



Lecture 3

Circuit Theorems



Outline

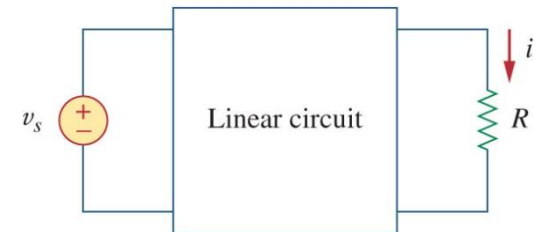
- Linearity property
- Superposition
- Thevenin's theorem
- Source transformation
- Norton's theorem
- Power transfer



Linear Circuit

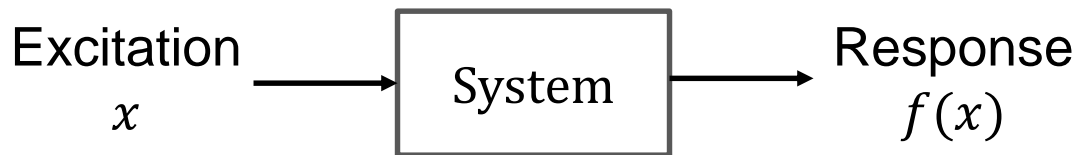
- A linear circuit consists of only linear elements (resistors, capacitors and inductors), linear dependent sources, and independent sources.
- In a circuit,
 - Excitation: Sources
 - Response: Voltage or current in the branches

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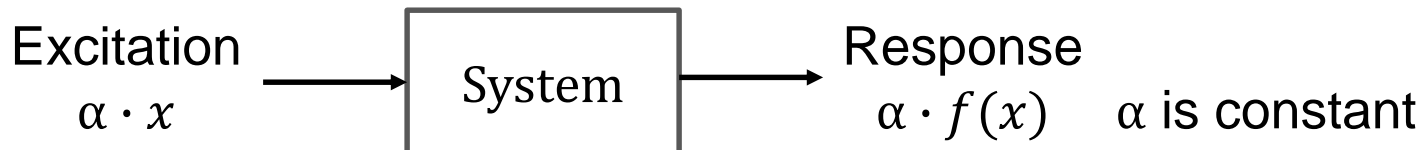




Linearity Property



- Linearity is a combination of
 - homogeneity (scaling) property

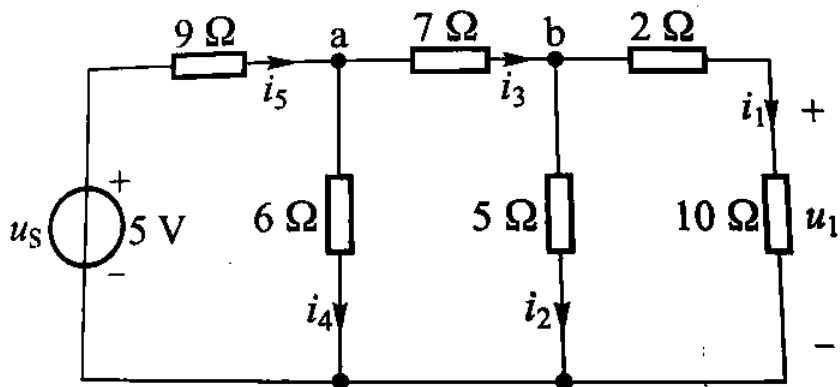


- additivity property



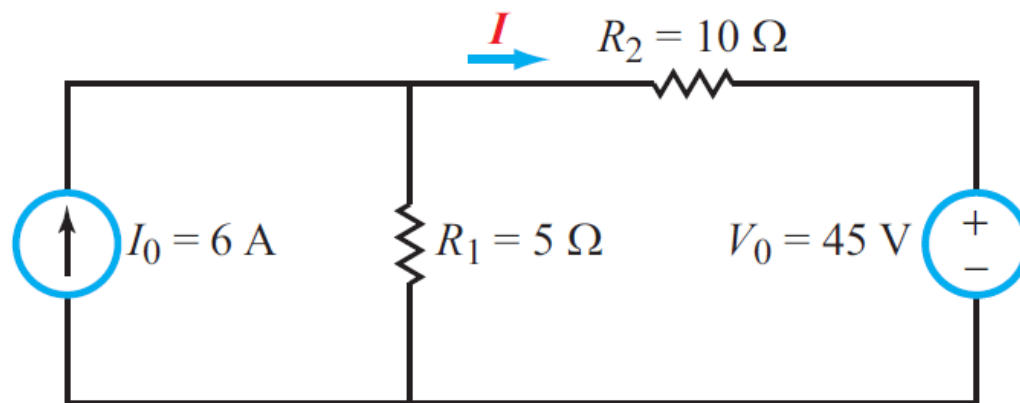


Example of homogeneity (scaling) property



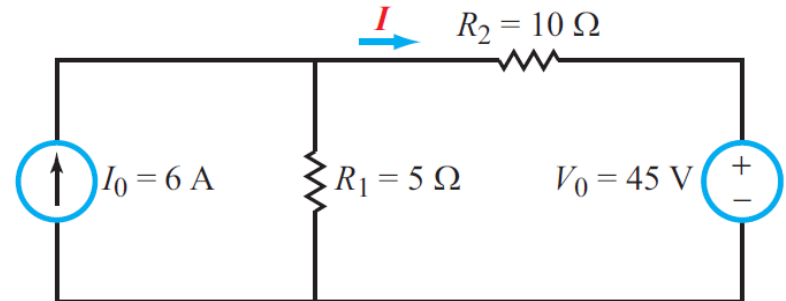
Superposition

- The superposition principle states that the voltage across (or current through) an element in *a linear circuit* is the algebraic sum of the voltages across (or currents through) that element due to each independent source acting alone.





Applying Superposition



- The steps are:
 1. Turn off all other **independent** sources except for the source of interest. Find the output (voltage or current) due to that **active** source.
 - “Turn off” means to replace **independent** voltage source by short circuit (0 V), **independent** current source by open circuit (0 A).
 2. Repeat step 1 for **each independent** source.
 3. Find the total contribution by adding algebraically **all** the contributions due to the **independent** sources.

Note that

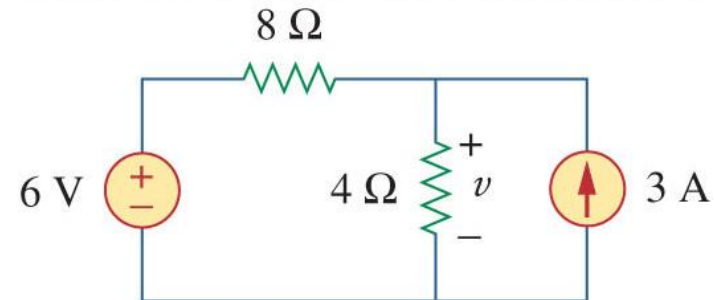
- 1) Using superposition means applying one independent source at a time.
- 2) **Dependent sources are left alone.**



Open Circuit and Short Circuit

- Turn off an independent voltage source means
 - $v=0$
 - Replace by wire
 - Short circuit
- Turn off an independent current source means
 - $i=0$
 - Cut off the branch
 - Open circuit

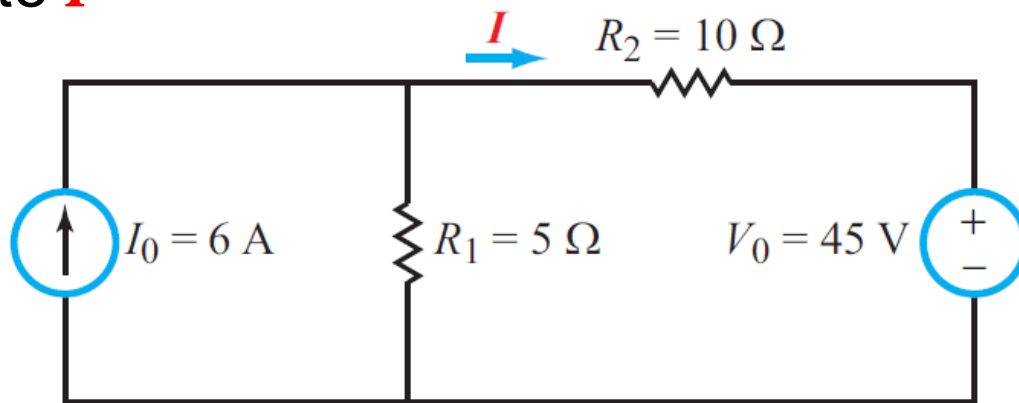
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Example: Superposition

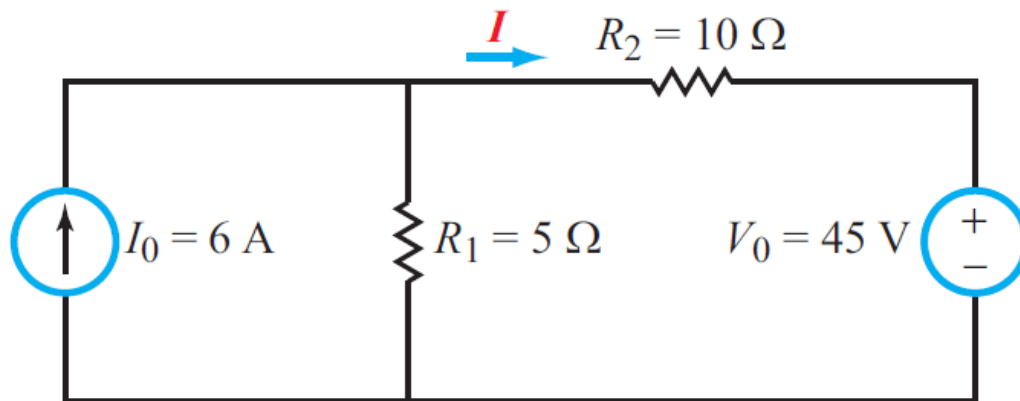
Calculate I



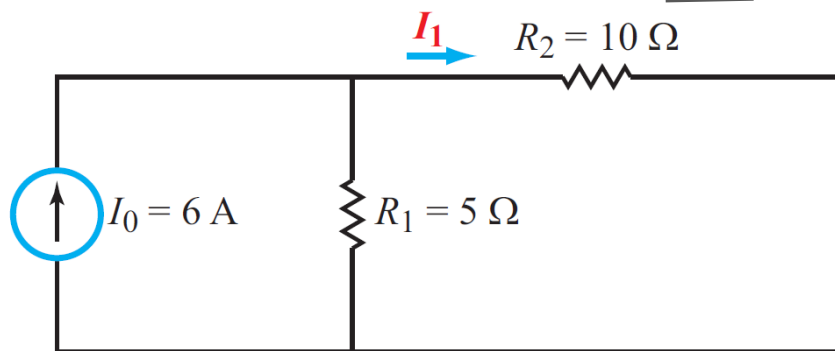


Example: Superposition

Calculate I

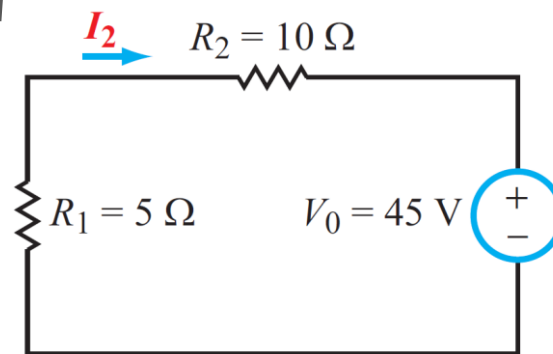


Contribution from I_0 alone



$$I_1 = 2\text{ A}$$

Contribution from V_0 alone

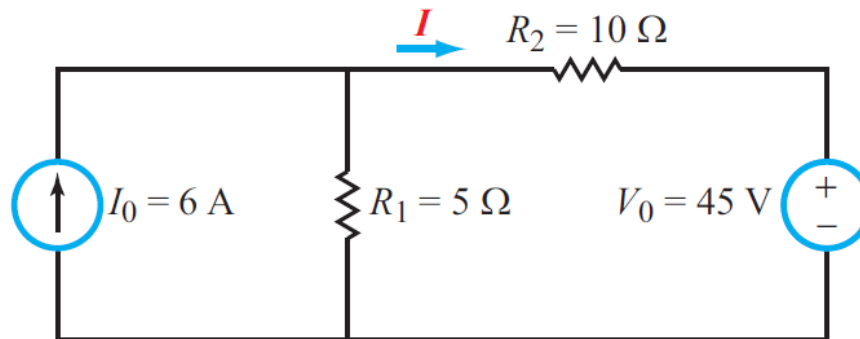


$$I_2 = -3\text{ A}$$

$$I = I_1 + I_2 = 2 - 3 = -1\text{ A}$$

Why Superposition?

- It is useful to evaluate the sensitivity of a response to specific sources in the circuit.
- Because it entails solving a circuit multiple times, this source-superposition method may not be attractive.

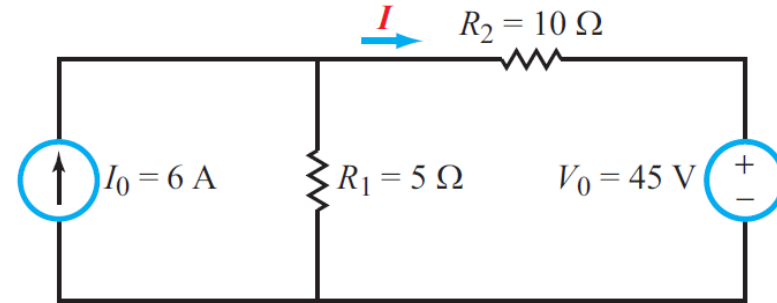


$$I = aI_0 + bV_0$$



How about Power absorbed by R_2

- Power due to I_0 , $P_1 = ?$
- Power due to V_0 , $P_2 = ?$
- Power due to both V_0 and I_0 , $P = ?$





Practice 1

- Find i_o in the circuit shown below.

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