

# Equations

Amanda Wei

June 22, 2022

From the paper *Exclusive Photoproduction of Vector Meson of NLO from CGC* by Cai, Xiang, Wang, and Zhou:

Cai, Yanbing Xiang, Wenchang Wang, Mengliang Zhou, Daicui. (2020). Exclusive photoproduction of vector meson at next-to-leading order from color glass condensate. Chinese Physics C. 44. 074110. 10.1088/1674-1137/44/7/074110.

Under eq. 10, the following definitions are given:

$$r = x_{\perp} - y_{\perp} \quad (1)$$

$$r_1 = x_{\perp} - z_{\perp} \quad (2)$$

$$r_2 = z_{\perp} - y_{\perp} \quad (3)$$

where  $x_{\perp}$  is the transverse coordinate of quark,  $y_{\perp}$  is the transverse coordinate of the anti-quark, and  $z_{\perp}$  is the transverse coordinate of the emitted gluon.  $r$  is passed in through  $N(r, Y)$ , so we aren't really concerned with what  $x_{\perp}$  and  $y_{\perp}$  are exactly, only that their difference equals  $r$ . In that case then, let  $x_{\perp} = \frac{1}{2}r$ , and  $y_{\perp} = -\frac{1}{2}r$ . Then,  $r = x_{\perp} - y_{\perp} = \frac{1}{2}r - (-\frac{1}{2}r) = r$ . Plugging these into the values for  $r_1$  and  $r_2$ , and simplifying expressions in terms of  $z_{\perp}$  and  $r$ :

$$r_1 = x_{\perp} - z_{\perp} = \frac{1}{2}r - z_{\perp} \quad (4)$$

$$|r_1| = \sqrt{\left(\frac{1}{2}r\right)^2 + (z_{\perp})^2 - 2\left(\frac{1}{2}r\right)(z_{\perp})\cos\theta} \quad (5)$$

$$|r_1| = \sqrt{\frac{1}{4}r^2 + z_{\perp}^2 - rz_{\perp}\cos\theta} \quad (6)$$

$$r_2 = z_{\perp} - y_{\perp} = \frac{1}{2}r + z_{\perp} \quad (7)$$

$$|r_2| = \sqrt{\left(\frac{1}{2}r\right)^2 + (z_{\perp})^2 + 2\left(\frac{1}{2}r\right)(z_{\perp})\cos\theta} \quad (8)$$

$$|r_2| = \sqrt{\frac{1}{4}r^2 + z_{\perp}^2 + rz_{\perp}\cos\theta} \quad (9)$$