

## Operation Research: Mini Project

**Transportation Problem:**

If there are more than one centres, called origins from where goods need to be shipped to more than one places called “destinations” and the cost of shipping from each of the origins to each of the destinations being different and known, the problem is to ship the goods from various origins to different destinations in a such manner that the cost of shipping or transportation is minimum.

The transportation problem is to transport various amounts of single homogenous commodity, that are initially stored at various origins to different destinations in such a way that the total transportation cost is minimum.

There are 3 methods in transportation problem:

1. Least Cost Cell Method
2. Northwest Corner Method
3. Vogel's Approximation Method

Solving the below problem using transportation method.

The DREAM - DRINK Company has to work out a minimum cost transportation schedule to distribute crates of drinks from three of its factories X, Y, and Z to its three warehouses A, B, and C. The required particulars are given below. Find the least cost transportation schedule.

| From/To          | A    | B   | C   | Crates Available |
|------------------|------|-----|-----|------------------|
| X                | 75   | 50  | 50  | 1040             |
| Y                | 50   | 25  | 75  | 975              |
| Z                | 25   | 125 | 25  | 715              |
| Crates required. | 1300 | 910 | 520 | 2730             |

## 1. Solve using Least Cost Method.

Q1 The DREAM-DRINK company has to work out a minimum cost transportation schedule to distribute crates of drinks from three of its factories X, Y & Z to its warehouse houses A, B & C.

| From/To                      | A    | B   | C   | Supply<br>Crates |
|------------------------------|------|-----|-----|------------------|
| X                            | 75   | 50  | 50  | 1040             |
| Y                            | 50   | 25  | 75  | 975              |
| Z                            | 25   | 125 | 25  | 715              |
| Crates<br>Required<br>Demand | 1300 | 910 | 520 | 2730             |

Solving using Least cost cell method.

|        | A    | B   | C   | SUPPLY |
|--------|------|-----|-----|--------|
| X      | 75   | 50  | 50  | 1040   |
| Y      | 50   | 25  | 75  | 975    |
| Z      | 25   | 125 | 25  | 715    |
| Demand | 1300 | 910 | 520 | 2730   |

$\text{Demand} = 1300 + 910 + 520 = 2730$   
 $\text{Supply} = 1040 + 975 + 715 = 2730$   
 $\therefore \text{Demand} = \text{Supply}$   
 Hence, it is a balanced transportation problem.

Now, using Least cost cell method.

|        | A    | B   | C   | Supply |
|--------|------|-----|-----|--------|
| X      | 75   | 50  | 50  | 1040   |
| Y      | 50   | 25  | 75  | 975    |
| Z      | 25   | 125 | 25  | 745    |
| Demand | 1300 | 910 | 520 | 2730   |
|        | 485  | 0   | 0   | 1040   |

$\therefore \text{Demand} = \text{Supply} = 1040$

$\text{Cost} = \sum (\text{allocated Value} \times \text{cell value})$

$= (75 \times 1040) + (50 \times 65) + (25 \times 195) + (25 \times 910) + (25 \times 520)$

$\therefore 78,000 + 3250 + 4875 + 22,750 + 13,000$

$\underline{\underline{121,875}}$

Implementation of above problem in R language.

Code:

```
library(lpSolve)
```

```
costs <- matrix(c(75,50,50,
  75,25,75,
  25,125,25), nrow = 3, byrow = TRUE)
```

```
colnames(costs) <- c("A","B","C")
```

```
rownames(costs) <- c("X","Y","Z")
```

```
row.signs <- rep("<=",3)
row.rhs <- c(1040, 975, 715)
```

```
col.signs <- rep(">=",3)
col.rhs <- c(1300, 910, 520)
```

```
TotalCost <- lp.transport(costs,"min",row.signs,row.rhs,col.signs,col.rhs)
```

```
lp.transport(costs,"min",row.signs,row.rhs,col.signs,col.rhs)$solution
print(TotalCost)
```

```
> lp.transport(costs,"min",row.signs,row.rhs,col.signs,col.rhs)$solution
      [,1] [,2] [,3]
[1,]  520    0  520
[2,]   65  910    0
[3,]  715    0    0
> print(TotalCost)
Success: the objective function is 110500
> |
```