



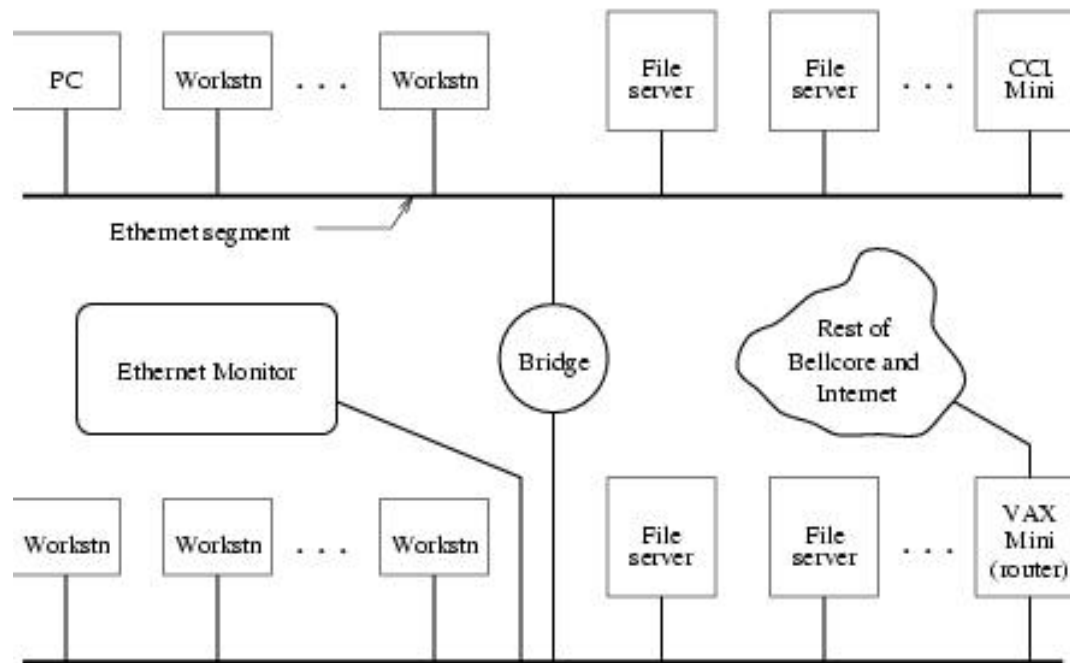
Internet Measurement  
& Analysis (IMA)

# Topics in Internet Measurement

## Modeling Network Traffic

Prof. Georgios Smaragdakis, Ph.D.

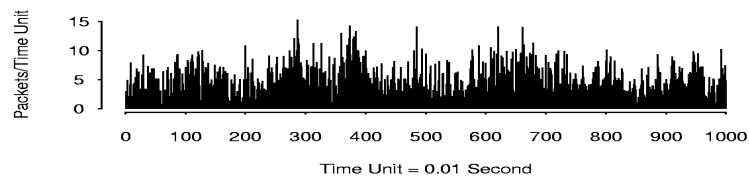
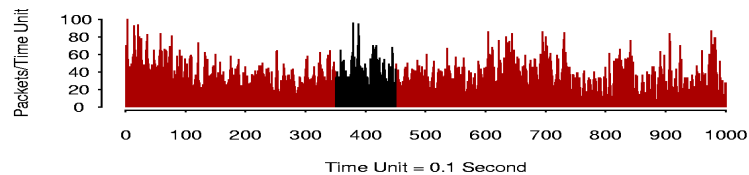
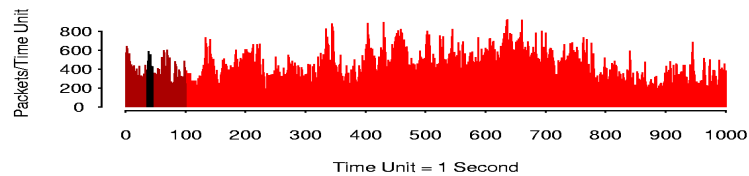
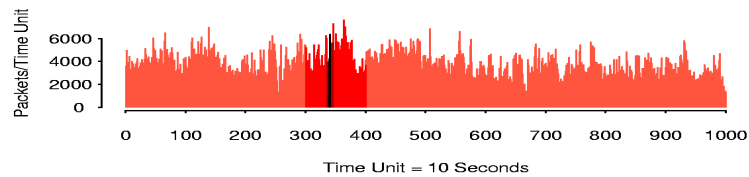
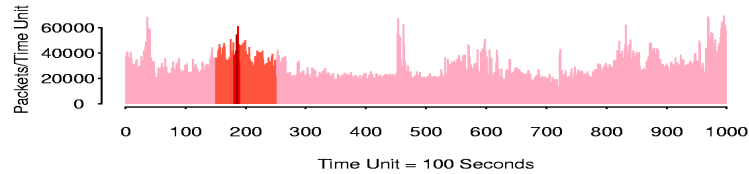
# Network topology 1989



# Network Traffic: Poisson?

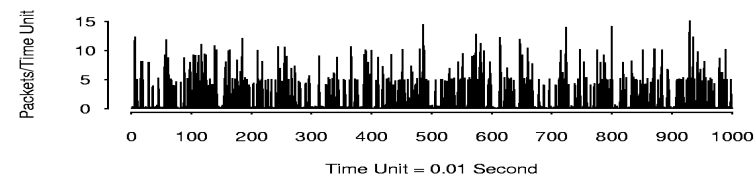
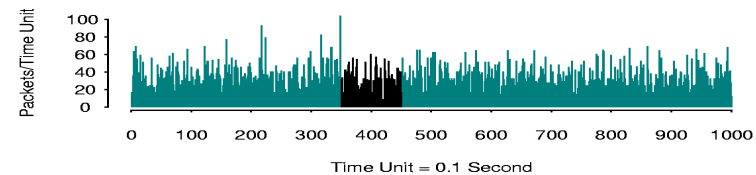
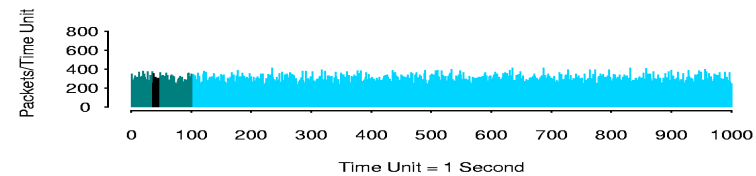
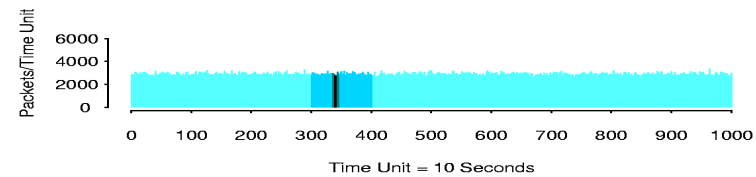
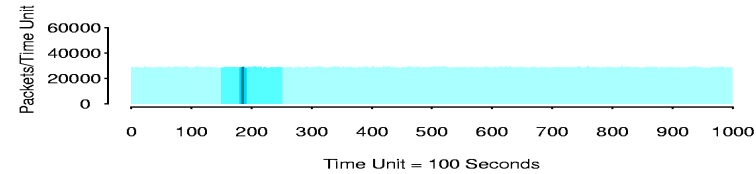
## Realization

Measured Data Traffic (Ethernet LAN)

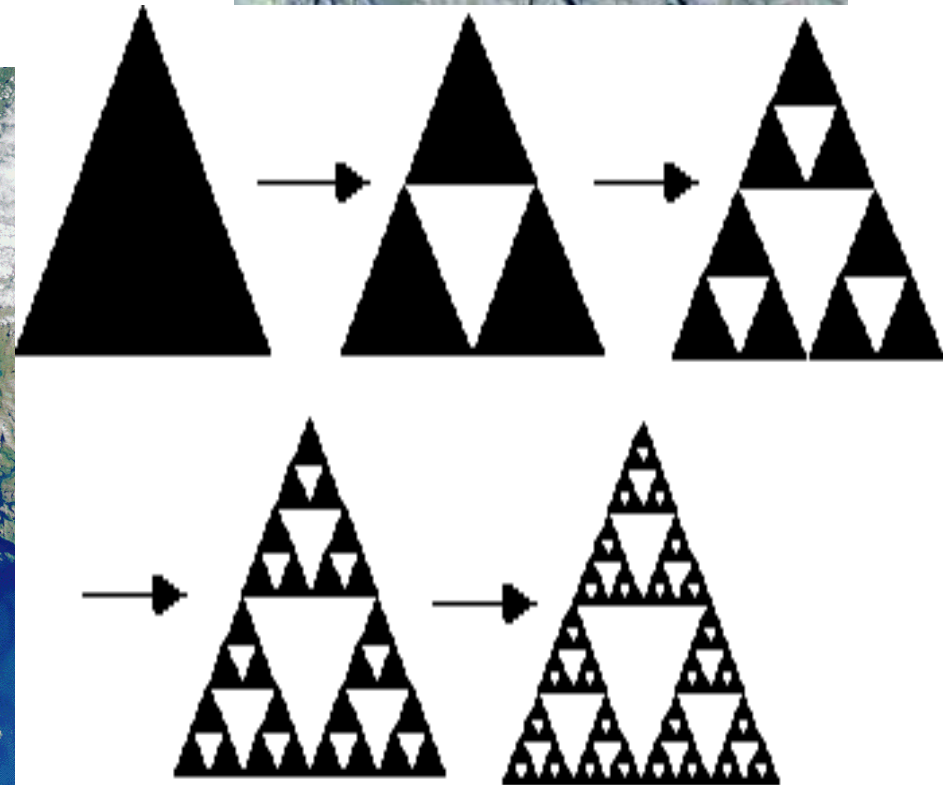
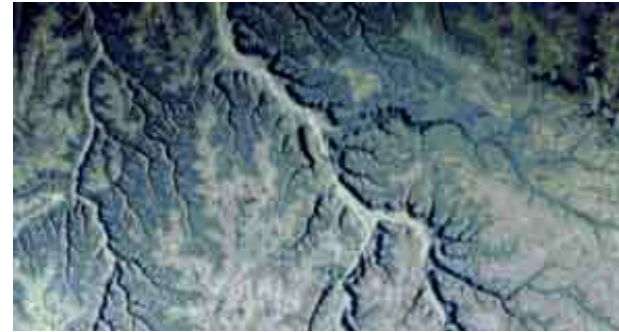
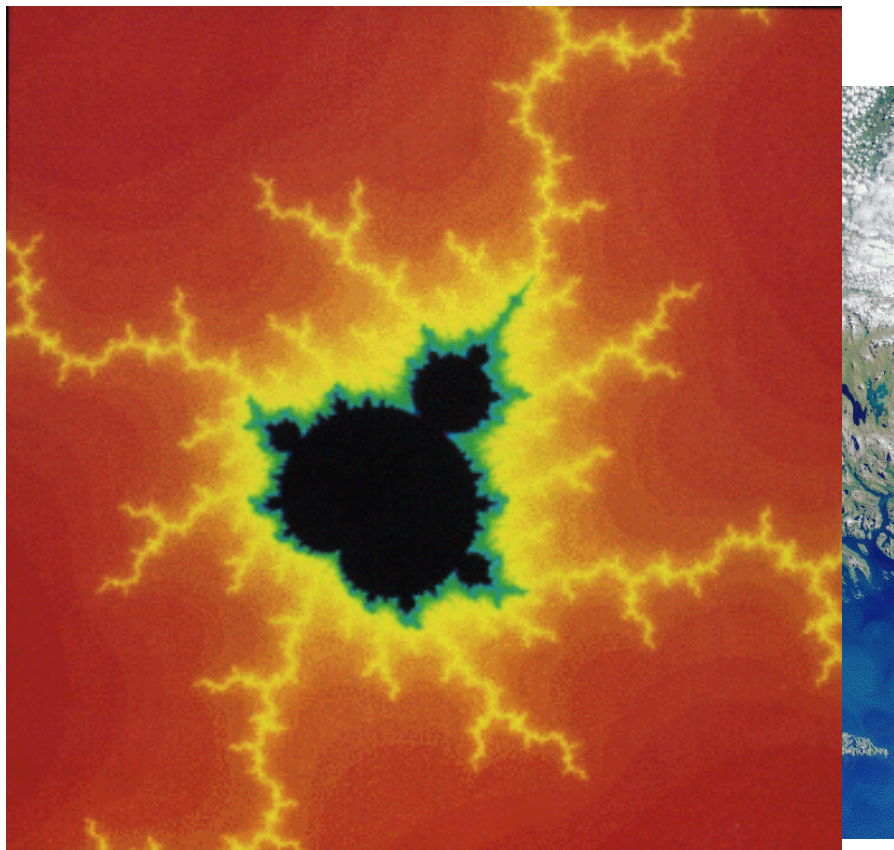


Traditional Models for Data Traffic

Poisson

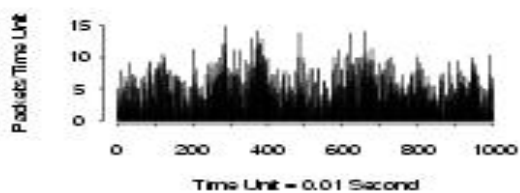
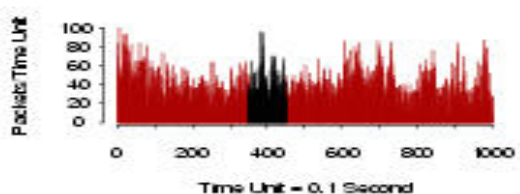
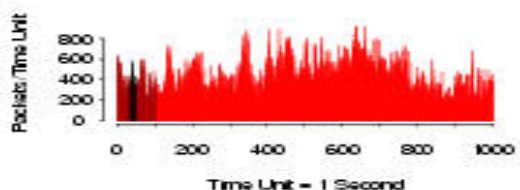
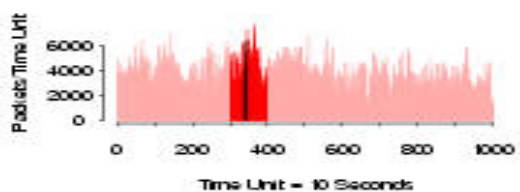
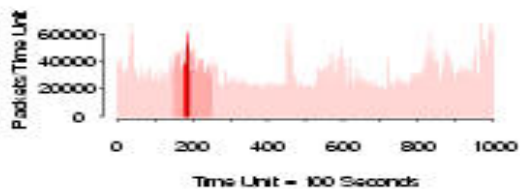


# Self-similarity

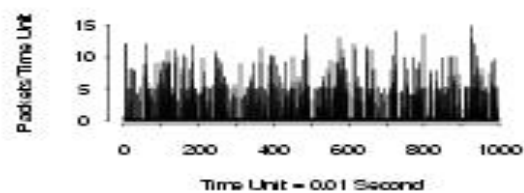
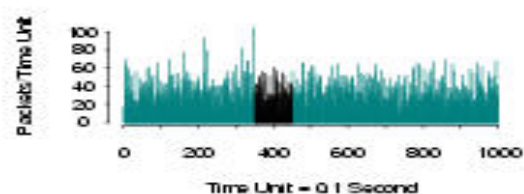
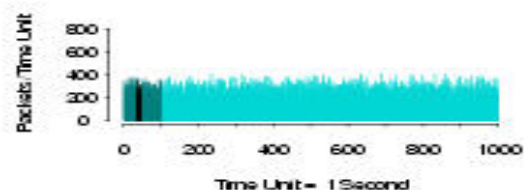
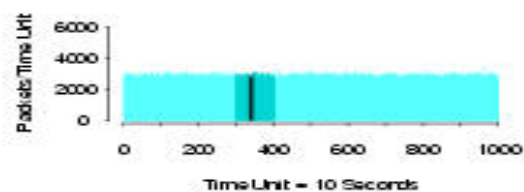
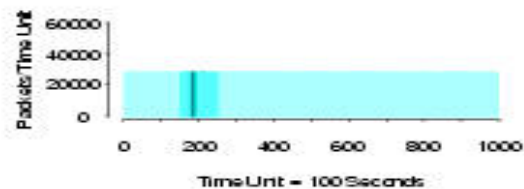


Examples: Nature (rivers, coastline)

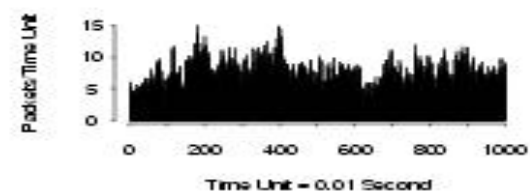
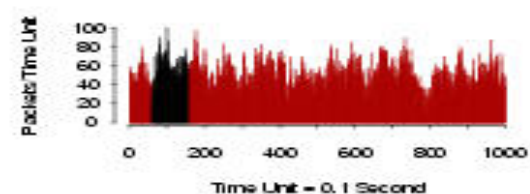
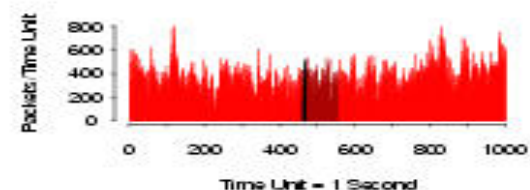
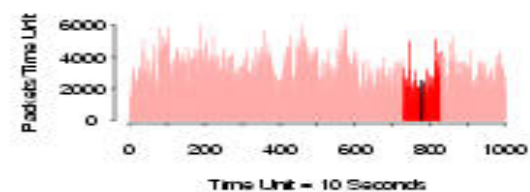
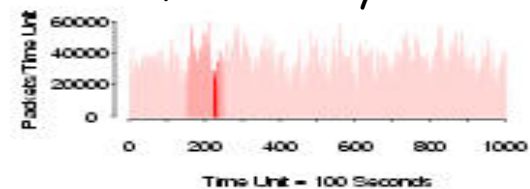
### Realization



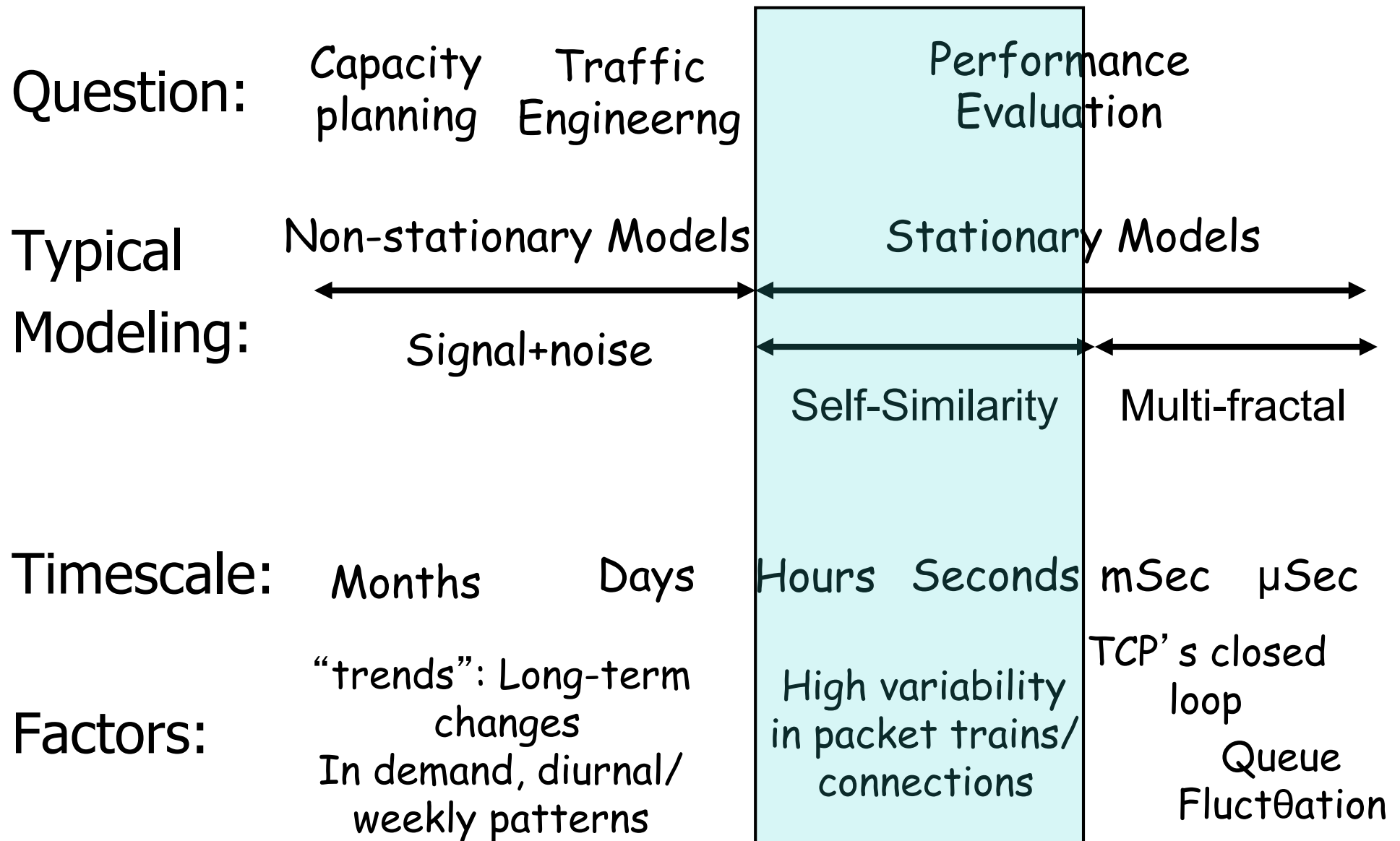
### Poisson



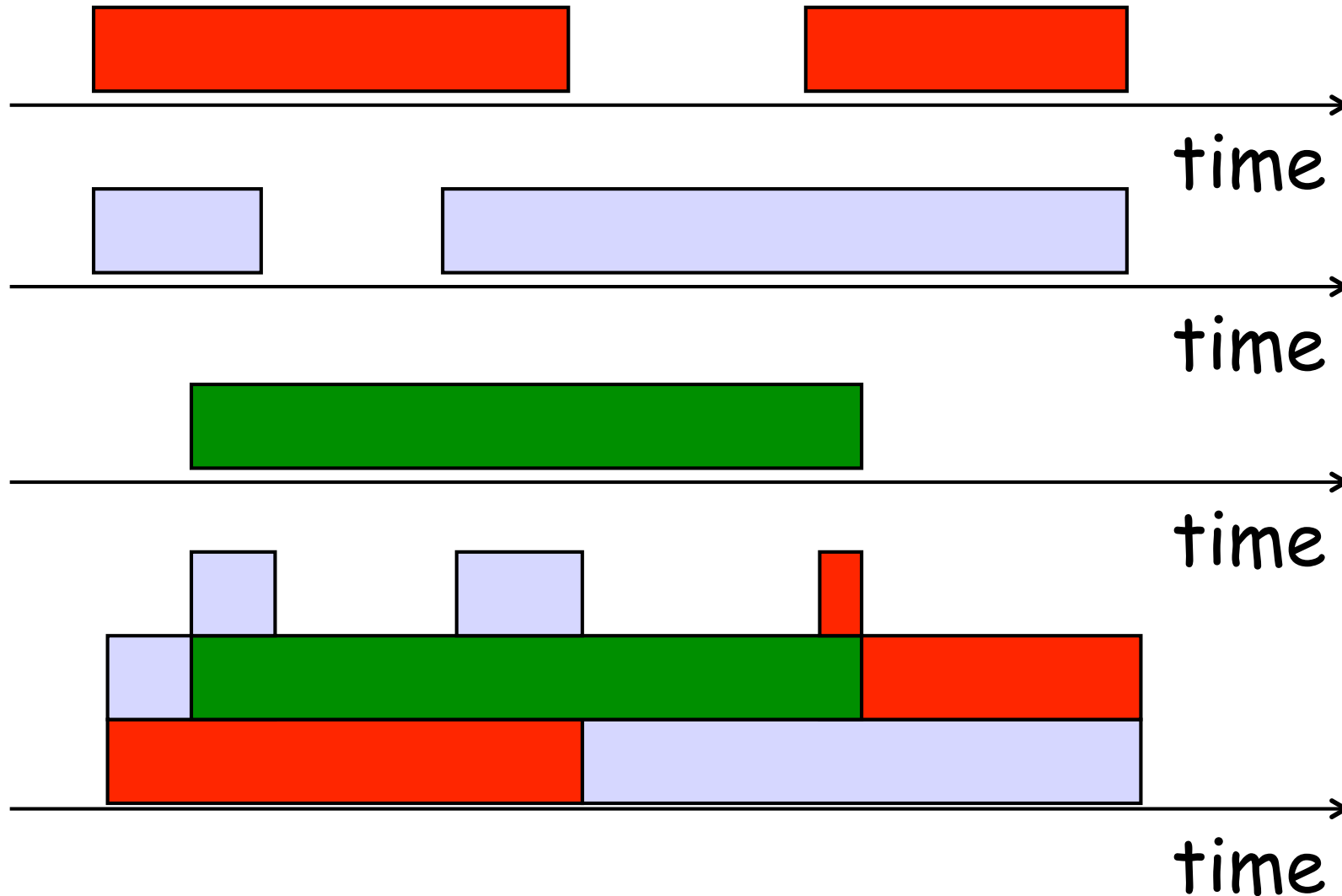
### Self-similar synthetic



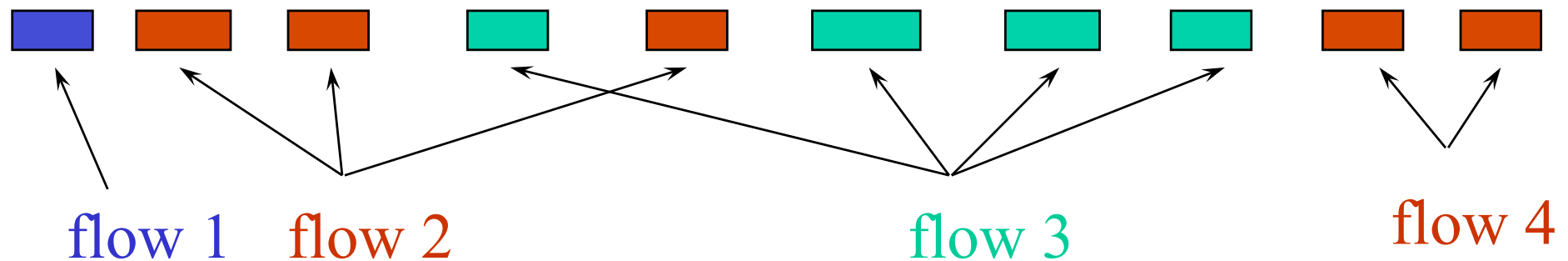
# Overview of Traffic Analysis



# Route Causes? Superposition of sources (e.g., computer processes, human activity)



# Grouping IP packets into flows



- ❑ Group packets with the “same” address
  - Application-level:** single transfer web server to client
  - Host-level:** multiple transfers from server to client
  - Subnet-level:** multiple transfers to a group of clients
- ❑ Group packets that are “close” in time
  - 60-second spacing between consecutive packets



# Light tails

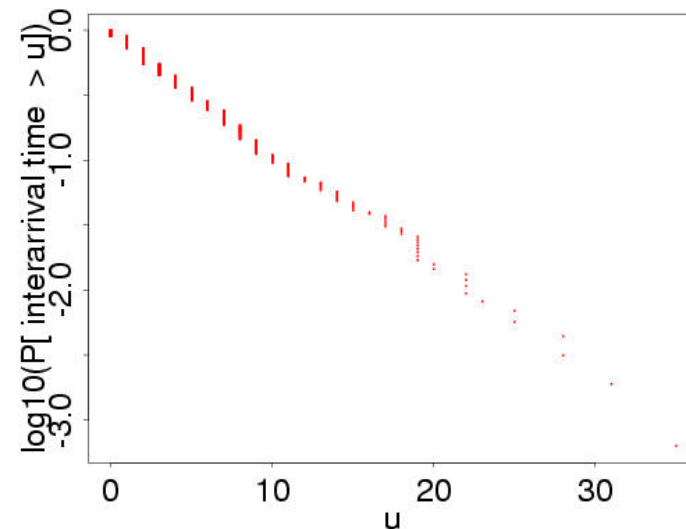
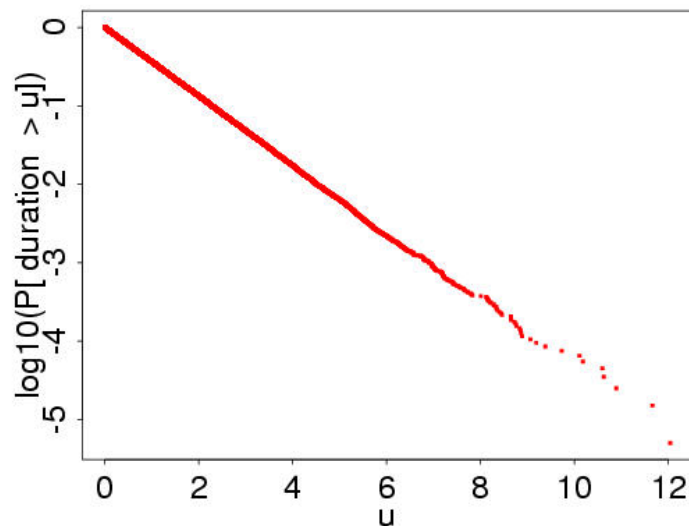
Definitions:

Short-range Dependent:

Superposition of independent ON/OFF sources is **short-range dependent**, if durations of periods are **light-tailed**

# Light-tailed distributions

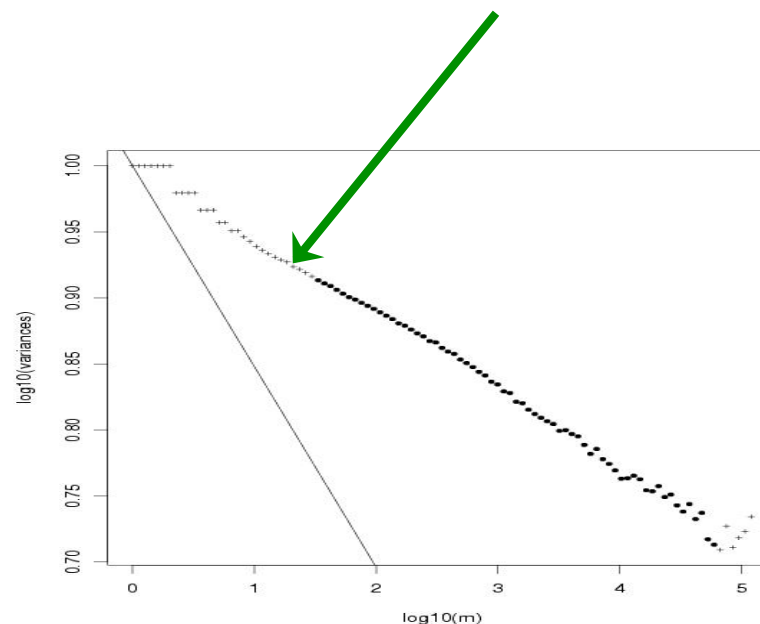
- ❑ Examples: Exponential, Normal, Poisson, Binomial
- ❑ Key features of Function (F):
  - F has limited variability
  - F is tightly concentrated around its mean
  - F has finite moments
  - $P[X > x]$  (CCDF) vs.  $x$  on log-linear scale is linear for large  $x$



# Short-range dependence (SRD)

## □ Key features

- Short range dependence = **finite correlation length**
- Fluctuations over **narrow range of time scales**
- Plotting  $\text{var}(X^{(m)})$  vs.  $m$  on log-log scale shows linear relationship for large  $m$ , with **slope  $-1$  ( $\beta=1$ )**



# Self-similarity via heavy tails

Definitions:

Self-similar:

Superposition of independent ON/OFF sources is **self-similar**, if durations of periods are **heavy-tailed** with **infinite variance**

Long-range Dependent:

Superposition of independent ON/OFF sources is **long-range dependent**, if durations of periods are **heavy-tailed**

# Self-Similarity via heavy tails

## Statistical analysis of LAN traffic traces:

- Users are ON/OFF
- ON periods are heavy-tailed (file sizes)
- OFF periods are heavy-tailed (think times)
- Distributions of ON/OFF-periods show heavy tails with infinite variance

# Why is LAN traffic self-similar

## Possible explanations:

- Network?
- User behavior?

## User behavior:

- Examine characteristics of individual src-dst pairs
- Clustering of packets between src-dst pairs
- Define clusters as ON/OFF periods
- Distribution of ON/OFF periods

# Summary of light-tails and SRD

- ❑ Distributional assumptions
  - Light-tails imply **limited variability in space**
- ❑ Assumptions about temporal dynamics
  - SRD implies **limited variability over time**
- ❑ Common characteristics of traditional traffic processes
  - **Limited burstiness (in time and space)**

# Heavy-tailed distributions

- $X$  random variable with distribution function  $F$
- $F$  is said to be heavy-tailed if there exists  $c > 0$

$$1 - F(X) = P[X > x] \sim cx^{-\alpha} \quad \text{as } x \rightarrow \infty$$

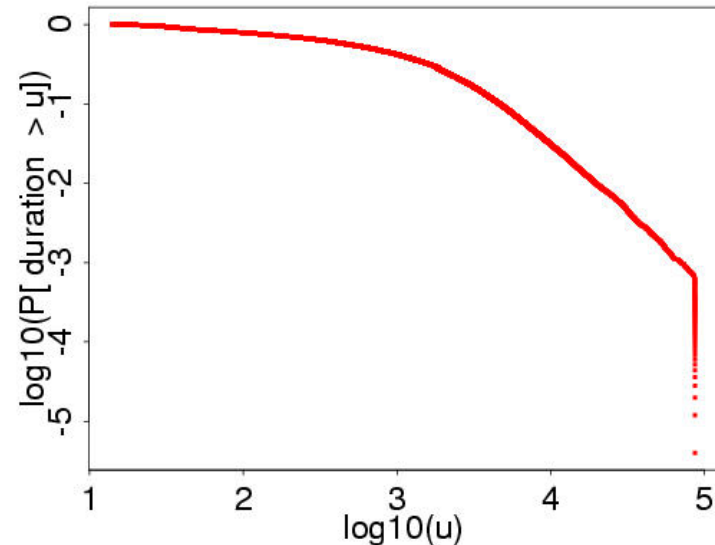
$1 < \alpha < 2$ ,  $X$  has finite mean but **infinite variance**.

Where:  $\alpha = \beta + 1$

→ **parsimonious model** (small number of parameters)



# Heavy-tailed distributions



## □ Important features:

- Finite mean but **infinite variance**
- Heavy-tailed implies **high variability**
- Tail decays like a power, hence **power-law distribution**
- Plotting  $P[X > x]$  (CCDF) vs.  $x$  on **log-log scale** is linear for large  $x$  with slope  $\alpha$

## □ LRD is not a characteristic only of Heavy-tailed distributions

# Aggregate traffic - exact self-similarity

Intuition: self-similar processes “look the same” at all (i.e., over a wide range of) time scales

Def.: A stationary process  $X = (X_k : k \geq 1)$  is called **exactly self-similar** (self-similarity parameter  $H$ ) if for all  $m \geq 1$ ,

$$X = m^{1-H} X^{(m)}$$

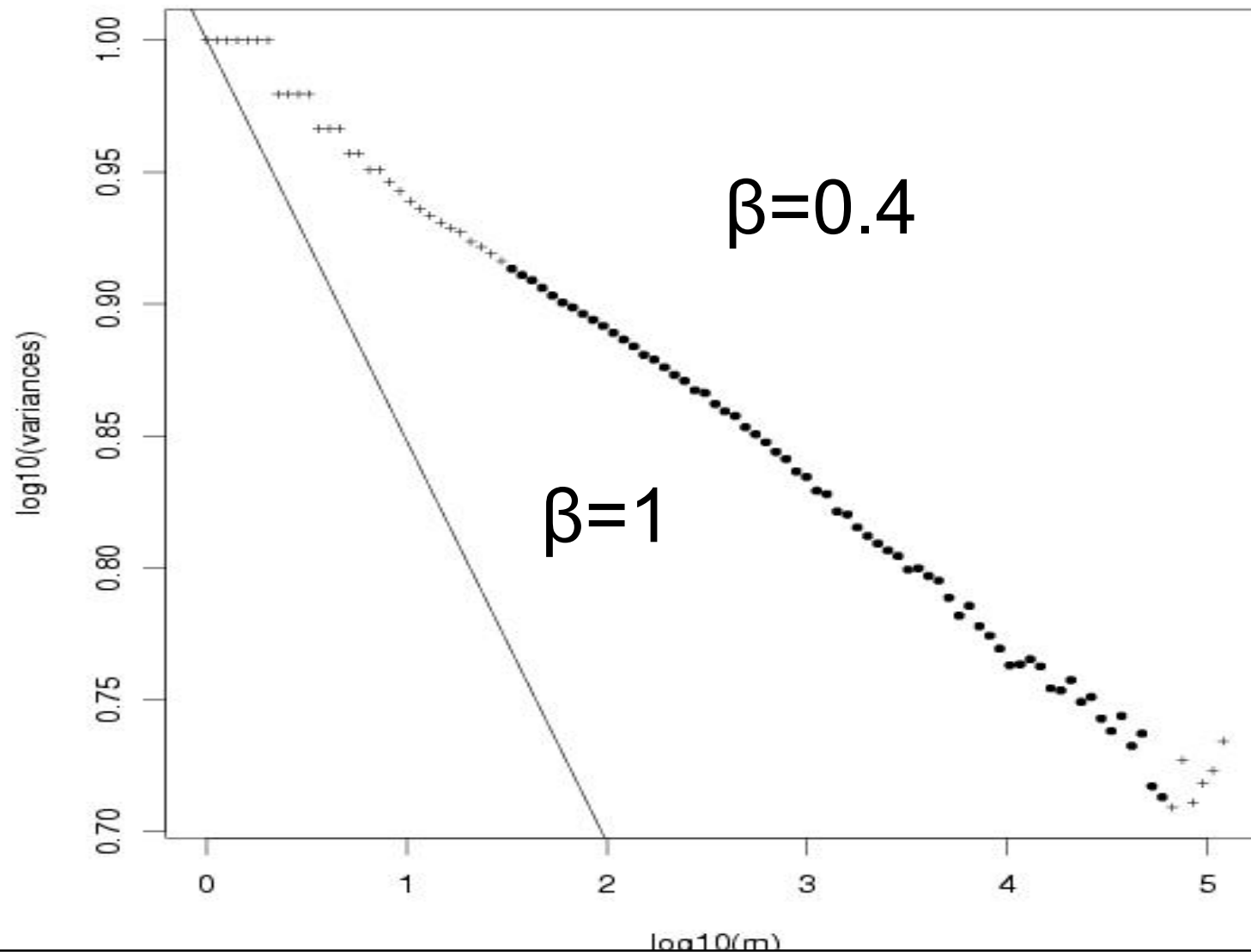
$H$  is called the **Hurst** parameter. To be self-similar,  $0.5 < H < 1$

Test of *variance*, i.e., the measure of how far a set of samples is spread out,  $\text{var}(X) = E((X - E(X))^2)$ .

$$\text{var}(X^{(m)}) \sim cm^{-2H-2} \quad \text{as } m \rightarrow \infty$$

# Variance time plot

$$H=1-\beta/2=0.8 \text{ in } (0.5,1)$$



# Long-range dependence (LRD) & Heavy-tail Distributions

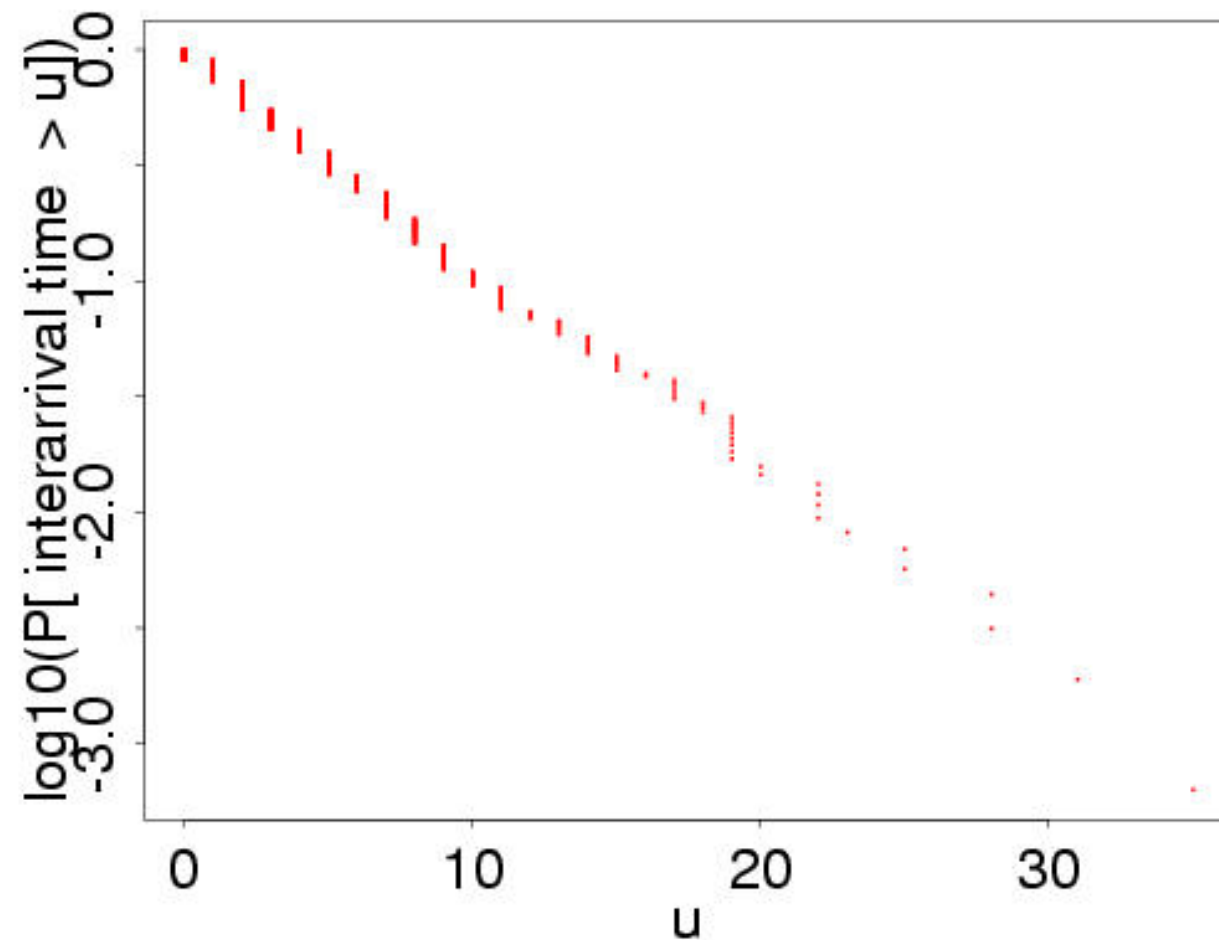
- ❑ There are observations in the past that are correlated with current observations
- ❑ Parsimonious models available
- ❑ It changes the way we design systems  
(e.g., how to deal with bursts, effect of queuing, protocol design)



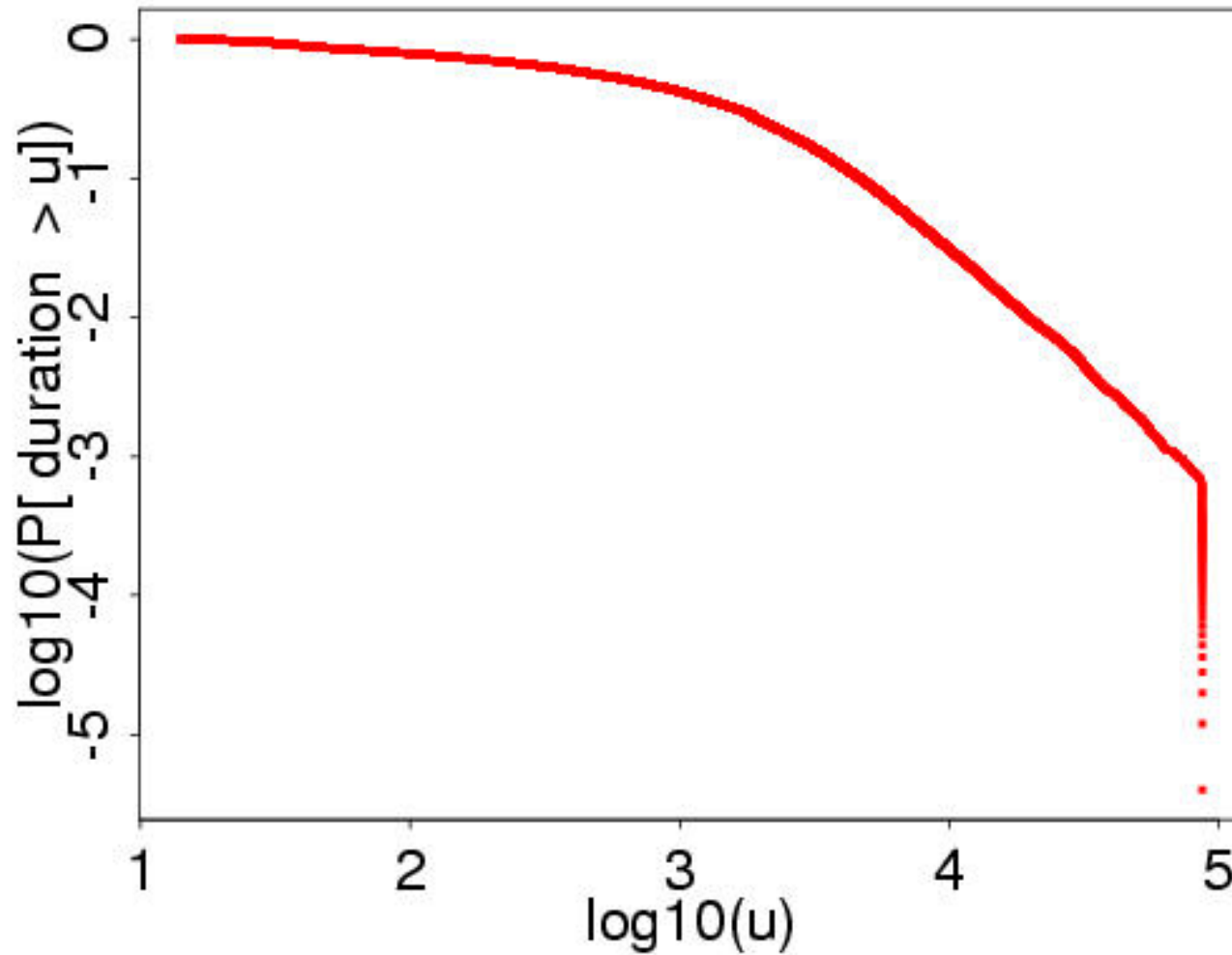
# Detour

## Characteristics of modem calls (~1999)

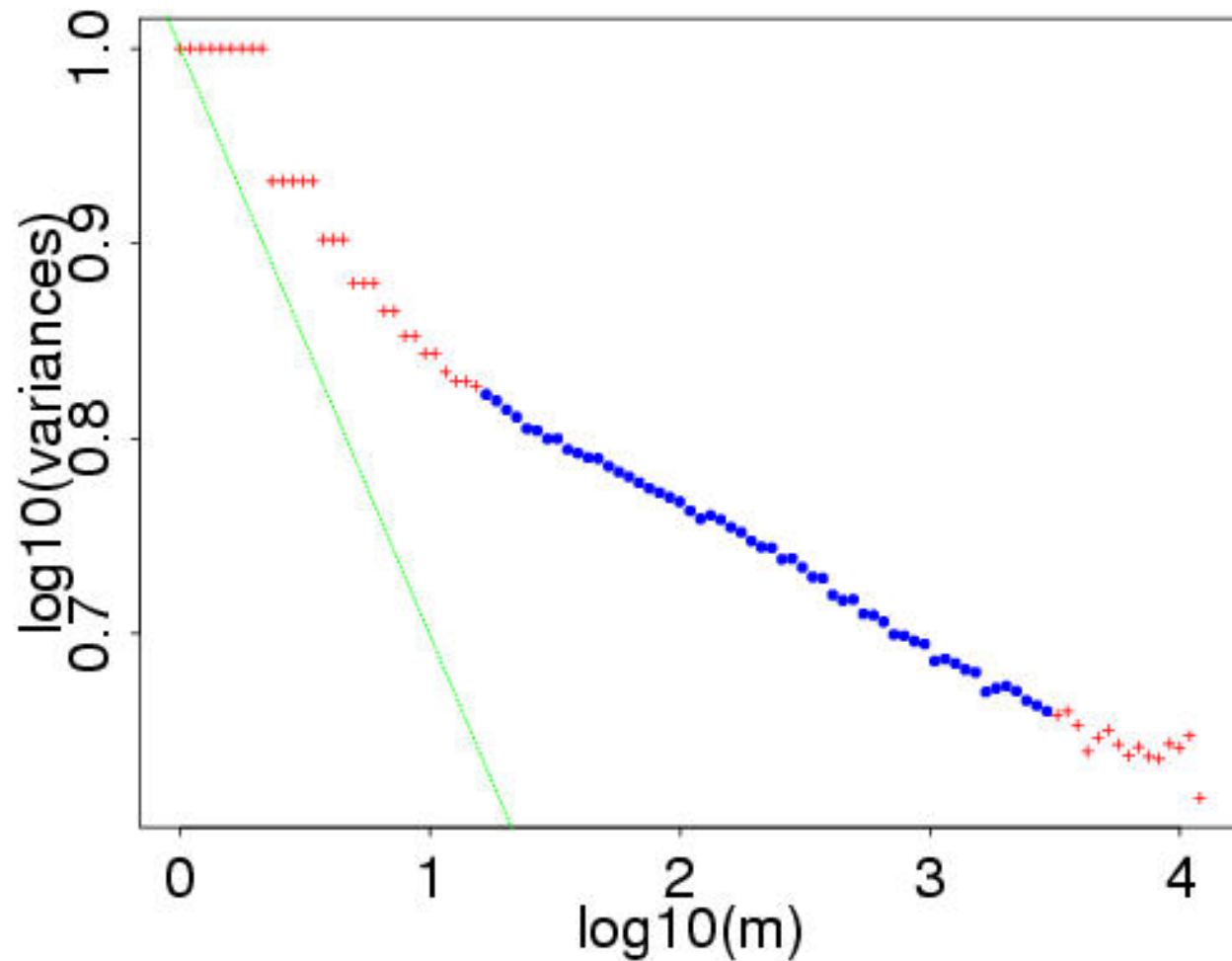
# Interarrival times of modem calls



# Durations of modem calls



# What about packets from modem calls

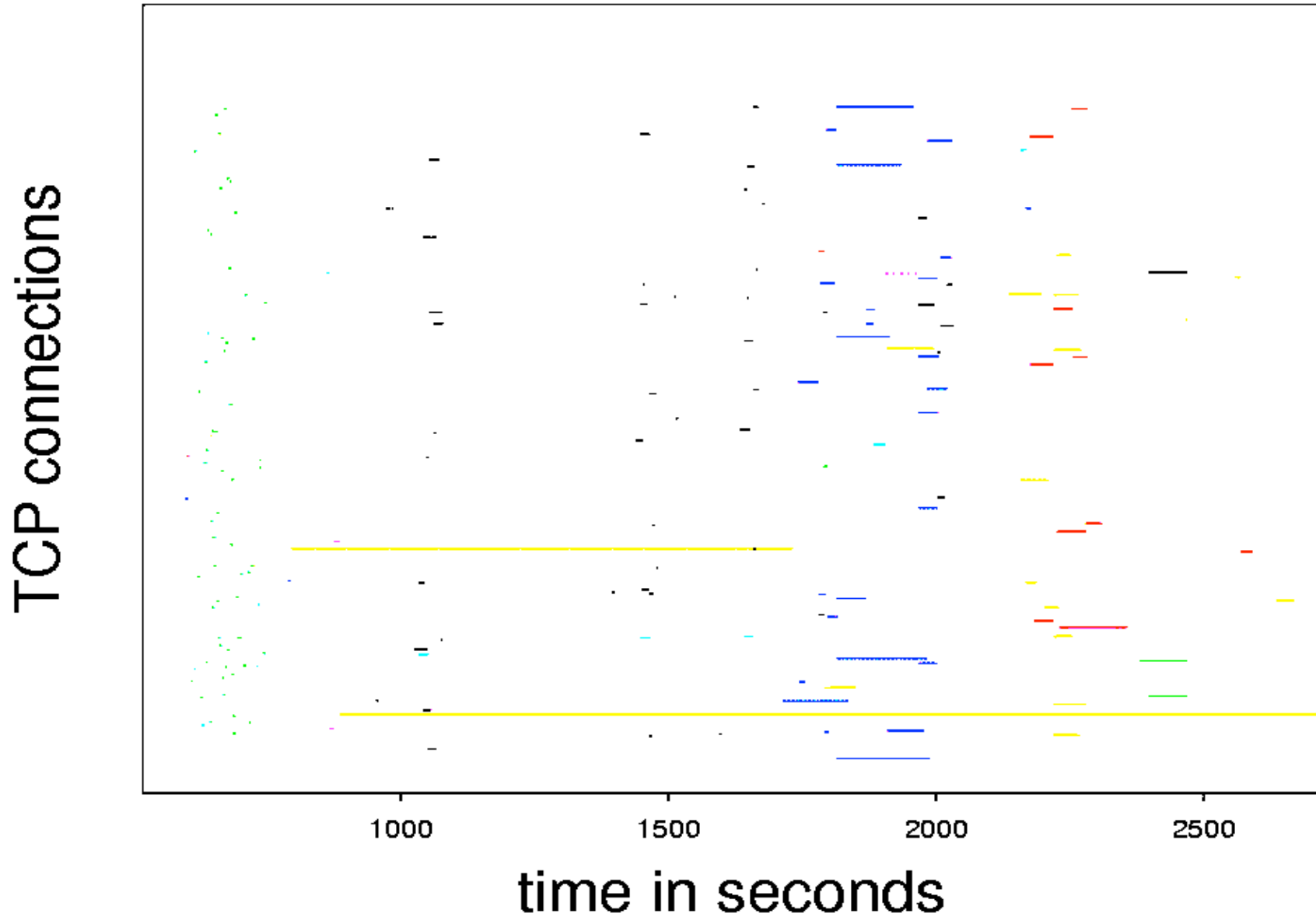




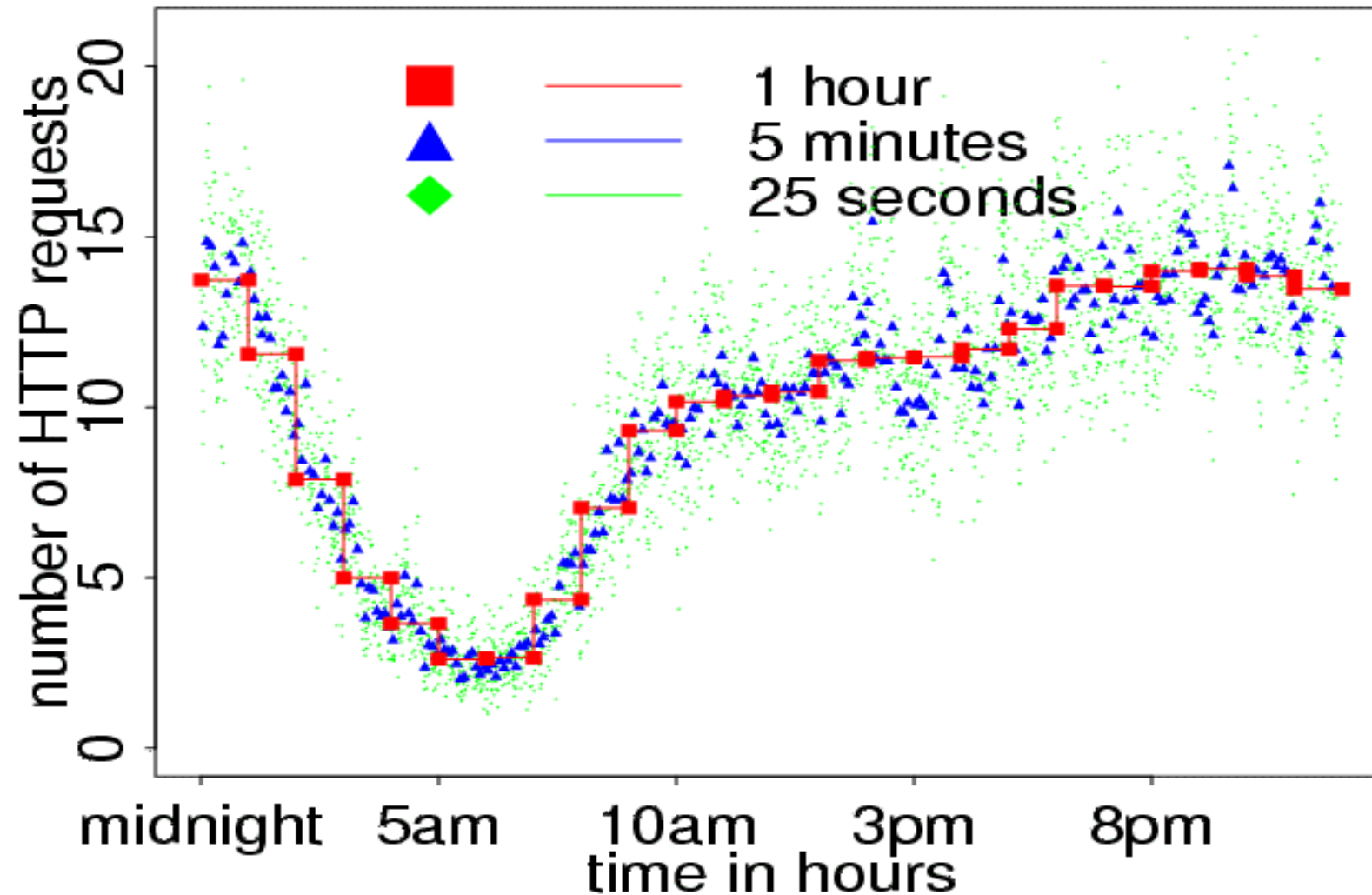
# Detour

## Characteristics of Web (~2000)

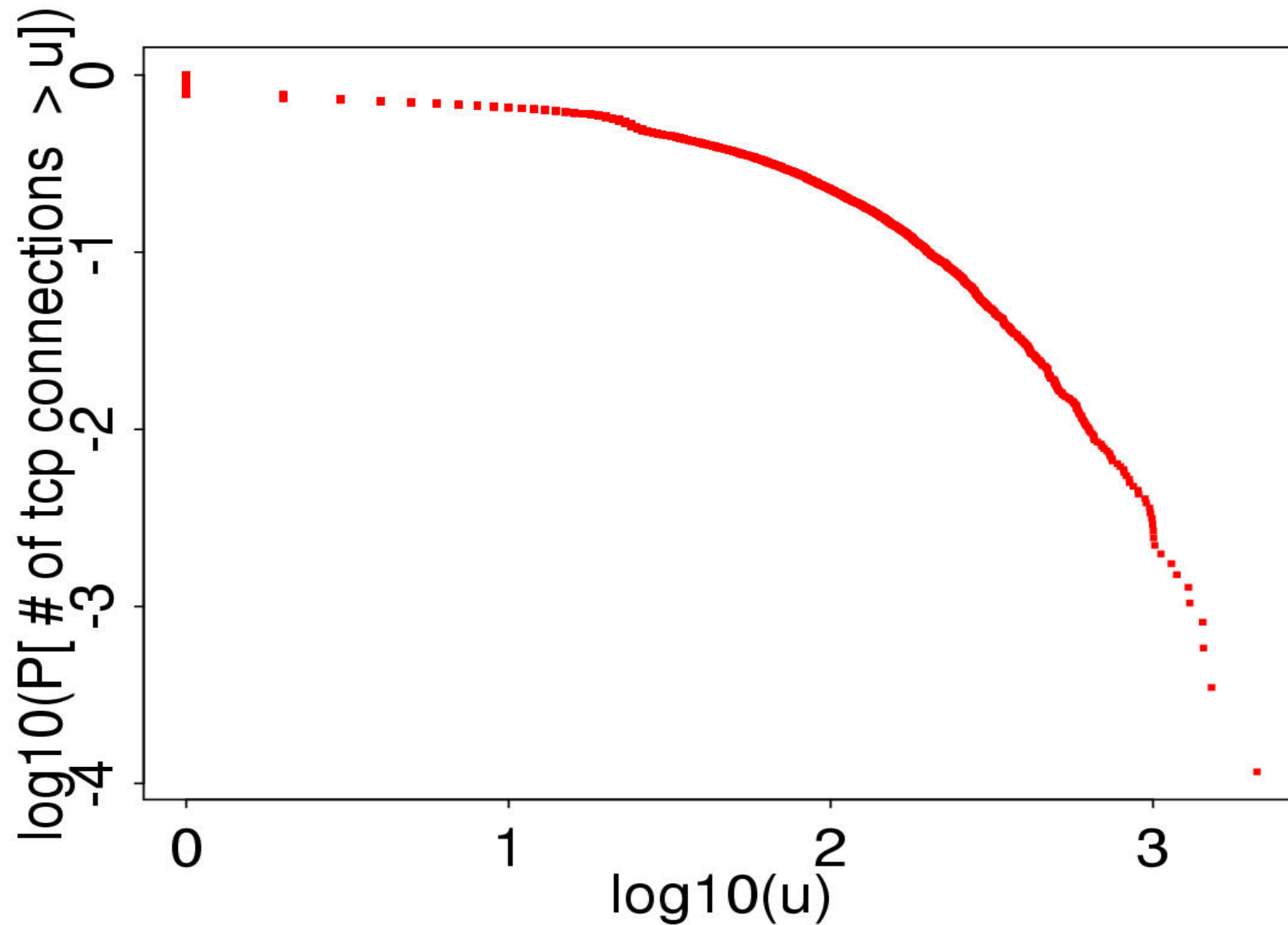
# General characteristics of WWW transfers



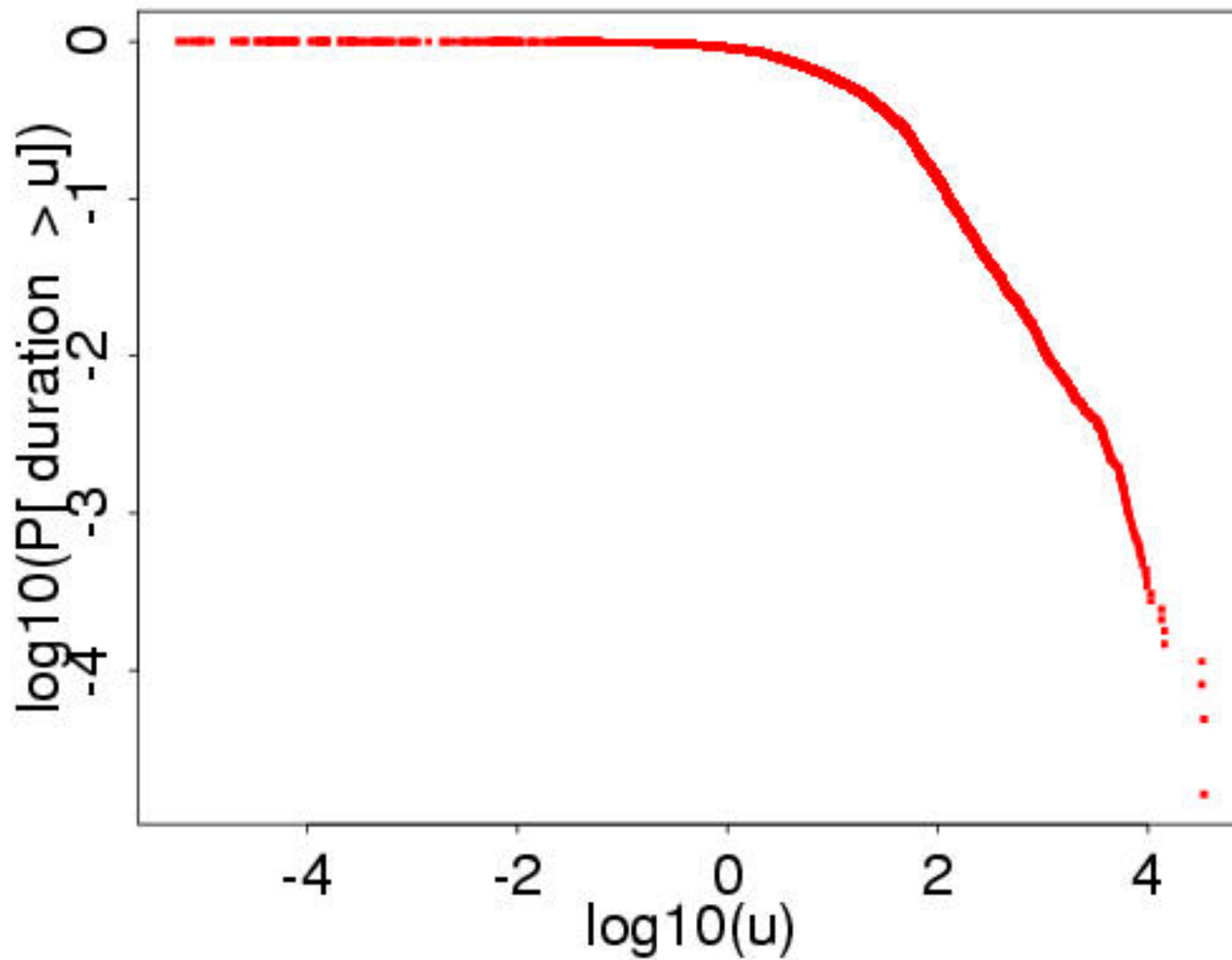
# General characteristics of WWW transfers



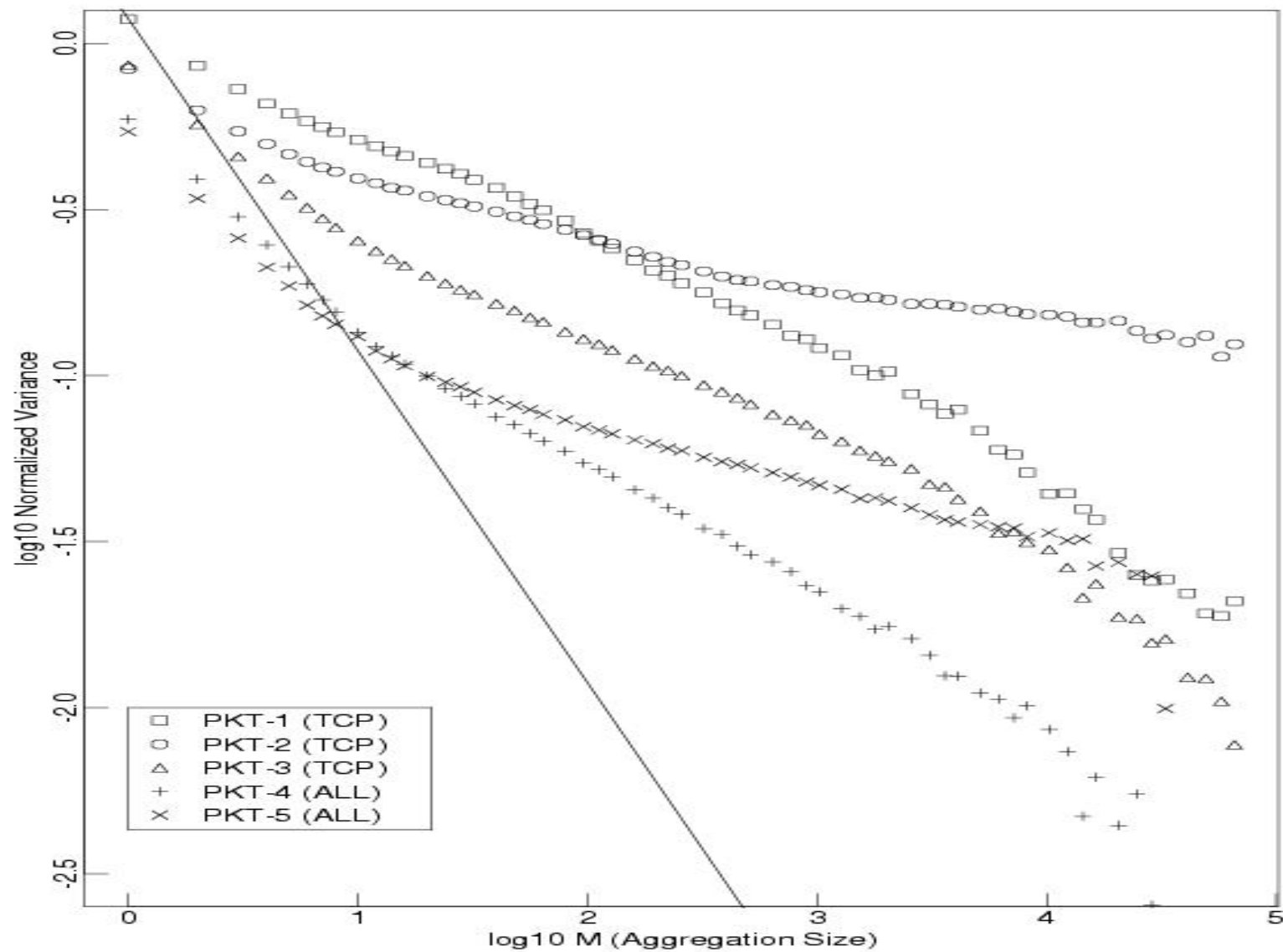
# # of TCP connections per session



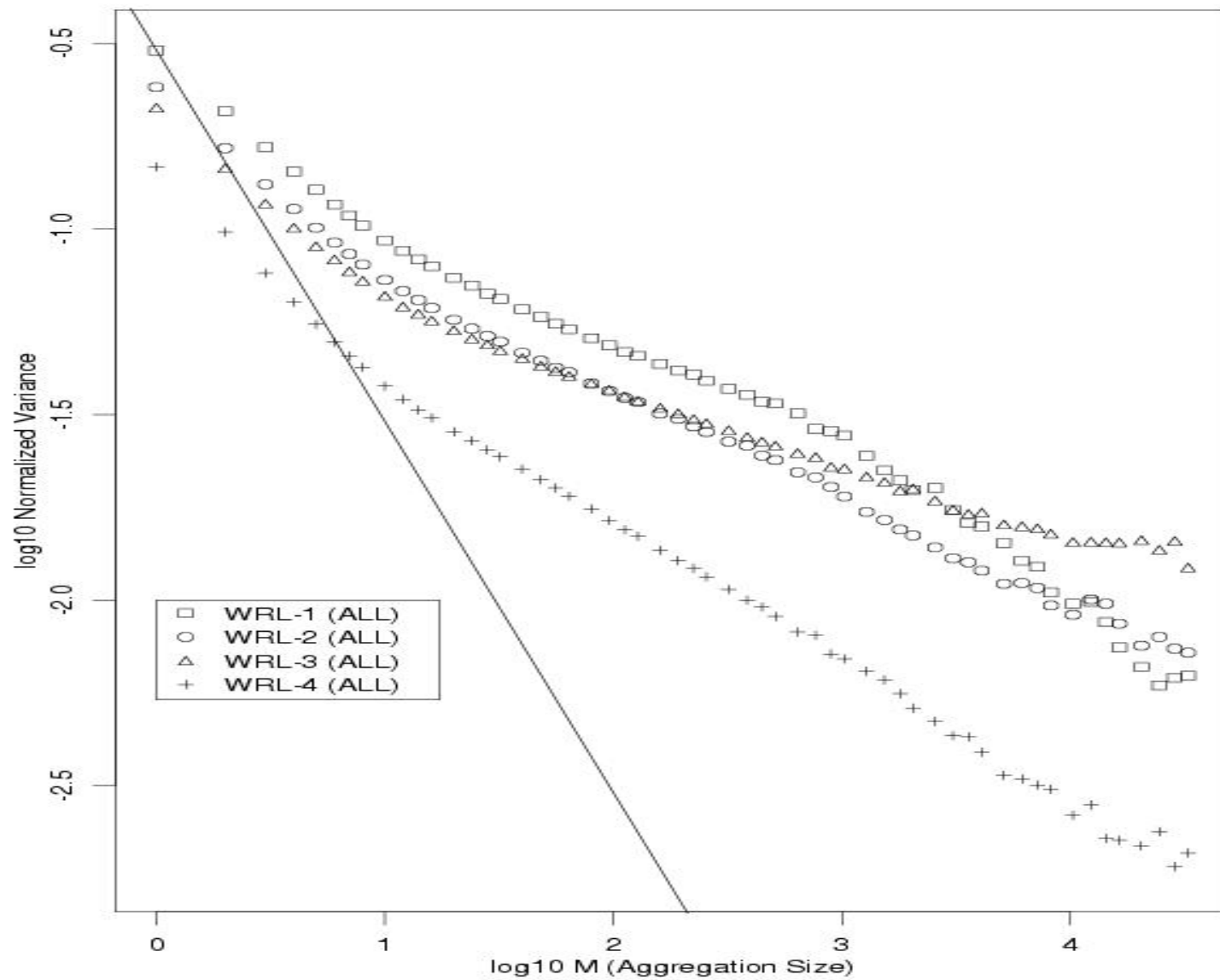
# Flow durations



# Self-similar?



# Self-similar?



# Results

## LAN:

- Superposition of independent ON/OFF sources
- ON/OFF periods are **heavy-tailed** with **infinite variance**

Packets per unit time is **exactly** self-similar

## WAN:

- Sessions arriving in a Poisson manner
- sizes (# packets) are **heavy-tailed** with **infinite variance**

Packets per unit time is **asymptotically** self-similar



# Statistical analysis of WEB

Before Web (1994):

Self-similarity at packets per time unit

- Poisson arrivals at application layer (FTP, Telnet)
- Heavy-tailed session durations/sizes

Since Web (1995)????

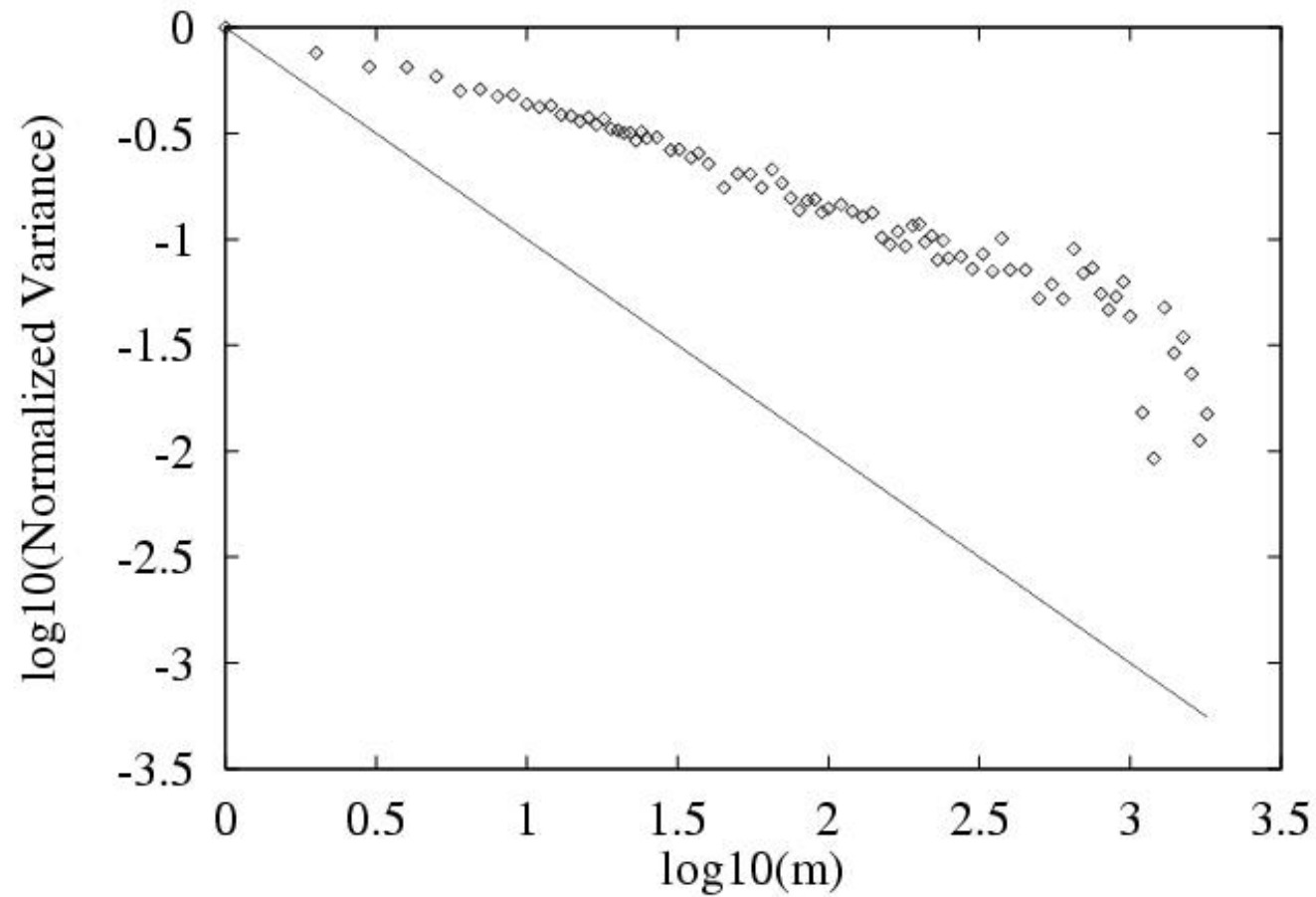
- Arrivals of User session
- # of Web requests per session
- Dist. of # of bytes, pkts, duration per request?

# Web client trace analysis 1995

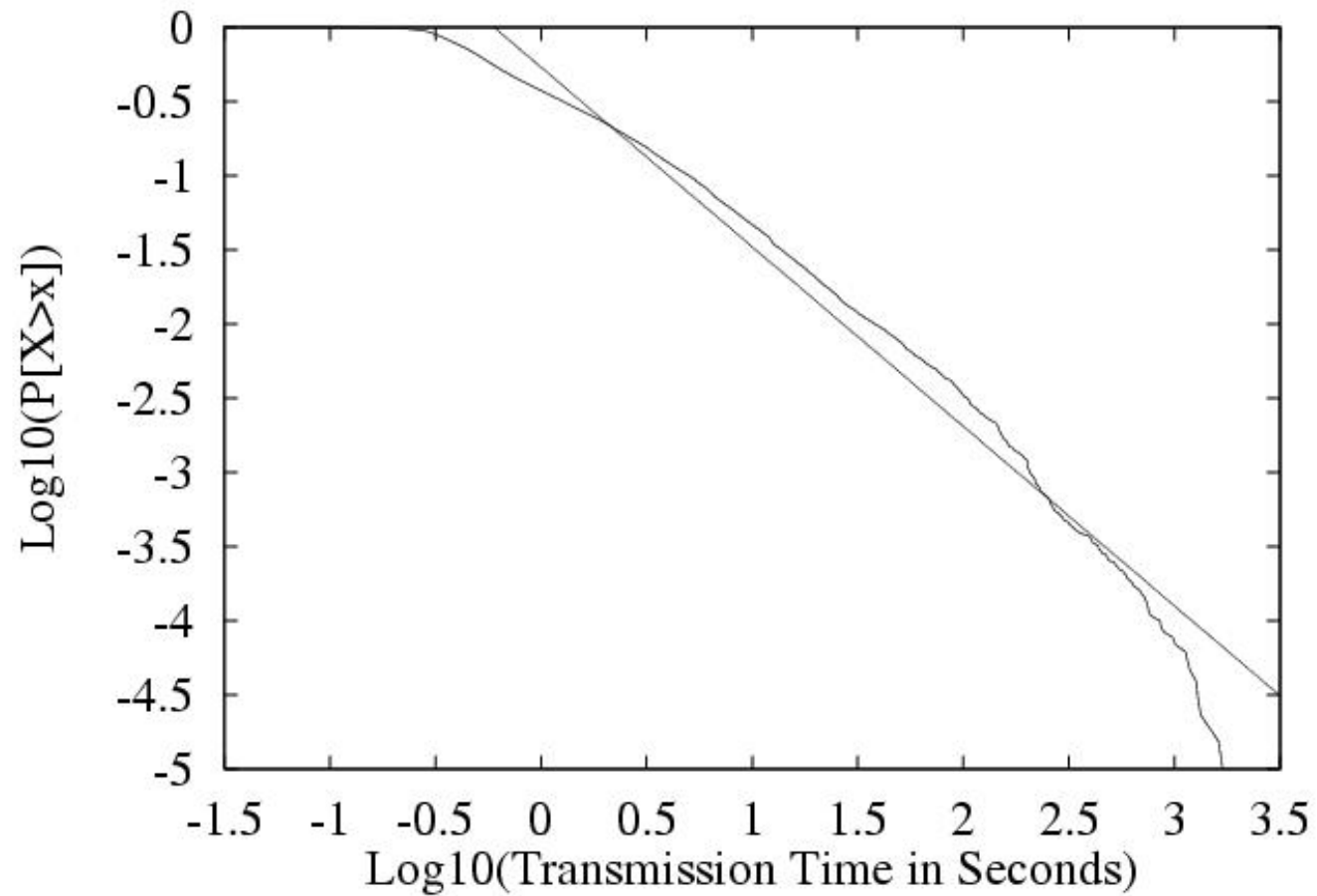
- ❑ Modified Web browser (Mosaic)
- ❑ Population: students at BU
- ❑ Duration: 21 Nov 94 to 8 May 95

Sessions	4,700
Users	591
URLs Requested	575,775
Files Transferred	130,140
Unique Files Requested	46,830
Bytes Requested	2,713 MB
Bytes Transferred	1,849 MB
Unique Bytes Requested	1,088 MB

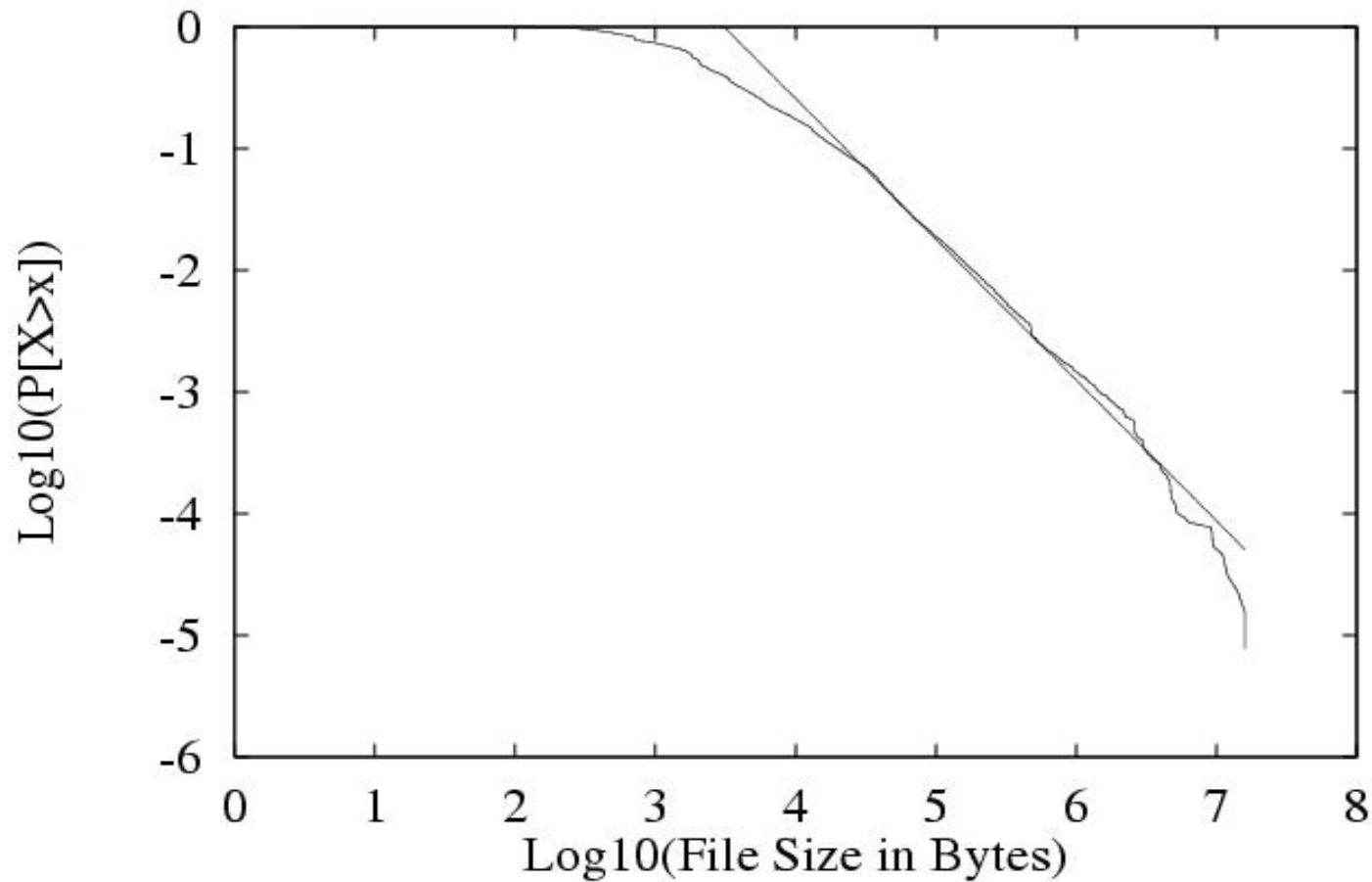
# What about WEB traffic



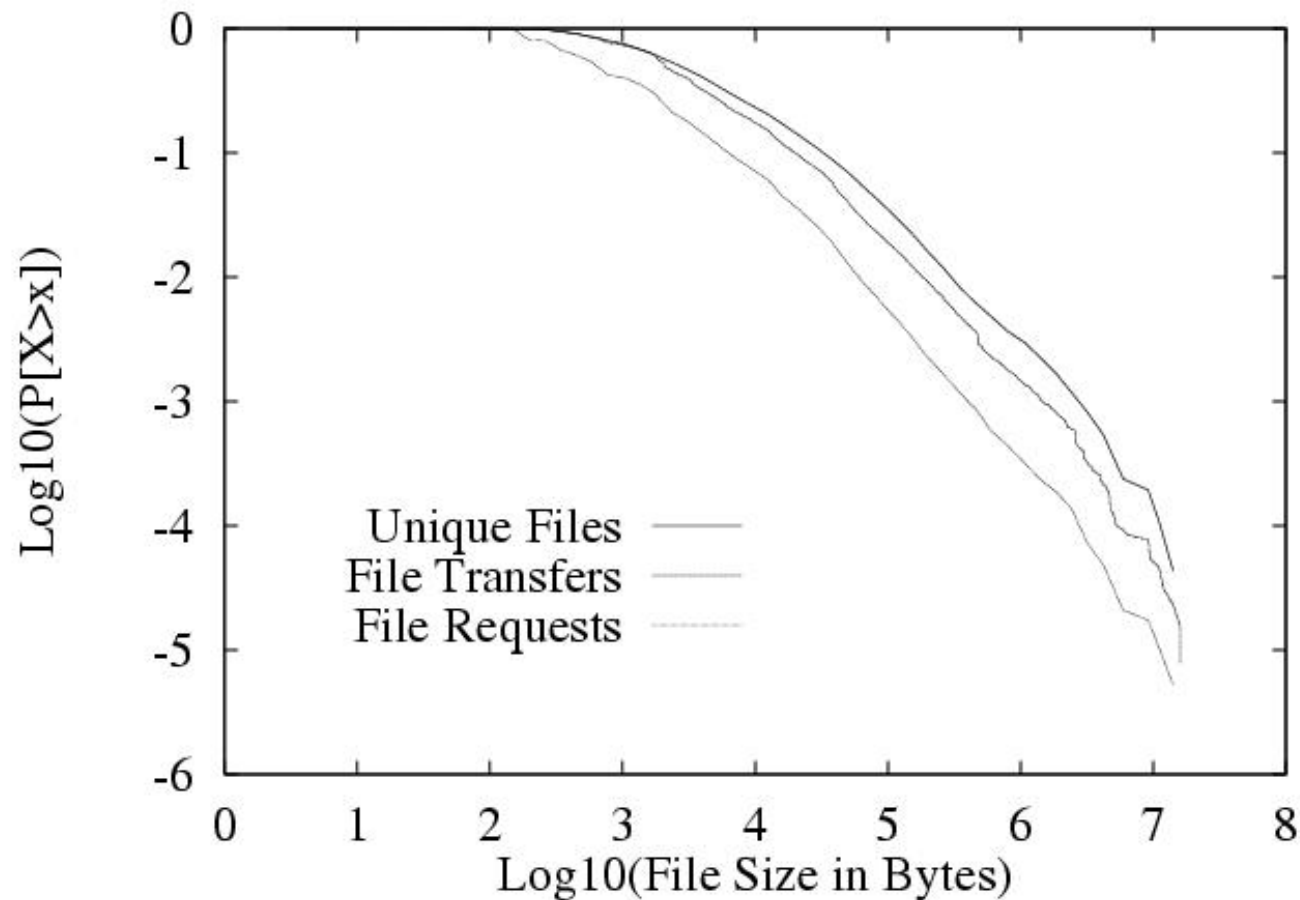
# Durations of WEB transfers???



# File size of WEB transfers???

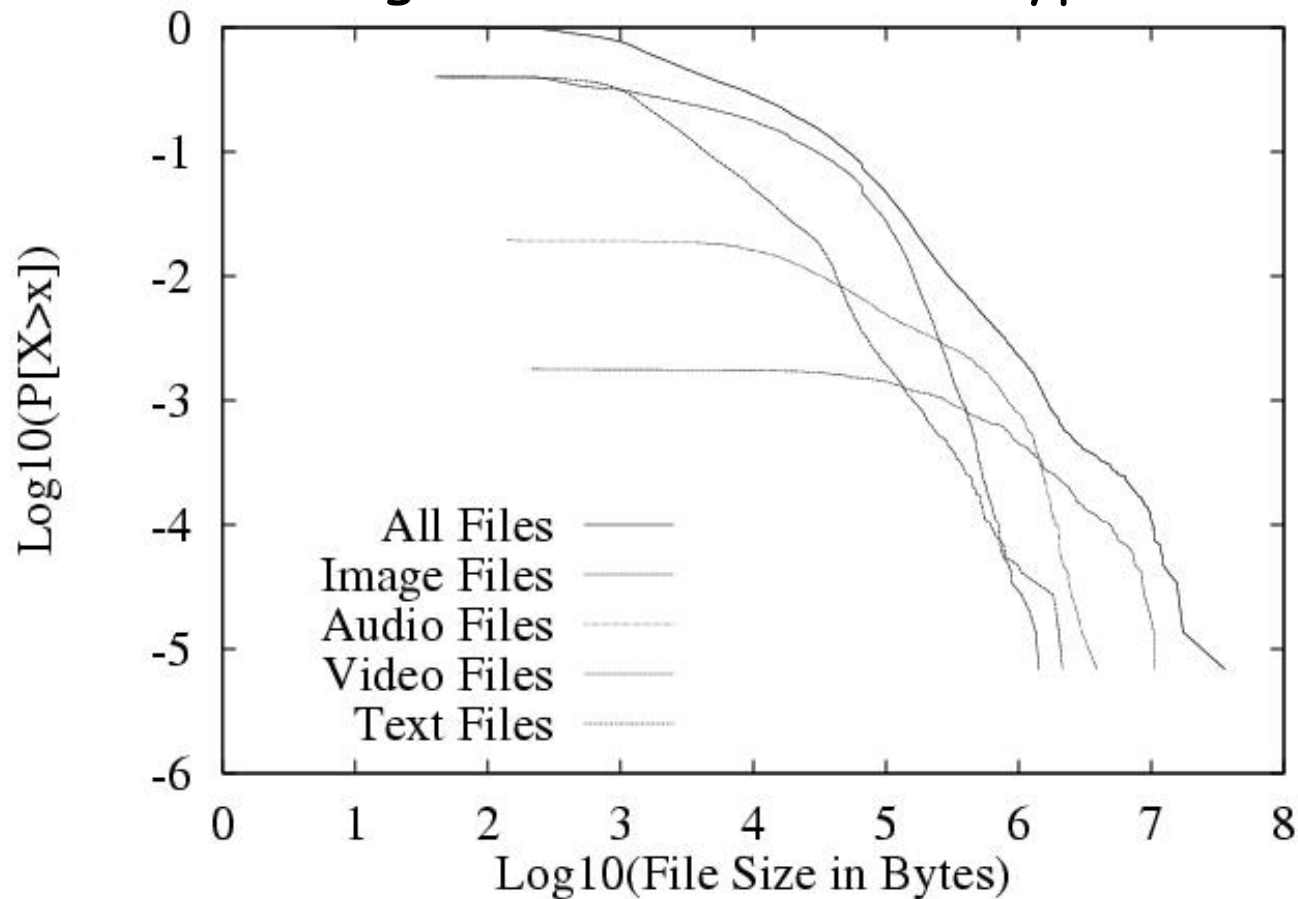


# Unique files vs. files transferred?



# What about the available files?

Long tail due to superposition of heterogeneous filesizes/filetypes



# References

“On the Self-Similar Nature of Ethernet Traffic”

WE Leland, MS Taqqu, W Willinger, DV Wilson,  
SIGCOMM 1993

“Self-similarity in World Wide Web traffic: evidence  
and possible causes”

Mark Crovella and Azer Bestavros

IEEE/ACM Transactions on networking 5 (6), 835-846,  
1997