

1. (4*6'=24') Plot the asymptotic magnitude-frequency response curve of the following transfer functions. **(Please plot on the provided Bode plot graph paper, ensuring that all key information is clearly labeled.)**

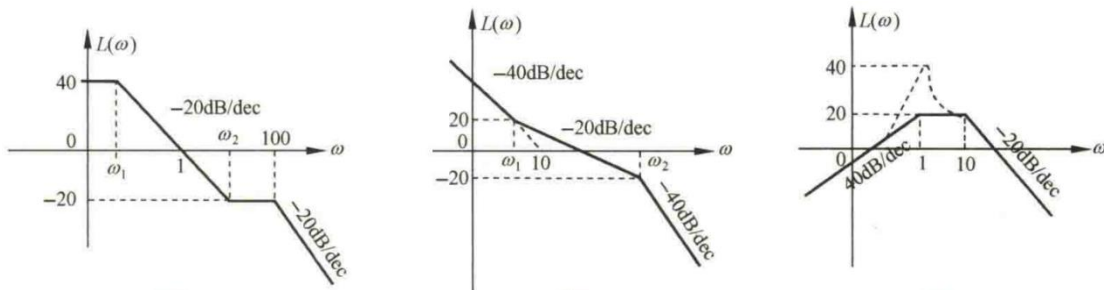
a. $G(s) = \frac{2}{(2s+1)(8s+1)}$

b. $G(s) = \frac{200}{s^2(s+1)(10s+1)}$

c. $G(s) = \frac{8(10s+1)}{s(s^2+s+1)(0.5s+1)}$

d. $G(s) = \frac{10(0.0025s^2+0.1s+1)}{s(s+1)(10s+1)}$

2. (3*6'=18') Given the log-magnitude frequency response curve of a minimum-phase system as shown in the figure, determine the system's open-loop transfer function. (The unit of ω is radians per second (rad/s).)



3. (13') The open-loop transfer function of the system is given as:

$$G(s) = \frac{K(-T_2s + 1)}{s(T_1s + 1)}, K, T_1, T_2 > 0$$

When $\omega = 1 \text{ rad/s}$, $\angle[G(j\omega)] = -180^\circ$, $|G(j\omega)| = 0.5$, when the input is a unit velocity signal, the steady-state error of the system is 0.1. Please derive the open-loop frequency expression for the system.

4. (10*2=20') The open-loop transfer functions of the following systems are known ($K, T, T_i > 0; i = 1, 2, \dots, 6$):

(a) $G(s) = \frac{K}{(T_1s+1)(T_2s+1)(T_3s+1)}$

(b) $G(s) = \frac{K}{s(T_1s+1)(T_2s+1)}$

(c) $G(s) = \frac{K}{s^2(Ts+1)}$

(d) $G(s) = \frac{K(T_1s+1)}{s^2(T_2s+1)}$

(e) $G(s) = \frac{K}{s^3}$

(f) $G(s) = \frac{K(T_1s+1)(T_2s+1)}{s^3}$

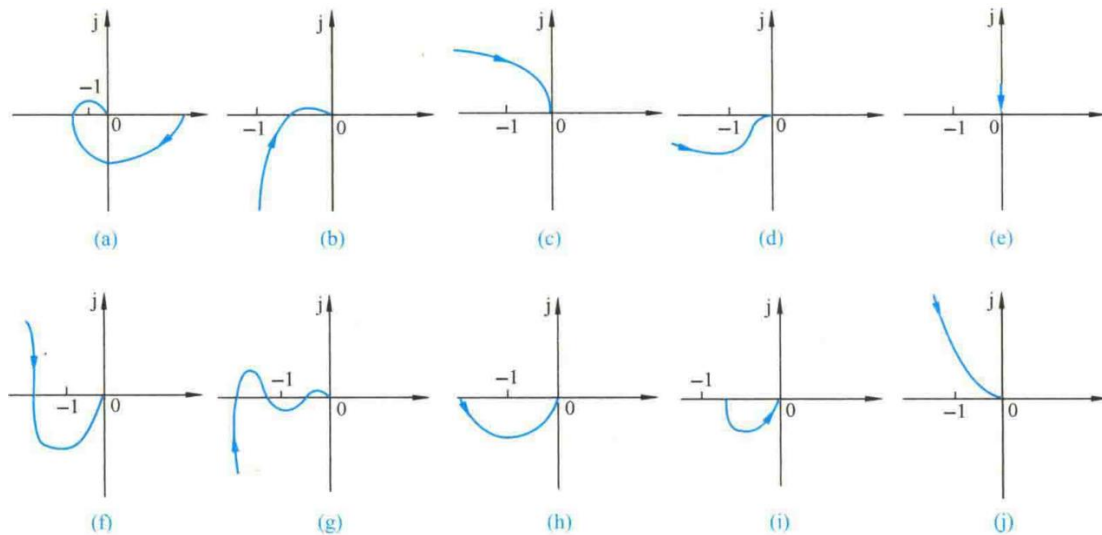
(g) $G(s) = \frac{K(T_5s+1)(T_6s+1)}{s(T_1s+1)(T_2s+1)(T_3s+1)(T_4s+1)}$

(h) $G(s) = \frac{K}{Ts-1}$

(i) $G(s) = \frac{-K}{-Ts+1}$

(j) $G(s) = \frac{K}{s(Ts-1)}$

, and their open-loop amplitude-phase characteristic curves are illustrated in the figure below. Based on the Nyquist stability criterion, determine the closed-loop stability of each system. If a system is closed-loop unstable, identify the number of closed-loop poles in the right half of the s-plane.



5. (5*5'=25') For the system in Figure below. (Calculators may be used to compute the results)
- Calculate the phase margin if the system is stable for time delays of 0, 0.1, 0.2, 0.5, and 1 second.
 - Calculate the gain margin if the system is stable for each one of the time delays in Part **a**.
 - Find out for which of the time delays in Part **a** the system is closed-loop stable.
 - Find out by what amount the gain should be reduced to obtain a stable closed-loop system for those time delays for which the system was closed-loop unstable.

