

Sort an array of 0's, 1's and 2's

Brute force

0	2	1	1	0	0	1	2	0	2	1	2	2	0	0
0	1	2	3	4	5	6	7	8	9	10	11	12		

1) Step:

$$\left. \begin{array}{l} \text{count0} = \cancel{0} \cancel{1} \cancel{2} \cancel{3} \cancel{4} \cancel{5} 6 \\ \text{count1} = \cancel{0} \cancel{1} \cancel{2} \cancel{3} 4 \\ \text{count2} = \cancel{0} \cancel{1} \cancel{2} \cancel{3} \cancel{4} 5 \end{array} \right\} \begin{array}{l} O(n) \\ \text{(one traversal)} \\ \text{(first time)} \end{array}$$

2) Step: Modify the given array and 6 0's followed by 4 1's followed by 5 2's.

0	0	0	0	0	0	1	1	1	1	2	2	2	2	2
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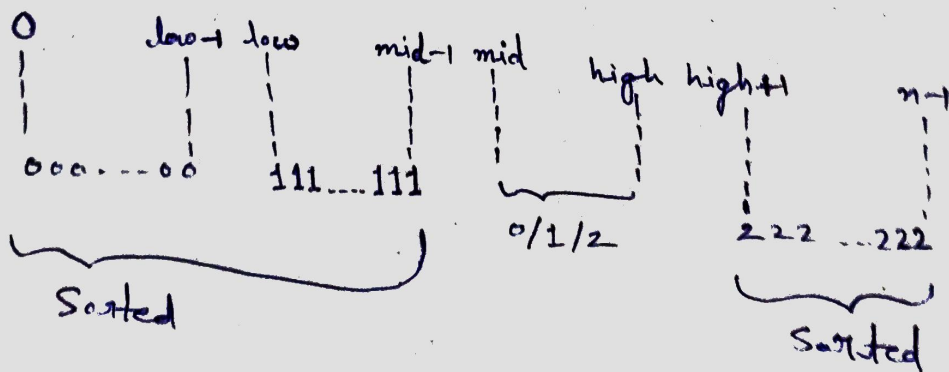
It will also take $O(n)$

$$\begin{aligned} \text{So, Total } T &= O(n) + O(n) \\ &= O(2n) \\ S &= O(1) \end{aligned}$$

Optimal

We will be using DNF algorithm

↓
Dutch National Flag Algorithm



conditions

```
{ if (a[mid] == 0) {  
    swap(a[low], a[mid]);  
    low = low + 1;  
    mid = mid + 1;  
} else if (a[mid] == 1) {  
    mid = mid + 1;  
}  
else if (a[mid] == 2) {  
    swap(a[mid], a[high]);  
    high = high - 1;  
}  
}  
→ Repeat this till (mid > high)
```