



# HE386: MID-TERM PRESENTATION

---

CHERENKOV DETECTORS AND TRANSITION RADIATION

Aman Sahoo, UG 3<sup>rd</sup> Year

# Types of Particle-Matter Interactions

## 1. Ionization (or excitation) of detector material

- The incoming particle loses energy by ionizing or exciting the atoms

## 2. Interaction with the nucleus

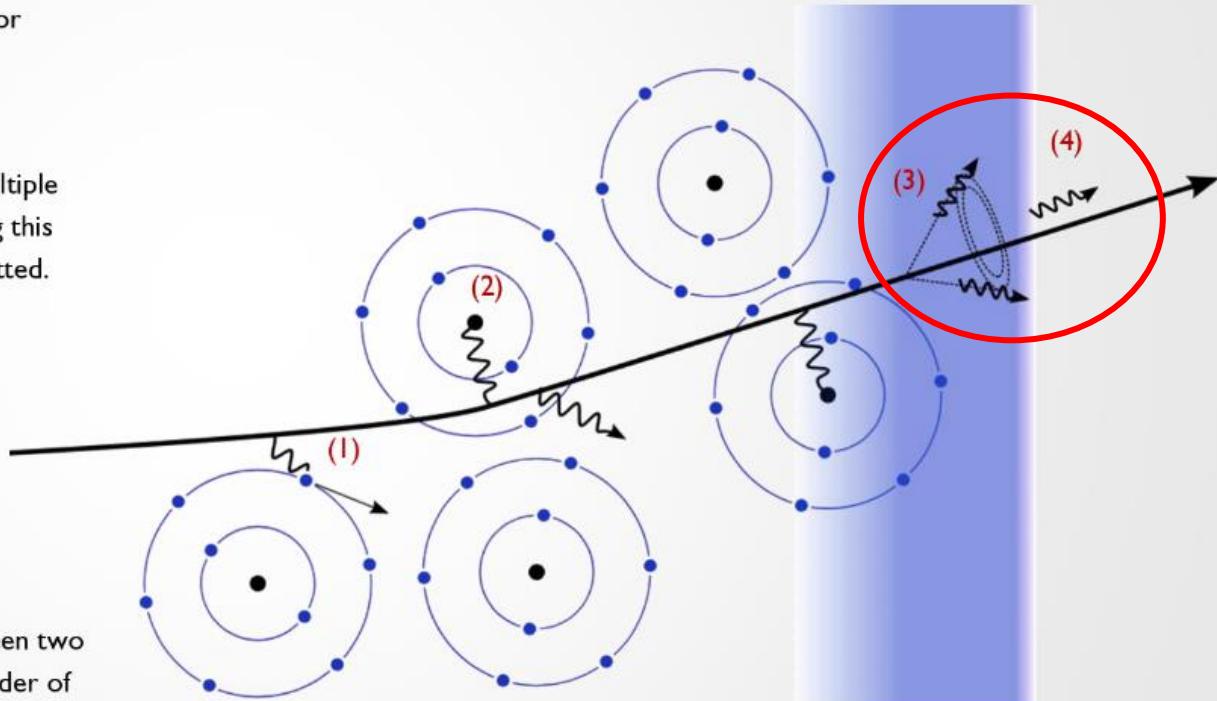
- The particle is deflected (scattered) causing multiple scattering of the particle in the material. During this scattering a **bremsstrahlung** photon can be emitted.

## 3. Emission of Cherenkov light

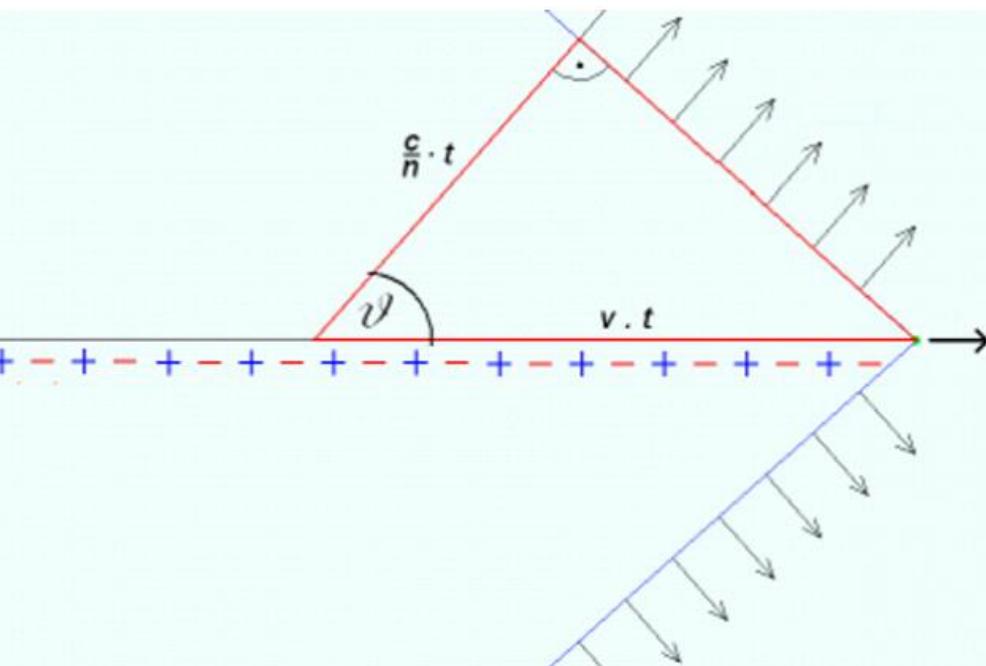
- In case the particle's velocity is larger than the velocity of light in the medium, the resulting EM shockwave manifests itself as Cherenkov Radiation.

## 4. Emission of transition radiation

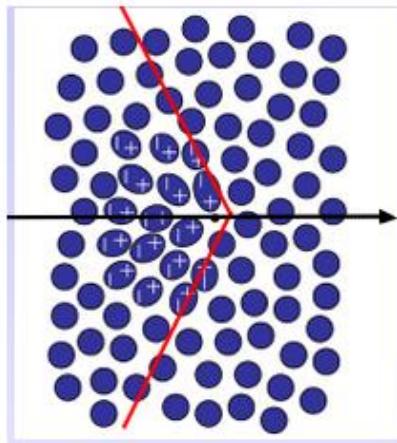
- When the particle crosses the boundary between two refractive media, there is a probability of the order of  $\approx 1\%$  to produce an X ray photon, called Transition radiation.



# Cherenkov Radiation



- Applicable to charged and massive particles only
- Speed of light in dielectric medium:  $c_n = \frac{c}{n}$ ; where  $n > 1$
- For  $v_p < c_n$ , wavefronts do not interact.
- Excitation radiation like normal
- For  $v_p > c_n$ , wavefronts cross each other and produce interference
- Constructive interference causes Cherenkov radiation

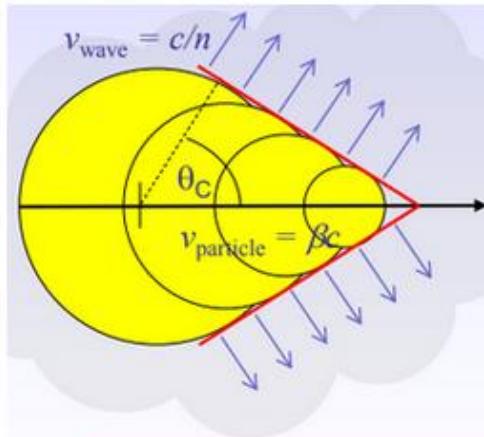


The dielectric medium is polarized by the passing particle.

Jackson, John David (1999). Classical electrodynamics (3rd ed.)

$$v_{\text{particle}} \geq c_{\text{medium}} = \frac{c}{n}$$

$$\beta_{\text{particle}} \geq \frac{1}{n} \quad (n = \text{refr. index})$$



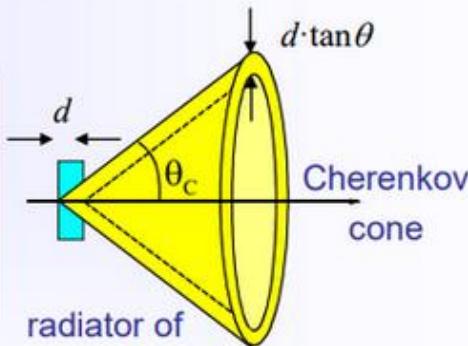
$$\cos \theta_C = \frac{v_{\text{wave}}}{v_{\text{particle}}} = \frac{1}{n\beta}$$

with  $n = n(\lambda) \geq 1$

$$\frac{d^2N}{dxd\lambda} = \frac{4\pi^2 z^2 e^2}{hc\lambda^2} \left(1 - \frac{1}{n^2\beta^2}\right) \text{ limited thickness}$$

$$\beta_{\text{thr}} = \frac{1}{n} \rightarrow \theta_C \approx 0 \quad \text{Cherenkov threshold}$$

$$\theta_{\text{max}} = \arccos \frac{1}{n} \quad \text{'saturated' angle } (\beta=1)$$



## Components of a Cherenkov Detector

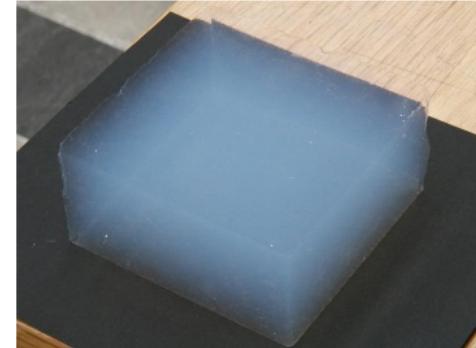
- Main Components:
  - Radiator : To produce photons
  - Mirror/lens/quartz bar etc. : To help with the transport of photons
  - Photon detector : To detect the photons

➤ Radiator: Any medium with a Refractive Index.

### Example of radiators

Medium	n-1	$\gamma_{th}$	Photons/m
He (STP)	$3.5 \cdot 10^{-5}$	120	3
CO <sub>2</sub> (STP)	$4.1 \cdot 10^{-4}$	35	40
Silica aerogel	0.025-0.075	4.6-2.7	2400-6600
water	0.33	1.52	21300
Glass	0.46-0.75	1.37-1.22	26100-33100

Aerogel: network of  
SiO<sub>2</sub> nano-crystals



$$\gamma = 1/\sqrt{1 - \beta^2}$$

## Cherenkov detectors can exploit ...

1

$N_{ph}(\beta)$  → Threshold detector. Do not measure  $\theta_C$

2

$\theta(\beta)$  → Ring Imaging Cherenkov detectors “RICH”

→ Detection of Internally reflected Cherenkov light “DIRC”.

} Measure  $\theta_C$

Knowing both the speed  $\beta = v/c$  and the momentum  $p$  of the particle allows to derive the mass of the particle and hence identify it (e.g.  $\pi$ ,  $K$ ,  $p$ ,  $d$ ,...).

Particle ID.

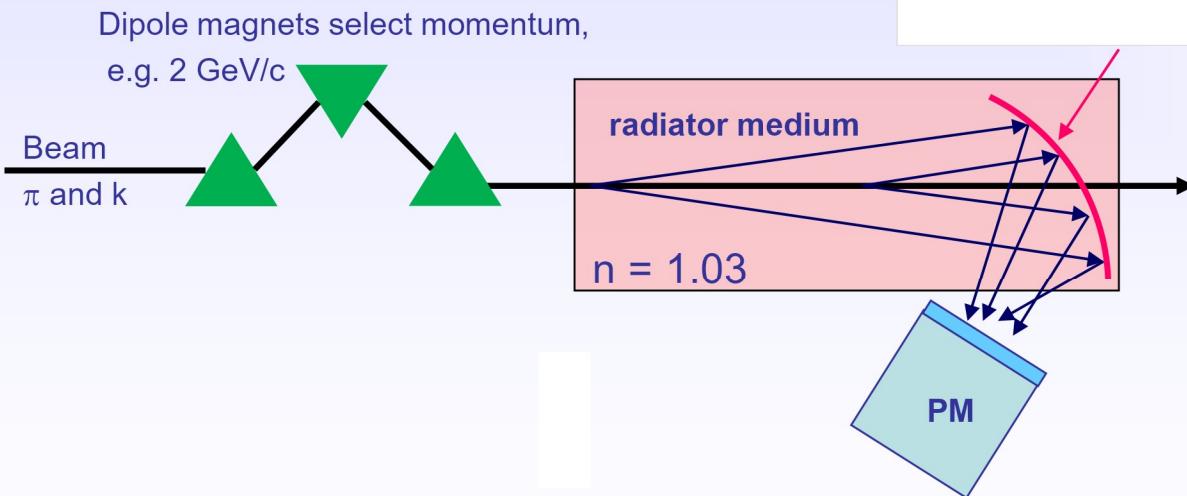
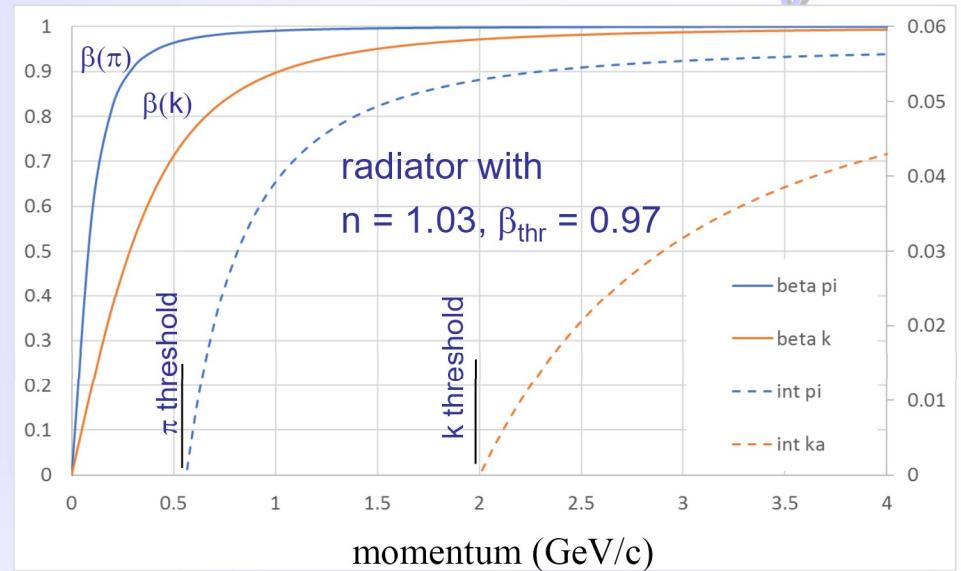
3

Prompt emission of Cherenkov light (different from scintillation) plus angular information → very fast timing detectors. TOP, TORCH

## Threshold Cherenkov detectors

$$N_{ph} \approx 1 - \frac{1}{n^2 \beta^2} = 1 - \frac{1}{n^2} \cdot \left(1 + m^2 / p^2\right)$$

Often used in secondary beamlines (e.g. CERN PS, SPS) to tag particle type



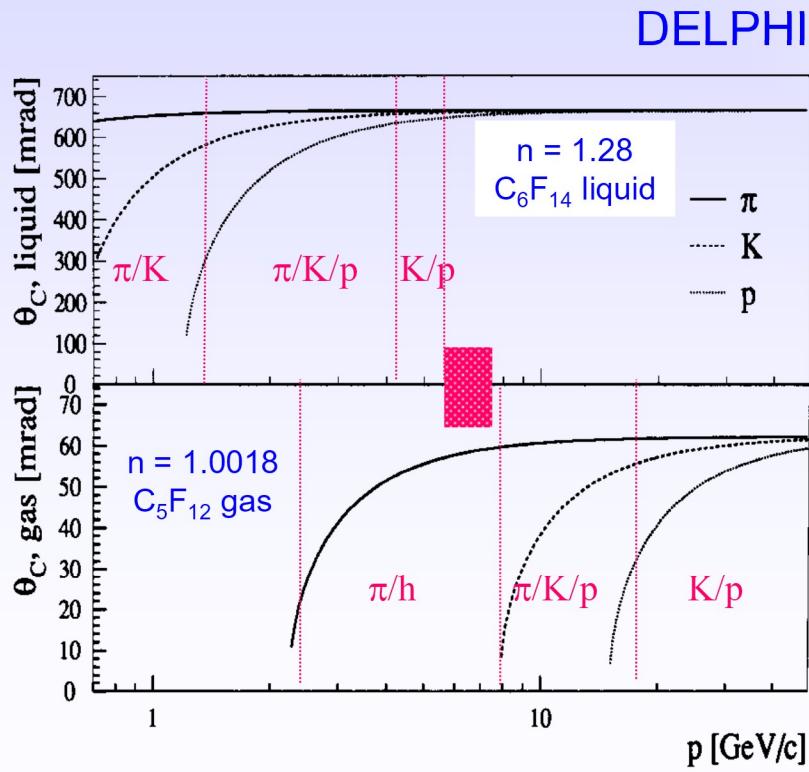
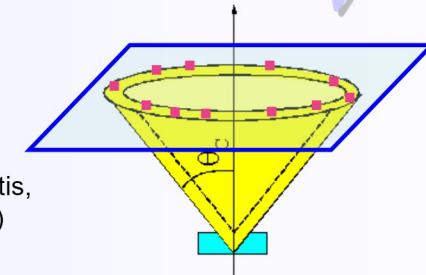
Principle of a simple in-beam threshold Cherenkov counter

RICH detectors determine  $\theta_C$  by intersecting the Cherenkov cone with a photosensitive plane

→ requires **large area photosensitive detectors**, e.g.

- wire chambers with photosensitive detector gas
- PMT arrays

(J. Seguinot, T. Ypsilantis,  
NIM 142 (1977) 377)



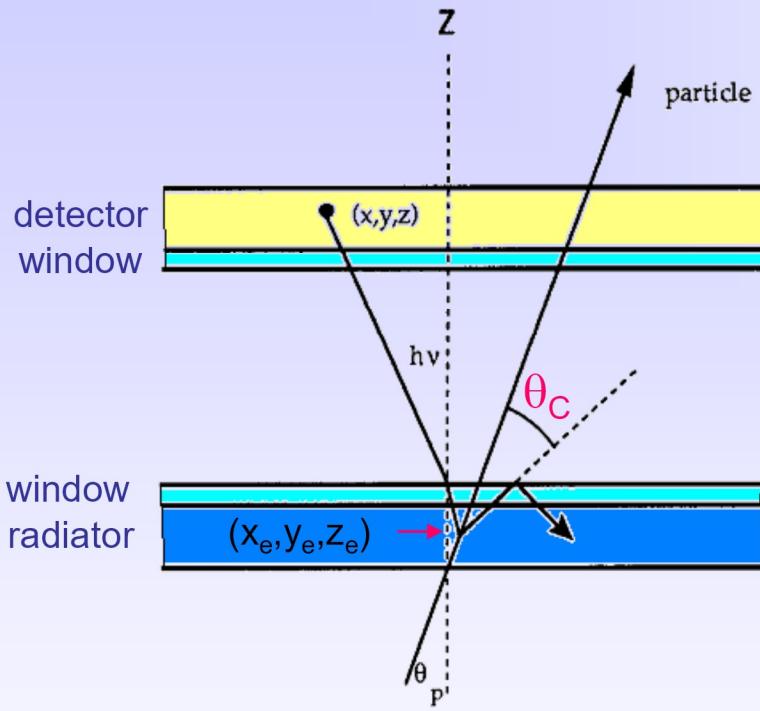
$$\begin{aligned}\theta_C &= \arccos\left(\frac{1}{n\beta}\right) = \arccos\left(\frac{1}{n} \cdot \frac{E}{p}\right) \\ &= \arccos\left(\frac{1}{n} \cdot \frac{\sqrt{p^2 + m^2}}{p}\right)\end{aligned}$$

$$\cos\theta_C = \frac{1}{n\beta} \quad \rightarrow \quad \frac{\sigma_\beta}{\beta} = \tan\theta \cdot \sigma_\theta$$

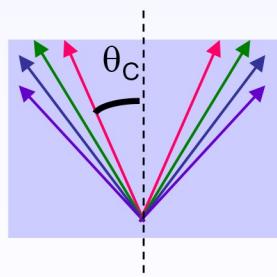
Detect  $N_{p.e.}$  photons (photoelectrons) →

$$\sigma_\theta \approx \frac{\sigma_\theta^{p.e.}}{\sqrt{N_{p.e.}}} \quad \rightarrow \text{minimize } \sigma_\theta^{p.e.} \quad \rightarrow \text{maximize } N_{p.e.}$$

## Reconstruction and resolution of Cherenkov angle



- the chromatic error - an 'irreducible' error



$$n_{rad} = n(E)$$

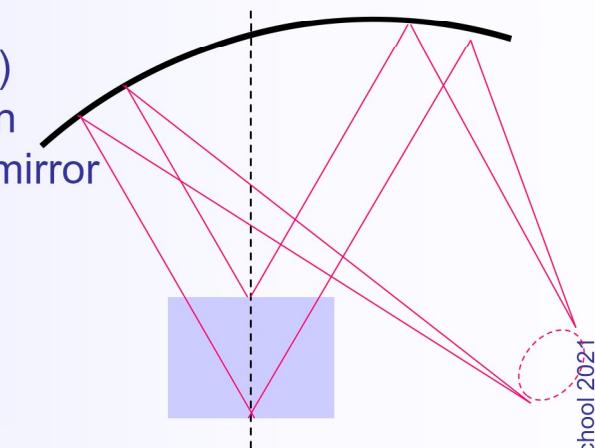
$$\sigma_\theta^c = \frac{1}{n \tan \theta} \sigma_n = \frac{1}{n \tan \theta} \frac{dn}{dE} \sigma_E$$

$\sigma_E$  is related to the sensitivity range of the photodetector  $\Delta E$

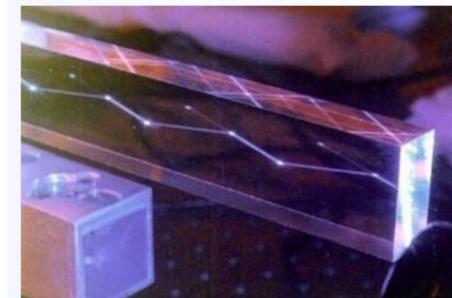
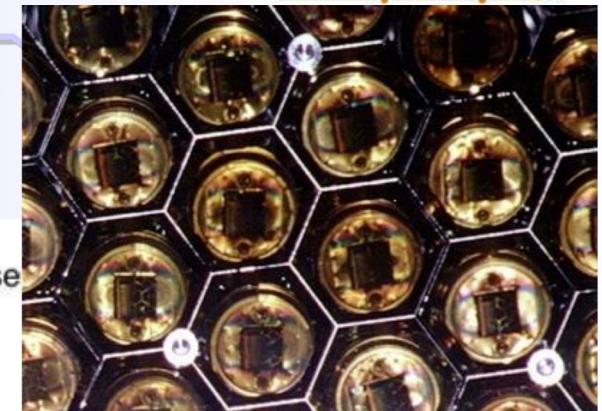
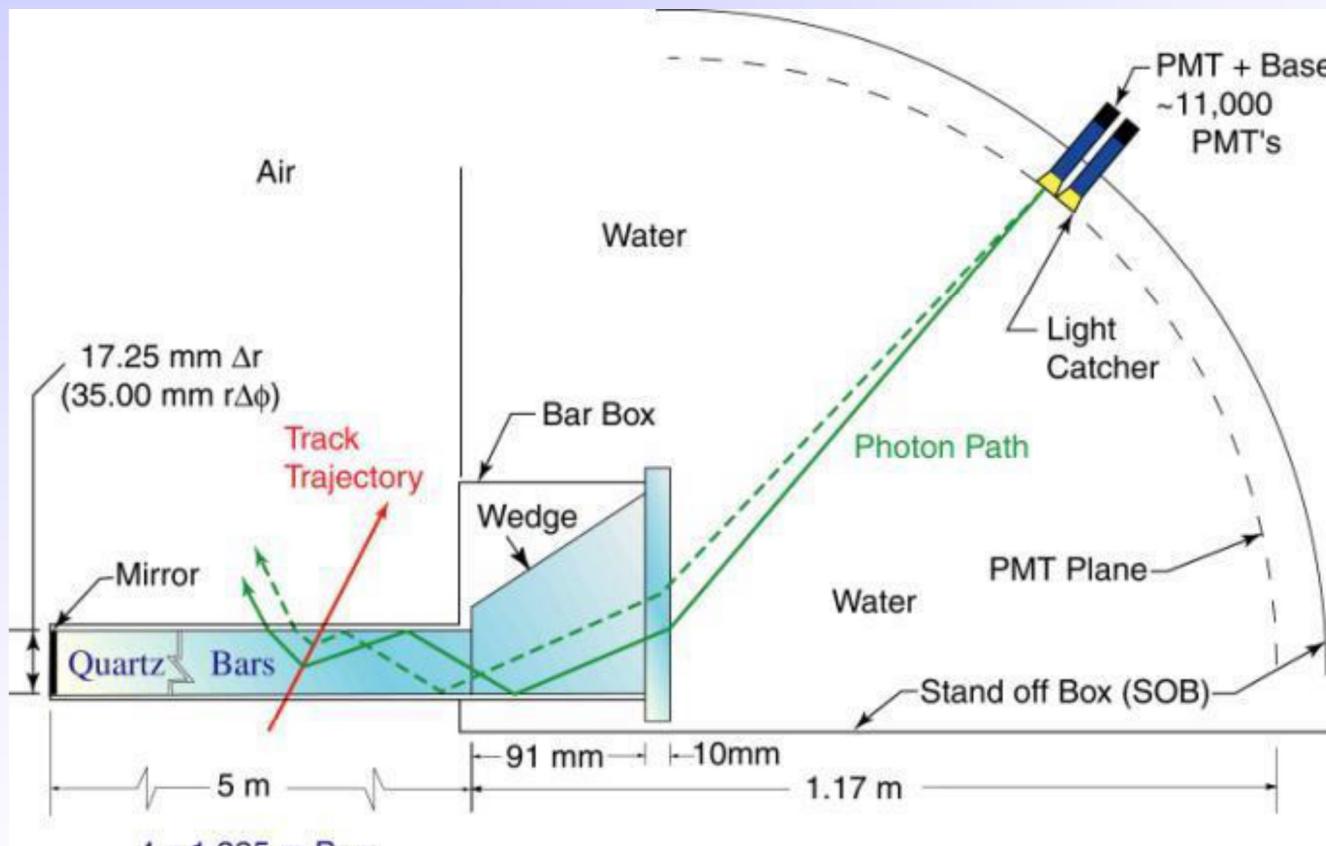
$$\begin{array}{ccc} \Delta E \uparrow & \rightarrow & N_{pe} \uparrow \text{ good} \\ \Delta E \downarrow & \rightarrow & N_{pe} \downarrow \text{ bad} \end{array} \quad \begin{array}{ccc} \sigma_E \uparrow \text{ bad} \\ \sigma_E \downarrow \text{ good} \end{array}$$

### Determination of $\theta_C$ requires:

- space point of the detected photon ( $x,y,z$ )
  - photodetector granularity ( $\sigma_x, \sigma_y$ ), depth of interaction ( $\sigma_z$ )
- emission point ( $x_e, y_e, z_e$ )
  - keep radiator thin or use focusing mirror
- particle direction  $\theta_p, \phi_p$ 
  - RICH requires good tracker

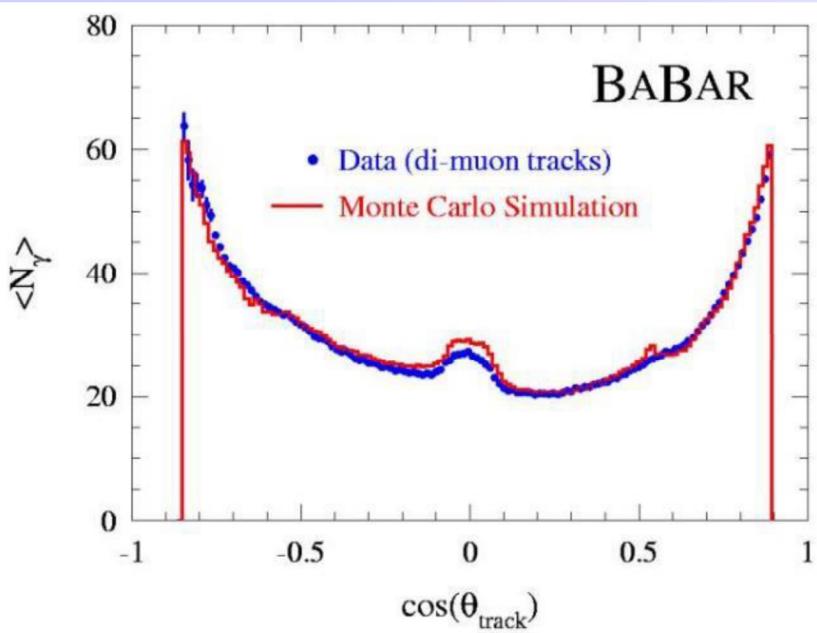


Use the internally reflected C-light, which would normally be lost!



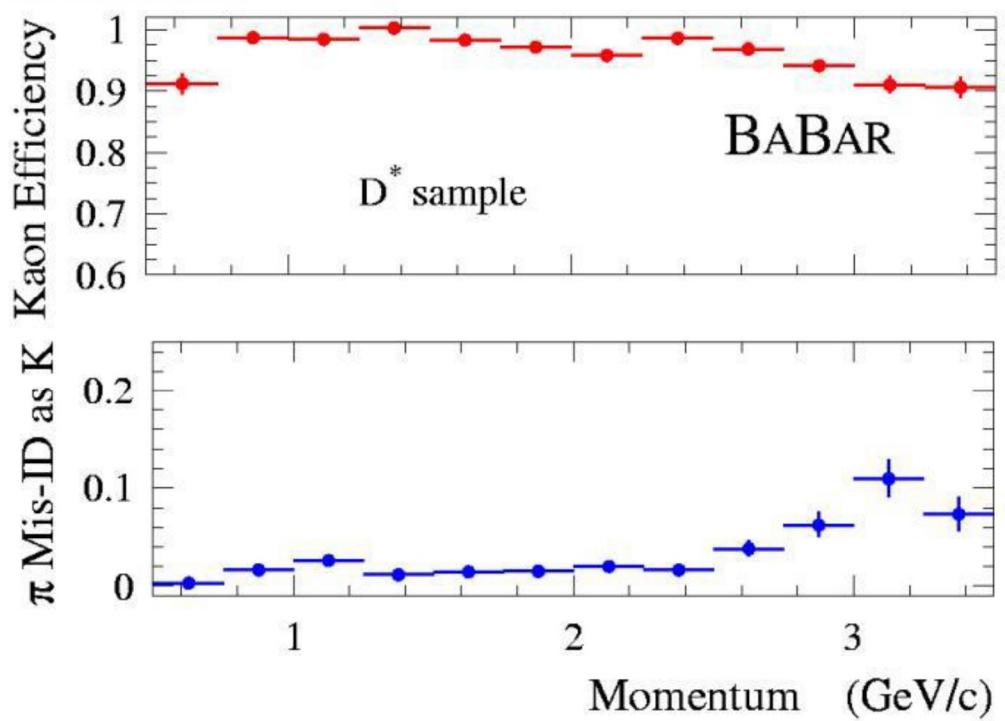
During propagation: angle of Cherenkov light is conserved, except of left/right and up/down ambiguities

I. Adam, et al.  
Nucl. Instr. and Meth. A, 433 (1999), p. 121



← Lots of photons!

Excellent  $\pi/K$  separation



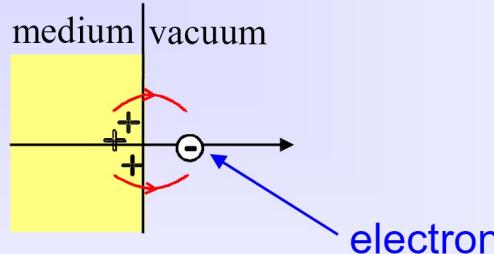
NIM A553 (2005) 317

(there is an excellent review article by B. Dolgoshein (NIM A 326 (1993) 434))

Transition Radiation was predicted by Ginzburg and Franck in 1946

TR is electromagnetic radiation, emitted when a charged particle traverses a medium with a discontinuous refractive index, e.g. the boundaries between vacuum and a dielectric layer.

A (too) simple picture



A correct relativistic treatment shows that...

(G. Garibian, Sov. Phys. JETP63 (1958) 1079)

- Radiated energy per medium/vacuum boundary

$$W = \frac{1}{3} \alpha \hbar \omega_p \gamma$$

$$W \propto \gamma$$



only high energetic  $e^\pm$  emit TR  
of detectable intensity.  
→ particle ID

Lorentz boost

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$\omega_p = \sqrt{\frac{N_e e^2}{\epsilon_0 m_e}} \quad \begin{pmatrix} \text{plasma} \\ \text{frequency} \end{pmatrix} \quad \hbar \omega_p \approx 20 \text{eV} \text{ (plastic radiators)}$$

- Number of emitted photons / boundary is small

$$N_{ph} \approx \frac{W}{\hbar\omega} \propto \alpha \approx \frac{1}{137}$$

→ Need many transitions → build a stack of many thin foils with gas gaps

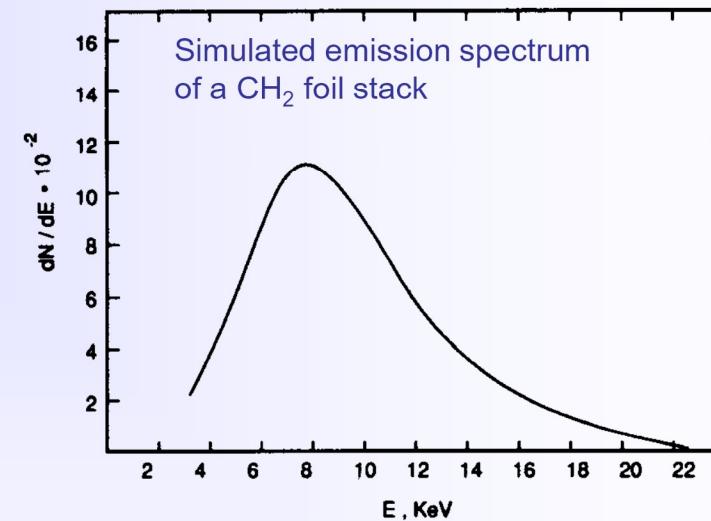
- Emission spectrum of TR = f(material,  $\gamma$ )

Typical energy:  $\hbar\omega \approx \frac{1}{4}\hbar\omega_p\gamma$

→ photons in the keV range

- X-rays are emitted with a sharp maximum at small angles  $\theta \propto 1/\gamma$

→ TR stay close to track



- Particle must traverse a minimum distance, the so-called **formation zone  $Z_f$** , in order to efficiently emit TR.

$$Z_f = \frac{2c}{\omega(\gamma^{-2} + \theta^2 + \xi^2)}, \quad \xi = \omega_p / \omega$$

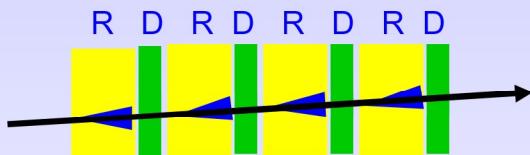
$Z_f$  depends on the material ( $\omega_p$ ), TR frequency ( $\omega$ ) and on  $\gamma$ .

$Z_f(\text{air}) \sim \text{mm}$ ,  $Z_f(\text{CH}_2) \sim 20 \mu\text{m}$  → important consequences for design of TR radiator.

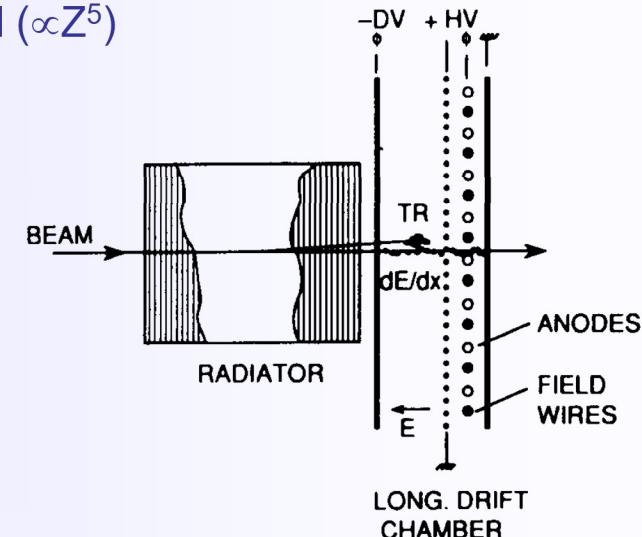
## ■ TR Radiators:

- stacks of thin foils made out of  $\text{CH}_2$  (polyethylene),  $\text{C}_5\text{H}_4\text{O}_2$  (Mylar)
- hydrocarbon foam and fiber materials

Low Z material preferred to keep re-absorption small ( $\propto Z^5$ )

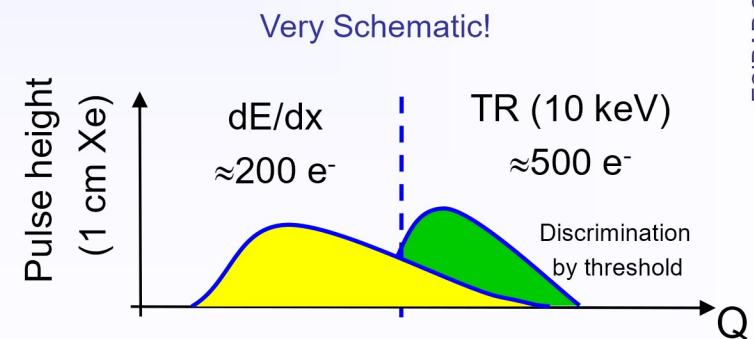


alternating arrangement of radiators stacks and detectors  
→ minimizes reabsorption



## ■ TR X-ray detectors:

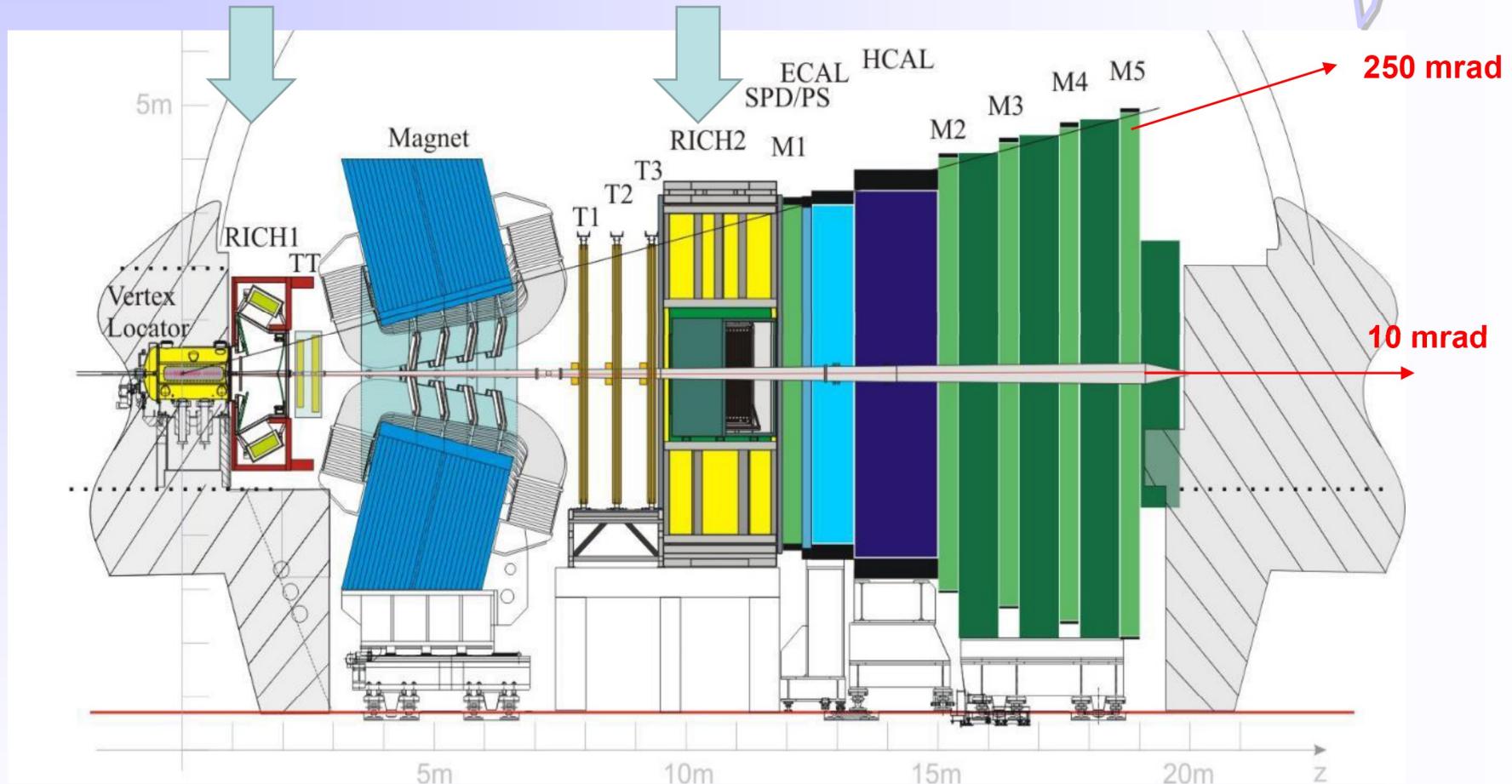
- Detector should be sensitive for  $3 \leq E_\gamma \leq 30 \text{ keV}$ .
- Mainly used: Gas detectors: MWPC, drift chamber, straw tubes...
- Detector gas:  $\sigma_{\text{photo effect}} \propto Z^5$   
→ gas with high Z required, e.g. Xenon ( $Z=54$ )
- Intrinsic problem: detector “sees” TR and  $dE/dx$



# The LHCb RICH counters

<https://doi.org/10.1140/epjc/s10052-013-2431-9>

Generation 2

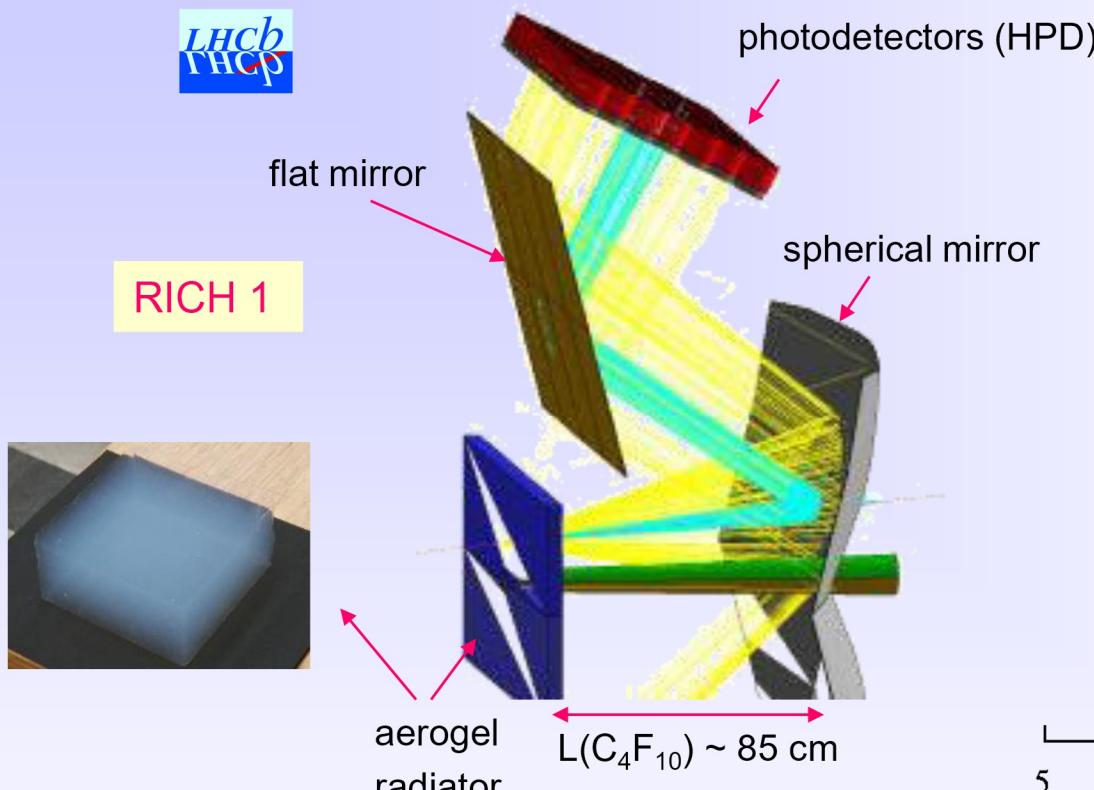


**Vertex  
reconstruction:  
VELO**

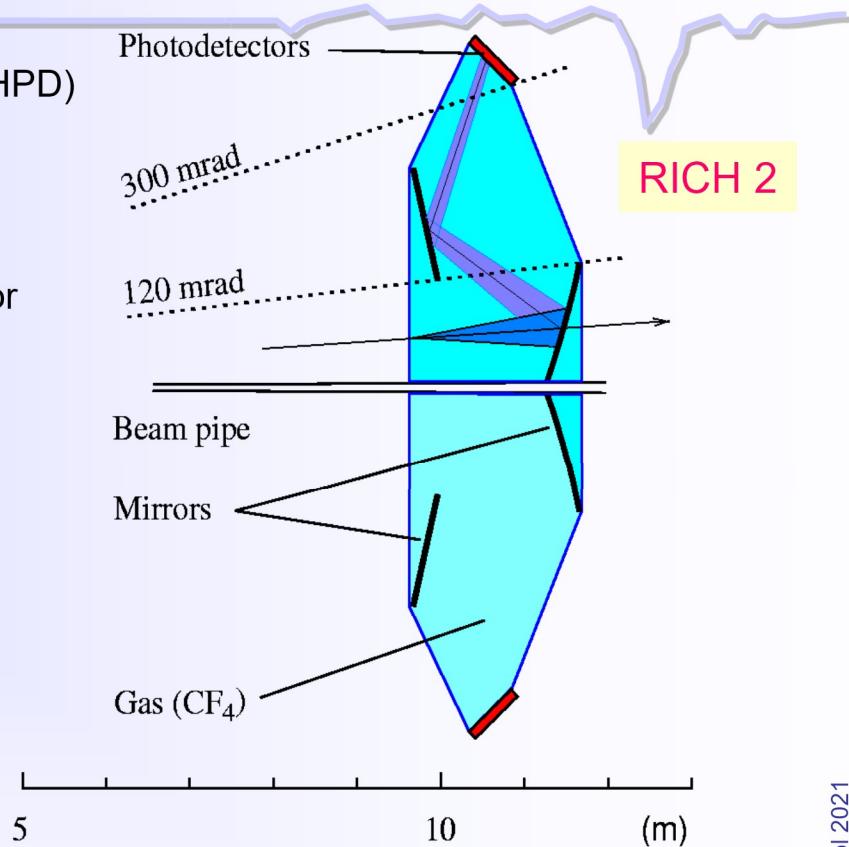
**Trigger:  
Muon Chambers  
Calorimeters  
Tracker**

**PID:  
RICHes  
Calorimeters  
Muon Chambers**

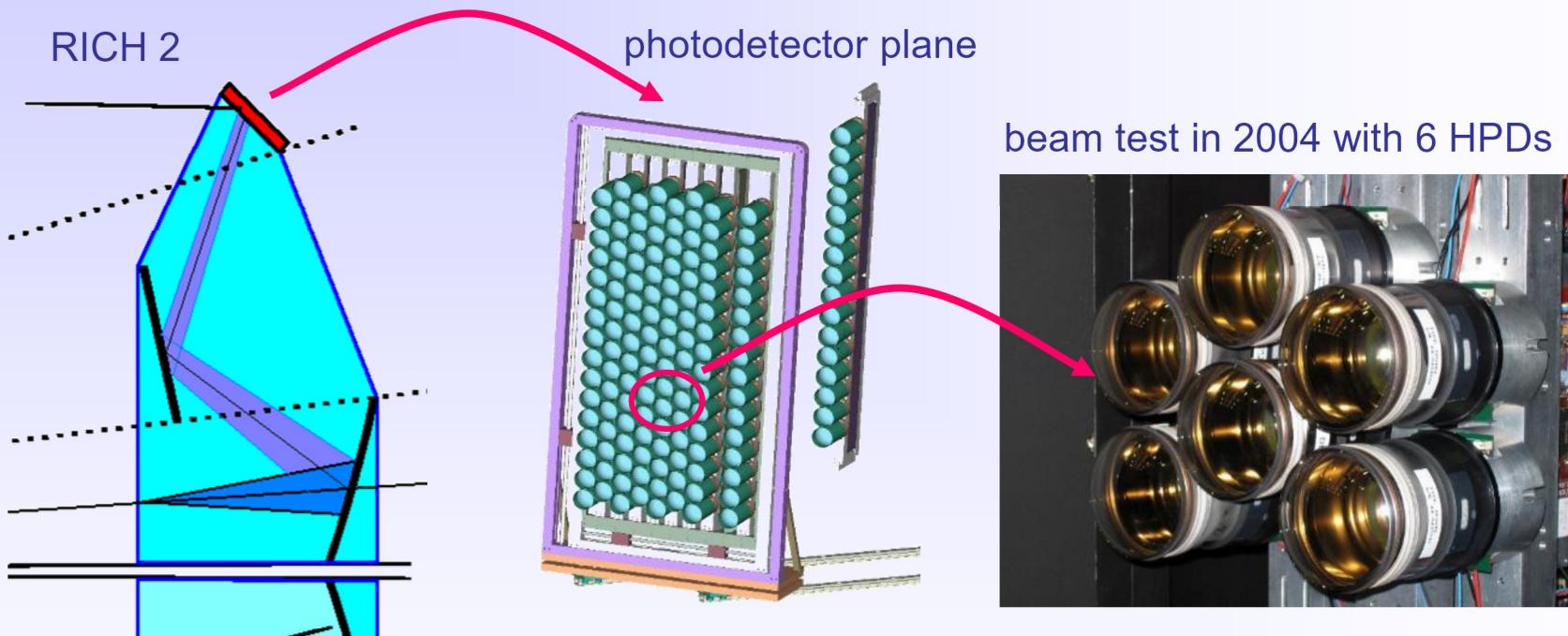
**Kinematics:  
Magnet  
Tracker  
Calorimeters**



radiator	$C_4F_{10}$	aerogel
$\theta_C$	$3.03^\circ$	$13.8^\circ$
$n$	1.0014	1.03
$p_{\text{thresh}}(\pi)$	2.6	0.6 GeV/c
$N_{p.e.}$	31	6.8
$\sigma_\theta$	1.29	2.19 mrad
$p(3\sigma)$	56	13.5 GeV/c

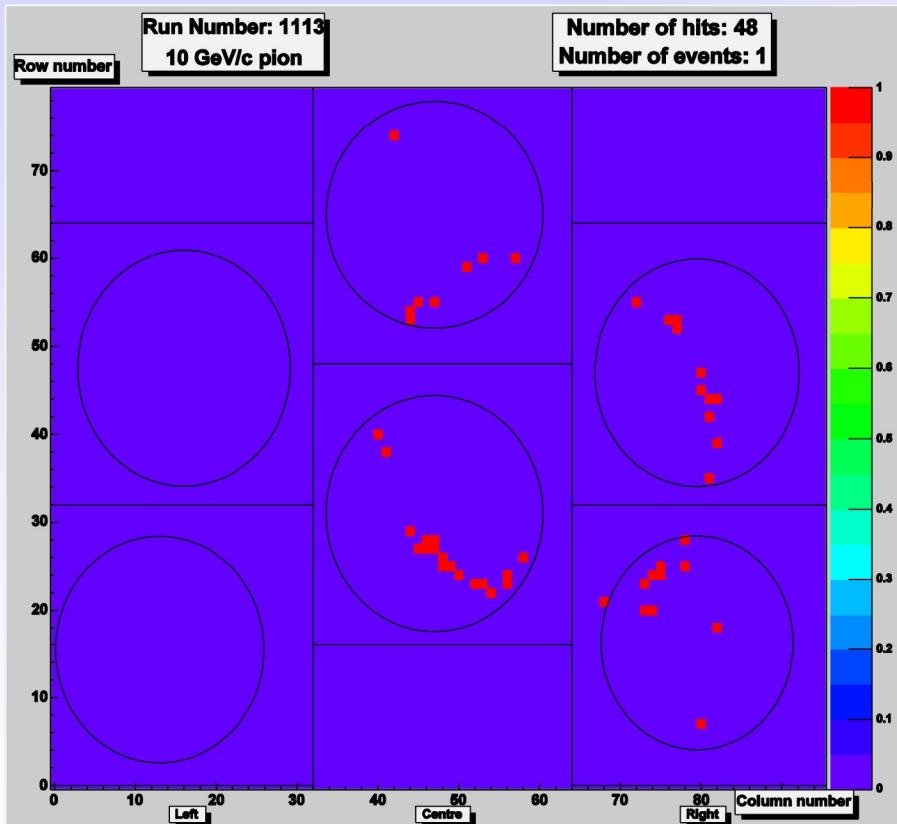


radiator	$CF_4$
$\theta_C$	$1.8^\circ$
$n$	1.0005
$p_{\text{thresh}}(\pi)$	4.4 GeV/c
$N_{p.e.}$	23
$\sigma_\theta$	0.6 mrad
$p(3\sigma)$	98.5 GeV/c

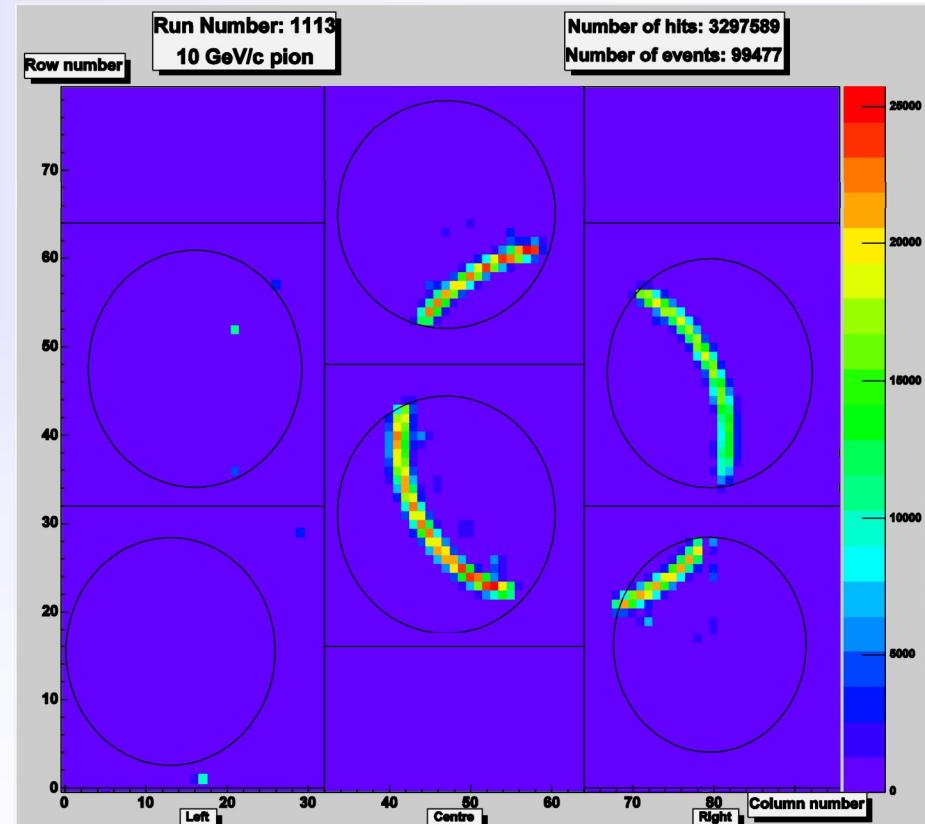


Beam test results with  $\text{C}_4\text{F}_{10}$  radiator gas (autumn 2004).

Single pion (10 GeV/c)

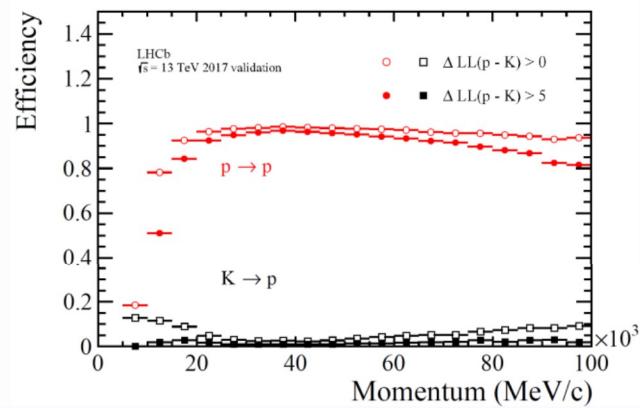
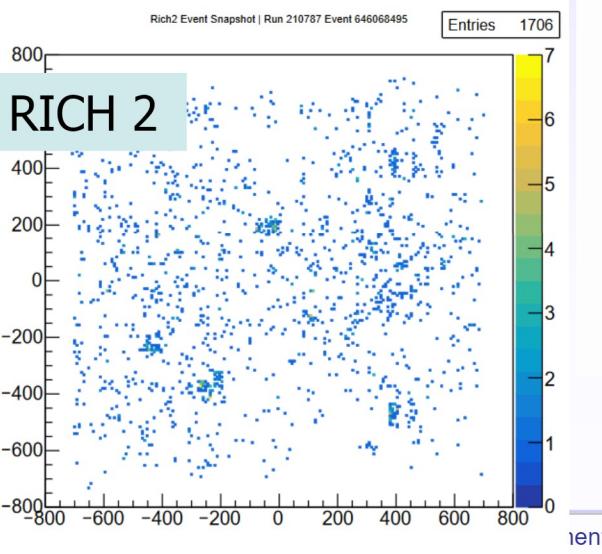
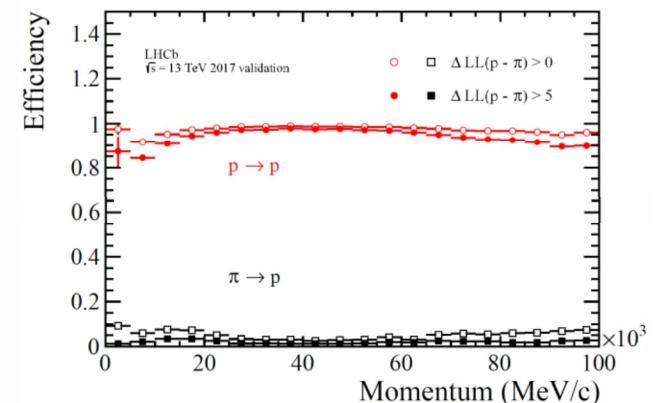
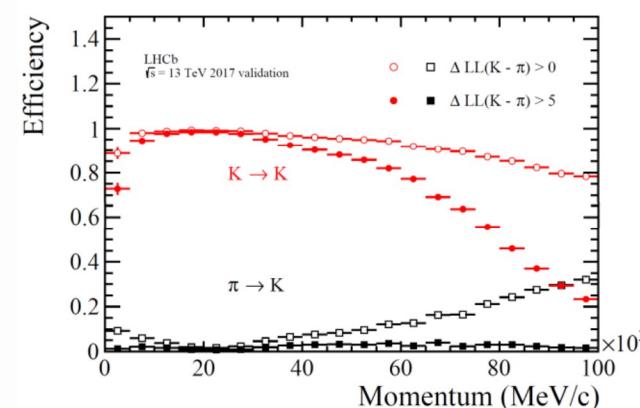
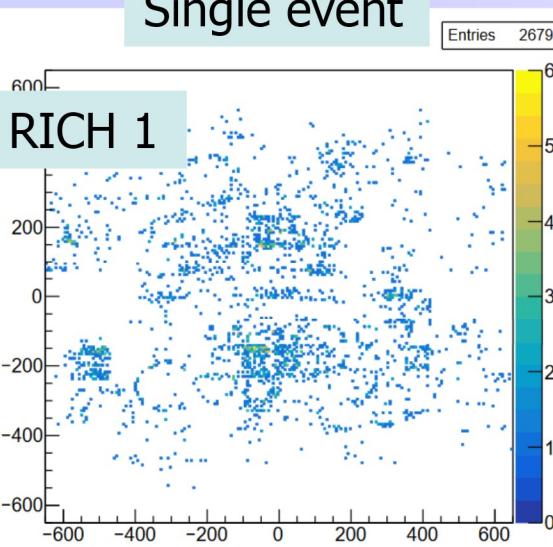


Superimposed events (100 k pions, 10 GeV/c)



<https://doi.org/10.1016/j.nima.2005.08.083>

## Single event

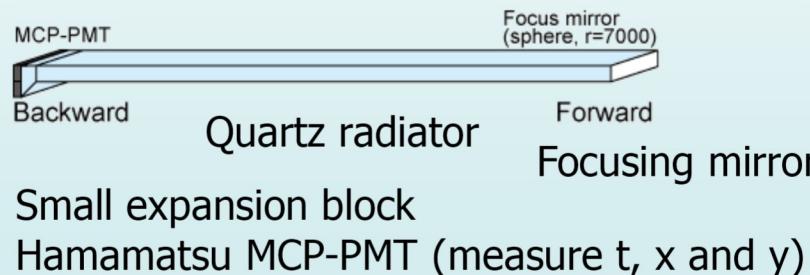


<https://doi.org/10.1140/epjc/s10052-013-2431-9>

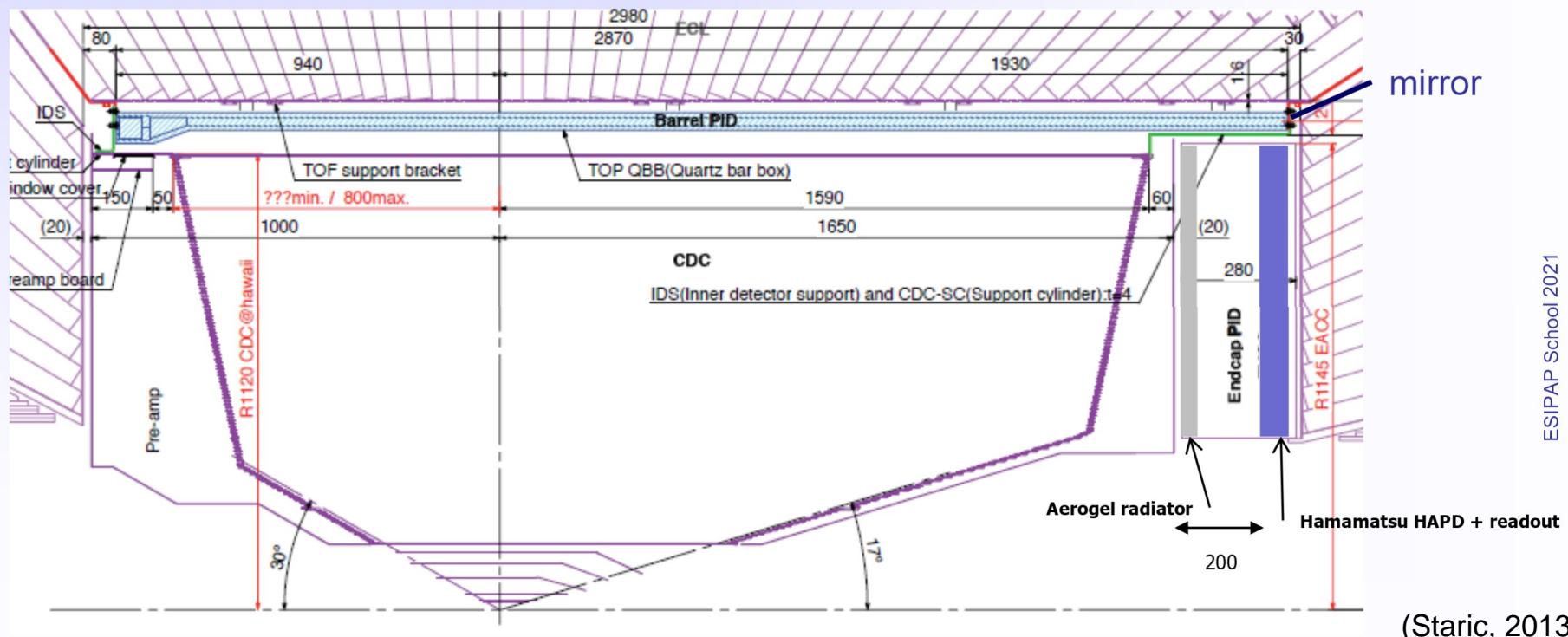
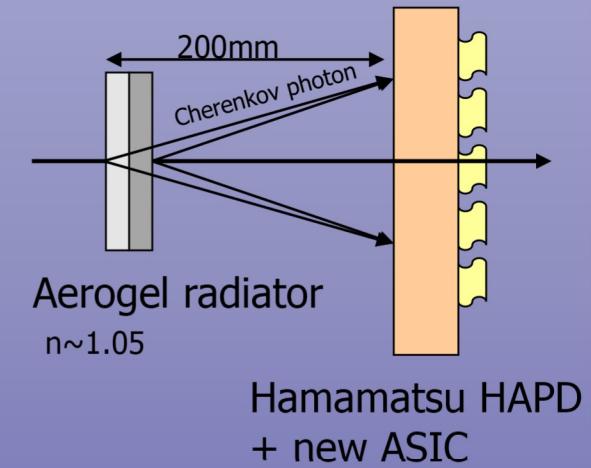


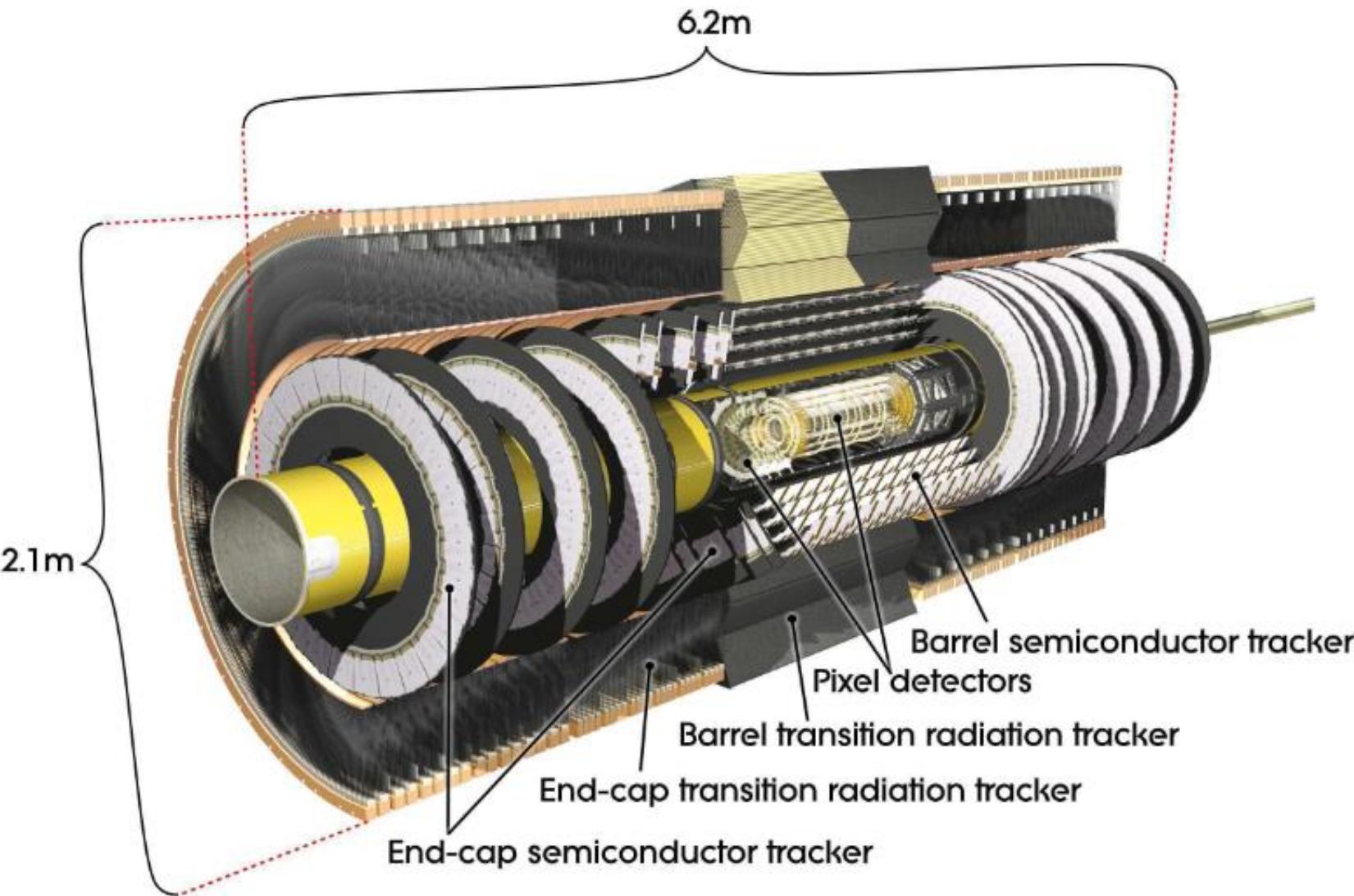
# Belle II Cherenkov detectors

Barrel PID: Time of Propagation Counter (TOP)

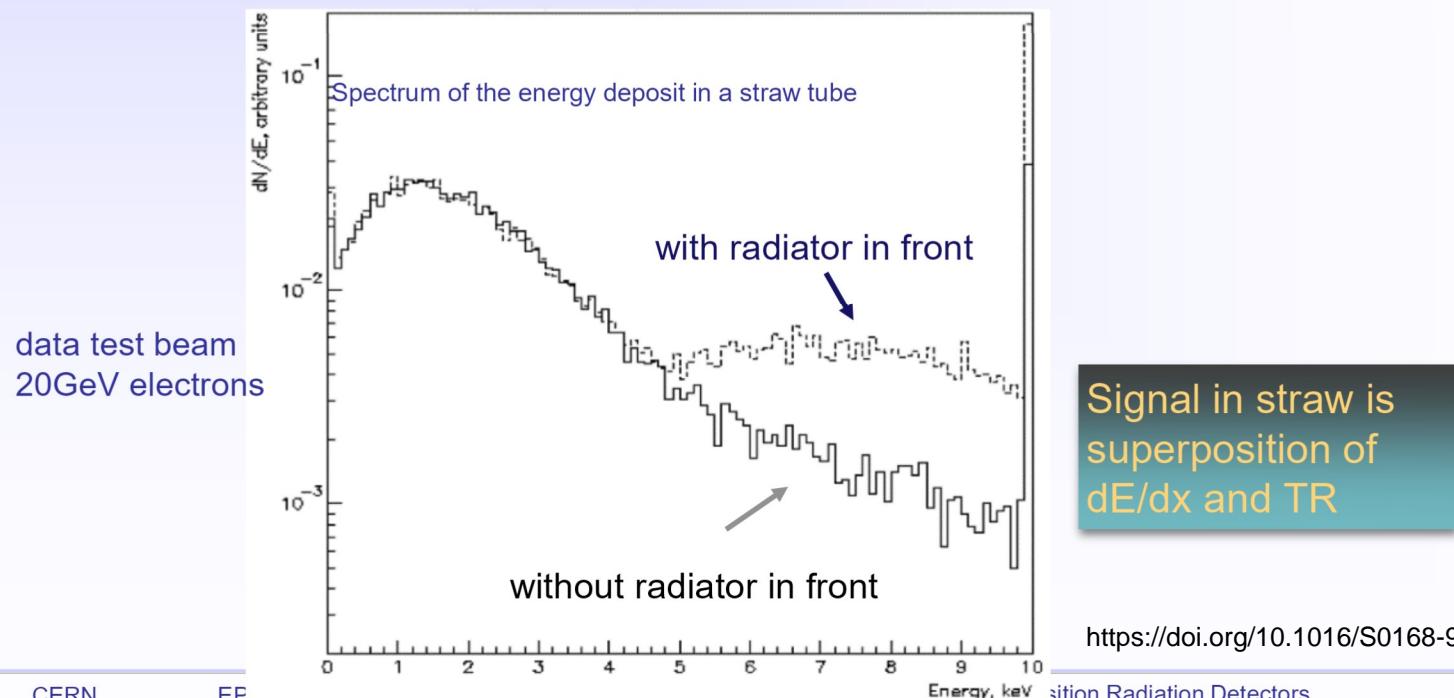
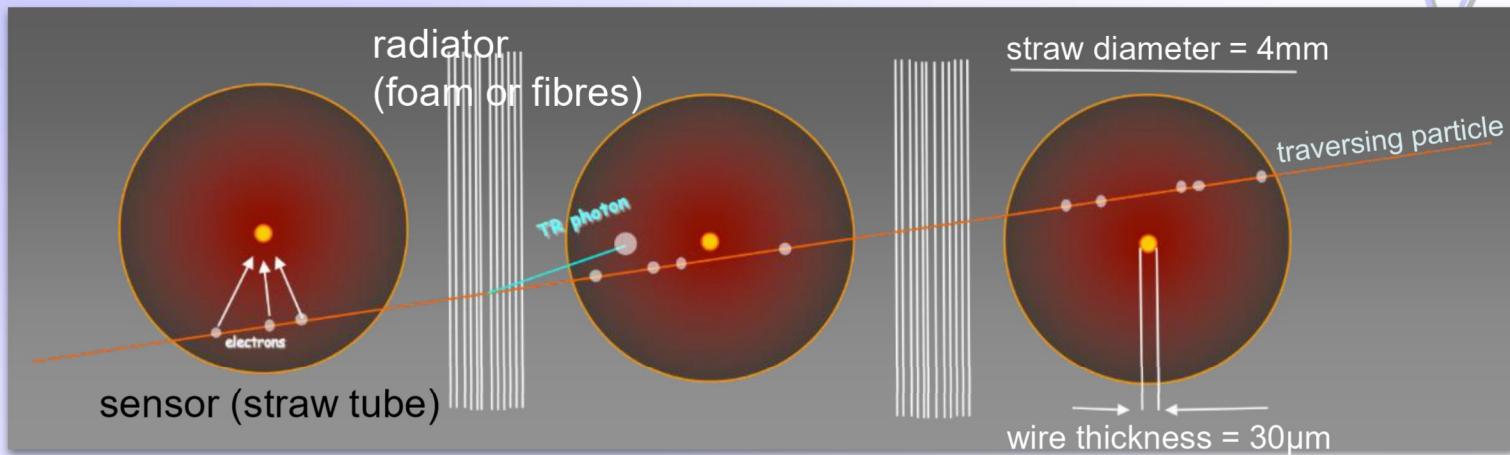


Endcap PID: Aerogel RICH (ARICH)





- Transition Radiation detector in ATLAS
- Based on straw like sensors and fiber-based radiators



# Pros and Cons of Transition and Cherenkov Detectors

Cherenkov Detectors (RICH)	Transition Detectors
<p>Pros:</p> <ol style="list-style-type: none"> <li>1. Highest efficiency for PID</li> <li>2. Can handle large flux of particles</li> <li>3. At low p, spread of ring is low</li> </ol>	<p>Pros:</p> <ol style="list-style-type: none"> <li>1. Precise trajectory tracking of ultra-relativistic electrons</li> <li>2. High efficiency and fast discrimination between electrons and pions with high momentum (1 GeV)</li> </ol>
<p>Cons:</p> <ol style="list-style-type: none"> <li>1. High complexity and cost for building</li> <li>2. At higher p or E, spread of ring is high. Leads to higher chance of mis-PID</li> </ol>	<p>Cons:</p> <ol style="list-style-type: none"> <li>1. Very low intensity of transition radiation</li> <li>2. Alternating layers in the detectors lead to increased complexity and cost</li> </ol>

$$n_{rad} = n(E)$$

$$\sigma_{\theta}^c = \frac{1}{n \tan \theta} \sigma_n = \frac{1}{n \tan \theta} \frac{dn}{dE} \sigma_E$$

$\sigma_E$  is related to the sensitivity range of the photodetector  $\Delta E$

$\Delta E \uparrow \rightarrow N_{pe} \uparrow$  good     $\sigma_E \uparrow \rightarrow$  bad  
 $\Delta E \downarrow \rightarrow N_{pe} \downarrow$  bad     $\sigma_E \downarrow \rightarrow$  good

# THANK YOU!

---