

## Assignment 4- Stacks & Queues

Amalia Karaman

### 1) Stacking

→ Given an empty stack, what'll be the contents of stack after following operations?

1.  $\text{push}(8)$  →  $[8]$
  2.  $\text{push}(2)$  →  $[8, 2]$
  3.  $\text{pop}()$  →  $[8]$  (remove 2)
  4.  $\text{push}(\text{pop()} \times 2)$  →  $[]$  →  $[16]$  ( $\text{pop } 8, \times 2$ )
  5.  $\text{push}(10)$  →  $[16, 10]$
  6.  $\text{push}(\text{pop()}/2)$  →  $[16, 5]$  ( $\text{pop } 10, \div 2$ )
- Fin:  $[16, 5]$

### 2) Queuing

Given empty queue, what are contents of stack after following operations?

1.  $\text{push}(4)$  →  $[4]$  (push 4)
2.  $\text{push}(\text{pop()} + 4)$  →  $[8]$  ( $\text{pop } 4 + \text{add } 4$ )
3.  $\text{push}(8)$  →  $[8, 8]$  (8)
4.  $\text{push}(\text{pop()}/2)$  →  $[8, 4]$  ( $\text{pop } 8 + \text{divide by } 2$ )
5.  $\text{pop}()$  →  $[4]$  (remove 8)
6.  $\text{pop}()$  →  $[]$  (remove 4)

Fin:  $[]$

empty queue, no values remain

### 3) <sup>Directed</sup> Given a doubly-linked list, you can search an element in $O(n)$ , same true for deque.

Given a deque  $q$  & an element  $x$ , provide an algorithm that finds the position in the deque in which element  $x$  is stored in  $O(n)$ .



3) (cont.) Pseudocode:

```
int findInDeque(Deque<Integer> q, int x) {  
    int index = 0  
    for (int num: q) {  
        if (num == x) {  
            return index; // return position  
        }  
        index++;  
    }  
    return -1; // if not found  
}
```

Worst case  
time complexity  
for deque

A deque allows you to insert or delete from both ends but you still have to search through each element sequentially which resonates w/ the way worst-case scenarios operate by scanning all elements, so I'm giving  $O(n)$  time complexity.  $\ddot{\smile}$   
I started @ index = 0, to find the position of  $x$  in the deque. Then it went through each element individually at a time, and as soon as it'd find  $x$ , it'd return the index. Otherwise, the index continues increasing as it moves through the deque, and if it never finds  $x$ , it returns -1 to indicate that it's not in the deque.



7) For algorithms written in #4-6, explain their time complexity + space complexity in Big-O notation. Explain how.

#### #4) Balanced Brackets

Time:  $O(n)$

Space:  $O(n)$

Time: Input is scanned once by one + each bracket is processed once, + each character is push/popped onto/from the stack. Pushing/popping takes  $O(1)$  time so for  $n$  brackets it's  $O(n)$ .

Space: In worst case all  $n$  brackets are stored in the stack so max stack size is  $O(n)$ .

#### #5) Decode String

Time:  $O(n)$

Space:  $O(n)$

Time: Since stack operations take  $O(1)$  time, this time complexity is  $O(1)$  also b/c each character processed @ MOST twice.

Space: The stack stores nested sequences + repeat counts + in worst case output is  $O(n)$  in size.

#### #6) Infix to Postfix

Time:  $O(n)$

Space:  $O(n)$

Time: It scans each <sup>character</sup> ~~operation~~ once + push/pop operators once as well, and stack operations are  $O(1)$  so we have  $O(n)$  for this algorithm.

Space: It holds the operators ~~TEMPORARILY~~, + each the stack are processed once. In worst case all  $n$  operators ~~are stored~~ could be held at once.