

Problem 4

(a) Activated state is more favorable since the Gibbs free energy at the activated state is lower than the not activated state; Therefore, it takes less energy for the gate to go to the activated state from the not activated state than to go from the activated state to the not activated state. $V_m = 0$

In a biological membrane, when the cell is depolarized, the potassium ions tend to flow outside the membrane, to counteract with the unbalanced state. Therefore, more potassium gates tend to open.

$$(b) \text{ state 1} = \Delta G - zFV - G_c$$

$$\text{state 2} = \Delta G + (1-\lambda)zFV.$$

$$\alpha_n = \frac{kT}{h} \exp\left(-\frac{\text{state 1}}{RT}\right) = \frac{kT}{h} \exp\left(-\frac{\Delta G}{RT}\right) \exp\left(\frac{zFV}{RT}\right) \exp\left(\frac{G_c}{RT}\right)$$

$$\beta_n = \frac{kT}{h} \exp\left(-\frac{\text{state 2}}{RT}\right) = \frac{kT}{h} \exp\left(-\frac{\Delta G}{RT}\right) \exp\left(\frac{(1-\lambda)zFV}{RT}\right)$$

$$\frac{dn}{dt} = (1-n)\alpha_n - n\beta_n =$$

$$\begin{aligned} \frac{dn}{dt} &= (1-n) \frac{kT}{h} \exp\left(-\frac{\Delta G}{RT}\right) \exp\left(\frac{zFV}{RT}\right) \exp\left(\frac{G_c}{RT}\right) \\ &\quad - n \frac{kT}{h} \exp\left(-\frac{\Delta G}{RT}\right) \exp\left(\frac{(1-\lambda)zFV}{RT}\right). \end{aligned}$$

$$= \frac{kT}{h} \exp\left(-\frac{\Delta G - G_c}{RT}\right) \exp(\lambda zV) \left[1 - n \exp\left(-zV - \frac{G_c}{RT}\right)\right]$$

$$y = \left[\frac{kT}{h} \exp\left(-\frac{\Delta G - G_c}{RT}\right) \right] \exp(-zV - \frac{G_c}{RT}) = -z(V + V_n) \quad V_n = -\frac{G_c}{zRT}$$

(c). $\frac{\partial n}{\partial t} = 0$ at steady state.

$$(1-n)\alpha_n = n\beta_n$$

$$n_{\infty} = \frac{\alpha_n}{\alpha_n + \beta_n} \Rightarrow n_{\infty} =$$

$$\alpha_n = \gamma \exp(\lambda z V).$$

$$\beta_n = \gamma \exp((\lambda - 1)zV - zV_n).$$

$$n_{\infty} = \frac{1}{1 + \exp(-z(V + V_n))}$$

$$\boxed{\frac{\partial n}{\partial t} = \frac{n_{\infty} - n}{\tau_n}}$$

$$\tau_n = \frac{1}{\alpha_n + \beta_n}.$$

$$\therefore \tau_n = \frac{1}{\gamma \exp(\lambda z V) [1 + \exp[z(V + V_n)]]}$$