^j . Calculation of the communication latency requires dividing the number of bits by the bandwidth of the shortest path.

Given the filter-graph and the resource-graph, let \mathcal{M} be some mapping of the application on the resource-graph. For a particular allocation onto some resource node $r_s \in V_r$, we define its computation and communication latency as in Equation (2).

$$((T_1^i/R_1^j \times T_0^i)/R_0^j) + (e^c/E^{c'})|c = (t_i, t_k), t_k \neq t_i,$$

$$\forall t_k \in V_t, c' = (r_j, r_l), r_l \neq r_j, \forall r_l \in V_r$$

$$L_s^{\mathcal{M}} = Lcomp_s^{\mathcal{M}} + Lcomm_s^{\mathcal{M}}$$

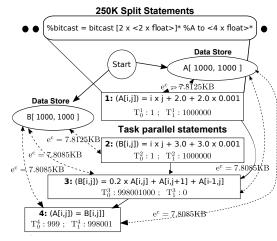
$$Lcomp_s^{\mathcal{M}} = \sum_{\forall t_i \in V_t} ((T_1^i/R_1^s \times T_0^i)/R_0^s)$$

$$Lcomm_s^{\mathcal{M}} = \sum_{\forall t_i \in V_t} e^c/E^{c'}$$

$$s.t., d = (t_i, t_k), t_k \neq t_i, \forall t_k \in V_t \land c' = (r_s, r_l), r_l \neq r_s, \forall r_l \in V_r$$

$$\land d \text{ is routed on } c'$$

$$(21)$$



(b) The filter graph for the Jacobi example ¹

Figure 1: Jacobi example and its filter-graph

Finally, the complete application latency can then be defined as:

$$L^{\mathcal{M}} = max(L_s^{\mathcal{M}}), \forall r_s \in V_r \tag{3}$$

The objective of our framework is to find a mapping \mathcal{M} that minimizes the total application latency as described in Equation (3).

III. HMAP FRAMEWORK

A common approach to solving the homogeneous case is to *partition* the graph across the processing elements [4], [5], [6]. However, we have found that such heuristic partitioning approaches do not work well for heterogeneous architectures. Instead we propose a novel approach where the architecture is hierarchically partitioned into sub-clusters. Each sub-cluster at the same level of the architecture hierarchy has approximately the same computing capability and has relatively local communication. This allows us to use existing approaches that work well for the homogeneous case to partition *heterogeneous* architectures across the sub-clusters at each level of the hierarchy. We show that this is an effective approach if the sub-clusters are well balanced at each level of the hierarchy.

In this section we describe our heuristic framework HMAP. There are two important concepts that need description. First, we describe how the topology clusters are formed from the resource graphs accounting for communication and heterogeneity of the topology. Secondly, given a filter graph with data parallel filters, task parallel filters, and communication extracted as shown in Figure 1(b) how the mapping is performed.

¹Ellipses represent data stores. Rectangles represent filter nodes. Rounded rectangle represents data parallel nodes. The dots represent other data parallel nodes not shown in the figure. Dashed arrows represent communication between data stores and execution statements. Solid arrows represent dependence edges.

A. Clustering the resource graph

The resource graph represents the cluster of compute nodes on which the filter graph will be executed. A sample resource graph is shown in Figure 2 at level 0. The resource graph that is shown is heterogeneous in both computation and communication. The properties of the resource graph are described below:

- Compute nodes: The compute nodes (PEs) are assumed to belong under two categories of processing units, mainly CPUs and GPUs. Following the current trend, the CPUs have a larger MIPS count. The MIPS capacity of a PE is denoted by the first decoration $R_0^i, \forall i \in V_r$. The GPU nodes have a lower MIPS count, but have a large resident vector length, denoted by the second decoration $R_1^i, \forall i \in V_r$. For example, the fifth PE (E0) at level 0 is a CPU, since it has a small vector count and a large MIPS count, the first PE (A0) on the other hand is a GPU, since the capabilities are reversed.
- Communication links: The resource graph shown in Figure 2 at level 0, follows a 2D mesh topology. In this topology the PEs are connected in a grid with individual communication links between them. The bandwidth of these links is non uniform. The different bandwidths on the communication links is represented by the decoration E^C . Our framework can handle any kind of topology, the 2D mesh shown in Figure 2, is just an example topology.
- 1) Clustering the topology: The main idea behind our partitioning approach is to first hierarchically cluster the nodes in the heterogeneous topology, provided by the designer, thereby forming fewer contracted resource nodes. The application is then partitioned in stages (levels) onto the resulting hierarchy. The intuition behind this approach is two fold:
 - Heterogeneous K-way partitioning: The process of partitioning an application onto a given architecture is

equivalent to a heterogeneous K-way partitioning problem. Hierarchically clustering a heterogeneous topology such that the resulting hierarchy consists of contracted PEs with equivalent compute capabilities can reduce the heterogeneous K-way partitioning problem to a homogeneous one.

Considering communication links: The communication
can be considered into the equation, while building
the hierarchical cluster using the min-cut technique.
Thus, a min-cut load-balancing of the PEs in a topology
intuitively means: we are clustering together PEs, which
have large bandwidth together into a single contracted
node, while making an attempt to load balance the two
capabilities: MIPS and vector lengths.

The hierarchical cluster built for the synthetic topology at level 0 of Figure 2, is shown in the levels 1-3. The stages used to build the hierarchy are as follows:

- Effective computation during contraction: Given a topology graph with $|V_r|$ resources, we cluster the PEs in levels, whereby the height of the cluster is $log_2|V_r|$. For example, consider the PEs at level 0 in Figure 2. Contraction from level 0 to level 1 results in 4 PEs at level 1, where the two capabilities, R_0^k , R_1^k for each contracted node $k=\{i,j\}, \exists i\in V_r \land \exists j\in V_r$ is computed as: $R_0^k=R_0^i+R_0^j$, and $R_1^k=R_1^k+R_1^j$. Without loss of generality we assume this for any $k = \{i, j, ..., n\}, \forall n \in V_r$. This process is continued until we reach the top-level with just 1 contracted node. We end up with a load-balanced hierarchy, with each level showing a larger amount of homogeneity, and a smaller number of contracted PEs. The reason for a level based contraction, instead of contracting all nodes into a single 2 node partition, is that when partitioning the application on the resulting top-down cluster, we have fine grained details within each of the contracted node.
- Effective communication during contraction: It is essential that we handle communication correctly while contracting nodes. There are a number of paths that communication between two nodes might follow. The effective bandwidth between any two contracted nodes depends upon the route in the topology graph between these contracted nodes. We use the all-pair Floyd-Warshall [7] algorithm to calculate the shortest path, in terms of latency of data-transfer, for every communication link in the topology. Once the nodes are contracted we use the bottleneck amongst these possible links as our effective bandwidth.

For the topology, at level 0, in Figure 2, we first calculate the best possible paths between every pair of nodes $(i,j) \in (V_r \times V_r)$. Now let us consider the example of the contracted nodes B1 and C1. Node B1 is a contraction of the set of children nodes $\{3,8,6\}$

and C1 is the contraction of the node set $\{2,1\}$. Being an undirected graph with loss of generality we can consider B1 to be the source and C1 to be the destination. Hence, the worst path, in terms of latency of data-transfer, following the all-pair Floyd-Warshall algorithm, between nodes 3 and 2 within the contracted nodes is given by the maximum latency path amongst the memoized best edges: max((3,2), (8,2), (6,2)). Similar computation is carried out for all link pairs in the contracted node with 1 as the destination node to find the minimum latency path. Finally, the addition of these two latencies and its reciprocal gives us the effective bandwidth between the two contracted nodes. This effective bandwidth is the overall bottleneck between the two contracted nodes.

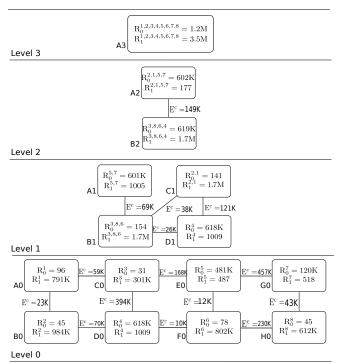


Figure 2: Clustering of a resource graph

B. Task graph partitioning

The filter partitioning on the resulting hierarchical cluster takes a top-down approach. We start with the filter graph extracted from the application (Figure 1). We then recursively partition the filter graph (using K-way partitioning) on the hierarchical cluster of the resource-graph. For the example cluster in Figure 2, we start by partitioning the filter graph in Figure 1, first into two (K=2) partitions considering two equally weighted compute nodes at level 2. Once a partition is obtained for this level, we move onto the next level (level 1), whereby all the filter graph nodes allocated onto node A2 are further partitioned onto the nodes A1 and C1 (again K=2), which are coupled into the contracted node A2. This process is continued recursively for all contracted nodes until

the final level (level 0). During each partition we make sure that the filter node requirements are closely matched to the resource node capabilities.

Doing it in this top down manner has two important consequences.

- Increase in the time complexity: As stated previously, the partitioning problem is equivalent to the K-way partitioning problem. The multi-level K-way partitioning results in the worst cast time complexity of $O(|E_t| \times log_2|V_r|)$ [8]. Our algorithm gives a worst case complexity of $log_2|V_r| \times O(|E_t| \times log_2|V_r|)$ when using the multi-level K-way partitioning. But, in the average case we ask for a balanced 2-way partition at all levels, which results in a complexity of $log_2|V_r| \times O(E_t)$ in the average case.
- Refined mapping: By dividing the mapping on to several levels we can achieve much better load balancing by considering only fewer nodes to map than if we were to do it directly on to the resource graph.

IV. EXPERIMENTS AND RESULTS

A. Our implementation

We use the Metis [9] graph partitioning library to implement our partitioning algorithm. We are not tied to Metis and any other graph partitioner such as Zoltan [10] or Scotch [11] can be used for implementing our algorithm. Herein, we describe how we used Metis to implement the graph partitioning.

The resource graph is represented in the Metis graph format. We represent the PEs' capabilities as constraints of the nodes and the links' bandwidths as communication weight on the edges. We then construct our clustered structure (Figure 2) by asking for a 2-way partition at each level of the $log_2|V_r|$ height. Metis partitions the graph by load balancing the constraints and performing a minimum edge cut. In partitioning the filter graph, we need to balance the constraints on to the available partitions. Metis offers the ability to load balance multiple constraints on to different partitions based on the metric 'tp-weight'. We calculate the ratios between the capabilities of different partitions and represent them as this metric in order to load balance on to the available partitions.

B. The experimental set-up

The experimental set-up consists of the resource graph generation and the filter graph generation. Herein, we describe the two set-ups.

- 1) The resource graph set-up: The experimental set up consists of the following.
 - 1) An interconnection network with $|V_r|$ nodes. $|V_r|$ vary from 64 to 4096 PEs. A node can be just a multi-core CPU or a multi-core CPU with an attached GPU.
 - 2) A set of N_G GPUs where N_G is at most $|V_r|$. The GPUs are connected in the network at locations,

- chosen randomly in the normal distribution of 25% to 75% of $|V_r|$.
- 3) A set $G = \{G_1, G_2, G_3, ... G_{|G|}\}$ Every GPU in this experiment has a vector length of G_i where G_i is sampled randomly from the set G. The elements of set G are chosen from a normal distribution ranging from: 10000 to 100000.
- 4) A set $C = \{C_1, C_2, C_3, ... C_{|C|}\}$ Every CPU in this experiment has C_i cores where C_i is sampled randomly from the set C.
- 5) A set $M = \{M_1, M_2, M_3, ... M_{|M|}\}$ Every $C_i \in C$ and GPU in this experiment has a MIPS count of M_i where M_i is sampled randomly from the set M. The elements of set M are chosen from a normal distribution ranging from: 1000 to 100000.
- 6) A set $\boldsymbol{B} = \{B_1, B_2, B_3, ... B_{|B|}\}$ Every $|V_r|$ node in this experiment has a bandwidth of B_i in MB/s where B_i is sampled randomly from a normal distribution ranging from: 100 to 100000

For given values of $|V_r|$, N_G , G, G, M and B and a given application, let the k-th <u>trial</u> be defined as one execution of the following sequence of steps.

- For each GPU G_i , sample G and M randomly to determine its vector length V_i and MIPS count M_i .
- For each CPU P_i , sample C randomly to determine the number of cores C_i in the processor P_i .
- For each core C_i in the processor P_i sample V_i and M_i randomly from set G and M.
- Use our framework to extract data and filter parallelism that is best utilizable by the heterogeneity created by parameters in items 1, 2, and 3 above. Determine the execution time $L^{\mathcal{M}}$.

An experiment, $E(|V_r|, N_G, G, CM, B)$, consists of conducting enough of the above trials so that width of the 95% confidence interval on the average value of $Latency^{\zeta_M}$ is less than 10% of the average value. This results in a variable number of trials with different experimental setups. Note that two trials differ from each other only in the seed for the random number generator. This reduces the dependence of our results on a lucky sequence of numbers from the random number generator.

- 2) Random filter graph generation: We built a random graph generator to test our partitioning methodology rigorously. The random graph generator needs as input the following parameters:
 - Number of nodes (n) Total number of nodes to be present in the filter graph
 - Indegree (i) Average indegree of every vertex
 - Outdegree (o) Average outdegree of every vertex
 - Communication to Computation Ratio CCR (c) It is the ratio of the average communication cost of an outedge the average computation cost of the vertex itself.
 If a DAG's c is low, then it can be called a computation

- intensive application and if it is greater than 1 it can be called a communication intensive application
- Structure of the graph (α) We generate the height of the graph based on α as $\frac{\sqrt{n}}{\alpha}$. This implies the width of the graph becomes $\sqrt{n}*\alpha$. Higher values of α give wider graphs which means the graph has more inherent task parallelism, while lower values give taller graphs which means the graph is inherently serial
- Beta (β) We use this parameter to decide if an actor in the filter graph is CPU intensive or GPU intensive. Smaller values of β makes actors CPU intensive (by making first constraint larger than the second), while larger values make it GPU intensive (by making the second constraint larger than the first)
- ullet Skewedness factor (γ) This parameter dictates how computation is spread across the graph. Smaller values of γ give uniformly distributed values for the constraints of the actors while larger values produces skewed graphs

For our experiments we generated random graphs by choosing values for the input parameters from the following sets:

- $\chi_n = \{128, 256, 512, 1024, 4096, 8192, 16384\}$
- $\chi_i = \{1\}$
- $\chi_o = \{2, 4, 8\}$
- $\chi_c = \{0.0001, 0.001, 0.01, 0.1, 1\}$
- $\chi_{\alpha} = \{0.1, 1.0, 10.0\}$
- $\chi_{\beta} = \{5, 25, 50, 75, 95\}$
- $\chi_{\gamma} = \{5, 25, 50, 75, 95\}$

We generated one graph per combination for a total of 7875 application graphs. Since the random graph generator has a variety of inputs and these inputs are filled in from a large set of possible values, a diverse set of DAGs are generated with various characteristics. Experiments based on diverse set of DAGs prevent biasing towards a particular partitioning algorithm.

C. Experimental Results

The experimental set-up consists of a dual socket system consisting of Intel Xeon E5620 CPU running at 2.4Ghz with 24GB DDR3 RAM. The system is running Linux kernel ver 3.0.40-1. Our framework was compiled using gcc version 4.7.1 with '-O3' optimization flag.

A total of 55120 experiments were performed on each case individually. The results comparing K-way partitioning using metis and HMAP framework are shown in 3. The results are divided into a total of 5 graphs each representing a common characteristic of the application and finally fig:overall shows the average application latency based on all the input graphs. Overall it just took us 50 seconds more than metis for the biggest architecture of 4096 nodes to determine a partition.

Figure 3(a) and 3(b) represents application graphs that consists of proportionally larger CPU and GPU intensive

filters respectively. On all architectures we perform consistently better and on an average we achieve better results in the case of GPU intesive applications, whereas metis which uses k-way partitioning alone provides almost similar latencies.

In the case of figure 3(c) and 3(d) which represents applications that are tall consisting of more filters that can only be executed serially and fat consisting of more task parallel filters, the trend continues and we are able to provide better latencies in the case of larger archtiectures when compared with metis alone.

The figure 3(e) which shows the set of application graphs which are highly communication intensive determined by the CCR c=1, we perform significantly better in comparison to metis for larger archtiectures. This is due to our clustering approach that ensures topology nodes that communicate with high bandwidths are combined together at each level.

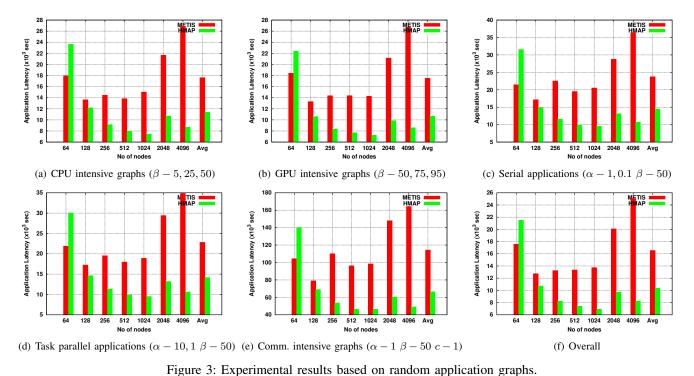
Finally, in figure 3(f) we see that we are able to scale better when compared with metis. In smaller architecture sizes metis is able to produce good mapping, whereas on larger architecture sizes we are able to perform over several magnitudes better in comparison.

V. RELATED WORK

A significant amount of research literature exists for extracting parallelism from programs [12], [13], [14], [15], [16]. The polyhedral optimization model [12] concentrates on extracting parallelism from loops, which is a form of data-parallelism. The polyhedral optimization community has concentrated on optimizing for CPUs and GPUs separately, but to our knowledge has not explored the combination of the two. Carpenter et. al [16] have again explored ideas for partitioning onto heterogeneous architectures, but at a much smaller scale and again ignoring data-allocation costs and depending upon the polyhedral model for vectorization. The StreamIt [17] community has also explored parallelization techniques, but they have only targeted homogeneous RAW [18] architecture. There are the classical algorithms such as critical path scheduling [19] and list scheduling [20], which have been used for scheduling task parallel process onto homogeneous architectures. The list scheduling techniques targeting heterogeneous architectures such as [21] do not exploit SIMD parallelism onto vector processors. Declustering [15], is another technique, which misses the opportunity to mix SIMD and task-parallel optimizations together.

Cluster based partitioning techniques [22], [23], [24] only consider independent tasks without communication. The proposed heuristics for partitioning data-parallel applications onto clusters [25], [26] do not consider vectorization potential available on the compute clusters and only concentrate on partitioning task parallel processes.

Random search techniques use a specific objective and random choices to guide them through a search space to



Each graph shows the latency for a given architecture and application graphs that belong to a certain criteria

arrive at a solution. The objective is usually derived from information obtained from previous random searches or prior knowledge about the system. Genetic Algorithms (GA) [27], [28], [29], [30] is a commonly used algorithm from this technique and generate reasonably good results. The drawback being this requires significantly more time than heusristic based algorithms [24]. Moreover these techniques often give such good results due to a unique set of parameters. Determining such optimal parameters to fine tune these random techniques to get good results is a challenge of its own. Moreover Parameters that give good results for a certain scenario may not be the same for a different one.

Several other techniques also exist that belong to the same category in addition to GA such as simulated annealing [28], [31] and local search methods [32], [33] which suffer from the same disadvantages.

VI. CONCLUSION

In this paper we have described a novel staged graph based partitioning technique to partition and schedule applications onto heterogeneous execution architectures. HMAP framework considers both filter and data parallelism, which allows the application writers to design and tune their applications to extract parallelism. We also consider communication along application and underlying architecture edges, which when combined with the filter and data parallelism gives a better estimate of the application latency than the currently described research literature targeting similar problems.

We have tested our framework on a statistical sample of randomly generated filter graphs with varying compute, vector, communication requirements.

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