

# Effectively Using Public Data in Privacy Preserving Machine Learning

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## We Are Wasting The Public Data!

- State of the art differentially private models use public data! (and it is necessary in some settings!\*)
- Places we can use public data:

Augmentation

Pretraining

Training



Currently we only use it here!

Is this the *optimal* way of using the public data ?

## Public Data is Scarce!

- We should utilize the public data as much as possible!
- Augmentation helps! Let's do it better!
- Leverage generative models trained on public datasets for a powerful data augmentation strategy. Notably, diffusion models show exceptional performance, even when trained on smaller datasets
- Use *augmented* public data to improve:
  - Pre-training (**warm-aug**),
  - private training (**extended**).

| Setting  | Test Acc (%) |
|--|--------------|
| Baseline (WRN16-4) (cold)  | 64.9         |
| + Pretraining on the public data (warm)                                    | 68.1         |
| + Pretraining on the generated data using public data ( <b>warm-aug</b> )  | 72.0         |
| + Including the generated data in the training dataset ( <b>extended</b> ) | 73.7         |

## How To Use Public Data To Improve The Private Training?

How does DP-SGD work?

### Step 1

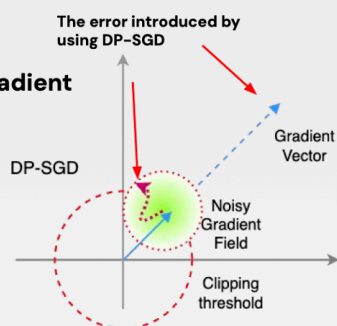
Take the per example gradient

### Step 2

Clip the gradient

### Step 3

Add noise



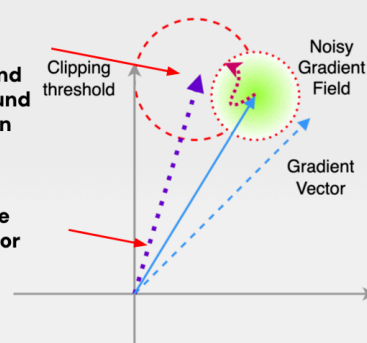
**Proposition** Let  $X$  and  $\Theta$  be example and model spaces and let  $\ell$  be a  $\mathcal{L}$ -lipschitz and  $r$ -concentrated loss function for  $X$  and  $\Theta$ . DOPE-SGD achieves  $(c \frac{\sqrt{q}}{\sigma} \sqrt{T \ln(1/\delta)} \ln(T/\delta), \delta)$ -DP, where as DP-SGD achieves  $(c \frac{\sqrt{q}}{\sigma} \sqrt{T \ln(1/\delta)} \ln(T/\delta), \delta)$ -DP, for a constant  $c$ , sampling rate  $q$ , and number of iterations  $T$  and sufficiently large  $\sigma$ .

| Epsilon | DP-SGD (pretraining) | DOPE-SGD (ours) |
|---------|----------------------|-----------------|
| 1       | 60.1%                | <b>72.1%</b>    |
| 2       | 68.1%                | <b>75.1%</b>    |
| 4       | 72.4%                | <b>77.9%</b>    |
| 6       | 77.1%                | <b>80.0%</b>    |

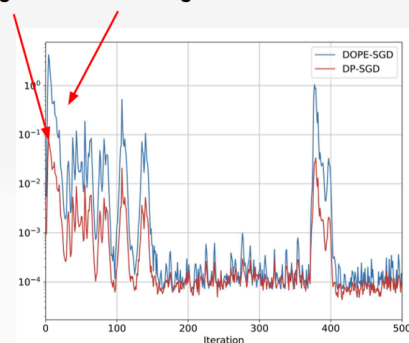
DOPE-SGD

2. Instead of clipping around zero, clip around the estimation

1. Estimate the gradient vector



Significantly less noise compared to the original gradient with using DOPE-SGD



\*Catch our other work: Ganesh, Arun, Mahdi Haghighi, Milad Nasr, Sewoong Oh, Thomas Steinke, Om Thakkar, Abhradeep Guha Thakurta, and Lun Wang. "Why Is Public Pretraining Necessary for Private Model Training?" ICLR'23

Read our work in detail:

