

Digital Communication (UEC-639)

Tutorial-4

Dr. Amit Mishra

Question-1

Given an audio waveform

$$f(t) = 3 \sin(500t) + 4 \sin(1000t) + 4 \sin(1500t)$$

find the signal to quantization noise ratio if this is coded using delta modulation for sampling at

- a) Nyquist rate
- b) 32 times of Nyquist rate

Comment which one among 'a' and 'b' is practically suitable

Solution-1 (a)

Signal is $f(t) = 3 \sin(500t) + 4 \sin(1000t) + 4 \sin(1500t)$

Therefore signal power is

$$S = \frac{3^2 + 4^2 + 4^2}{2} = 20.5$$

In delta modulation, the sampling period is flexible, the smaller is the sampling period, the smaller is the quantization error.

The maximum sampling period is at Nyquist rate, i.e.

$$T_{\text{max}} = \pi/1500.$$

$$\omega = 2\pi f_m = 1500$$

$$f_m = \frac{1500}{2\pi}$$

Now the slope of the signal is

$$f_s = \frac{1}{T_s} = 2 \times f_m$$

$$\frac{df}{dt} = 3 \times 500 \cos(500t) + 4 \times 1000 \cos(1000t) + 4 \times 1500 \cos(1500t)$$

The maximum slope is

$$\begin{aligned}\left.\frac{df}{dt}\right|_{\max} &= 3 \times 500 + 4 \times 1000 + 4 \times 1500 \\ &= 11500\end{aligned}$$

To ensure no overloading, we have

$$\frac{\Delta}{T_s} \geq \left.\frac{df}{dt}\right|_{\max}, \quad \text{i.e.} \quad \Delta \geq 11500T_s$$

where Δ is the quantization step-size.

quantization noise power is

$$\begin{aligned}N_q &= \frac{\Delta^2 \omega_m T_s}{6\pi} \\ &= \frac{(11500T_s)^2 (1500T_s)}{6\pi}\end{aligned}$$

We know that : $T_{s\max} = \pi/1500$

At Nyquist rate,

$$N_q = 11500 \times 11500 \times 1500 \times \frac{\pi^3}{1500^3} / (6\pi) \\ = 96.69$$

Therefore,

$$\frac{S}{N_q} = \frac{20.5}{96.69} = -6.74\text{dB}$$

This value is unacceptable.

Suppose, we increase the sampling rate 32 times, then

$$T_s = \pi / (32 \times 1500),$$

we have

$$\begin{aligned} N_q &= 11500 \times 11500 \times 1500 \times \frac{\pi^3}{1500^3} \times \frac{1}{32^3} / (6\pi) \\ &= 2.95 \times 10^{-3} \end{aligned}$$

At this sampling rate

$$\frac{S}{N_q} = \frac{20.5}{2.95 \times 10^{-3}} = 38.42\text{dB}$$

which is acceptable.

Question-2

Determine the output SNR of a DM system if input signal is given as

$$x(t) = \cos(2000 \pi t).$$

Assume sampling frequency 16 kHz, no slope overload condition.

Also determine the output if it is followed by a 4 kHz post reconstruction filter

Solution-2

We know that:

$$\frac{S}{N_q} = 3 \frac{f_s^3}{8 \pi^2 f_m^2 f_M}$$

Given $f_m = 1000 \text{ Hz}$, $f_s = 16000 \text{ Hz}$, $f_M = 4000 \text{ Hz}$

$$\frac{S}{N_q} = 3 \frac{(16 * 10^3)^3}{8 \pi^2 (10^3)^2 4 * 10^3}$$

$$= 38.94$$

$$= 15.9 \text{ dB}$$

Question-3

What is the data rate of DM system given in above question (Q2)?

What configuration is required for a PCM system to obtain same data rate?

Determine the SNR of this PCM system.

Solution-3

$$R_b = n \cdot f_s$$

(a) Since data is transmitted using one-bit quantizer,
so the data rate is 16 kbps

(b) For PCM, 16 kbps can be achieved by using following:

Case-1 Sampling frequency = $f_s = 8 \text{ kHz}$;

no of bit in encoder = $n = 2$;

SNR for this system is = $1.76 + 6.02 \cdot 2$
= 13.8 dB

Case-2

Sampling frequency = $f_s = 4 \text{ kHz}$;

no of bit in encoder = $n = 4$;

$$\begin{aligned}\text{SNR for this system is} &= 1.76 + 6.02 * 4 \\ &= 25.84 \text{ dB}\end{aligned}$$

Case-3

Sampling frequency = $f_s = 2 \text{ kHz}$;

no of bit in encoder = $n = 8$

$$\begin{aligned}\text{SNR for this system is} &= 1.76 + 6.02 * 8 \\ &= 49.92 \text{ dB}\end{aligned}$$

Question-4

Draw the block diagram of adaptive delta modulation system and explain the algorithm of step generation.

Consider a suitable example with different sample values.

Note: Every students has to consider a different example.

Solution-4

Attempt yourself.

Question-5

Consider a mid-rise uniform quantizer (quantization level = 8, step size $\Delta = 1 V$).

Find DPCM output to be coded for sampled sequence

$$\{0, 0.5, 1.5, 0.7, 1, 2.3, 3.5, 2.8\}$$

using first order prediction filter $\hat{m}[n] = m_q[n - 1]$

Solution-5

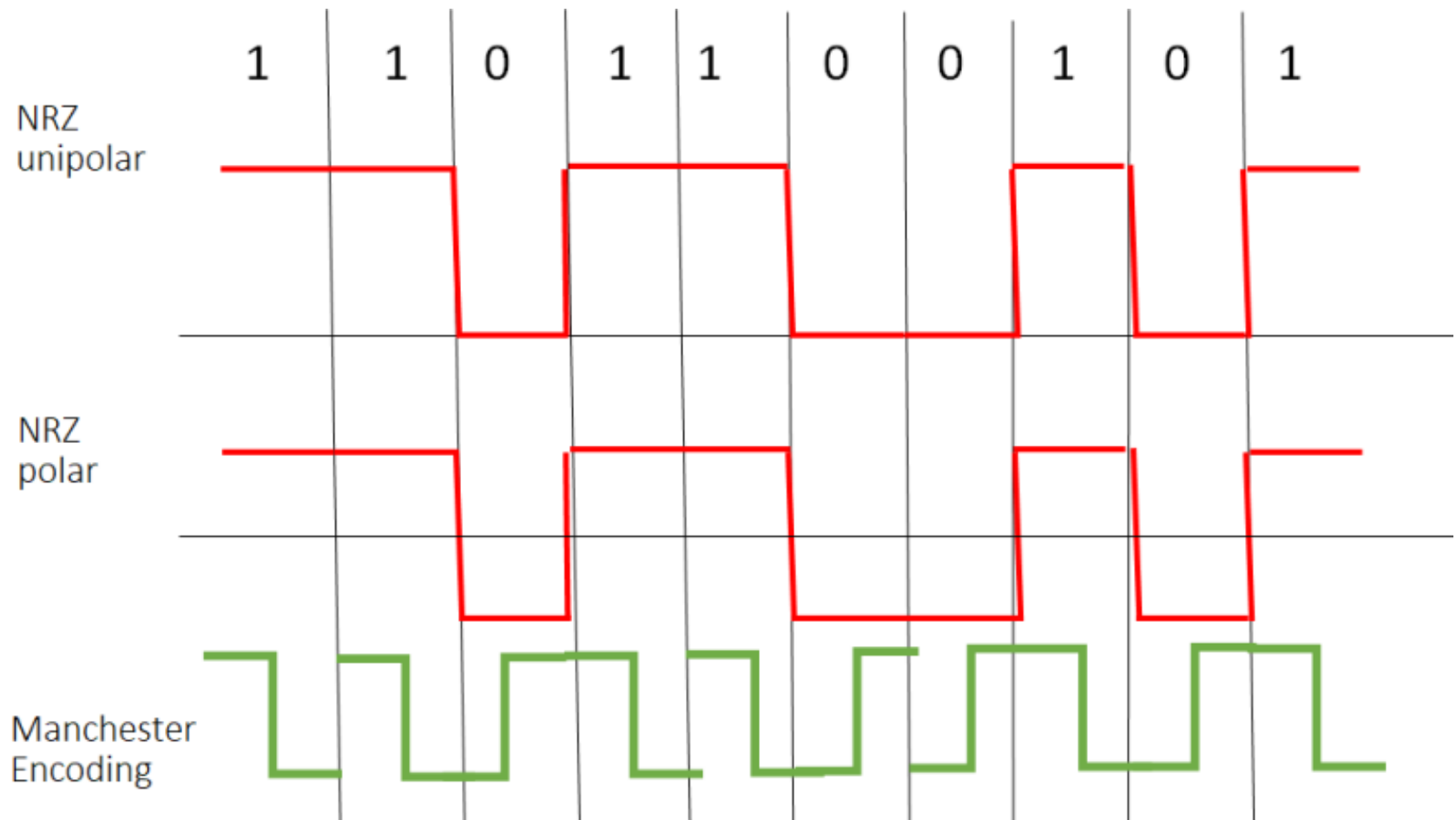
Attempt yourself.

Question-6

For a binary sequence 1101100101, draw the line coded waveform for the following signalling scheme

- a) NRZ unipolar
- b) NRZ bipolar
- c) NRZ polar
- d) Manchester coding

Solution-6



Thanks !