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Each Problem is on it's own page

```
(a) (define (listfromTo a b)
1.
               (cond\ ((>\ a\ b)\ '())
                     (else\ (cons\ a\ (listfromTo\ (+\ a\ 1)\ b)))
                     ))
     (b) (define (removeMult a L)
               (cond\ ((null?\ L)\ '())
                     (else
                           (if (= (modulo (car L) a) 0)
                                  (removeMult\ a\ (cdr\ L))
                                  (cons\ (car\ L)\ (removeMult\ a\ (cdr\ L)))
                                  ))))
     (c) (define (sieve n)
               (sieveHelper\ (listfromTo\ 2\ n)))
         (define\ (sieveHelper\ L)
               (cond\ ((null?\ L)\ '())
                     (else\ (cons\ (car\ L)\ (sieveHelper\ (removeMult\ (car\ L)\ (cdr\ L)))))
                     ))
```

- 2. (a) My solution will require 3 pieces of code to be added into the interpreter.
 - (i) Code in my-eval that will recognize calls to **longest**
 - (ii) Function **handle-longest** that is called from my eval and takes all the $(exp_i...result_i)$ pairs in a list
 - (iii) handle-longest-helper That will find the longest *exp* return list and call handle block on the result.
 - (i) This code will be in the my eval and be used to to recognize **longest** and appropriately call **handle-longest**

```
((eq? (car \ exp) 'longest) 
(handle - longest (cddr \ exp) \ env))
```

(ii) This handle-longest will call the helper method, handle-longest-helper that does the bulk of the work. We are giving it an extra empty list. We do the bulk of the work in the helper method because we want an extra parameter that stores the current longest length (expression...result), which is what we pass in as an empty list originally. The first condition is the base case checking if we have anymore remaining Expression Result combos to check, and if we do not, we execute whatever is in LongestER. If the remaining Expression Result list still has elements, we check length and recursively call, updating LongestER with the appropriate value.

```
(define\ (handle-longest\ ERList\ env)\ (handle-longest-helper\ ERList\ ()'\ env)
```

(iii) This **handle-longest-helper** is where the bulk of the work is being done. The first contains the remaining (Exp...result) list that need to be evaluate, and the second argument will always contain the current longest (exp...result) value.

```
 \begin{array}{l} (define \ (handle-longest-helper \ RemainingER \ LongestER \ env) \\ (cond \ ((null? \ RemainingER) \ (my-eval \ (cadr \ LongestEr) \ env)) \\ (else \\ (cond \ ((> \ (length \ (my-eval \ (caar \ RemainingER) \ env)) \\ (length \ (my-eval \ (car \ LongestER) \ env))) \\ (handle-longest-helper \ (cdr \ RemainingER) \ env)) \\ (car \ RemainingER) \ env)) \\ (else \ (handle-longest-helper \ (cdr \ RemainingER) \ LongestER \ env))) \\ ))) \end{array}
```

(b) We are able to use let and cond within our handle-let and our handle-cond because our interpreter is actually using the if, cond, let, etc. functionality of the Scheme interpreter below it. It is not using it's own if, cond, etc.

For example, lets say we have Interpreter A that is interpreting itself, which we will call

Interpreter B. When we see a cond statement within B, we will call A's handle-cond. This A: Handle-Cond will be using the cond of the original scheme interpreter below it, allowing us to use cond in handle-cond.

I love this question, for when I was implementing the Scheme Interpreter, I was a bit confused about this issue, and it was a nice little light bulb when I learned why this was ok.

3. (a) In ML, the reason all lists have to be of the same type is because ML is a statically typed language. This means that all type checking is done at compile time. This means that it is not possible for there to be a run time type error.

If a list has different types within it, and we map a function through every element of an array, we can easily hit a run time type error. To eliminate this case, ML does not allow lists of different types.

- (b) $fun\ foo\ (one)\ (two)\ bar = let\ val\ x = one\ bar in\ two\ x$ end
- (c) The type of the following function is

```
'a -> ('b * 'c -> bool) -> 'b * 'c -> int list -> int list
```

- (d) In order to prove this we have to prove the type of each input.
- **Arg z:** The line where we define Bar, we can see that bar will return either z or a. This means that z and a must be the same type. The next line we pass [1,2,3], into bar as a. We know that [1,2,3] is explicitly type $int\ list$. We are passing in this $int\ list$ into bar, so now we know that a is an $int\ list$. Because a's type and z's type is the same, and a's type is $int\ list$, we can now deduce that z's type is $int\ list$
- **Arg f:** We never use argument f, we f can store anything, meaning that it is polymorphic. When organizing arguments left to right, this is the first polymorphic item we see, it is labeled as 'a
- **Arg** (x,y): All we do with these two variables is we pass them into another function that is another of foo's arguments. Because passing them into another function gives us no more information on the type that x and y are, we know that they are polymorphic. They also have nothing to do with argument f at all, so they do not get the same lettering as f. a' is already taken so (x,y) get b'c
- **Arg** (op >): In the definition of bar, we see that whatever is returned from the (op >) is used in an if statement. This means that it's return type must be a boolean. The (op >) is also being used between argument x and y, which we previously deduced were type 'b and 'c respectively. This means that (op >) will be of type (b* c) bool

4. (a) This would not be an **ADT** for a stack because with this implementation, you cannot declare an object of queue. This is because currently queue is in a package.

It is now possible to to declare a type queue.

5. (a) In order to be an Object Oriented Language the three elements you need are Encapsulation, Inheritance, Subtyping with dynamic dispatch

(i) Encapsulation:

We have to be able to encapsulate data and code into **objects** In java we have Methods and instance variables. In C++ we have Data members and member functions. Abstract Data types are also a good indicator of encapsulation. Abstract Data types have visible parts and non visible parts. Abstract Data types also have procedures that you can call.

(ii) Inheritance:

This means that we do not have to re-write code. Code for one type can be re-used with another type

(iii) Subtyping with dynamic dispatch

This refers to the ability to treat one class as if it were another type. Type B is a subtype of A if all the values in A are also in B.

- (b) (i) Subset interpretation of subtyping is saying that if B <: A, then every value of type B is also of type A. More specifically, if B <: A, then we can treat type B as if it was a type A.
 - (ii) Class derivation in Java satisfies the subset interpretation of subtyping because if we have a Class A and Class B, and B <: A, then we can use class B whenever we are expecting a Class A. This shows that subtying of classes is Covariant. Here is an example.

Lets say we can an Animal class, and we have a Dog class. As we know, a dog is an animal, and should have all the same functionality of all animals. We can then make the Dog class Extend the Animal class, so now Dog <: Animal. This means that if we have a function that takes in an object of the class Animal, we can now give that function an object of the class Dog instead.

(iii) Functions in Scala satisfy the subset interpretation of subtyping this way. If B <: A and D <: C, then $A \to D <: B \to C$. This means that We are Contravarient on the Input Types and Covarient on the output types.

If we have Classes, Bat <: Animal and Dodge <: Car, then we have $Animal \rightarrow Dodge <: Bat \rightarrow Car$

As for the Contravarient input type, here is an explanation. Lets say we have a function foo that takes in our $Bat \rightarrow Car$ function, creates a new Bat and runs our Bat through the $Bat \rightarrow Car$ function. Now we get the output Car easy peasy.

Now lets imaging passing in the Animal $\rightarrow Dodge$ function into foo instead. If we

do that, now we pass the created Bat into the Animal o Dodge function, which we know is ok. When it comes to inputs of functions being contravarient, it helps to think of it this way. If we have Dog <: Animal, we know that Dog contains all the information of Animal and anything that is a supertype of Animal. That means that if a function can safely operate on all values within a dog, we know that this function can easily operate on Animal and other supertypes because dog already contains that information.

As for the return type of Covariance, this is the simple example. We have already established that in part (ii). We know that the return value from the function will just be a single value, and single variables act the same as Java classes. Subtypes of a single value can be used in place of a supertype, meaning return values act with Covariance.

```
(c) def maxTree[T <: Ordered](t: Tree[T <: Ordered[T]]) {</pre>
       t match {
         case Node(v,1,r) =>
              val maxL = maxTree(1);
              val maxR = maxTree(r);
              if (maxL < maxR)
              {
                  max = maxR;
              }
              else
              {
                  max = maxL;
              }
              if (max < v)
              {
                  max = v;
              }
              max
         case Leaf(v) => v;
         case Empty() => ();
       }
```

(d) Solution on next page in order to not break up code

```
(d) (i) Class A {...}
       Class B extends A { ...}
       void foo (ArrayList<A> a)
           A c = new A();
           a.add (c);
       }
       ArrayList<A> x = new ArrayList<A>();
       ArrayList<B> y = new ArrayList<B>();
       foo(y); // Now ArrayList<A> an element of type B, which is not appropriate
   (ii) void foo (ArrayList<? super B> b)
           B c = new B();
           b.add (c);
       }
       ArrayList<A> x = new ArrayList<A>();
       ArrayList<B> y = new ArrayList<B>();
       foo(x);
(e) (i) class E[+T] (val bar: T){
           val baz = bar;
           def get = baz;
       }
```

(ii) Code on new page to avoid a break in code

```
(ii) class A {
          val x = 12;
      }
      class B extends A {
          val y = 21;
      class E[+T] (val bar: T){
          val baz = bar;
          def get = baz;
      }
      def main(args: Array[String]) {
          val b: B = new B();
          val bb: Foo = new Foo(b);
          val a: A = new A();
          val aa: Foo = new Foo(a);
          aa = bb;
          // With generics we are now using
          // type b when an A is expected
          // This is covariance at work
(f) (i) class E[-T] (val bar: List[T]){
          val foo: T = new T();
          val listT = bar + foo;
          bar = bar + foo;
          def get listT;
      }
```

(ii) On new page to avoid code break