

Topic: Bayes' theorem**Question:** When should you use Bayes' Theorem?**Answer choices:**

- A When you have $P(A \cap B)$ but want to find $P(A)$.
- B When you have $P(A | B)$ but want to find $P(B | A)$.
- C When you have $P(A)$ but want to find $P(B)$.
- D When you have $P(A | B)$ but want to find $P(A)$.



Solution: B

Bayes' Theorem is used when you have a conditional probability of two events, and you're interested in the reversed conditional probability. For example, when you have $P(A|B)$ but want to find $P(B|A)$.



Topic: Bayes' theorem

Question: Three factories A , B , and C produce car seats. What is the probability that a defective car seat comes from factory C , given that factory C produces 40 % of all the car seats, that there's a 1 % chance that any given car seat is defective, and that the defective rate at factory C is 0.8 % ?

Answer choices:

A 28 %

B 32 %

C 36 %

D 40 %



Solution: B

We could name these events.

A represents a car seat from factory A

B represents a car seat from factory B

C represents a car seat from factory C

D represents a defective car seat

We're looking for $P(C|D)$, the probability that a car seat came from factory C , given that it was defective. We know

$$P(C) = 0.4$$

$$P(D) = 0.01$$

$$P(D|C) = 0.008$$

Bayes' theorem therefore tells us that the probability of $P(C|D)$ is given by

$$P(C|D) = \frac{P(D|C) \cdot P(C)}{P(D)}$$

$$P(C|D) = \frac{(0.008)(0.4)}{0.01}$$

$$P(C|D) = \frac{0.0032}{0.01}$$

$$P(C|D) = 0.32$$



Topic: Bayes' theorem**Question:** Which choice is equivalent to $P(C|D)$?**Answer choices:**

A $\frac{P(D|C) \cdot P(C)}{P(D)}$

B $\frac{P(C \cap D)}{P(D)}$

C $\frac{P(C \cup D)}{P(D)}$

D Both A and B



Solution: D

Bayes' theorem is

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)}$$

This problem uses different variables. If you replace A with C and B with D , then Bayes' theorem is

$$P(C|D) = \frac{P(D|C) \cdot P(C)}{P(D)}$$

For dependent events, the multiplication rule says that

$P(C \cap D) = P(C) \cdot P(D|C)$, which means we could also write Bayes' theorem as

$$P(C|D) = \frac{P(D|C) \cdot P(C)}{P(D)} = \frac{P(C \cap D)}{P(D)}$$

