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Unit 5

Push Down Automata

PDA = FA + Stack

Formal definition :-

It has 7 tupples namely

Z_0 = starting symbol of stack

Γ = ~~Set of~~ stacks alphabets

q_0 F Σ Q δ

$\delta : Q \times (\Sigma \cup \wedge) \times \Gamma \rightarrow Q \times \Gamma^*$

Case 1 -

Γ and Γ^* are same then skip operation has been done.

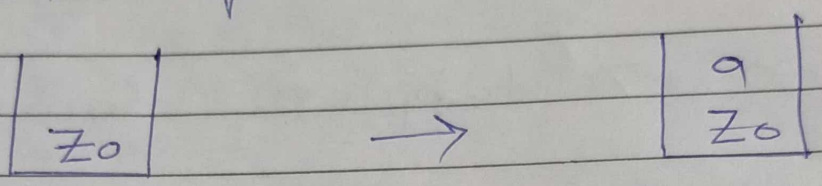
Case 2 -

When Γ and Γ^* are different then push operation been done.

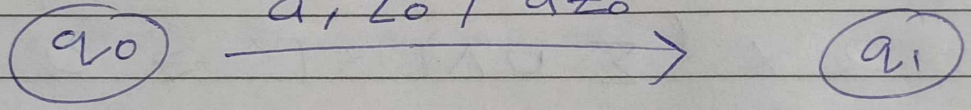
(iii) Case 3 –

When Γ is any stack alphabet and Γ^* is null then pop - operation has been done.

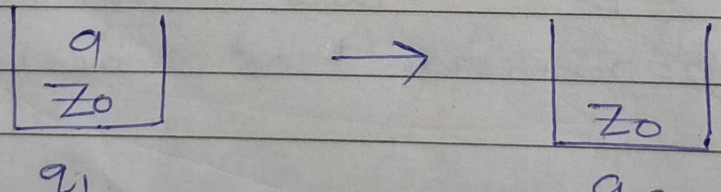
Push operation



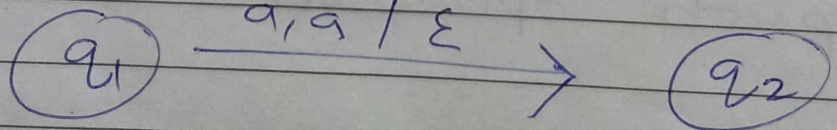
$(q_0, a, Z_0) \rightarrow (q_1, aZ_0)$



Pop Operation



$(q_1, a, a) \rightarrow (q_2, \varepsilon)$



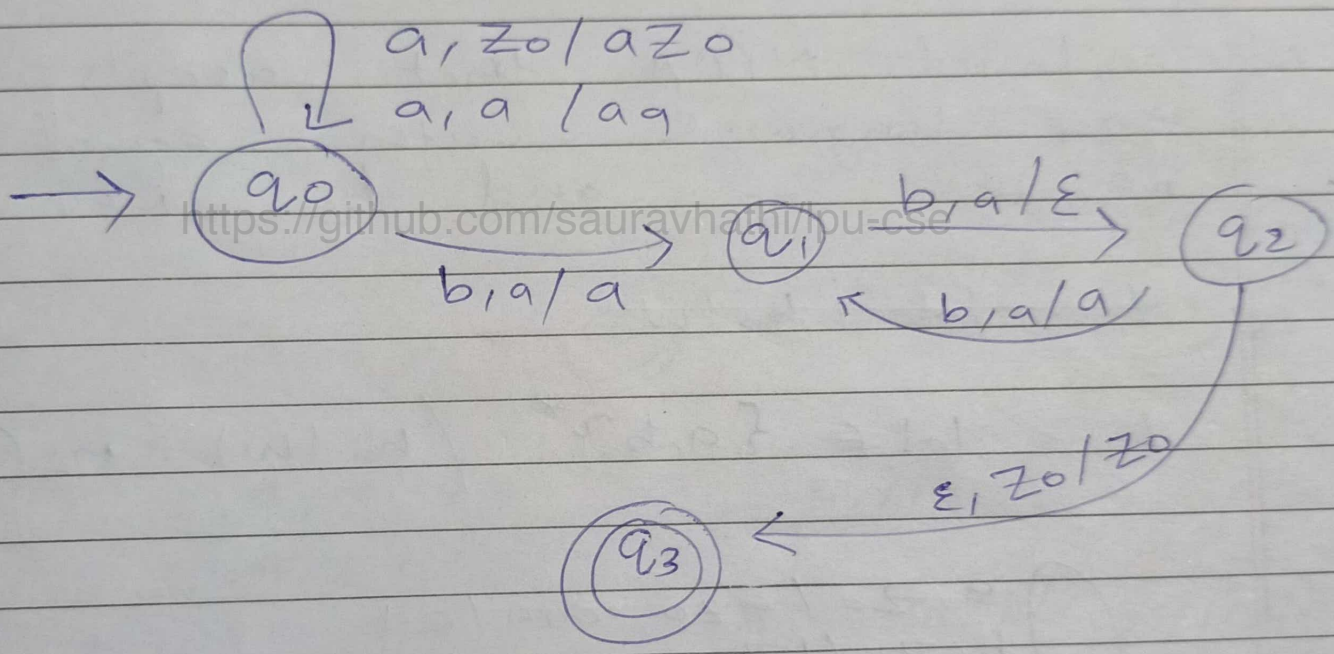
Skip Operation

$$\begin{bmatrix} a \\ Z_0 \end{bmatrix} \longrightarrow \begin{bmatrix} a \\ Z_0 \end{bmatrix}$$

q_0 q_1

$(q_0, a, a) \rightarrow (q_1, a)$

(2) $L = a^n \cdot b^{2n}$; $n \geq 1$



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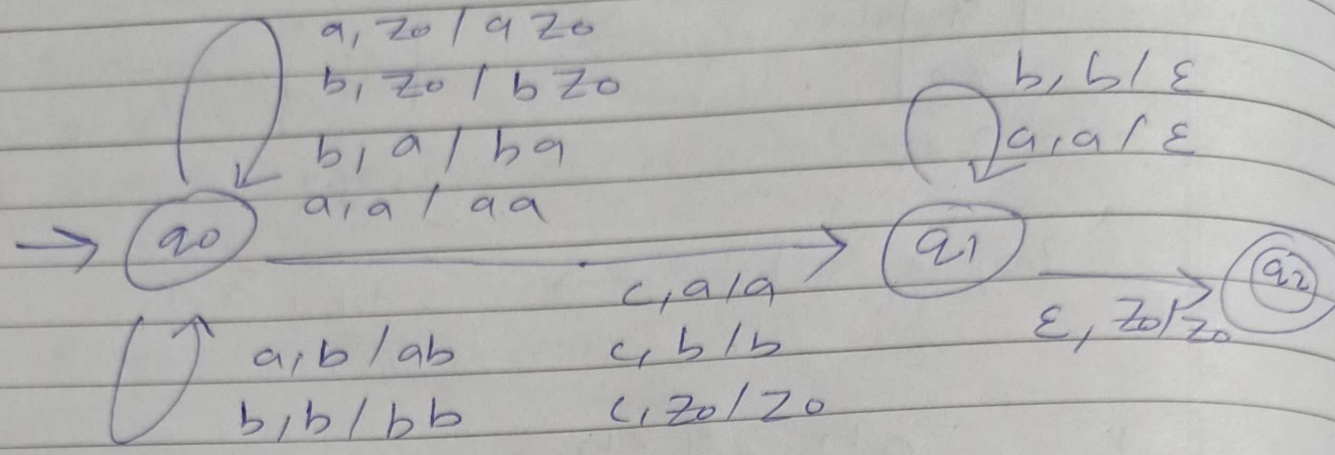
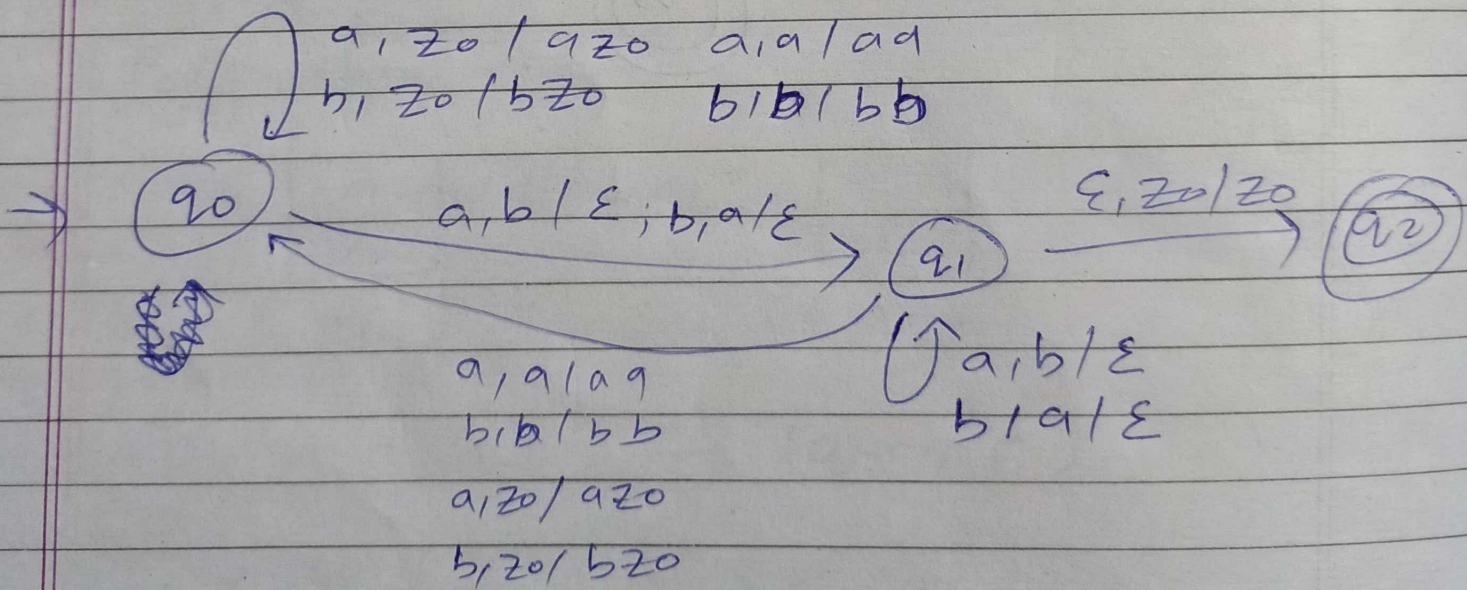
(c) $L = wCw^R \quad ; \quad w \in \{a, b\}^*$



(d) Construct NPDA that accepts the language with equal no of as and bs i.e.

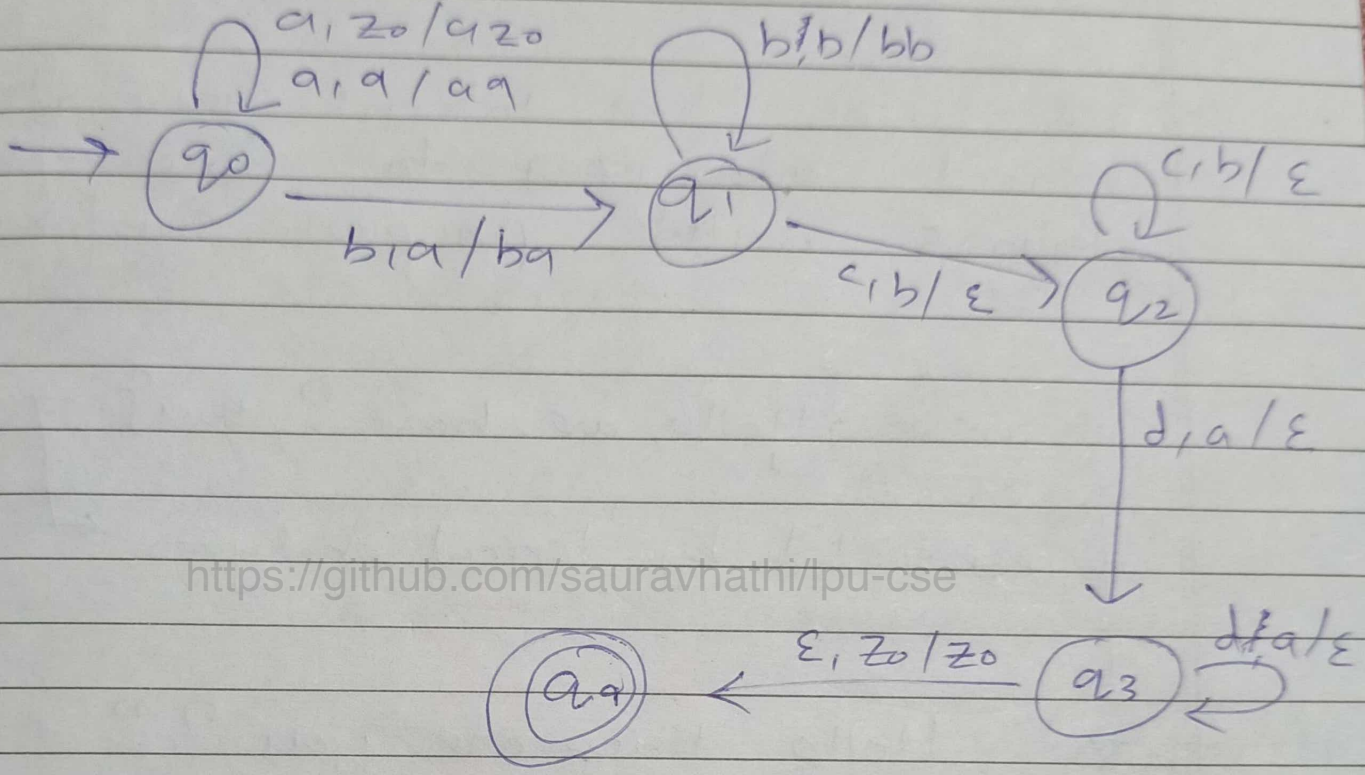
~~$L = \{w \mid n_a(w)\}$~~

$L = \{w \in \{a, b\}^* \mid n_a(w) = n_b(w)\}$

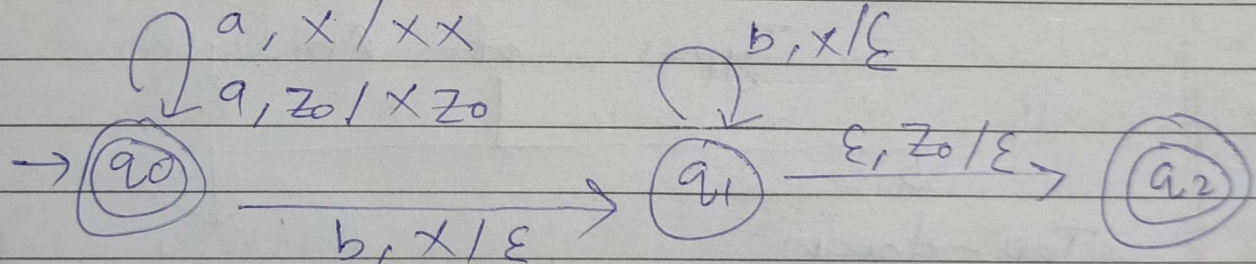


Q) $L = a^n b^m c^m d^n$; $n, m \geq 1$

Construct PDA



Q)



$\Sigma = \{a, b\}$ $\Gamma = \{X, z_0\}$

(A) $L = \{a^n ; n > 0\}$

✓ (B) $L = \{a^n\} \cup \{a^n b^n ; n > 0\}$

✓ (C) L is accepted by any Turing machine.

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Parser

→ It is syntax analyzer which is used to generate the string from the grammar.

→ It uses the tokens generated by lexical analyzer to form the strings with proper syntax

Tokens = {Hello, are, how, ?, you}

Generated by lexical analyzer

→ " Hello how are you ? "

Types of Analyser

- Top-down Analyzer
  - recursively Decent parser
  - LL(K) {Predictive}
    - Left to right
    - LMD
    - Look after Symbol
- Bottom-up analyzer
  - LR(0)
    - SLR(0)
  - LR(1)
    - LALR(1)
    - CLR(1)

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→ Recursive decent parser backtracking could be there

→ LL(1c) → No Back tracking

→ SLR → Simple LR

→ LALR → look at LR

→ LR → Left to Right RMD

LL(1c) Parser

→ ~~fd~~ It uses top-down approach

→ A grammar can be in LL(2) ~~parser~~ however not in LL(1), therefore if a grammar is in LL(1+1) it may or may not be in LL(K)

ex → ~~show~~ check the following grammar is in LL(1) or not by considering the string = aaabd

S → aA/bB
A → aB/cB
B → bC/aC
C → bD
D → d

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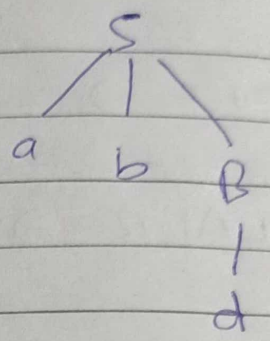
* Check whether the grammar is in LL(1), LL(2), LL(3) with string : abd

S → abB / aaA
A → c/d
B → d



LL(2) and LL(3)

Q) LL(k) grammar is which type of gramar

(i) ~~LL(0)~~ type 0 (ii) ~~LL(2)~~ type 2 ✓

(iii) type 3 (iv) type 1

Q) LL(k) gramar is

(i) always ambiguous

✓(ii) always unambiguous

✓(iii) Need to be converted to unambiguous

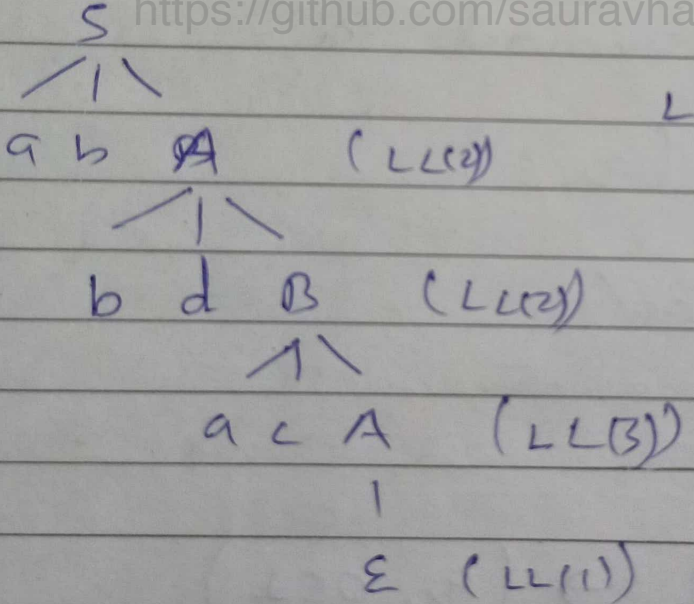
(iv) None

Handle is combination of terminals and non terminals.

Yield is output string in terms of terminals

* String = aabdac

$S \rightarrow aaA / abB / \varepsilon$
$A \rightarrow bdB / bcA / \varepsilon$
$B \rightarrow acA / acB$



LL(3) Parser

Q) Simplify the grammar

$S \to aXb$
$X \to aXb / \varepsilon$

(i) $S \to ab$; ~~$X \to aXb /$~~ $X \to ab$

✓ (ii) $S \to aXb / ab$; $X \to aXb / ab$

(iii) $S \to ab$; $X \to aXb / ab$

Q) CF Languages are applied in

✓ (i) Parser Design

(ii) DFA (iii) NFA

Q) A derivation $A \to x$ is a _____ if we apply to Right most variable on every step.

(i) LMD (ii) RMD ✓

Q) A Grammar in CNF has the following property of derivation tree, i.e. every node has atmost 2 descendants

(i) Either single instead vertex on

(ii) Either 2 internal vertices or 2 leaves

✓(iii) Either 2 internal vertices or single leaf

Q) In which normal form of CFG left recursing is not possible

⇒ GNF

Q) Top down parsing is equivalent to finding a

(i) RMD

✓(ii) LMD

(iii) Both (i) and (ii)

Q) The use of variable dependency graph is in

✓(i) Removal of useless variable

(ii) Removal of null production

(iii) Removal of unit production