

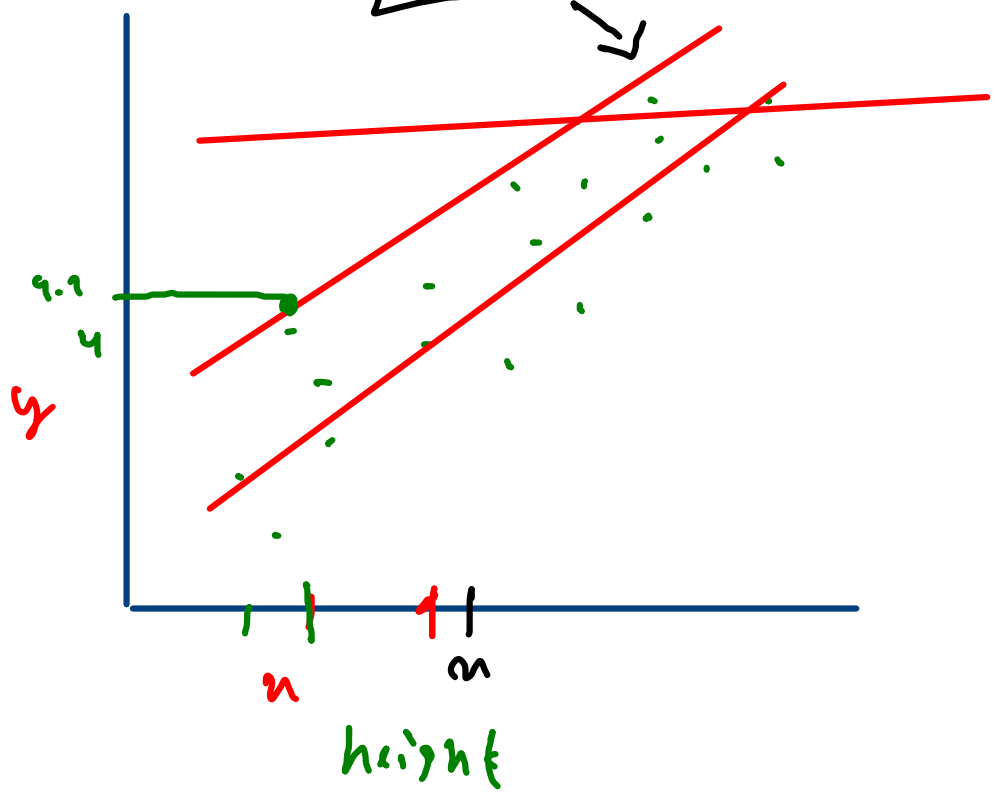
$$\text{Loss error} = \frac{\sum (y_{\text{ack}} - y_{\text{pv}})^2}{N}$$

x  
height

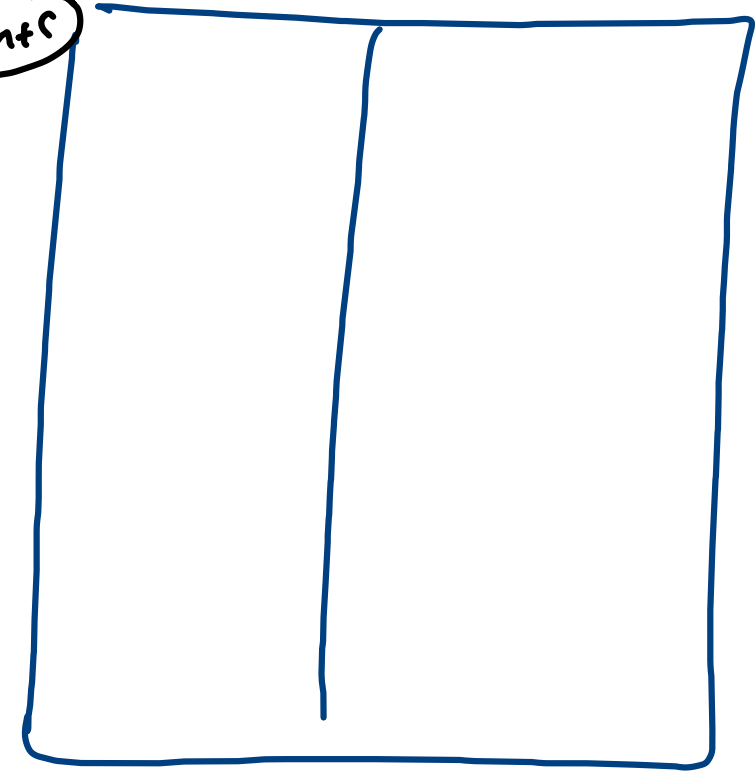
y  
weight

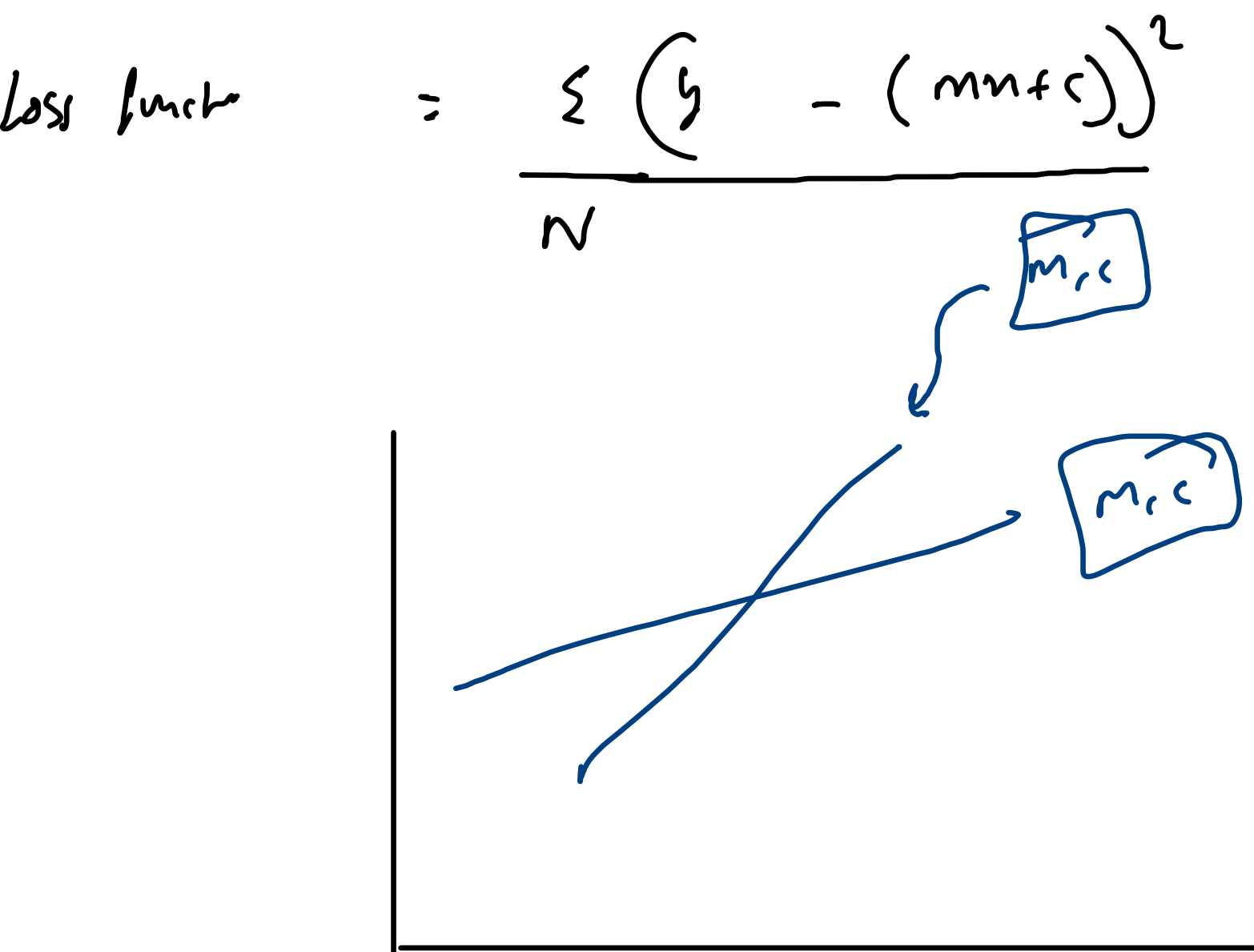
$$y = mx + c$$

weight  
 0.2  
 0.04  
 ↑



$$mx + c$$





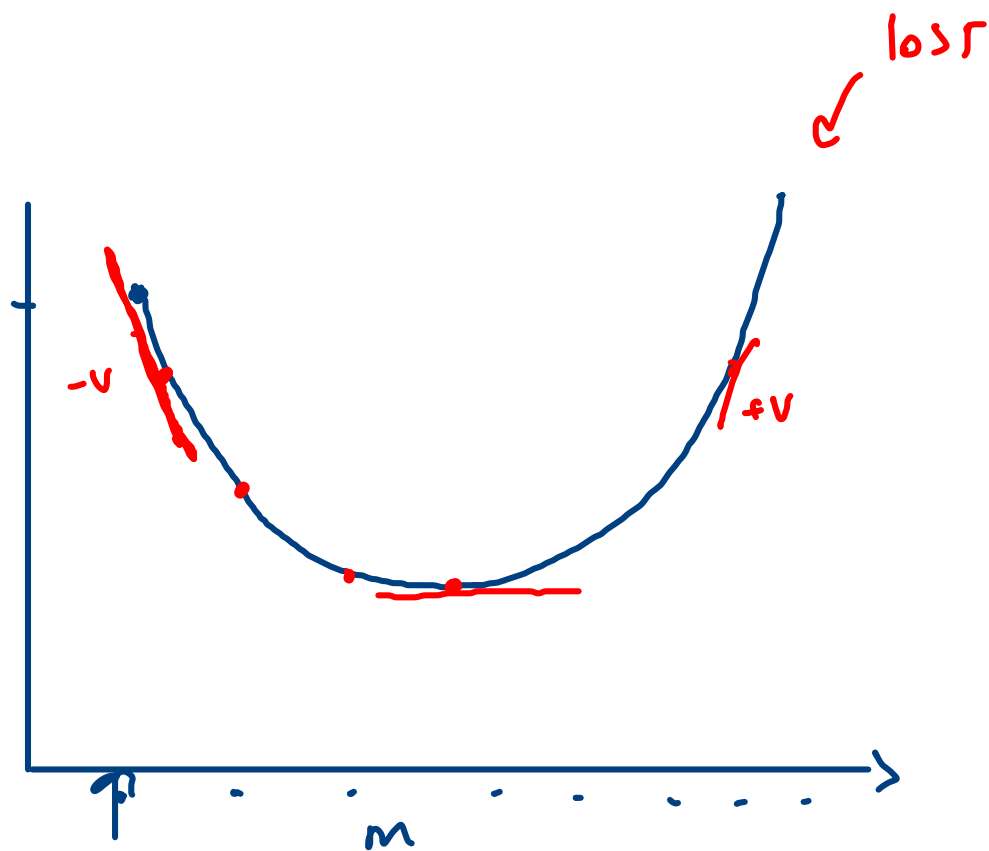
$mn+c$

$m, c$

Gradient  
Descent

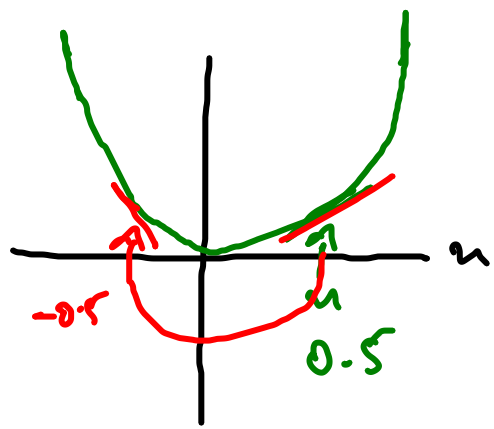
$f(m)$

$$\frac{d f(m)}{d m} = 0$$



$$\text{slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{dz}{dn}$$

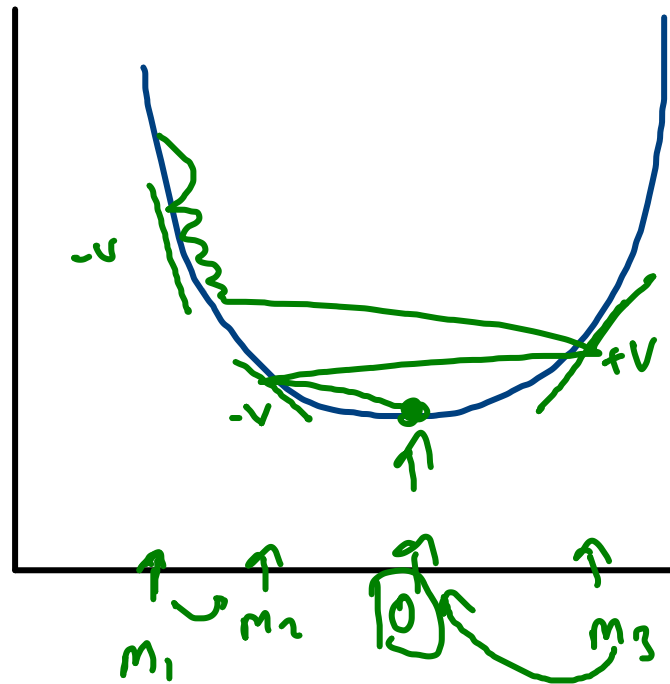




$$y = x^2$$

$$\frac{dy}{dx} = 2x$$

$$-0.5 - (-1) = -0.5 + 1 = 0.5$$



$$M_{new} = M_{old} - \lambda \frac{d f(m)}{d m} \leftarrow \text{slope}$$

learning rate

$$M_1 = (-v)$$

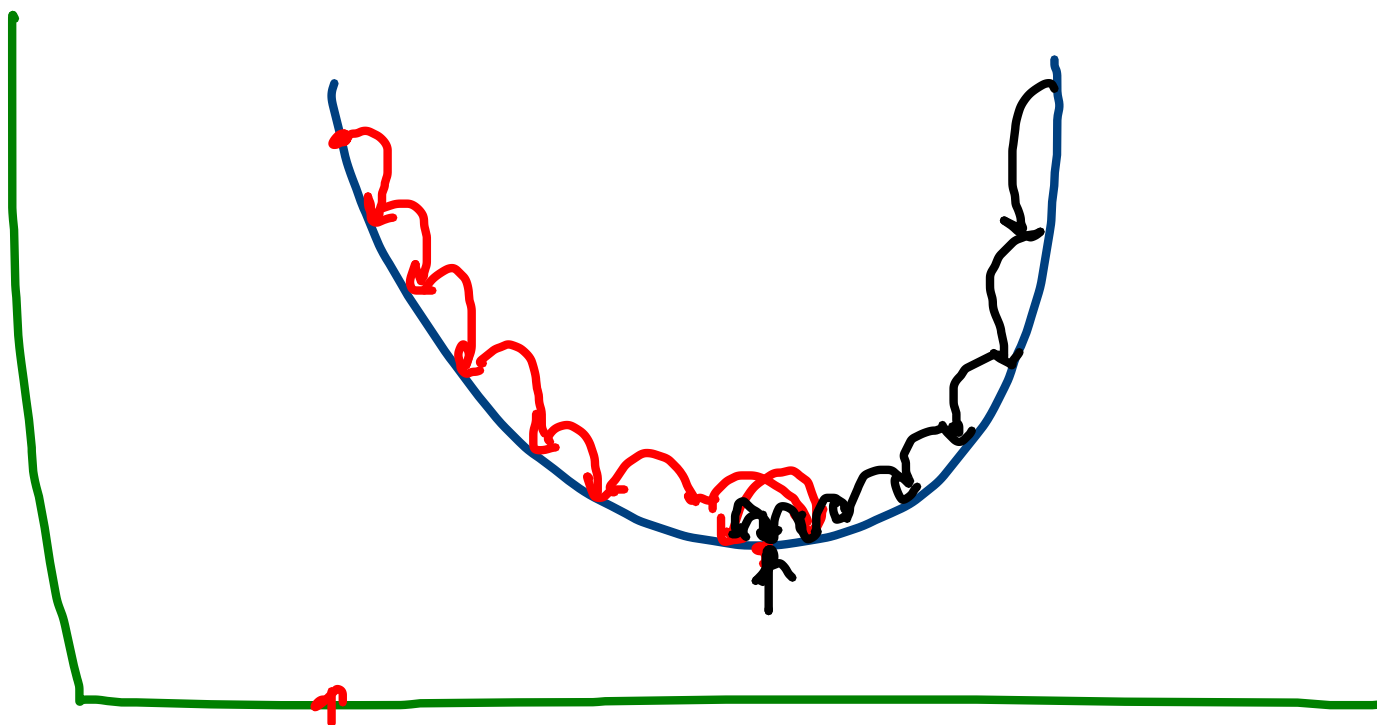
$$M_2 = M_1 + v$$

$$M_3 = M_2 - (-v) = M_2 + v$$

$$M_4 = M_3 - (+v) = M_3 - v$$

$$\lambda = f(i)$$

$$\lambda = f(i)$$



$$\frac{d l(m)}{d n} = \frac{d}{d n} \left( \frac{1}{2} \sum \left( y - (mn+c) \right)^2 \right)$$

$$= \frac{1}{2} 2 (y - [mn+c]) \times (-n)$$

$$= - \frac{2}{2} n (y - mn - c)$$

lik equation  $\rightarrow y = m_1x + c$

3D

$$z = m_1x + m_2y + c$$

x	y
$x_1$	$y_1$
$x_2$	$y_2$

slopes  
 $[m_1, m_2, m_3, \dots, m_d]$

lik equation  $\rightarrow$

$$y = x_1m_1 + c_1 + x_2m_2 + c_2$$

$\downarrow$

$$y = x_1m_1 + x_2m_2 + c + x_3m_3 + \dots + x_dm_d$$

$x$		$y$
$x_1$	$x_2$	$x_3$
		$y$
5	8	7

$$\begin{bmatrix} u_1 & u_2 & u_3 \\ \mathbf{u} \end{bmatrix} \quad \begin{bmatrix} m_1 & m_2 & m_3 \\ \mathbf{m} \end{bmatrix}$$

$$\begin{bmatrix} u_1 & u_2 & u_3 \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \\ m_3 \end{bmatrix} \rightarrow \left[ u_1 m_1 + u_2 m_2 + u_3 m_3 \right]$$

$$\begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix} \quad \begin{bmatrix} m_1 \\ m_2 \\ m_3 \end{bmatrix}$$

$\mathbf{u}$        $\mathbf{m}$

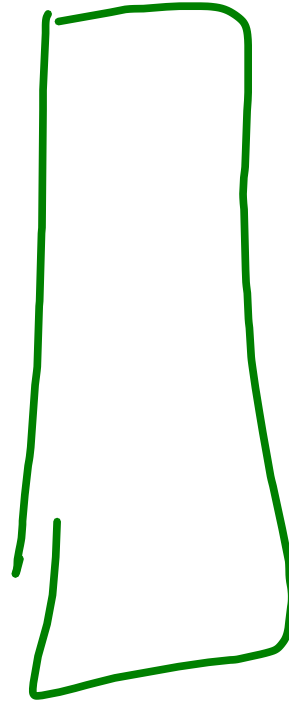
$$\mathbf{u}^T \mathbf{m}$$



$x$   $y$   
height age

$h_1$	$a_1$
$h_2$	$a_2$
$h_3$	$a_3$

$z$   
weight



$x_1$	$x_2$	$x_3$
1	2	3
2	1	4
7	8	3
4	2	1

$y$
12.4
13.3
42.5

$$y = 3x_1 + 2x_2 + 0x_3 + 5$$

$$3 \times 1 + 2 \times 2 + 0 + 5 = 3 + 4 + 5$$

$$3 \times 2 + 2 \times 1 + 0 + 5 = 6 + 2 + 5 = 13$$

$$3 \times 7 + 2 \times 8 + 0 + 5 = 42$$

$$\text{loss} = \min \left( \sum y_{\text{act}} - y_{\text{pred}} \right)$$

$$y = m_1 x_1 + m_2 x_2 + m_3 x_3 + c$$

$\uparrow$	$\uparrow$	$\uparrow$	$\uparrow$
3	2	0	5
3.2	2.1	0.3	5.2

$w \rightarrow (m_1, m_2)$

$$+ \lambda (w)^2$$

regularizer  $\rightarrow$

regularizer, L2 norm, Ridge

