

left ~~right~~ $j=0$

2	6	12	13	21
0	1	2	3	4
x	x	x	x	j

count=0

$j=0$

right

4	5	7	9	10	11
0	1	2	3	4	5
x	x	x	x	x	j

2 > 2x4 (X) ⁽²⁾ (i++) ⁽¹⁾ count = count + j = 0 + 0 = 0

6 > 2x4 (X) (i++) count = count + j = 0 + 0 = 0

12 > 2x4 (✓) (j++)

12 > 2x5 (✓) (j++)

12 > 2x7 (X) ⁽³⁾ (i++) ⁽¹⁾ count = count + j = 0 + 2 = 2

13 > 2x7 (X) ⁽²⁾ (i++) ⁽¹⁾ count = count + j = 2 + 2 = 4

21 > 2x7 (✓) (j++)

21 > 2x9 (✓) (j++)

21 > 2x10 (✓) (j++)

21 > 2x11 (X) ⁽²⁾ (i++) ⁽¹⁾ count = count + j = 4 + 5 = 9

int j=0, count=0;

for (int i=0; i < left.length; i++) {

while (j < right.length && left[i] > 2 * right[j]) {

j++;

count = count + j;

}

Now, the above question converted in terms of p, q, n like merge (during merge sort)

p				q
2	6	12	13	21

q+1					n
4	5	7	9	10	11
	6	7	8	9	10

index

i = p (start)

j = q+1 (start)

int j = q + 1, count = 0

for(int i = p; i <= q; i++) {

while(j <= r && ~~right~~ left[i] > 2 * right[j]) {
j++;

}

count = count + (j - (q + 1));

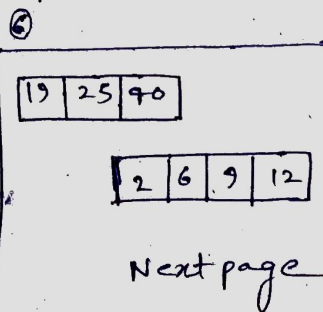
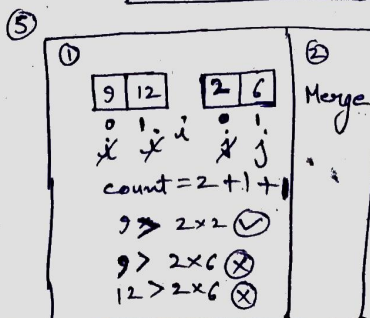
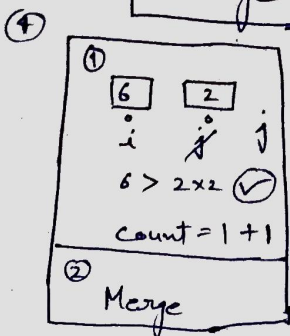
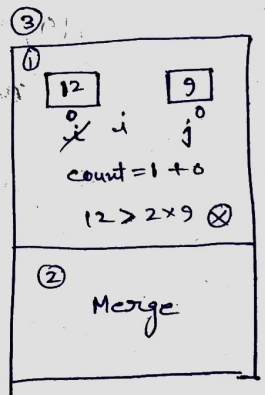
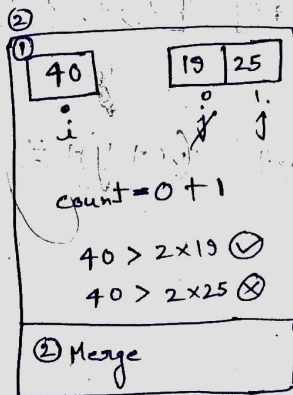
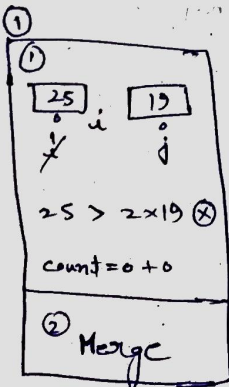
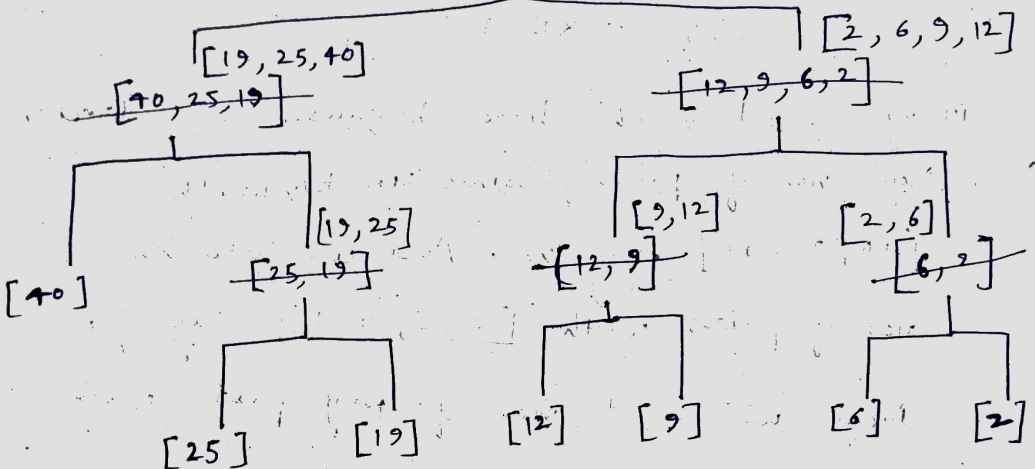
}

Now, we have an array:

40	25	19	12	9	6	2
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Merge Sort

[40, 25, 19, 12, 9, 6, 2]



19	25	40
----	----	----

0 1 2 i
~~j~~ ~~j~~ ~~j~~ i

2	6	9	12
---	---	---	----

0 1 2 3 j
~~j~~ ~~j~~ ~~j~~ ~~j~~ j

$$\text{count} = 4 + 3 + 4 + 4 = 15$$

$$19 > 2 \times 2 \quad \checkmark$$

$$19 > 2 \times 6 \quad \checkmark$$

$$19 > 2 \times 9 \quad \checkmark$$

$$19 > 2 \times 12 \quad \times$$

$$25 > 2 \times 12 \quad \checkmark$$

Merge Sort works here because we already know no. of pairs possible in ~~19~~ with [19, 25, 40] say x. And we also know no. of pairs with [2, 6, 9, 12] say y.

Now, we want no. of ~~pair~~ pairs with

[19, 25, 40] [2, 6, 9, 12] say z

$$\text{So, count} = (x + y) + z$$

Length of left sorted array

Length of right sorted array

Time Complexity for our countReversePair() method = $O(n_1 + n_2) = O(n)$

So, total time complexity = $O(\log n) * (O(n) + O(n_1 + n_2)) = O(\log n) * (O(n) + O(n))$

$T = O(\log(n)) * O(2n)$

$T = O(n * \log(n))$

Merge

CountReversePair Method