

3) $C_i \geq 2C_{i+1}$ for $i = 2 \dots n$

The greedy algorithm does not always optimally solve the problem.

Assume a system which satisfies the above but not all valuations are equal integer multiples of each other.

eg: 140, 70, 35, 15, 1

60 would result in 1-35, 1-15, 10-1 12 COINS
 OPTIMAL would be 4-15 4 COINS

the key is when the values is a multiple of a smaller amount which is in turn a multiple of the smallest amount another could be

59, 27, 13, 1

Change for 39 give 27 + 12

Greedy 1-27, 12-1 13 COINS
 OPTIMAL 3-13 3 COINS