

03-gradient-descent

September 24, 2024

Implement Gradient Descent Algorithm to find the local minima of a function. For example, find the local minima of the function $y=(x+3)**2$ starting from the point $x=2$.

```
[7]: import matplotlib.pyplot as plt
```

```
[8]: def cost_function(x):  
    # ithe given function yenar  
    return (x + 3) ** 2
```

```
[9]: def gradient(x):  
    # ithe derivate of given function yenar  
    return 2 * (x + 3)
```

```
[10]: learning_rate = 0.1  
    initial_x = 2.0  
    num_iterations = 100
```

```
[13]: x_values = []  
    y_values = []  
    x = initial_x  
    for i in range(num_iterations):  
        x_values.append(x)  
        y_values.append(cost_function(x))  
        gradient_value = gradient(x)  
        x = x - learning_rate * gradient_value  
  
        print(f'Iteration {i+1}: x = {x}, Cost = {cost_function(x)}')  
  
    print(f'Optimal x: {x}')
```

```
Iteration 1: x = 1.0, Cost = 16.0  
Iteration 2: x = 0.19999999999999996, Cost = 10.240000000000002  
Iteration 3: x = -0.440000000000000017, Cost = 6.553599999999998  
Iteration 4: x = -0.95200000000000001, Cost = 4.194304  
Iteration 5: x = -1.36160000000000001, Cost = 2.6843545599999996  
Iteration 6: x = -1.68928000000000001, Cost = 1.7179869183999996  
Iteration 7: x = -1.951424, Cost = 1.099511627776  
Iteration 8: x = -2.1611392, Cost = 0.7036874417766399
```

Iteration 9: $x = -2.32891136$, Cost = 0.4503599627370493
 Iteration 10: $x = -2.463129088$, Cost = 0.28823037615171165
 Iteration 11: $x = -2.5705032704$, Cost = 0.1844674407370954
 Iteration 12: $x = -2.6564026163200003$, Cost = 0.11805916207174093
 Iteration 13: $x = -2.725122093056$, Cost = 0.07555786372591429
 Iteration 14: $x = -2.7800976744448$, Cost = 0.04835703278458515
 Iteration 15: $x = -2.82407813955584$, Cost = 0.030948500982134555
 Iteration 16: $x = -2.8592625116446717$, Cost = 0.019807040628566166
 Iteration 17: $x = -2.8874100093157375$, Cost = 0.012676506002282305
 Iteration 18: $x = -2.90992800745259$, Cost = 0.008112963841460692
 Iteration 19: $x = -2.927942405962072$, Cost = 0.005192296858534868
 Iteration 20: $x = -2.9423539247696575$, Cost = 0.0033230699894623056
 Iteration 21: $x = -2.953883139815726$, Cost = 0.002126764793255884
 Iteration 22: $x = -2.9631065118525806$, Cost = 0.0013611294676837786
 Iteration 23: $x = -2.9704852094820646$, Cost = 0.0008711228593176078
 Iteration 24: $x = -2.9763881675856516$, Cost = 0.0005575186299632732
 Iteration 25: $x = -2.981110534068521$, Cost = 0.00035681192317650156
 Iteration 26: $x = -2.984888427254817$, Cost = 0.00022835963083295564
 Iteration 27: $x = -2.9879107418038537$, Cost = 0.00014615016373308945
 Iteration 28: $x = -2.990328593443083$, Cost = 9.353610478917726e-05
 Iteration 29: $x = -2.9922628747544664$, Cost = 5.986310706507345e-05
 Iteration 30: $x = -2.993810299803573$, Cost = 3.83123885216492e-05
 Iteration 31: $x = -2.995048239842858$, Cost = 2.451992865385725e-05
 Iteration 32: $x = -2.9960385918742864$, Cost = 1.5692754338469342e-05
 Iteration 33: $x = -2.9968308734994293$, Cost = 1.0043362776619253e-05
 Iteration 34: $x = -2.9974646987995435$, Cost = 6.427752177036323e-06
 Iteration 35: $x = -2.997971759039635$, Cost = 4.113761393302886e-06
 Iteration 36: $x = -2.998377407231708$, Cost = 2.6328072917135587e-06
 Iteration 37: $x = -2.998701925785366$, Cost = 1.6849966666971388e-06
 Iteration 38: $x = -2.998961540628293$, Cost = 1.0783978666865378e-06
 Iteration 39: $x = -2.9991692325026342$, Cost = 6.901746346793842e-07
 Iteration 40: $x = -2.9993353860021075$, Cost = 4.417117661946878e-07
 Iteration 41: $x = -2.999468308801686$, Cost = 2.826955303647891e-07
 Iteration 42: $x = -2.9995746470413485$, Cost = 1.8092513943361614e-07
 Iteration 43: $x = -2.9996597176330786$, Cost = 1.1579208923763523e-07
 Iteration 44: $x = -2.999727774106463$, Cost = 7.410693711203819e-08
 Iteration 45: $x = -2.99978221928517$, Cost = 4.7428439751781807e-08
 Iteration 46: $x = -2.9998257754281363$, Cost = 3.035420144107846e-08
 Iteration 47: $x = -2.999860620342509$, Cost = 1.9426688922339734e-08
 Iteration 48: $x = -2.999888496274007$, Cost = 1.243308091029743e-08
 Iteration 49: $x = -2.9999107970192056$, Cost = 7.9571717826062e-09
 Iteration 50: $x = -2.9999286376153647$, Cost = 5.092589940842615e-09
 Iteration 51: $x = -2.9999429100922916$, Cost = 3.259257562149415e-09
 Iteration 52: $x = -2.999954328073833$, Cost = 2.0859248397837384e-09
 Iteration 53: $x = -2.9999634624590668$, Cost = 1.3349918974486118e-09
 Iteration 54: $x = -2.9999707699672533$, Cost = 8.543948143723039e-10
 Iteration 55: $x = -2.999976615973803$, Cost = 5.468126811899669e-10
 Iteration 56: $x = -2.9999812927790424$, Cost = 3.499601159582557e-10

Iteration 57: $x = -2.9999850342232337$, Cost = $2.2397447421860056e-10$
 Iteration 58: $x = -2.999988027378587$, Cost = $1.433436634977776e-10$
 Iteration 59: $x = -2.9999904219028695$, Cost = $9.173994464198049e-11$
 Iteration 60: $x = -2.9999923375222957$, Cost = $5.871356456950638e-11$
 Iteration 61: $x = -2.9999938700178364$, Cost = $3.757668132666189e-11$
 Iteration 62: $x = -2.999995096014269$, Cost = $2.4049076048192486e-11$
 Iteration 63: $x = -2.9999960768114153$, Cost = $1.5391408670843192e-11$
 Iteration 64: $x = -2.9999968614491324$, Cost = $9.850501548782124e-12$
 Iteration 65: $x = -2.999997489159306$, Cost = $6.3043209907745444e-12$
 Iteration 66: $x = -2.9999979913274446$, Cost = $4.034765434809332e-12$
 Iteration 67: $x = -2.9999983930619556$, Cost = $2.5822498785634223e-12$
 Iteration 68: $x = -2.9999987144495646$, Cost = $1.6526399220522305e-12$
 Iteration 69: $x = -2.9999989715596516$, Cost = $1.0576895502961154e-12$
 Iteration 70: $x = -2.9999991772477212$, Cost = $6.769213121895138e-13$
 Iteration 71: $x = -2.999999341798177$, Cost = $4.3322963956744853e-13$
 Iteration 72: $x = -2.9999994734385416$, Cost = $2.7726696951023927e-13$
 Iteration 73: $x = -2.9999995787508333$, Cost = $1.7745086041172427e-13$
 Iteration 74: $x = -2.9999996630006667$, Cost = $1.1356855066350352e-13$
 Iteration 75: $x = -2.9999997304005332$, Cost = $7.268387247253274e-14$
 Iteration 76: $x = -2.9999997843204267$, Cost = $4.651767834410857e-14$
 Iteration 77: $x = -2.9999998274563415$, Cost = $2.977131407892966e-14$
 Iteration 78: $x = -2.9999998619650734$, Cost = $1.9053640961475125e-14$
 Iteration 79: $x = -2.9999998895720585$, Cost = $1.2194330254575965e-14$
 Iteration 80: $x = -2.999999911657647$, Cost = $7.804371331543109e-15$
 Iteration 81: $x = -2.9999999293261177$, Cost = $4.994797639633387e-15$
 Iteration 82: $x = -2.999999943460894$, Cost = $3.1966704893653676e-15$
 Iteration 83: $x = -2.9999999547687155$, Cost = $2.045869097124455e-15$
 Iteration 84: $x = -2.9999999638149726$, Cost = $1.309356209304147e-15$
 Iteration 85: $x = -2.9999999710519782$, Cost = $8.379879636702507e-16$
 Iteration 86: $x = -2.9999999768415826$, Cost = $5.363122967489605e-16$
 Iteration 87: $x = -2.999999981473266$, Cost = $3.432398699193347e-16$
 Iteration 88: $x = -2.9999999851786128$, Cost = $2.1967351938118145e-16$
 Iteration 89: $x = -2.99999998814289$, Cost = $1.4059105661644777e-16$
 Iteration 90: $x = -2.999999990514312$, Cost = $8.997827286453327e-17$
 Iteration 91: $x = -2.9999999924114498$, Cost = $5.758609463330129e-17$
 Iteration 92: $x = -2.9999999939291597$, Cost = $3.685510164371068e-17$
 Iteration 93: $x = -2.9999999951433276$, Cost = $2.358726677741145e-17$
 Iteration 94: $x = -2.999999996114662$, Cost = $1.5095850047368678e-17$
 Iteration 95: $x = -2.99999999689173$, Cost = $9.661342926036557e-18$
 Iteration 96: $x = -2.9999999975133838$, Cost = $6.18326035608692e-18$
 Iteration 97: $x = -2.999999998010707$, Cost = $3.957287334634505e-18$
 Iteration 98: $x = -2.9999999984085655$, Cost = $2.532663894166083e-18$
 Iteration 99: $x = -2.999999998726852$, Cost = $1.6209053445792253e-18$
 Iteration 100: $x = -2.999999998981482$, Cost = $1.0373792396055266e-18$
 Optimal x : -2.999999998981482

```
[20]: plt.plot(x_values, y_values, 'ro-')  
plt.title('Gradient Descent Visualization for  $y = (x + 3)^2$  by AB')  
plt.xlabel('x')  
plt.ylabel('y')  
plt.show()
```

