

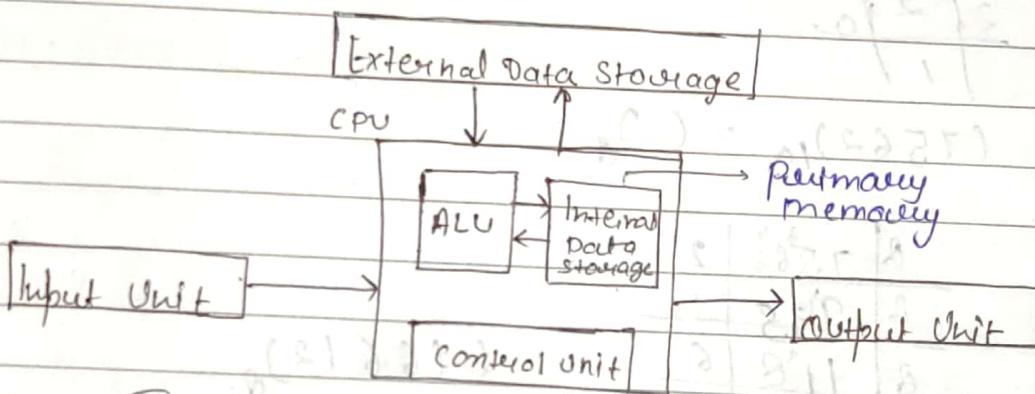
# Computer Organisation (BCSC 0005)

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Objective :-

- How computer Works
- What are different components in Computer.
- And how all those components are connected together to form a complete computer system.

## Secondary Memory



## • FUNCTIONAL BLOCKS OF COMPUTER

### → Number Representation

- Decimal
- Binary
- Octal
- Hexadecimal.

$$(i) \quad (100)_{10} = (?)_2 \\ = (1100100)_2.$$

$$\textcircled{1} \quad (175)_{10} = (?)_2.$$

$$\begin{array}{r|rr|l} 2 & 175 & 1 \\ \hline 2 & 87 & 1 \\ 2 & 43 & 1 \\ 2 & 21 & 1 \\ 2 & 10 & 0 \\ 2 & 5 & 1 \\ \hline 2 & 2 & 0 \\ \hline & 1 & \end{array} \quad (1010111)_2.$$

want quotient

$$\textcircled{2} \quad (7562)_{10} = (?)_8.$$

$$\begin{array}{r|rr|l} 8 & 7562 & 2 \\ \hline 8 & 945 & 1 \\ 8 & 118 & 6 \\ 8 & 14 & 6 \\ \hline & 1 & \end{array} \quad (16612)_8.$$

want quotient

$$\textcircled{3} \quad (1938)_{10} = (?)_{16}$$

$$\begin{array}{r|rr|l} 16 & 1938 & 2 \\ \hline 16 & 121 & 9 \\ \hline & 7 & \end{array} \quad (792)_{16}.$$

$$\textcircled{4} \quad (80)_{10} = (?)_3$$

$$\begin{array}{r|rr|l} 3 & 80 & 2 \\ \hline 3 & 16 & 1 \\ 3 & 5 & 2 \\ \hline & 1 & \end{array} \quad (1212)_3$$

$$\Rightarrow (1212)_3 = (?)_{10}$$

$$2 \times 10^0 + 2 \times 10^1 + 2 \times 10^2 + 1 \times 10^3$$

$$2 + 10 + 200 + 1000$$

$$\underline{+ 1000} \quad 2 \times 3^0 + 1 \times 3^1 + 2 \times 3^2 + 1 \times 3^3$$

$$\underline{\cancel{2} + \cancel{1} + \cancel{2} + \cancel{1}} \quad 2 + 3 + 18 + 27$$

$$2 + 3 + 18 + 27$$

$$(1212)_3 = (?)_{10}$$

$$\textcircled{V} \quad (41.6875)_{10} = (?)_2$$

$$\begin{array}{r} 2 | 41 | 1 \\ 2 | 20 | 0 \\ 2 | 10 | 0 \\ \hline 2 | 5 | 1 \\ 2 | 2 | 0 \\ \hline 1 \end{array} \quad (101001)_2$$

$$0 \cdot 6875 \times 2 = 1$$

$$0 \cdot 375 \times 2 = 0$$

$$0 \cdot 75 \times 2 = 1$$

$$(101001 \cdot 1011)_2 + 0 + 0 + 1$$

$$(11011)_2$$

$$\textcircled{VI} \quad (121)_8 = (?)_2$$

$$(001010001)_2$$

$$\textcircled{VII} \quad (A251)_{16} = (?)_2$$

$$(10100010010001)_2$$

$$\textcircled{VIII} \quad (121)_8 = (?)_{16}$$

$$8 \rightarrow 2 \rightarrow 16$$

## Questions:-

1). Convert:

a).  $(101110)_2 \rightarrow (\ )_{10}$

$$\begin{aligned}
 & 0 + 1 \times 2^1 + 1 \times 2^2 + 1 \times 2^3 + 0 + 1 \times 2^5 \\
 = & 2 + 4 + 8 + 32 \\
 = & (46)_{10}.
 \end{aligned}$$

b).  $(110110100)_2 \rightarrow (\ )_{10}$

$$\begin{aligned}
 & 0 + 0 + 1 \times 2^2 + 0 + 1 \times 2^4 + 1 \times 2^5 + 0 + 1 \times 2^7 + 1 \times 2^8 \\
 = & 4 + 16 + 32 + 128 + 256 \\
 \Rightarrow & (436)_{10}.
 \end{aligned}$$

c).  $(12121)_3 \rightarrow (\ )_{10}$

$$\begin{aligned}
 & 1 \times 3^0 + 2 \times 3^1 + 1 \times 3^2 + 2 \times 3^3 + 1 \times 3^4 \\
 = & 1 + 6 + 9 + 54 + 81 \\
 \Rightarrow & (151)_{10}.
 \end{aligned}$$

d).  $(4310)_5 \rightarrow (\ )_{10}$

$$\begin{aligned}
 & 0 + 1 \times 5^1 + 3 \times 5^2 + 4 \times 5^3 \\
 \Rightarrow & 5 + 75 + 500 \\
 \Rightarrow & (580)_{10}.
 \end{aligned}$$

e).  $(50)_7 \rightarrow (\ )_{10}$

$$\begin{aligned}
 & 0 + 5 \times 7^1 \\
 = & (35)_{10}.
 \end{aligned}$$

(f).  $(198)_{12} \rightarrow (?)_{10}$

$$8 \times 12^0 + 9 \times 12^1 + 1 \times 12^2$$

$$8 + 108 + 144$$

$$(260)_{10}$$

(g).  $(7562)_{10} \rightarrow (?)_8$

8	7562	?
8	945	1
8	118	6
8	14	6
	1	

$$(166)_{12},$$

(h).  $(1938)_{10} \rightarrow (?)_{16}$

16	1938	2
16	121	9
	7	

$$(792)_{16}, 2 + 1 \times 16 + 1 \times 16^2$$

$$(792)_{16}, 2 + 1 \times 16 + 1 \times 16^2$$

(i).  $(175)_{10} \rightarrow (?)_2$

2	175	1
2	87	1
2	43	1
2	21	1
2	10	0
2	5	1
2	2	0
	1	0

$$(10101111)_2.$$

(j).  $(FBA7C_2)_{16} \rightarrow (?)_2 \rightarrow (?)_8$

$(1111101110100111110000010)_2$ .

$(7672370_2)_8$ .

2):

9).  $(10110.0101)_2 \rightarrow (?)_{10}$ .

$$\begin{aligned}
 & 0 + 1 \times 2^1 + 1 \times 2^2 + 0 + 1 \times 2^4 \cdot 0 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} \\
 & 2 + 4 + 16 \cdot \cancel{0.25} + 0 \cdot 0.625 \\
 & (22 \cdot 3125)_{10}
 \end{aligned}$$

b).  $(16 \cdot 5)_{16} \rightarrow (?)_{10}$ .

$$\begin{aligned}
 & 1 \times 16^0 + 6 \times 16^1 \cdot 5 \times 16^{-1} \\
 & 6 + 96 \cdot 0 \cdot 3125 \\
 & (22 \cdot 3125)_{10}
 \end{aligned}$$

c).  $(26 \cdot 24)_{16} \rightarrow (?)_{10}$

$$\begin{aligned}
 & 6 \times 16^0 + 2 \times 16^1 \cdot 2 \times 16^{-1} + 4 \times 16^{-2} \\
 & 6 + 32 \cdot 0.125 + 0 \cdot 0.015625 \\
 & (38 \cdot 140625)_{10}
 \end{aligned}$$

3):

1).  $(33)_{10} \rightarrow (?)_2$ .

2	3	3	1
2	1	6	0
2	1	8	0
2	1	4	0
2	1	2	0
			1

$(100001)_2$ .

$$(100001)_2 \rightarrow (\ )_8 \Rightarrow (41)_8.$$

$$(41)_8 \rightarrow (\ )_{16}$$

$$\Rightarrow (101001)_2$$

$$\Rightarrow (29)_{16}.$$

2	41	1
2	20	0
2	10	0
2	5	1
2	2	0
		1

2).  $(1110101)_2 \rightarrow (\ )_{10}$

$$1 \times 2^9 + 0 + 1 \times 2^8 + 0 + 1 \times 2^4 + 1 \times 2^5 + 1 \times 2^6$$

$$1 + 4 + 16 + 32 + 64$$

$$\underline{(117)_{10}} \Rightarrow (165)_8 \Rightarrow (?)_{16}$$

$$(165)_8 \rightarrow (\ )_2 \Rightarrow (001110101)_2 \Rightarrow (75)_{16}.$$

$\Rightarrow$  Complement of a Number:-

$$x = (10)_{10}$$

9's complement  $\Rightarrow 99 - 10$

$$\Rightarrow 89$$

10's complement  $\Rightarrow$  9's complement + 1

$$\Rightarrow 89 + 1 = 100$$

$$\text{If } x = (1011)_2$$

1's complement  $\Rightarrow 1111$

$$\underline{0100}$$

$$\begin{array}{r} \text{2's complement :- } \\ \underline{0100} \\ + 1 \\ \hline \underline{0101} \end{array}$$

$$\Rightarrow x = 12389$$

9's complement  $\Rightarrow 99999$

$$\begin{array}{r} - 12389 \\ \hline \underline{87610} \end{array}$$

10's complement  $\Rightarrow$  87611

$$\Rightarrow x = 1011001$$

1's complement  $\Rightarrow 0100110$

2's complement  $=$  0100111

⇒ Rules for addition:-

$$0 + 0 = 0$$

$$0 + 1 = 1$$

$$1 + 0 = 1, \text{ carry } 0$$

$$1 + 1 + 1 = 1, \text{ carry } 1$$

Q)  $\begin{array}{r} 1011101 \\ + 1101101 \\ \hline 110111000 \end{array}$

Subtracted:-

~~$$\begin{array}{r} 11011101 \\ - 11011011 \\ \hline 00000010 \end{array}$$~~

Q) 
$$\begin{array}{r} 1101 \\ \times 010 \\ \hline 0000 \\ 1101 \times \\ 0000 \times \\ \hline 01110100 \end{array}$$

Q)  $10101.001$

1's  $\Rightarrow 01010.110$

2's  $\Rightarrow 01011.111$

(carry will be discarded)

Q)  $(1010.110)_10$

9's complement  $\Rightarrow 9999$

$$- 1010$$

$$\underline{(8989)}$$

$$+ 1$$

$$\underline{\underline{8990}}$$

$$999$$

$$- 110$$

$$\underline{889}$$

$$+ 1$$

$$\underline{\underline{890}}$$

My Write is My Future  $\Rightarrow 8990$

$$(8990.890)_10$$

(b)

2's complement  $(1010 \cdot 110)_{10}$

$$(1010)_{10} \rightarrow (?)_2$$

2	1010	0
2	505	1
2	252	0
2	126	0
2	63	1
2	31	1
2	15	1
2	7	1
2	3	1
1	0	0

$$(111110010)$$

2	110	0
2	55	1
2	27	1
2	13	1
2	6	0
2	3	0
1	0	0

$$+10 \times 2 =$$

$$-220$$

multiply.

$$11011011 - 110 \Rightarrow (0001)$$

$$(111110010)$$

$$1's \Rightarrow 0000001101$$

$$2's \Rightarrow \underline{0000001101} + 1$$

$$\underline{\underline{0000001101}}$$

$$1's \Rightarrow 0110011$$

$$2's \Rightarrow \underline{0110011} + 1$$

$$\underline{\underline{0110010}}$$

$$0000(0110 \cdot 0110010).0.$$

$$(110 \cdot 111)_2$$

$$+10 \times 2 = 0$$

$$+220 \times 2 = 0$$

$$+440 \times 2 = 0$$

$$+880 \times 2 = 1$$

$$+660$$

}

$$(0001)$$

$\Rightarrow$  Integer Representation

0  $\rightarrow$  Unsigned representation (By default positive)

+10, -10  $\rightarrow$  Signed representation.  
magnitude.

for Binary number:-

0  $\rightarrow$  represents +ve number

1  $\rightarrow$  represents -ve number.

ex:- +10

$(\underline{0}1010)_2$

$\downarrow$  sign

-10

$(\underline{1}010)_2$

$\downarrow$  sign

1st Method.

→ 2nd method for representing a negative binary number:-

1's complement.

$$-10 \Rightarrow \cancel{+10} + 10 \Rightarrow 01010$$

1's complement  $\Rightarrow$

$$\begin{array}{r} 0 \\ 10101 \\ \hline 10101 \end{array}$$

→ 3rd method (2's complement).

$$-10 \Rightarrow +10 \Rightarrow 01010$$

$$1's \Rightarrow 10101$$

$$2's \Rightarrow \underline{+1}$$

$$\underline{10110}$$

(1)

$$\begin{array}{r} 2 | 32 \\ 2 | 16 \\ 2 | 8 \\ 2 | 4 \\ 2 | 2 \\ \hline & 0 \end{array}$$

$$(100000)_2$$

$$(010000)_2$$

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$$\rightarrow -32 \Rightarrow +32 \Rightarrow 01000000 \\ (11000000) \quad 1's \Rightarrow (10111111)$$

$$2's \Rightarrow (11000000)$$

$\rightarrow$  Subtraction of two n-digit no. using 10's complement  
Method:-

Ex:-  $M - N$

$M \rightarrow$  Minuend

$N \rightarrow$  Subtrahend.

$M \rightarrow 72532$

$N \rightarrow 13250$

$$M - N = 59282.$$

$\rightarrow 72532 + (10's \text{ complement of subtrahend})$

13250

$$\begin{array}{r} 99999 \\ - 83280 \\ \hline 86749 \\ + 1 \\ \hline 86750 \end{array} \rightarrow 72532$$

$$\begin{array}{r} & + 86750 \\ \hline \textcircled{1} 59282 \end{array}$$

Discard.

$\rightarrow N - M$

~~$$\begin{array}{r} 13250 \\ - 72532 \\ \hline - 59282 \end{array}$$~~
~~$$\begin{array}{r} 13250 \\ + 86750 \\ \hline 99900 \end{array}$$~~
~~$$\begin{array}{r} 99999 \\ - 86750 \\ \hline 13250 \end{array}$$~~
~~$$\begin{array}{r} 99999 \\ - 86750 \\ \hline 13250 \end{array}$$~~
~~$$\begin{array}{r} 99999 \\ - 86750 \\ \hline 13250 \end{array}$$~~

~~-13250 + (10's complement of 72532)~~

$$\begin{array}{r} 99999 \\ - 72532 \\ \hline 86749 \end{array}$$

~~$$\begin{array}{r} 13250 \\ + 86749 \\ \hline 100000 \end{array}$$~~

~~$$\begin{array}{r} (t) \\ 86750 \end{array}$$~~

→ N-M

$$\begin{array}{r} 13250 \\ - 72532 \\ \hline 59282 \end{array}$$

$$\begin{array}{r} 99999 \\ - 72532 \\ \hline 27467 \end{array}$$

$$\begin{array}{r} 13250 \\ + 27468 \\ \hline 40718 \end{array}$$

+ 1

$$\begin{array}{r} 27468 \\ \hline 2746811111 \end{array}$$

$$\begin{array}{r} 999990001 \\ - 407181010 \\ \hline 592811011 \end{array}$$

Because there is no carry generated so for finding the final value we have to find 10's complement.

$$\begin{array}{r} + 1 \\ - 89282 \end{array}$$

→ Four Binary Number System

$$X = 10101000$$

$$Y = 1000011$$

$$X - Y = X + (2^8 \text{ complement of } Y)$$

$$\begin{array}{r} 1111111 \\ - 1000011 \\ \hline 0111100 \end{array}$$

$$\begin{array}{r} 0111101 \\ + 1 \\ \hline \end{array}$$

$$\begin{array}{r} 10101000 \\ + 00111101 \\ \hline \end{array}$$

$$\begin{array}{r} 01000101 \\ \hline \end{array}$$

discard.

$$\Rightarrow Y - X$$

$$Y - X = Y + (2^8 \text{ complement of } X).$$

$$\begin{array}{r} 1111111 \\ - 1010100 \\ \hline 0101011 \end{array}$$

$$\begin{array}{r} + 1 \\ \hline 0101100 \end{array}$$

$$\begin{array}{r} 1000011 \\ + 0101100 \\ \hline \end{array}$$

$$\begin{array}{r} 1101111 \\ \hline \end{array}$$

No carry.

Result is negative.

Again 2's complement

$$\begin{array}{r} 1111111 \\ - 1101111 \\ \hline 0010000 \end{array}$$

$$\begin{array}{r} + 1 \\ \hline \end{array}$$

$$\begin{array}{r} 0010001 \\ \hline \end{array}$$

Final answer

~~$-20 + (-10)$~~   
 ~~$-20 - 10$~~

Subtrahend will be reflected by seeing - sign before a number.  
i.e.  $-20 + 10$   
Subtrahend.

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→  $20 - 10 \rightarrow$  Subtraction by using 2's complement.

$$\begin{array}{r} 2 | 20 | 0 \\ 2 | 10 | 0 \\ \hline 2 | 5 | 1 \\ 2 | 2 | 0 \\ \hline 1 | 1 | \end{array}$$

$$(10100)_2.$$

$$\begin{array}{r} 2 | 10 | 0 \\ 2 | 5 | 1 \\ \hline 2 | 2 | 0 \\ \hline 1 | \end{array}$$

$(01010)_2$ .

$$(10100) - (01010).$$

$$20 + (2^{\text{'s complement of }} 01010)$$

$$\begin{array}{r} 10101 \\ + 1 \\ \hline 10110 \end{array}$$

$$\begin{array}{r} 10100 \\ + 1010 \\ \hline 101010 \end{array}$$

$$\begin{array}{r} 01010 \\ - 1 \\ \hline 10 \end{array}$$

(I)  $(+6) + (+13)$

$$\begin{array}{r}
 6 \\
 +13 \\
 \hline
 19
 \end{array}
 \Rightarrow 19.$$

(II)  $(-6) + (+13)$

$13 + (10^b \text{ complement of } 6)$ .

$$\begin{array}{r}
 9 \\
 -6 \\
 \hline
 3 \\
 +1 \\
 \hline
 4
 \end{array}$$

$$\text{.}(011010) - (001011)$$

$$-\cancel{+} 4$$

$$\text{.}(001010) - (\cancel{1}) - 2^6$$

(III)

$(+6) + (-13)$

$6 + (10^b \text{ complement of } 13)$ .

$$\begin{array}{r}
 99 \\
 -13 \\
 \hline
 86 \\
 +1 \\
 \hline
 87
 \end{array}$$

$$\begin{array}{r}
 13 \\
 + \cancel{87} \\
 \hline
 \cancel{00}
 \end{array}$$

$$\begin{array}{r}
 \cancel{87} \\
 + 6 \\
 \hline
 93
 \end{array}$$

Discard.

$$\begin{array}{r}
 99 \\
 -93 \\
 \hline
 -7
 \end{array}$$

(IV)  $(-6) + (-13)$ .

(v)

$$(-6) - (-13)$$

$$(-6) + (+13)$$

$13 + (2^6 \text{ complement of } 6)$

$$\begin{array}{r}
 & 9 \\
 -6 & \\
 \hline
 3 & \\
 \hline
 1 & \\
 4 & \\
 \hline
 \end{array}
 \quad
 \begin{array}{r}
 & 13 \\
 -4 & \\
 \hline
 7 \\
 \hline
 \end{array}$$

Using Binary :-

Arithmetical Addition and Subtraction

always using 2's complement representation.

$$(i) (-6) + (+13)$$

$$-6 \Rightarrow +6 \Rightarrow 00110$$

$$+13 \Rightarrow \underline{01101}$$

sign

$$00110$$

$$1's \text{ comp} - 11001$$

$$+1$$

$$2's \text{ complem } \underline{11010} \Rightarrow -6$$

$$+13 \rightarrow \underline{01101}$$

$$\underline{11010}$$

$$\underline{\underline{00111}}$$

Discarded

$$\Rightarrow +7$$

$$01101$$

$$1's \text{ comp} - \underline{10010}$$

$$+1$$

$$2's \text{ complem } \underline{10011}$$

(ii)  $+6 + (-13)$   
 $+6 \rightarrow 00110$

$+13 \rightarrow 01101$

1's comp  $\rightarrow 10010$

$$\begin{array}{r} +1 \\ \hline 10011 \end{array} \Rightarrow -13.$$

$$\begin{array}{r} 00110 \\ + 10011 \\ \hline \end{array} -$$

$$\underline{01001} \rightarrow \text{Again 2's comp}$$

Sign will be  $00110$   
 decided here.

$$\begin{array}{r} +1 \\ \hline 00111 \end{array} = -7$$

(iii)  $(+6) - (-13)$

$+6 \rightarrow 00110 \Rightarrow -6 \Rightarrow 11010$

$+13 \rightarrow 01101$

1's comp  $10010$

+1

$$\underline{10011} \Rightarrow -13.$$

$6 + (\text{2's complement of } 13)$

$$\begin{array}{r} 11111 \\ - 10011 \\ \hline 01100 \end{array}$$

$$\begin{array}{r} 11011 \\ + 01100 \\ \hline 10010 \end{array}$$

ans 1

$(11010) - (10011)$

$\rightarrow 2^4$  complement

$$\begin{array}{r}
 10011 \\
 1'8an \quad 01100 \\
 +1 \\
 \hline
 01101
 \end{array}
 \quad
 \begin{array}{r}
 11010 \\
 +01101 \\
 \hline
 100111
 \end{array}
 \quad
 +\textcircled{7}$$

Discard.

→ Overflow

unsigned Number.

$$x = 10010101$$

$$y = 10101010$$

$$\underline{10011111}$$

↓ And carry → Overflow is happening.

Signed Number

carry from sign bit → carry on sign bit

$$(1) \quad x = \overset{0}{\cancel{1}}010101$$

$$\begin{array}{r}
 01101010 \\
 \hline
 10111111
 \end{array}$$

Overflow is happening. because

carry on sign bit and carry from sign bit are different.

$$\begin{array}{r}
 \overset{1}{0} \overset{0}{0}0101011 \\
 \hline
 01000011 \\
 01101100
 \end{array}$$

no overflow because carry on sign bit and carry from sign bit are same.

→ fixed & floating point Representation of a number:-

•  $325.08$       exponent  
 ↳  $M \times e$       → scientific representation of  
 ↓      Base  
 Mantissa  
 $0.32508 \times 10^3$

•  $(11011.001)_2$ .

$$\Rightarrow 0.11011001 \times 2^5$$

→ Normalization.

$$001001.001 \Rightarrow 0.001001001 \times 2^6$$

$$\Rightarrow 0001001001 \times 2^4$$

$$\underline{01001001,0100}$$

(i)  $0.0000101101$

$$\Rightarrow 0.101101 \times 2^4$$

(ii)  $0110110101$

$$\Rightarrow 0.1101110101 \times 2^7$$

(iii)  $101.091 \times 2^{-2}$

$$\Rightarrow 0.101011 \times 2.$$

- ① Represent 1101011 in the floating point representation using 32-bit word length (including mantissa and exponent). Assume that 24 bit represent mantissa and 8 bits represents exponent.

$1101011 \cdot 0$   
 $\Rightarrow 0.1101011 \times 2^7 \rightarrow 0111 \rightarrow 00000111$

Mantissa → < 24 bit ← | Exponent  
 [ 11010110000 - 00100000111 ] ← 8 bit →  
 | sign. | 32-bit |

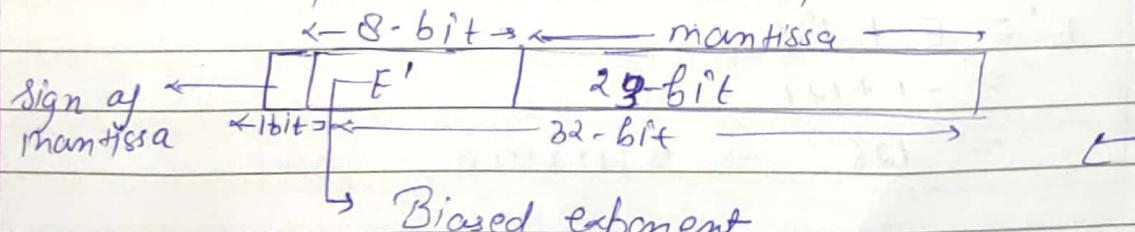
②  $-105 \Rightarrow -1101001$   
 ← 24-bit → ← 8-bit →  
 [ 1101001000 - 00100000111 ]  
 | sign. |

2	105	1
2	22	0
2	11	1
2	5	1
2	2	0
		1

## # IEEE Standard for floating point number Representation

- ① 32-Bit representation (Single precision)

- ② 64-bit representation (Double precision)



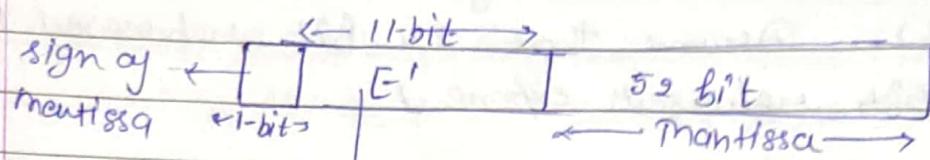
$$E' = E + 127 \text{ (Biased Value)}$$

$$(2^{E'-1} - 1) \Rightarrow (2^{E-127} - 1)$$

$$\Rightarrow 128 - 1$$

$$\Rightarrow 127.$$

## → 64-bit Representation.



$$E' = E + 1023$$

$$\begin{aligned} & (2^{e-1}-1) \\ \Rightarrow & (2^{11}-1) \\ = & 2^{10}-1 \\ \Rightarrow & 1023. \end{aligned}$$

(a) Represent -0.875 decimal in IEEE 754 floating point representation.

$$\begin{aligned} & \Rightarrow (-0.875)_{10} \\ & \Rightarrow (-0.111)_2 \end{aligned}$$

$$\begin{aligned} 0.875 \times 2 &= 1 \\ 0.750 \times 2 &= 1 \\ 0.500 \times 2 &= 1 \\ &\vdots \\ & 0.000 \end{aligned}$$

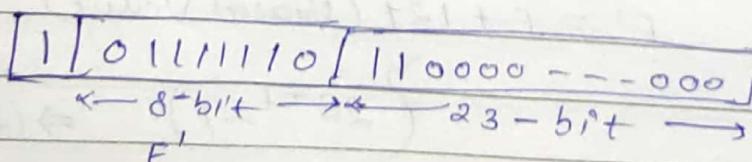
Value represented as  $\pm 1 \cdot M \times 2^e$

$$\Rightarrow -1 \cdot 11 \times 2^{-1}$$

$$E = -1$$

$$\begin{aligned} E' &= E + 127 \\ &= -1 + 127 \\ &= 126. \end{aligned}$$

Exponent value is always +ve.



## → Addition &amp; Subtraction

Operation      Add.  
magnitude

$$(+A) + (+B) \quad +(A+B)$$

$$(+A) + (-B)$$

$$(-A) + (+B)$$

$$(-A) + (-B) \quad -(A+B)$$

Subtraction, magnitude.

$$A > B$$

$$A < B$$

$$A = B$$

$$+(A-B)$$

$$-(A-B)$$

$$+(A-B) = 0$$

$$-(A-B)$$

$$+(A-B)$$

$$+(A-B)$$

$$(+A) - (+B)$$

$$+(A-B)$$

$$-(A-B)$$

$$(+A) - (-B) \quad + (A+B)$$

$$(-A) - (+B) \quad -(A+B)$$

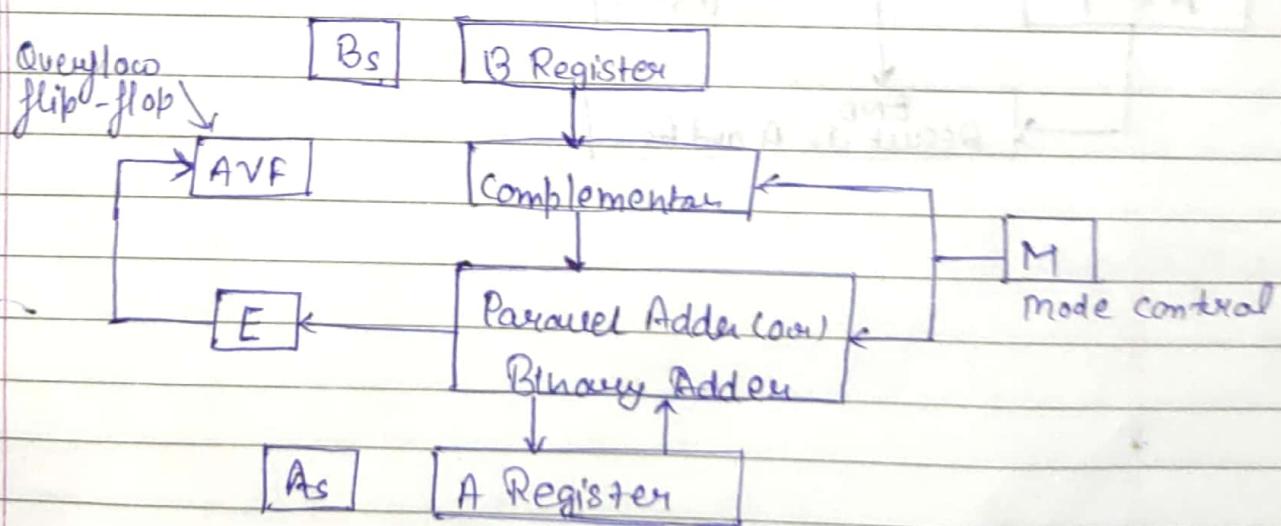
$$(-A) - (-B)$$

$$-(A-B)$$

$$+(A-B)$$

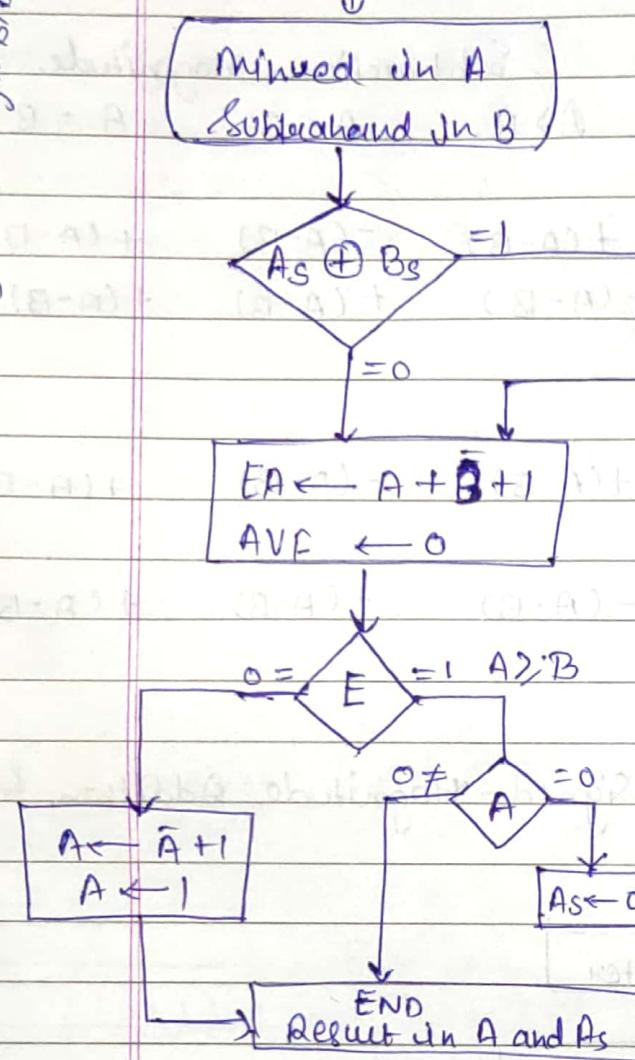
$$+(A-B)$$

# Hardware Required for Signed-Magnitude Addition & Subtraction :-



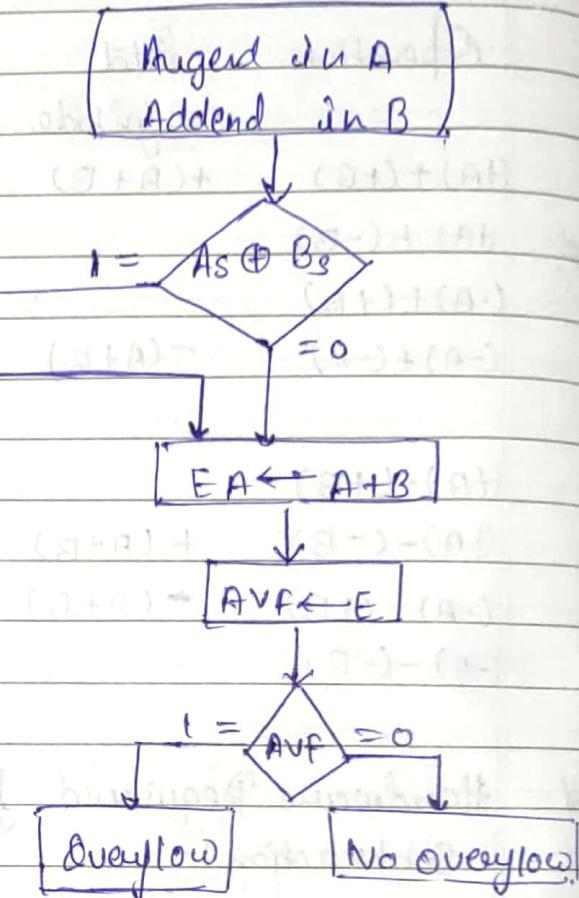
### Subtraction Operation

$A_s$  and  $B_s$  - sign 1276.



### Addition Operation

Augend in A  
Addend in B



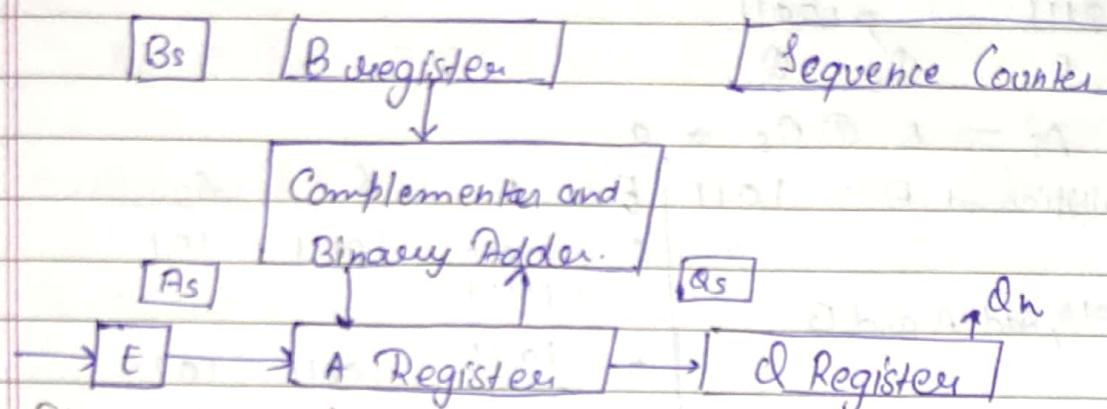
→ Multiplication Algorithm:-  
Hardware required.

$$++ = 0$$

$$-- = 0$$

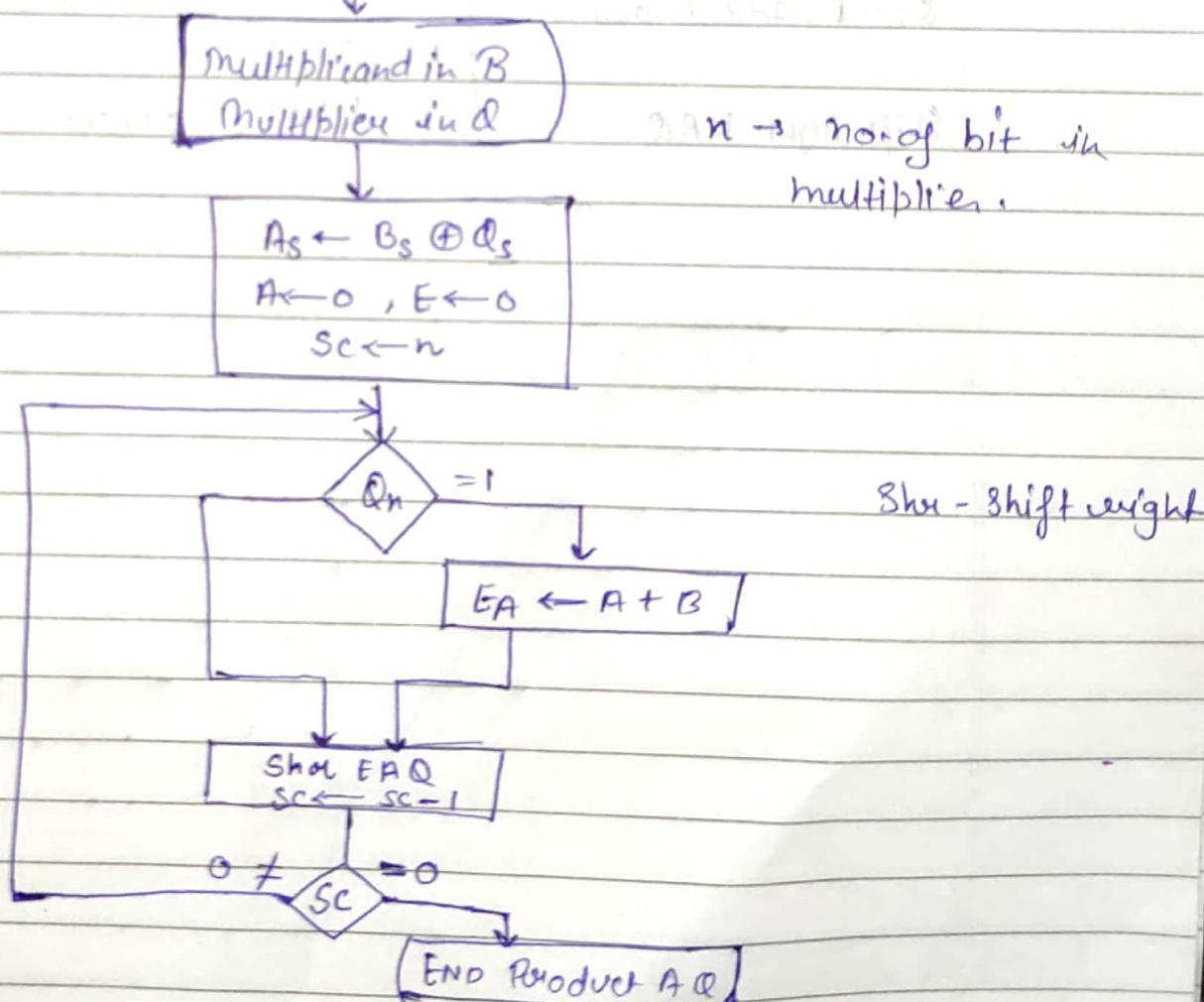
$$+- = -1$$

$$-+ = 1$$



- Flow chart for Multiplication operation

Multiply operation



64 32 16 8 4 2

→ Multiply:-

①  $+23$  and  $+19$   
 $\begin{array}{r} 01011 \\ \times 10011 \\ \hline 0s \quad Qs \end{array}$

$A_s \rightarrow B_s + Q_s \rightarrow 0$   
multiplicand  $B = 1011$

$Q_n=1$ , Add A and B

Shift Right EAQ

$Q_n=1$ , Add A and B

Shift Right RAQ

	E	A	Q	Sc
0	00000	10011	101	
	+ 10111			
0	10111	10011	101	
0	01011	11001	100	
	+ 10111			
1	00010	11001	011	
	+ 10001			
	10001	01100	011	

(11) (+3) and (+4)

$$\begin{array}{r} 0011 \\ \times 0100 \\ \hline B_s \quad D_s \end{array}$$

$$B_s \oplus D_s = 0 \text{ (+ve)}$$

$$\text{Multiplicand } B = 011 \quad E \quad A \quad Q \quad S_c \quad ? \text{ 3-binary}$$

$$0 \quad 000 \quad 100 \quad 011$$

$Q_n = 0$ , shift right EAD

$Q_n = 0$ , shift right " 0100 0 000 010 000

$Q_n = 1$ , Add B and D

$$+ 011 \quad 001 \quad 001$$

Shift right EAD

$$0 \quad 001 \quad 100 \quad 000$$

$$10001100$$

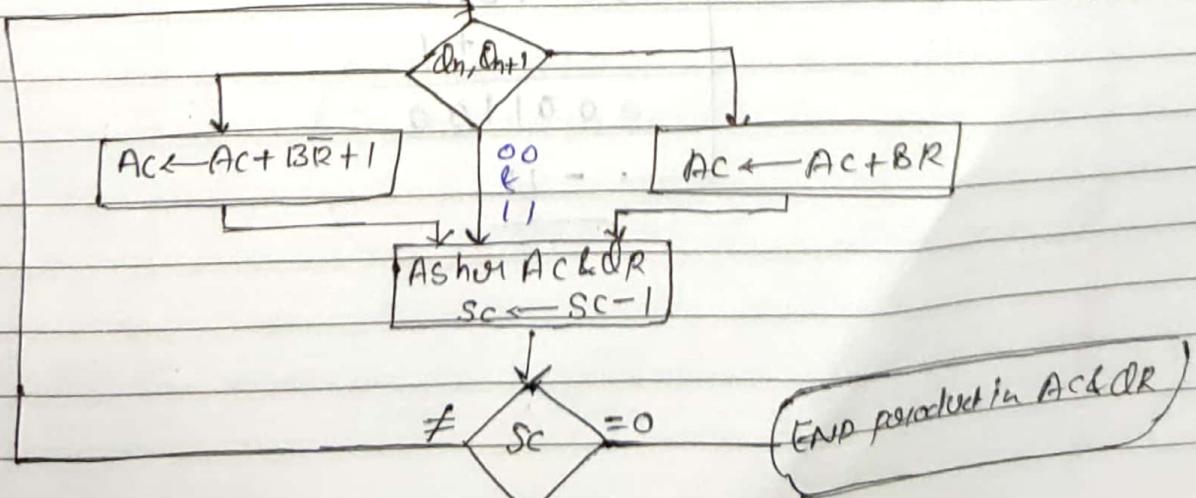
Sign 0 3 12.  $\Rightarrow +12$

## # Flow chart for Booth Algorithm :-

Multiply

(multiplicand in BR) - ve numbers stored in  
 (multiplier in DR) It's 2's complement form.

$AC \leftarrow 0$   
 $Count \leftarrow 0$   
 $S_c \leftarrow n$



$$\textcircled{1} \quad (-3) \times (+4)$$

$$\begin{array}{r} \downarrow \\ +3 \rightarrow 0011 \\ -3 \rightarrow 1101 \\ \downarrow \text{BR} \end{array}$$

OR.

$$(+7) \times (+4)$$

$$\begin{array}{r} \downarrow \\ 0010 \\ 0010 \\ \downarrow \\ (3+7)0 = 0010 \end{array}$$

$$\text{BR} = 1101$$

$$\text{BR} + 1 = 00110$$

$$\text{AC} = 1 \text{ Q.R}$$

$$Q_{n+1}$$

$$\text{Sc}$$

$$\begin{array}{r} 0000 \\ 0000 \\ 1101 \\ 0000 \\ 0001 \\ 0001 \\ 0011 \\ 0001 \end{array}$$

$$0000$$

$$0100$$

$$0$$

$$100$$

$$0000 \quad 0010$$

$$0$$

$$011$$

$$1101$$

$$0000$$

$$0$$

$$010$$

$$1000$$

$$0001$$

$$0$$

$$010$$

$$1000$$

$$0001$$

$$0$$

$$010$$

$$0011$$

$$0001$$

$$0$$

$$B_{n+1} \Rightarrow \text{subtract BR from AC}$$

$$0011$$

$$\text{Ashur AC \& QR}$$

$$1000$$

$$1000$$

$$1000$$

$$001$$

$$\rightarrow Q_n = 0, Q_{n+1} = 1 \quad + \underline{1101}$$

$$1110$$

$$1000$$

$$1$$

$$\text{Ashur AC \& QR}$$

$$0111$$

$$0100$$

$$0$$

$$000$$

$$\begin{array}{r} 1110100 \\ 0001011 \\ + 1 \\ \hline 0001100 \\ - 12 \\ \hline \end{array}$$

(11)  $(+17) \times (-6) \rightarrow$  Booth Algorithm.

$$\begin{array}{r} 010001 \\ \downarrow \qquad \downarrow \\ \text{Multiplicand} \quad 1's \quad 1010 \\ \downarrow BR \qquad \qquad \qquad +1 \\ -6 \Rightarrow 1010 \end{array}$$

→ Multiplier. → QR

$$AC = 0 \quad Q_{n+1} = 0 \quad SC \Rightarrow 100.$$

$$\bar{BR} + 1 = 101111$$

$\bar{BR} = 010001$	$AC$	$QR$	$Q_{n+1}$	$SC$
Initialization	000000	1010	0	100

$$Q_n = Q_{n+1} = 0$$

Push AC & QR	000000	0101	0	011
--------------	--------	------	---	-----

$$Q_n = 1 \& Q_{n+1} = 0 + \underline{\underline{101111}}$$

Add $\bar{BR} + 1$ in AC	000001	0101	0
--------------------------	--------	------	---

Push AC & QR	110011	1010	1	010
--------------	--------	------	---	-----

$$Q_n = 0, Q_{n+1} = 1 + \underline{\underline{010001}}$$

Add $\bar{BR} + 1$ in AC	001000	1010	1
--------------------------	--------	------	---

Push AC & QR	001000	0101	0	001
--------------	--------	------	---	-----

$$Q_n = 1 \& Q_{n+1} = 0 + \underline{\underline{101111}}$$

Add $\bar{BR} + 1$ in AC	110011	0101	0
--------------------------	--------	------	---

Push AC & QR	111001	1010	1	000
--------------	--------	------	---	-----

$$\begin{array}{r}
 1110011010 \\
 1's - 001100101 \\
 \hline
 1001100110 \rightarrow -102.75
 \end{array}$$

48  
32  
80

Qn  $(-10) \times (+20)$

## # Registers

Group of flip-flops is known as Register.

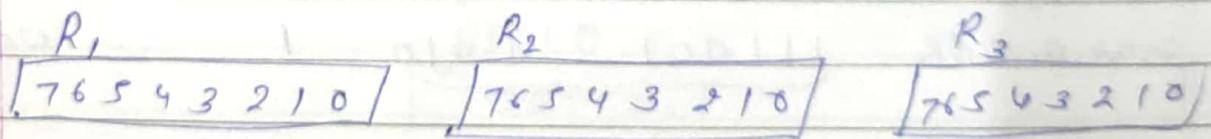
→ Two types:-

- 1). General Purpose Registers.
- 2). Special Purpose Registers.

→ Types of Special Purpose Registers.

- MDR (Memory Data Register)
- MAR (Memory Address " )
- AC (Accumulator)
- IR (Instruction Register)
- PC (Program Counter)
- TR (Temporary Register)
- INPR (Input Register)
- OUTR (Output " )

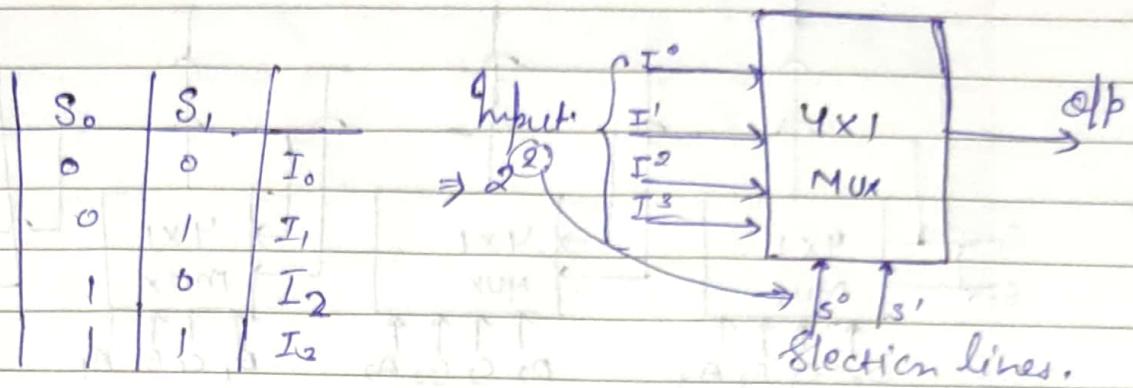
## # Register Transfer Language.



- 1).  $R_1 \leftarrow R_2$  (copy data of  $R_2$  in  $R_1$ )
- 2).  $R_3 \leftarrow R_1 + R_2$  (copy data of  $R_1 + R_2$  in  $R_3$ )
- 3). If ( $P$  is true)
  - ↳ Condition
  - ↳  $P: R_1 \leftarrow R_2$ .

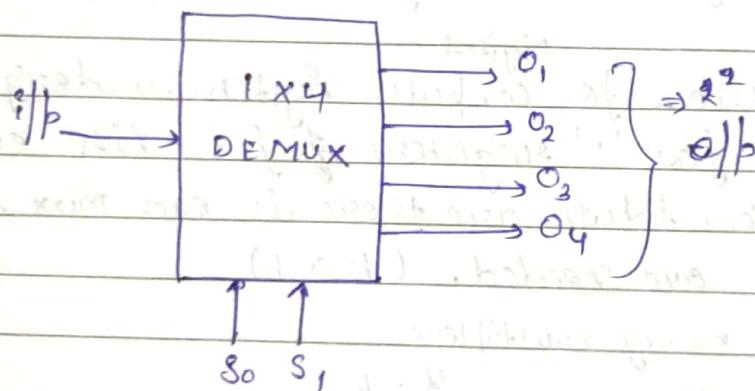
## ⇒ Multiplexer

Multiple input and Single Output:

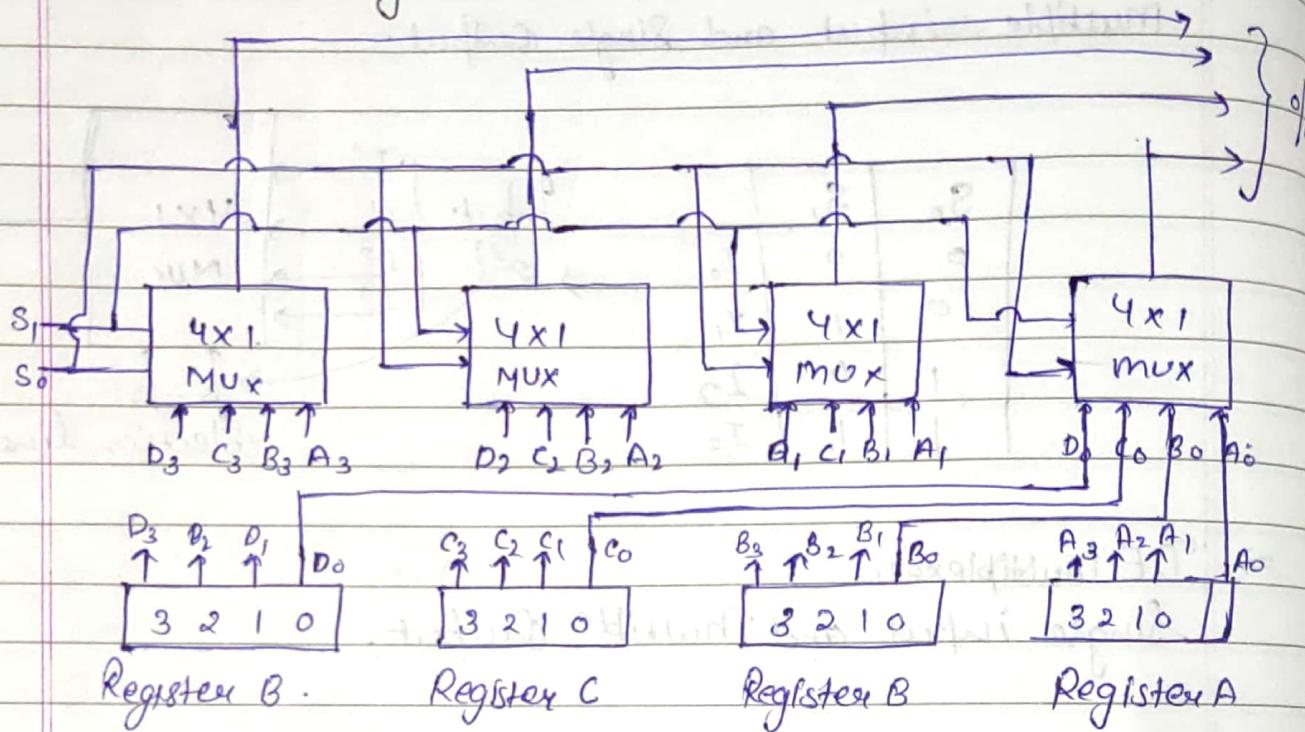


## ⇒ DE Multiplexer.

Single input and Multiple Output.



⇒ Common Bus System.



Ques. A common Bus System for computer system is designed using multiplexers for  $k$  registers of  $n$ -bits each.

- (i) How many selection inputs are there in each mux.
- (ii) What size of mux are needed. ( $K \times 1$ )

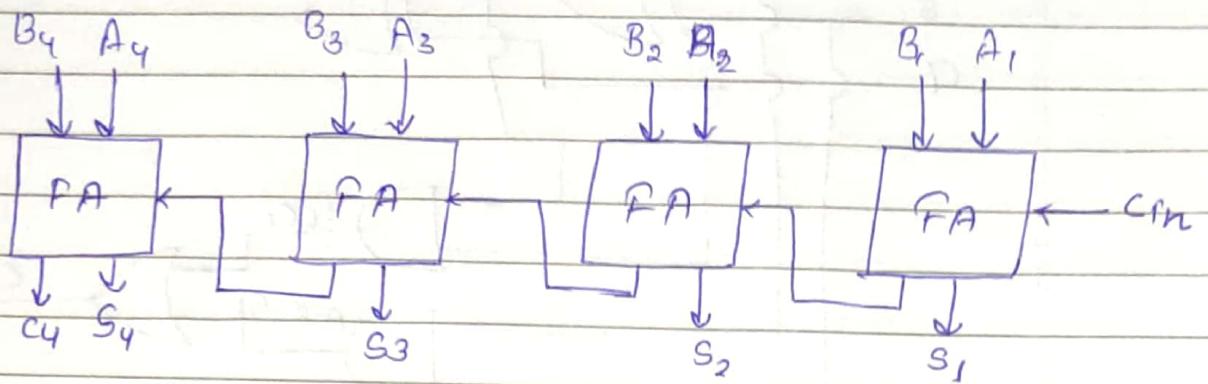
No. of bits  $\Rightarrow$  No. of Multiplexers.

Selection lines  $\rightarrow 2^x = k$

$$x = \log_2 k$$

⇒ Carry look Ahead Adder.

4-bit binary Adder.



The general strategy of designing fast adder or carry look ahead adder is to reduce the time required to form carry signal.

A	B	Ci	Sum	Carry (Ci+1)
0	0	0	0	0 } No carry
0	0	1	1	0 }
0	1	0	1	0 } carry propagate
0	1	1	0	0 } Ci = Couti
1	0	0	1	0 }
1	0	1	0	1 }
1	1	0	0	1 } carry generate.
1	1	1	1	1 }

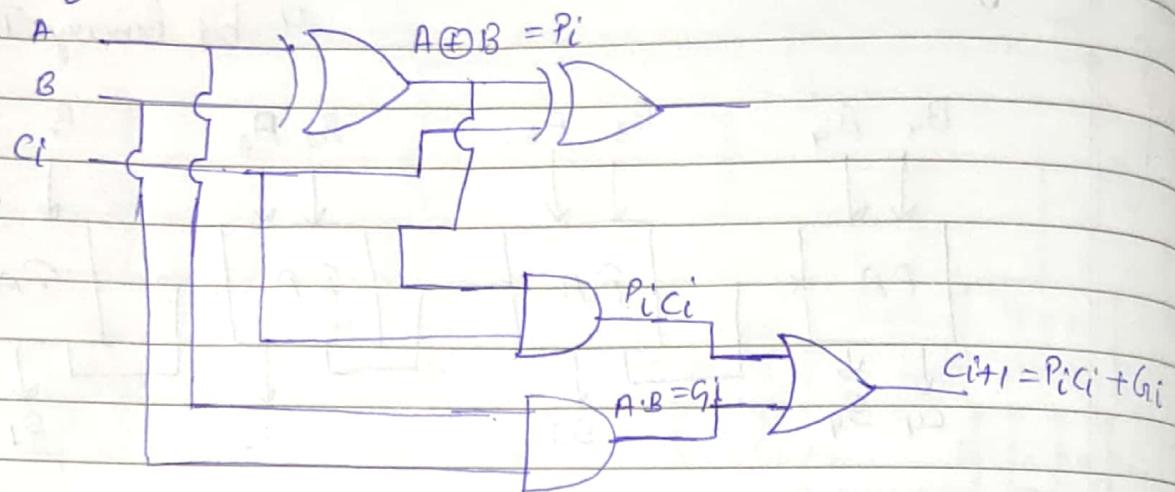
Carry Generate

$$\begin{aligned}
 Gi &= ABC\bar{C} + ABC \\
 &= AB(\bar{C} + C) \\
 &= AB
 \end{aligned}$$

Carry propagate

$$\begin{aligned}
 Pi &= \bar{A}B\bar{C} + \bar{A}Bc + AB\bar{C} + A\bar{B}C \\
 &= \bar{A}B(\bar{C} + C) + A\bar{B}(\bar{C} + C) \\
 &= \bar{A}B + A\bar{B} \Rightarrow A \oplus B
 \end{aligned}$$

## Carry look Ahead Adder.



$$C_{i+1} = P_i C_i + G_i$$

$i=0$

$$C_1 = P_0 C_0 + G_0$$

$$(A_0 \oplus B_0) \cdot C_0 + A_0 B_0$$

$i=1$

$$C_2 = P_1 C_1 + G_1$$

$$(A_1 \oplus B_1) \cdot C_1 + A_1 B_1$$

$$= A_1 \oplus B_1 [(A_0 \oplus B_0) \cdot C_0 + A_0 B_0] + A_1 B_1$$