Lecture 14Laplace Transform in Circuit Analysis

V-I relations of R,L,C

• R
$$U_R(s) = RI_R(s)$$

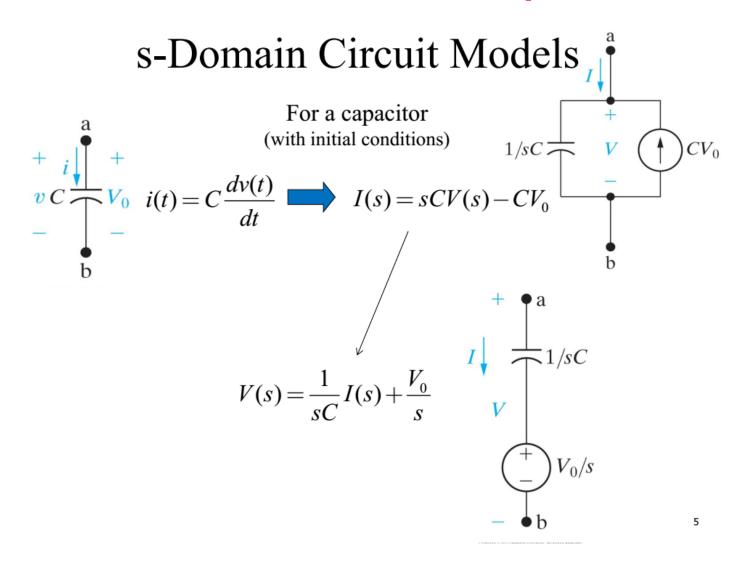
• C
$$V(s) = \frac{1}{sC}I(s) + \frac{V_0}{s}$$

$$I(s) = sCV(s) - CV_0$$

$$I(s) = \frac{1}{sL}V(s) + \frac{I_0}{s}$$

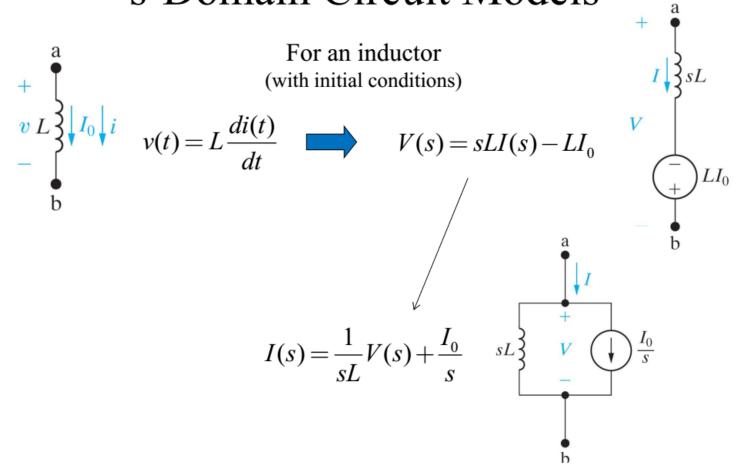
$$V(s) = sLI(s) - LI_0$$

S-domain circuit models for a capacitor



S-domain circuit models for an inductor

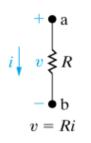


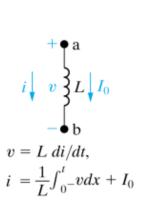


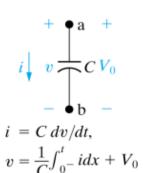


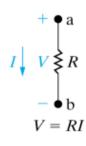
Time domain

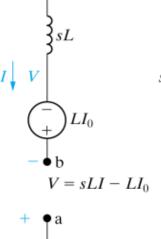
s-domain

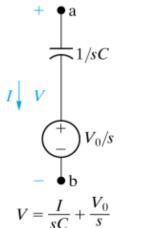


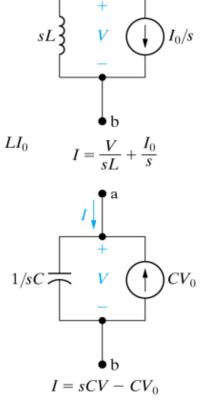












D.C. sources and Dependent Sources

 The models for dependent sources are easy to develop, drawing from the simple fact that if the Laplace transform of f(t) is F(s), then the Laplace transform of af(t) is aF(s) — the linearity property.

$$\mathcal{L}[av(t)] = aV(s)$$

$$\mathcal{L}[ai(t)] = aI(s)$$

Steps in Applying the Laplace transform

- Transform the circuit from the time domain to the Laplace (s) domain, including initial conditions.
- --The elegance of using the Laplace transform in circuit analysis lies in
- (1) transforming the differential equation into an *algebraic* equation; and (2) automatic inclusion of initial conditions in the transformation process, thus providing a complete (**transient and steady-state**) solution.
- Solve the circuit using nodal analysis, mesh analysis, source transformation, superposition, or any other analysis technique with which we are familiar.
- Take the inverse transform of the solution and thus obtain the solution in the time domain.

Example 1

Assuming no initial energy storage, find $i_1(t)$ and $i_2(t)$ for t > 0.

