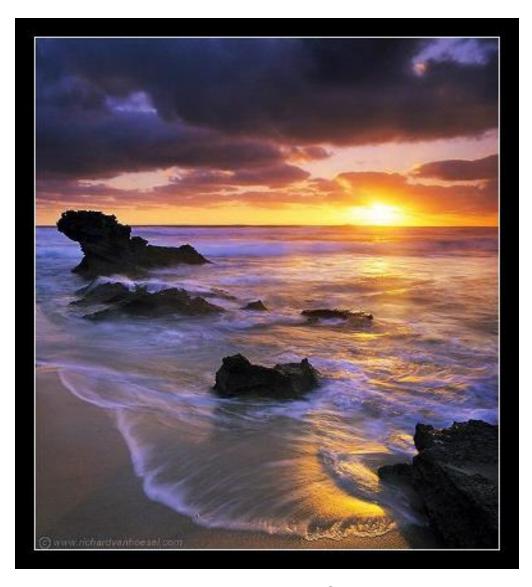
Light and shading

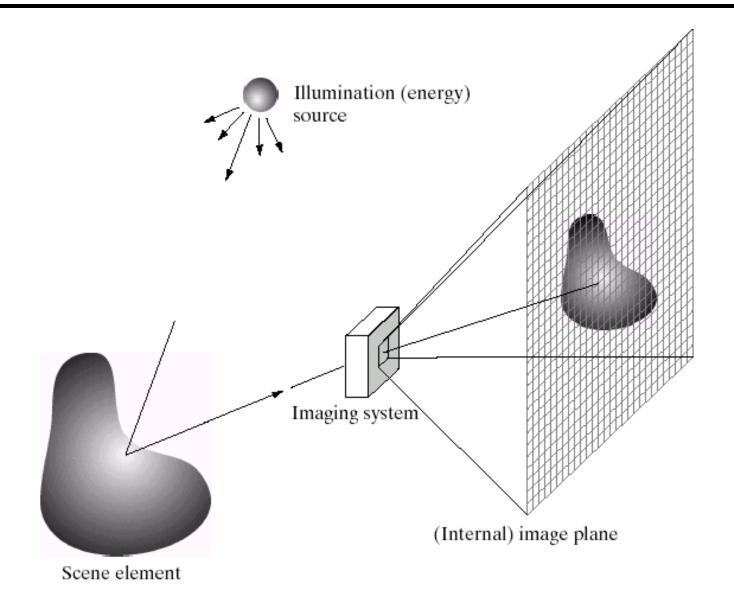


What determines a pixel's intensity?

What can we infer about the scene from pixel intensities?

Image Source: A. Efros

How light is recorded



Digital camera



A digital camera replaces film with a sensor array

Each cell in the array is light-sensitive diode that converts photons to electrons

Two common types: Charge Coupled Device (CCD) and CMOS http://electronics.howstuffworks.com/digital-camera.htm

Sensor Array

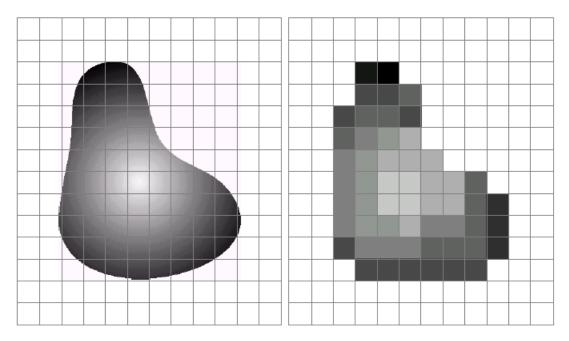
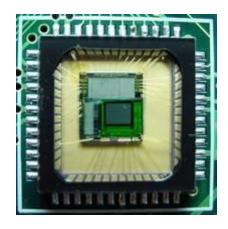
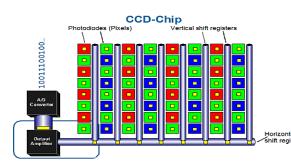




FIGURE 2.17 (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.



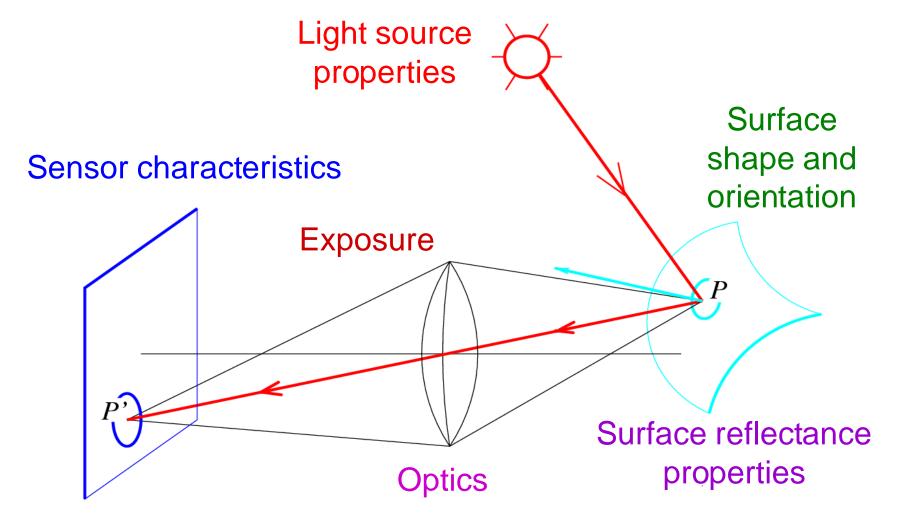
CMOS sensor



Each sensor cell record a small range of orientations amount of light coming in

Image formation

What determines the brightness of an image pixel?



Intensity and Surface Orientation

Intensity depends on illumination angle because less light comes in at oblique angles.

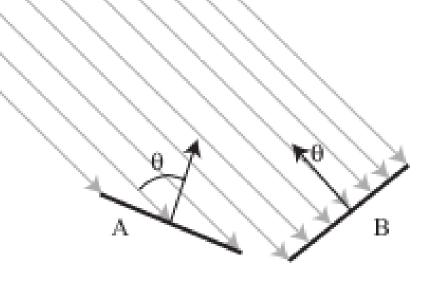
 ρ = albedo

S = directional source

N =surface normal

I = reflected intensity

$$I(x) = \rho(x)(S \cdot N(x))$$



Slide: Forsyth

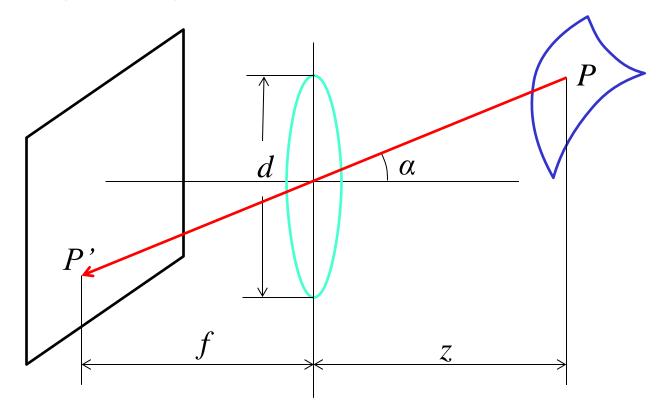
Fundamental radiometric relation

L: Radiance emitted from P toward P (辐射度)

Energy carried by a ray (Watts per sq. meter per steradian)

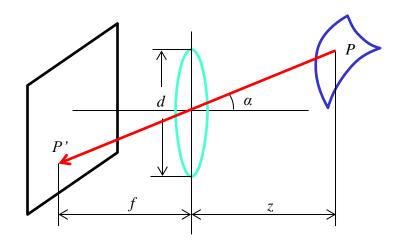
E: Irradiance falling on P from the lens (辐照度)

Energy arriving at a surface (Watts per sq. meter)



What is the relationship between *E* and *L*?

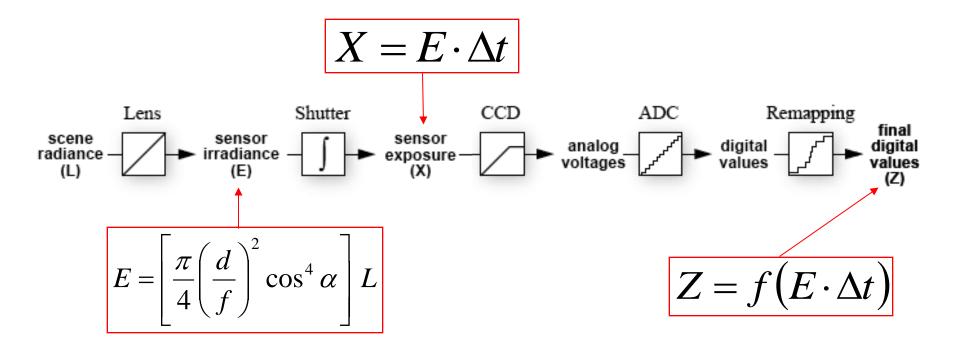
Fundamental radiometric relation



$$E = \left[\frac{\pi}{4} \left(\frac{d}{f} \right)^2 \cos^4 \alpha \right] L$$

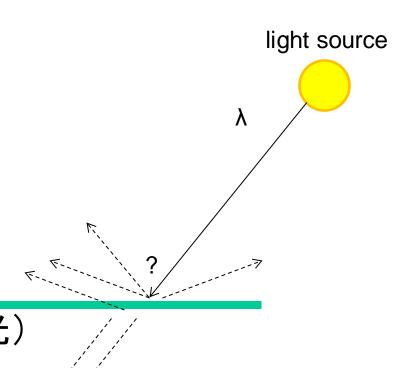
- Image irradiance is linearly related to scene radiance
- Irradiance is proportional to the area of the lens and inversely proportional to the squared distance between the lens and the image plane
- The irradiance falls off as the angle between the viewing ray and the optical axis increases (natural vignetting)

From light rays to pixel values



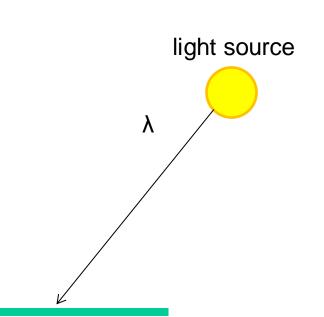
- Camera response function: the mapping f from irradiance to pixel values
 - Useful if we want to estimate material properties
 - Enables us to create high dynamic range images
 - For more info: P. E. Debevec and J. Malik, <u>Recovering High</u>
 <u>Dynamic Range Radiance Maps from Photographs</u>, SIGGRAPH 97

- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence (荧光)
- Subsurface scattering
- Phosphorescence (磷光)
- Interreflection

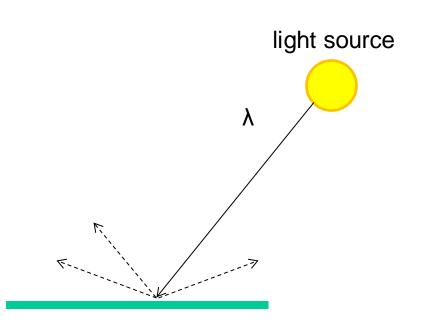


Absorption

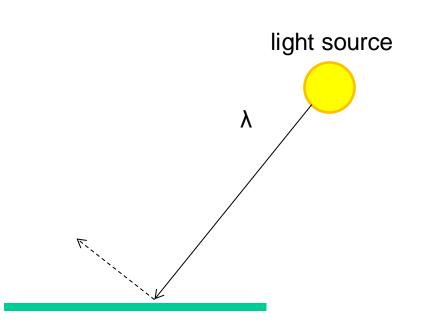
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



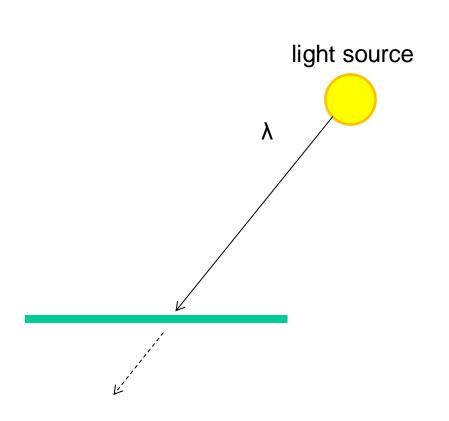
- Absorption
- Diffuse Reflection
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



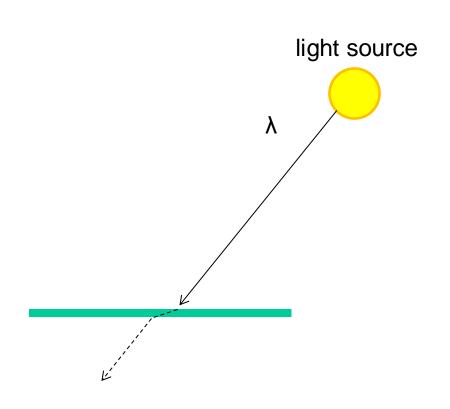
- Absorption
- Diffusion
- Specular Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



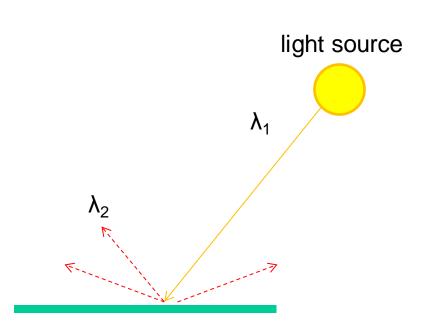
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



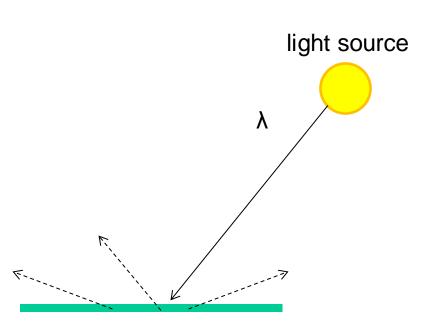
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



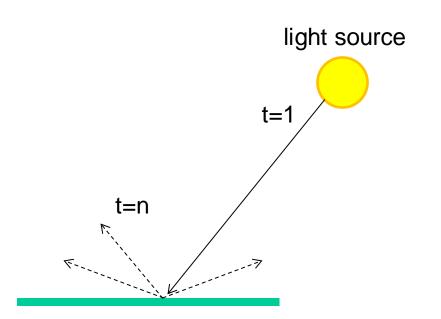
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



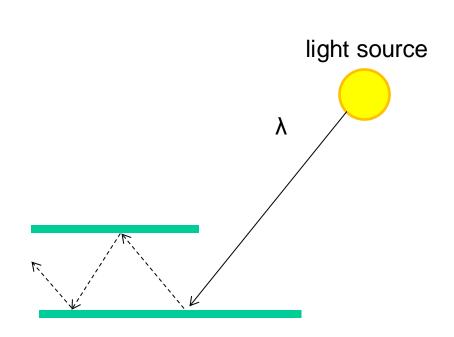
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection

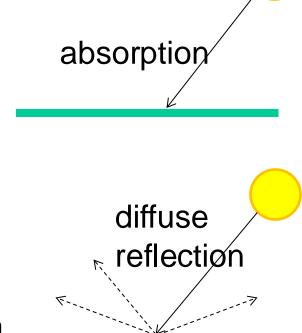


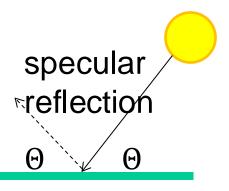
(Specular Interreflection)

Some common effects

When light hits a typical surface

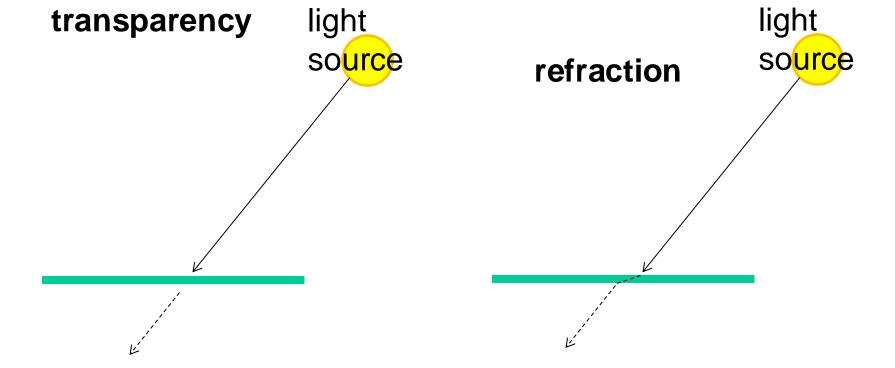
- Some light is absorbed $(1-\rho)$
 - More absorbed for low albedos
- Some light is reflected diffusely
 - Independent of viewing direction
- Some light is reflected specularly
 - Light bounces off (like a mirror), depends on viewing direction





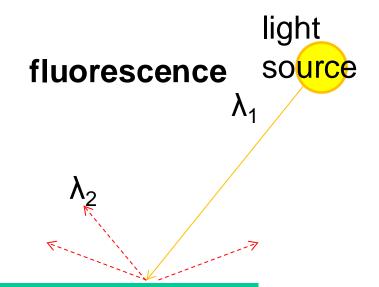
Other possible effects

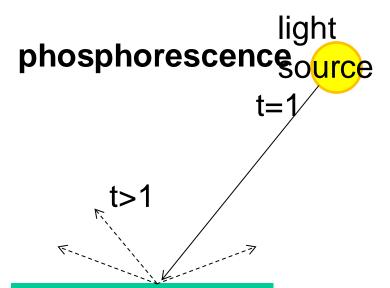










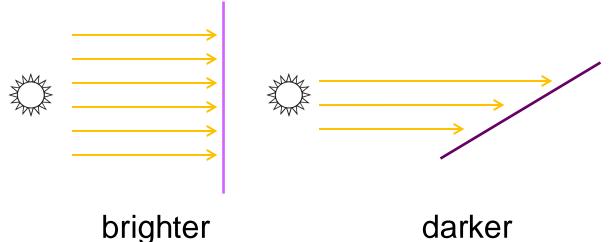




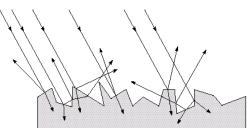


Diffuse reflection

- Light is reflected equally in all directions
 - Dull, matte surfaces like chalk or latex paint
 - Microfacets scatter incoming light randomly
 - Effect is that light is reflected equally in all directions
- Brightness of the surface depends on the incidence of illumination

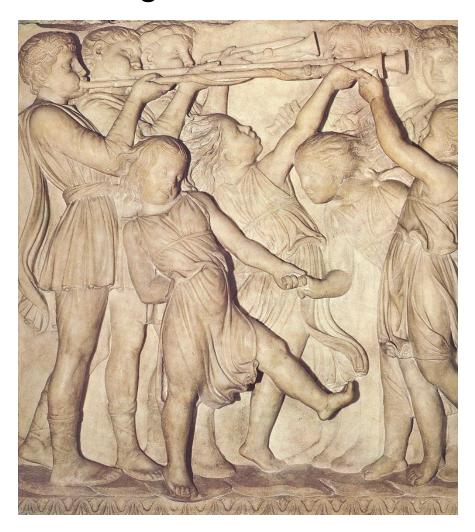






Photometric stereo (shape from shading)

 Can we reconstruct the shape of an object based on shading cues?



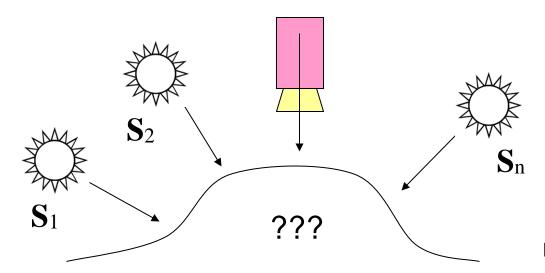
Luca della Robbia, Cantoria, 1438

Photometric stereo

Assume:

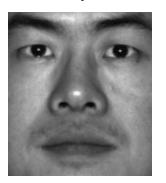
- A Lambertian object
- A local shading model (each point on a surface receives light only from sources visible at that point)
- A set of known light source directions
- A set of pictures of an object, obtained in exactly the same camera/object configuration but using different sources

Goal: reconstruct object shape and albedo



Example

Input







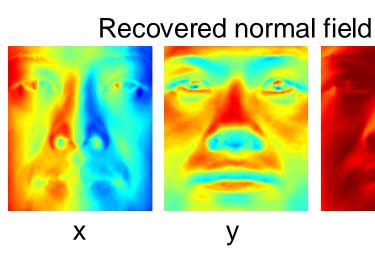


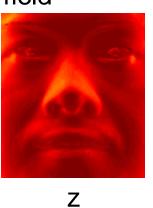
0



Recovered albedo







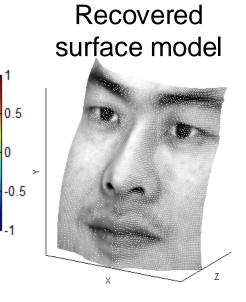


Image model

- **Known:** source vectors S_j and pixel values $I_j(x,y)$

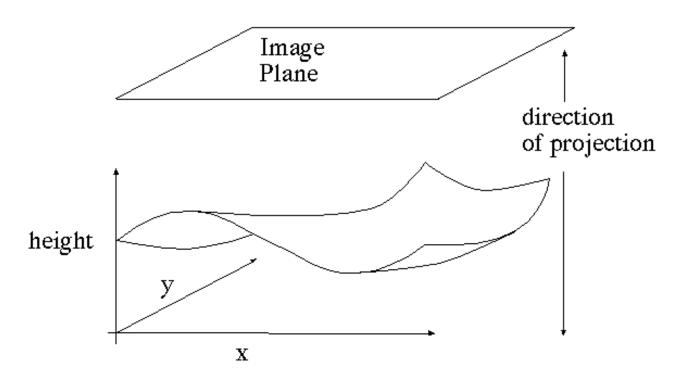


Image model

- **Known:** source vectors S_j and pixel values $I_j(x,y)$
- Unknown: surface normal N(x,y) and albedo 反照 p(x,y)
- Assume that the response function of the camera is a linear scaling by a factor of k
- Lambert's law:

$$I_{j}(x, y) = k \rho(x, y) (\mathbf{N}(x, y) \cdot \mathbf{S}_{j})$$

$$= (\rho(x, y) \mathbf{N}(x, y)) \cdot (k\mathbf{S}_{j})$$

$$= \mathbf{g}(x, y) \cdot \mathbf{V}_{j}$$

Least squares problem

For each pixel, set up a linear system:

$$\begin{bmatrix} I_{1}(x,y) \\ I_{2}(x,y) \\ \vdots \\ I_{n}(x,y) \end{bmatrix} = \begin{bmatrix} \mathbf{V}_{1}^{T} \\ \mathbf{V}_{2}^{T} \\ \vdots \\ \mathbf{V}_{n}^{T} \end{bmatrix} \mathbf{g}(x,y)$$

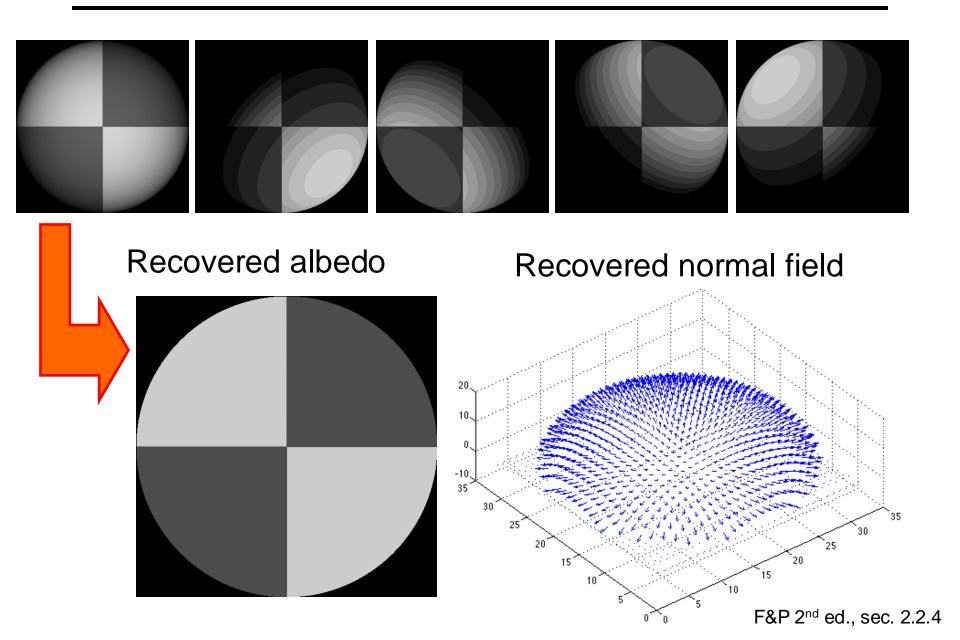
$$\vdots$$

$$(n \times 1) \quad (n \times 3) \quad (3 \times 1)$$

$$known \quad known \quad unknown$$

- Obtain least-squares solution for g(x,y) (which we defined as $N(x,y) \rho(x,y)$)
- Since N(x,y) is the unit normal, $\rho(x,y)$ is given by the magnitude of g(x,y)
- Finally, $N(x,y) = g(x,y) / \rho(x,y)$

Synthetic example



Recovering a surface from normals

Given a normal vector field

$$\mathbf{N}=(N_x,N_y,N_z)$$

we wish to recover the surface z(x, y)

The gradients of (z) can be derived from N

$$[rac{\partial z}{\partial x} = rac{N_x}{N_x}, \quad rac{\partial z}{\partial y} = rac{N_y}{N_x}]$$

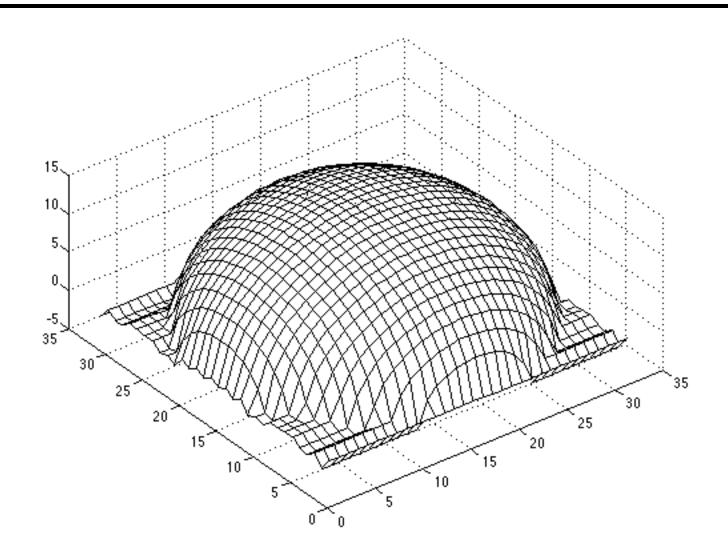
Integration of gradients can be performed directly using numerical

$$[z(x,y)=\int igg(rac{\partial z}{\partial x}dx+rac{\partial z}{\partial y}dyigg)]$$

Recovering a surface from normals

```
Input: Normal fields Nx, Ny, Nz
Output: Height map Z
# Normalize the normal vectors
Nx normalized = Nx / Nz
Ny_normalized = Ny / Nz
# Initialize height map Z
Z = zeros_like(Nx)
# Perform numerical integration
for x in range(width):
    for y in range(height):
        if x > 0:
            Z[x, y] += Z[x-1, y] + Nx_normalized[x, y]
        if y > 0:
            Z[x, y] += Z[x, y-1] + Ny_normalized[x, y]
```

Surface recovered by integration



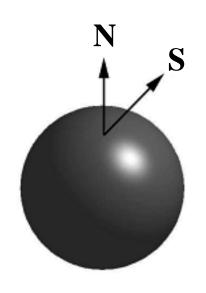
Limitations

- Simplistic reflectance and lighting model
- No shadows
- No interreflections
- No missing data
- Integration is tricky

Finding the direction of the light source

$$I(x,y) = \mathbf{N}(x,y) \cdot \mathbf{S}(x,y)$$

Full 3D case:



For points on the *occluding contour*:

$$\begin{pmatrix} N_{x}(x_{1}, y_{1}) & N_{y}(x_{1}, y_{1}) \\ N_{x}(x_{2}, y_{2}) & N_{y}(x_{2}, y_{2}) \\ \vdots & \vdots \\ N_{x}(x_{n}, y_{n}) & N_{y}(x_{n}, y_{n}) \end{pmatrix} \begin{pmatrix} S_{x} \\ S_{y} \end{pmatrix} = \begin{pmatrix} I(x_{1}, y_{1}) \\ I(x_{2}, y_{2}) \\ \vdots \\ I(x_{n}, y_{n}) \end{pmatrix}$$

P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

Finding the direction of the light source



P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

Application: Detecting composite photos

Real photo

Fake photo





M. K. Johnson and H. Farid, <u>Exposing Digital Forgeries by Detecting Inconsistencies in Lighting</u>, ACM Multimedia and Security Workshop, 2005.