Energy Systems Analysis

A.D. Smith 2019

Lecture 2. Review of General Thermodynamics of Energy Systems

"Economies, chemical reactions, ecosystems, and solar systems organize around energy gradients—natural differences in temperature, pressure, and chemistry that set up the conditions for energy flow."

— Eric D. Schneider & Dorion Sagan [3]

"Imperfection (friction, heat leaks, etc.) acts as a brake on the engines (the designs) that drive flow."

Bejan and Zane [1]

1 First Law

First Law, Closed System:

$$\Delta E = \Delta U + \Delta K E + \Delta P E = Q - W$$

Mass Conservation:

 $\dot{V} = V_{ave}A$ General: $m_{in} - m_{out} = \Delta m_{sys}$ $\dot{m} = \rho V_{avq} A$ (for uniform ρ)

First Law, Open System, per unit time:

$$\frac{dE}{dt} = \dot{Q} - \dot{W} + \sum_{i,j} \dot{m}(h + \frac{V^2}{2} + gz) \sum_{g,j} \dot{m}(h + \frac{V^2}{2} + gz)$$

Mass and Energy Balances, Steady State (Steady Flow) Process with negligible ΔKE , ΔPE :

$$\sum \dot{m}_{in} = \sum \dot{m}_{out}$$

$$0 = \dot{Q} - \dot{W} + \sum \dot{m}_i h_i - \sum \dot{m}_e h_e$$

First Law Simplifications

Closed system, heat transfer at constant volume:

$$\boxed{q_{ab} = u_b - u_a}$$
$$\boxed{q_{ab} = h_b - h_a}$$

Closed system, heat transfer at constant pressure:

 $w_{ab} = u_a - u_b$ Closed system, isentropic compression or expansion: (where a and b represent two states in the cycle.)

Open system, heat addition or rejection: $q = h_e - h_i$ Open system, isentropic compression or expansion: $w = h_i - h_e$

(where i and e represent inlet and exit states of a device in the cycle.)

First Law, Open System, Transient Process from state 1 to state 2 with negligible ΔKE , ΔPE :

$$(m_2u_2 - m_1u_1)_{system} = Q - W + \sum m_ih_i - \sum m_eh_e$$

1.1 Efficiency

First Law efficiency is a ratio between the benefit to us of a particular process (such as work) and the cost to us to run that process (such as thermal or chemical energy).

Heat Engines:

General efficiency:
$$\eta = \frac{W_{net}}{Q_{in}}$$
 Ideal cycle: $\eta = 1 - \frac{Q_{out}}{Q_{in}}$ Carnot cycle: $\eta = 1 - \frac{T_L}{T_H}$

Refrigerators:

$$\overline{\text{Coefficient of performance: } COP_R = \frac{Q_L}{W_{in}} \quad \text{Ideal: } COP_R = \frac{1}{Q_H/Q_L-1} \quad \text{Carnot: } COP_R = \frac{1}{T_H/T_L-1}$$

Heat Pumps:

Coeff. of performance:
$$COP_{HP} = \frac{Q_H}{W_{in}}$$
 Ideal: $COP_{HP} = \frac{1}{1 - Q_L/Q_H}$ Carnot: $COP_{HP} = \frac{1}{1 - T_L/T_H}$

2 Second Law

Clausius inequality:
$$\oint (\frac{\delta Q}{T}) \leq 0$$

Reversible (Ideal) Processes and the Property Entropy

Clausius definition of entropy:
$$S_2 - S_1 = \int (\frac{\delta Q}{T})$$
 Heat transfer: $Q = \int T dS$ per unit mass: $s = \frac{S}{m}$

Irreversible (Real) Processes

$$\frac{dS_{sys}}{S_2 - S_1 = \int (\frac{\delta Q}{T}) + S_{gen}} \qquad \Delta S_{sys} = S_{in} - S_{out} + S_{gen} \qquad \text{Rate form: } \frac{dS_{sys}}{dt} = \dot{S}_{in} - \dot{S}_{out} + \dot{S}_{gen}$$

Increase of entropy principle: $\Delta S_{sys,isolated} \geq 0$

Isentropic Efficiencies (Steady-flow Devices)

Turbines

$$\eta_t = \frac{w_a}{w_s} = \frac{h_1 - h_{2a}}{h_1 - h_{2s}}$$

Compressors and Pumps

$$\eta_c = \frac{w_s}{w_a} = \frac{h_{2s} - h_1}{h_{2a} - h_1}$$

$$\eta_p = \frac{w_s}{w_a} = \frac{h_{2s} - h_1}{h_{2a} - h_1} \approx \frac{v(P_2 - P_1)}{w_a}$$

Entropy Transfer

$$S_{heat} = \int (\frac{\delta Q}{T}) \approx \sum \frac{Q_k}{T_k}$$
 for each location k $S_{mass} = ms$

2.1 Efficiency

Second Law efficiency is a ratio between the performance of a particular device or system and the ideal theoretical performance for the same device or system.

$$\eta_{II} = rac{\eta_{th}}{\eta_{th,rev}}$$
 $\eta_{II} = rac{COP}{COP_{rev}}$

2.2 Entropy generation

Entropy generation is a quantitative measure indicating how irreversible an actual process is. See Chapter 7 of [2].

Entropy Balance

Closed:
$$S_2 - S_1 = \sum \frac{Q_k}{T_k} + S_{gen}$$

Open:
$$S_2 - S_1 = \sum \frac{Q_k}{T_k} + \sum m_i s_i - \sum m_e s_e + S_{gen}$$
 Rate: $\frac{dS_{sys}}{dt} = \sum \frac{\dot{Q}_k}{T_k} + \sum \dot{m}_i s_i - \sum \dot{m}_e s_e + \dot{S}_{gen}$

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2.3 Exergy destruction

Exergy destruction is proportional to entropy generation. The difference is that it's quantifying the *lost* available work, which is a measure of the reduction in (theoretically) available work due to the condition of the system and its surroundings. See Chapter 8 of [2].

3 Heat Transfer

Energy transferred due to a temperature difference falls under the category of heat transfer. I will assume you have familiarity with the basic modes of heat transfer (conduction, convection, and radiation) along with the fundamental equations describing them (Fourier's Law, Newton's Law of Cooling, Stefan-Boltzmann Law). This basic material is summarized in this video from LearnChemE: https://youtu.be/Nw0Z1tSe9hs.

For students who have not yet taken a heat transfer course, or those who want to refresh, I recommend:

- 1. Read the Topic of Special Interest section called "Mechanisms of Heat Transfer" at the end of the second chapter of our undergraduate thermo text [2].
- 2. Familiarize yourself with the idea of view factors as described in this video from LearnChemE: https://youtu.be/UIfRBB49MC4.

To begin connecting heat transfer concepts with building science, I recommend that you view this video on solar orientation from Solar Schoolhouse: https://youtu.be/OR8EQODWpPw.

4 Fluids

Energy and mass transferred due to fluid movement fall under the category of fluid mechanics. I will assume you have familiarity with the basic characteristics of a fluid and are able to formulate a control-volume analysis for a system with fluid flows. This basic material is summarized in this video from LearnChemE: https://youtu.be/-1DVqWmZ9tU. A simple control-volume mass conservation problem (solving for flow rate) is solved in this video from Water and Wastewater Courses: https://youtu.be/CzyWNamGizA.

Fluids are used to transfer energy to, from, and within buildings, primarily using just a few common fluid types:

- air
- water
- refrigerants

To begin connecting fluid flow concepts with building science, you will be assigned in the future to watch a video on HVAC systems from our first guest speaker, professional engineer Jane Guyer (https://youtu.be/Kt1j_aAApwg).

5 How thermodynamics affects energy systems analysis

The conservation laws that express the First Law and the limitations imposed by the Second Law are critical to include in a physics-based analysis. Energy conversion also has implications for the way that humans interact with energy systems, for the financial costs and benefits of energy systems, and for the environmental impacts of energy systems.

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References

- [1] A Bejan and J P Zane. Design in Nature: How the Constructal Law Governs Evolution in Biology, Physics, Technology, and Social Organizations. Knopf Doubleday Publishing Group, 2013. ISBN: 9780307744340.
- [2] Yunus Cengel and Michael Boles. *Thermodynamics: An Engineering Approach (Mechanical Engineering)*. en. 8 edition. McGraw-Hill Education, Jan. 2014. ISBN: 9780073398174.
- [3] Eric D Schneider and Dorion Sagan. Into the Cool: Energy Flow, Thermodynamics, and Life. en. University of Chicago Press, June 2005. ISBN: 9780226739366.