Lecture 11

**CS 131: COMPILERS** 

### **Announcements**

- HW3: LLVM lite
  - Available on Blackboard.
  - Due: November 6th at 11:59:59pm

you should have STARTED EARLY!!

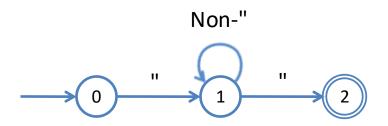
- Midterm: November 19<sup>th</sup> (tentative)
  - In class
  - One-page, letter-sized, double-sided "cheat sheet" of notes permitted
  - Coverage: interperters, x86, LLVMlite, lexing, parsing
  - See examples of previous exam on Blackboard

### **Finite Automata**

- Consider the regular expression: ""[^""]\*""
- An automaton (DFA) can be represented as:
  - A transition table:

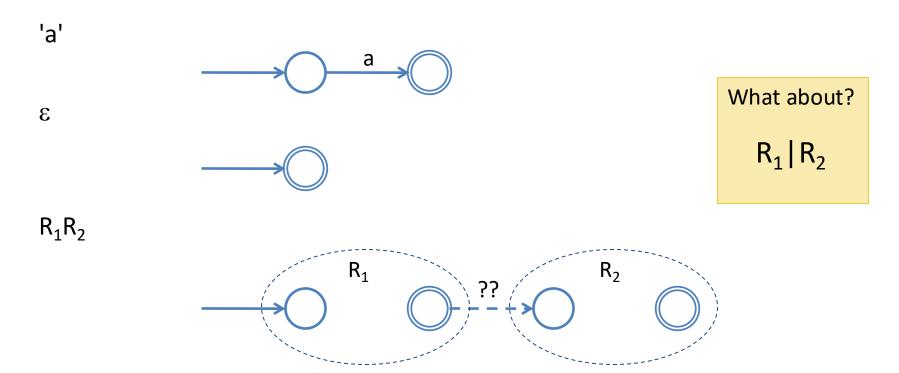
	III	Non-"
0	1	ERROR
1	2	1
2	ERROR	ERROR

– A graph:



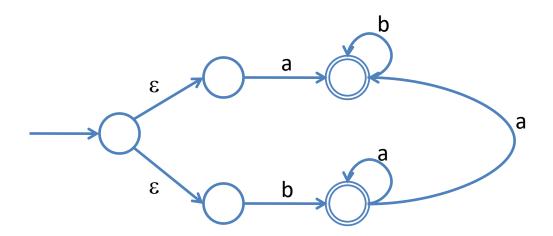
### **RE to Finite Automaton?**

- Can we build a finite automaton for every regular expression?
  - Yes!
- Strategy: consider every possible regular expression (by induction on the structure of the regular expressions):



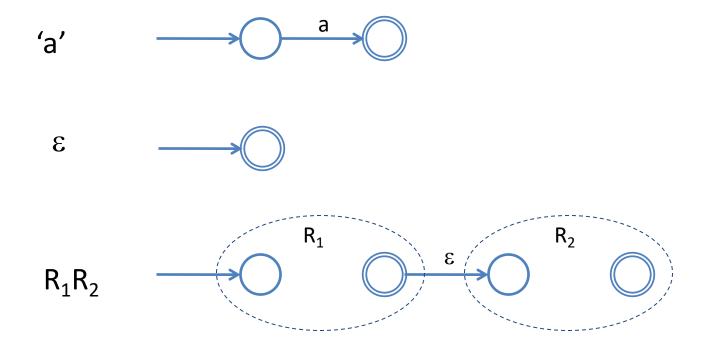
### **Nondeterministic Finite Automata**

- A finite set of states, a start state, and accepting state(s)
- Transition arrows connecting states
  - Labeled by input symbols
  - Or ε (which does not consume input)
- Nondeterministic: two arrows leaving the same state may have the same label



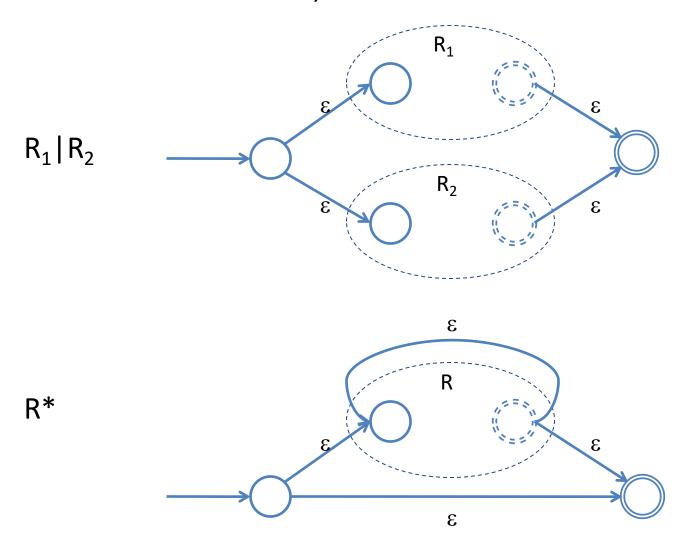
### **RE to NFA?**

- Converting regular expressions to NFAs is easy.
- Assume each NFA has one start state, unique accept state



# RE to NFA (cont'd)

Sums and Kleene star are easy with NFAs



### **DFA versus NFA**

#### DFA:

- Action of the automaton for each input is fully determined
- Automaton accepts if the input is consumed upon reaching an accepting state
- Obvious table-based implementation

#### NFA:

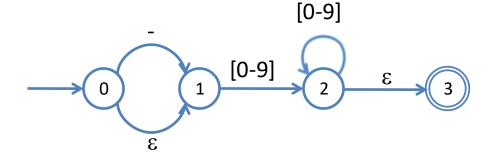
- Automaton potentially has a choice at every step
- Automaton accepts an input string if there exists a way to reach an accepting state
- Less obvious how to implement efficiently

CS 131: Compilers

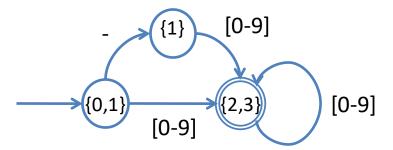
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## NFA to DFA conversion (Intuition)

- Idea: Run all possible executions of the NFA "in parallel"
- Keep track of a set of possible states: "finite fingers"
- Consider: -?[0-9]+
- NFA representation:



• DFA representation:



## **Summary of Lexer Generator Behavior**

- Take each regular expression R<sub>i</sub> and it's action A<sub>i</sub>
- Compute the NFA formed by  $(R_1 | R_2 | ... | R_n)$ 
  - Remember the actions associated with the accepting states of the R<sub>i</sub>
- Compute the DFA for this big NFA
  - There may be multiple accept states (why?)
  - A single accept state may correspond to one or more actions (why?)
- Compute the minimal equivalent DFA
  - There is a standard algorithm due to Myhill & Nerode
- Produce the transition table
- Implement longest match:
  - Start from initial state
  - Follow transitions, remember last accept state entered (if any)
  - Accept input until no transition is possible (i.e. next state is "ERROR")
  - Perform the highest-priority action associated with the last accept state; if no accept state there is a lexing error

### **Lexer Generators in Practice**

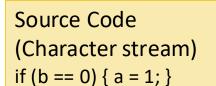
- Many existing implementations: lex, Flex, Jlex, ocamllex, ...
  - For example ocamllex program
    - see lexlex.mll, olex.mll, piglatin.mll on course website
- Error reporting:
  - Associate line number/character position with tokens
  - Use a rule to recognize '\n' and increment the line number
  - The lexer generator itself usually provides character position info.
- Sometimes useful to treat comments specially
  - Nested comments: keep track of nesting depth

Lexer generators are usually designed to work closely with parser generators...

Creating an abstract representation of program syntax.

## **PARSING**

## **Parsing**



#### Token stream:

if

b

==

0

a

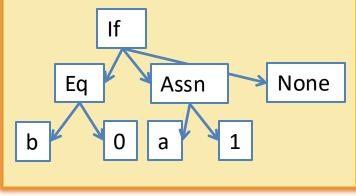
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**Parsing** 

**Lexical Analysis** 

#### Abstract Syntax Tree:



#### Intermediate code:

%cnd = icmp eq i64 %b, 0 br i1 %cnd, label %l2, label %l3 12: store i64\* %a, 1 br label %13 13:

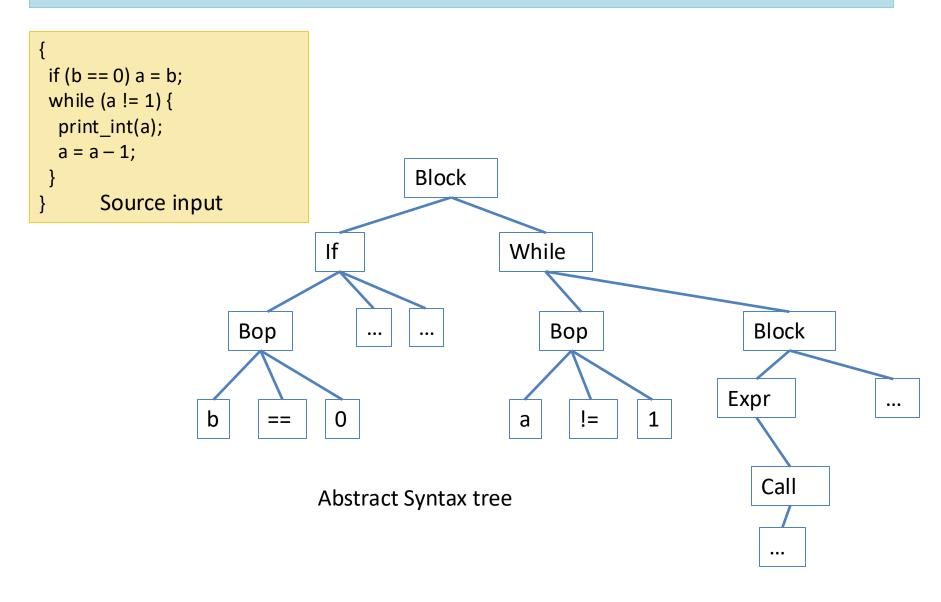
Analysis & **Transformation** 

**Backend** 

#### **Assembly Code**

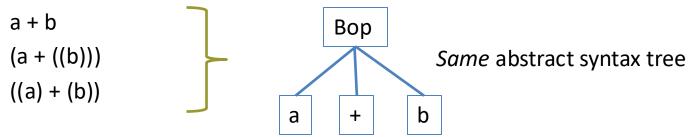
11: cmpq %eax, \$0 jeq l2 jmp I3 12:

# **Parsing: Finding Syntactic Structure**



# Syntactic Analysis (Parsing): Overview

- Input: stream of tokens (generated by lexer)
- Output: abstract syntax tree
- Strategy:
  - Parse the token stream to traverse the "concrete" syntax
  - During traversal, build a tree representing the "abstract" syntax
- Why abstract? Consider these three different concrete inputs:



- Note: parsing doesn't check many things:
  - Variable scoping, type agreement, initialization, ...

## **Specifying Language Syntax**

- First question: how to describe language syntax precisely and conveniently?
- Previously we described tokens using regular expressions
  - Easy to implement, efficient DFA representation
  - Why not use regular expressions on tokens to specify programming language syntax?
- Limits of regular expressions:
  - DFA's have only finite # of states
  - So... DFA's can't "count"
  - For example, consider the language of all strings that contain balanced parentheses – easier than most programming languages, but not regular.
- So: we need more expressive power than DFA's

# **CONTEXT FREE GRAMMARS**

### **Context-free Grammars**

Here is a specification of the language of balanced parens:

$$S \mapsto (S)S$$
  
 $S \mapsto \varepsilon$ 

Note: Once again we have to take care to distinguish meta-language elements (e.g. "S" and "→") from object-language elements (e.g. "(").\*

- The definition is recursive S mentions itself.
- Idea: "derive" a string in the language by starting with S and rewriting according to the rules:
  - Example:  $S \mapsto (S)S \mapsto ((S)S)S \mapsto ((\epsilon)S)S \mapsto ((\epsilon)S)E \mapsto ((\epsilon)E)E = (())E$
- You can replace the nonterminal S by one of its definitions anywhere
- A context-free grammar accepts a string iff there is a derivation from the start symbol

<sup>\*</sup> And, since we're writing this description in English, we are careful distinguish the meta-meta-language (e.g. words) from the meta-language and object-language (e.g. symbols) by using quotes.

# **CFGs Mathematically**

- A Context-free Grammar (CFG) consists of
  - A set of *terminals* (e.g., a lexical token or ε)
  - A set of nonterminals (e.g., S and other syntactic variables)
  - A designated nonterminal called the start symbol
  - A set of productions: LHS  $\mapsto$  RHS
    - LHS is a nonterminal
    - RHS is a *string* of terminals and nonterminals
- Example: The balanced parentheses language:

$$S \mapsto (S)S$$
  
 $S \mapsto \varepsilon$ 

How many terminals? How many nonterminals? Productions?

# **Another Example: Sum Grammar**

A grammar that accepts parenthesized sums of numbers:

$$S \mapsto E + S \mid E$$

$$E \mapsto number \mid (S)$$

e.g.: 
$$(1+2+(3+4))+5$$

Note the vertical bar '|' is shorthand for multiple productions:

$$S \mapsto E + S$$
 4 productions  
 $S \mapsto E$  2 nonterminals: S, E  
 $E \mapsto \text{number}$  4 terminals: (, ), +, number  
 $E \mapsto (S)$  Start symbol: S

### **Derivations in CFGs**

- Example: derive (1 + 2 + (3 + 4)) + 5
- $\underline{S} \mapsto \underline{E} + S$

$$\mapsto$$
 (S) + S

$$\mapsto$$
 (E + S) + S

$$\mapsto$$
  $(1 + \underline{S}) + S$ 

$$\mapsto$$
 (1 + E + S) + S

$$\mapsto$$
 (1 + 2 + S) + S

$$\mapsto$$
 (1 + 2 + E) + S

$$\mapsto$$
 (1 + 2 + (S)) + S

$$\mapsto$$
 (1 + 2 + (**E** + S)) + S

$$\mapsto$$
 (1 + 2 + (3 + **S**)) + S

$$\mapsto$$
 (1 + 2 + (3 + E)) + S

$$\mapsto$$
 (1 + 2 + (3 + 4)) + **S**

$$\mapsto$$
 (1 + 2 + (3 + 4)) + **E**

$$\mapsto$$
 (1 + 2 + (3 + 4)) + 5

$$S \mapsto E + S \mid E$$
  
  $E \mapsto \text{number} \mid (S)$ 

For arbitrary strings  $\alpha$ ,  $\beta$ ,  $\gamma$  and production rule  $A \mapsto \beta$  a single step of the derivation is:

$$\alpha A \gamma \mapsto \alpha \beta \gamma$$

( substitute  $\beta$  for an occurrence of A)

In general, there are many possible derivations for a given string.

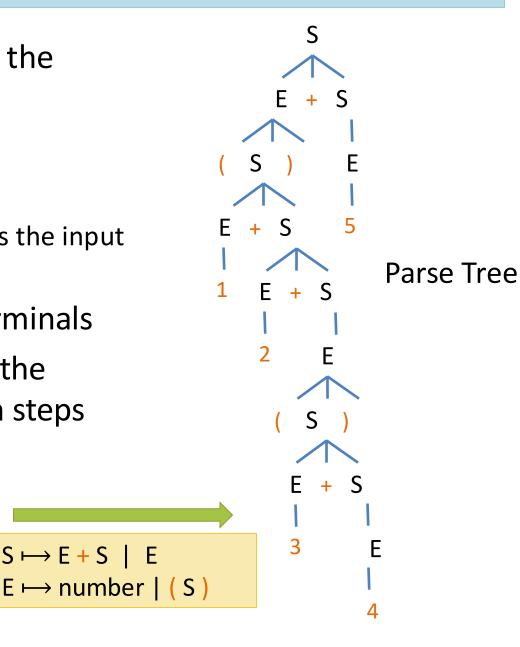
Note: Underline indicates symbol being expanded.

### From Derivations to Parse Trees

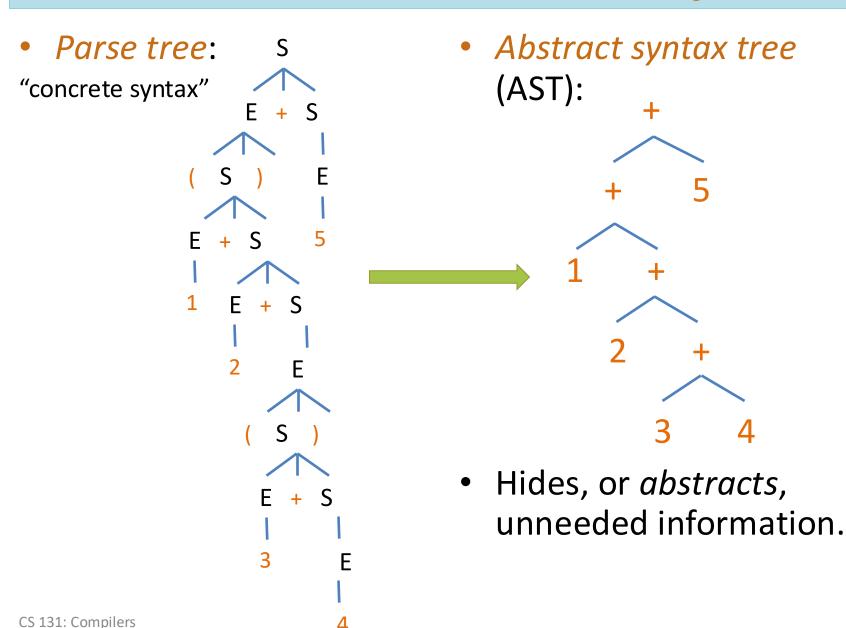
 $S \mapsto E + S \mid E$ 

- Tree representation of the derivation
- Leaves of the tree are terminals
  - In-order traversal yields the input sequence of tokens
- Internal nodes: nonterminals
- No information about the order of the derivation steps

$$(1 + 2 + (3 + 4)) + 5$$



## From Parse Trees to Abstract Syntax



### **Derivation Orders**

- Productions of the grammar can be applied in any order.
- There are two standard orders:
  - Leftmost derivation: Find the left-most nonterminal and apply a production to it.
  - Rightmost derivation: Find the right-most nonterminal and apply a production there.
- Note that both strategies (and any other) yield the same parse tree!
  - Parse tree doesn't contain the information about what order the productions were applied.

## **Example: Left- and rightmost derivations**

- Leftmost Derivation
- $S \mapsto E + S$  $\mapsto$  (S) + S  $\mapsto$  (E + S) + S  $\mapsto$  (1 + S) + S  $\mapsto$  (1 + E + S) + S  $\mapsto$  (1 + 2 + **S**) + S  $\mapsto$  (1 + 2 + E) + S  $\mapsto$  (1 + 2 + (**S**)) + S  $\mapsto$  (1 + 2 + (**E** + S)) + S  $\mapsto$  (1 + 2 + (3 + **S**)) + S  $\mapsto$  (1 + 2 + (3 + **E**)) + S  $\mapsto$  (1 + 2 + (3 + 4)) + **S**  $\mapsto$  (1 + 2 + (3 + 4)) + **E**  $\mapsto$  (1 + 2 + (3 + 4)) + 5

- Rightmost derivation:
- $S \mapsto E + S$  $\mapsto E + E$  $\mapsto$  E + 5  $\mapsto$  (S) + 5  $\mapsto$  (E + S) + 5  $\mapsto$  (E + E + S) + 5  $\mapsto$  (E + E + E) + 5  $\mapsto$  (E + E + (S)) + 5  $\mapsto$  (E + E + (E + S)) + 5  $\mapsto$  (E + E + (E + E)) + 5  $\mapsto$  (E + E + (**E** + 4)) + 5  $\mapsto$  (E + E + (3 + 4)) + 5  $\mapsto$  (**E** + 2 + (3 + 4)) + 5  $\mapsto$  (1 + 2 + (3 + 4)) + 5