

⑤ Ambiguous Grammar & An Ambiguous grammar is a context free grammar for which there exist a string that can have more than one leftmost <sup>or rightmost</sup> derivation or parse tree.

Example →

$$X \rightarrow X + X \mid X * X \mid D$$

$$D \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$$

Now, Suppose we have to generate a string  $1 + 1 + 1$

Using Left Most Derivation

$$X \rightarrow X + X$$

$$X \rightarrow X + X + X$$

$$X \rightarrow D + X + X$$

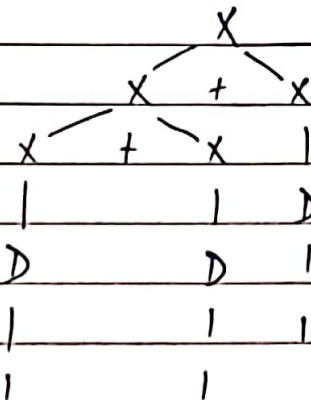
$$X \rightarrow 1 + X + X$$

$$X \rightarrow 1 + D + X$$

$$X \rightarrow 1 + 1 + X$$

$$X \rightarrow 1 + 1 + D$$

$$X \rightarrow 1 + 1 + 1$$



Using Right Most Derivation

$$X \rightarrow X + X$$

$$X \rightarrow X + X + X$$

$$X \rightarrow X + X + D$$

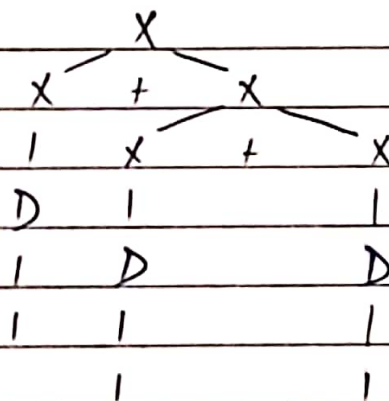
$$X \rightarrow X + X + 1$$

$$X \rightarrow X + D + 1$$

$$X \rightarrow X + 1 + 1$$

$$X \rightarrow D + 1 + 1$$

$$X \rightarrow 1 + 1 + 1$$



According to Definition we get two different parse tree for the same string with the same grammar.

Therefore we can conclude that given grammar is ambiguous.