Edwin Rodriguez, Jasmine Rodriguez, Amanda Shohdy

Algorithm 2

Defines a function greedyHamiltonian that takes three parameters: fuel city_distance, miles per hour, returns an integer representing the preferred starting city.

```
In the main function:
vector city_distances
vector fuel
int mpg (available fuel)
while(input does not equal 1) {
        (until the user enters -1)
        store distances in city ditances
}
while (!=1) {
                (prompt user to enter available fuel at every city)
(until user enters -1)
(prompt user to enter miles per gallon)
call the greedyHamiltonian function with fuel, city_distances, and mpg, and output the preferred
starting city returned by the function
int greedyHamiltonian(fuel, city_distances, mpg){
        for (iterate through each city as a potential starting city){
                fuel available = 0
                correct = true
                for(iterate through all the cities to check if Hamiltonian path is possible){
                         (Compute the index of the current city considering the starting city)
                         (Update fuel_available by adding fuel multiples by mpg and subtracting the
distance to the next city.
                         if(fuel available < 0){
                                 correct = false
}
}
        If(correct is true after the loop){
                return the current starting city as the preferred starting city
        }
```

If no correct starting city is found, return -1.

Step Count Analysis

Time complexity would be $O(n^2)$ because there is a function that iterates through each city to consider it as a potential starting city. It takes O(n) time. Inside the outer loop, another one iterates through all cities to check if a Hamiltonian path is possible. Traversing all the cities takes O(n) time which together comes out to $O(n^2)$.