

Outline

- Basic Laws
 - Ohm's Law
 - Kirchhoff's Laws -- KCL,KVL
- Circuit Analysis
 - Nodal Analysis
 - Mesh Analysis



Circuit Analysis

- Two techniques will be presented in this part:
 - Nodal analysis, which is based on KCL
 - Mesh analysis, which is based on KVL



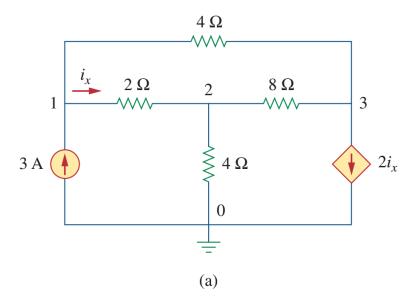
Nodal Analysis – Three Steps

- Given a circuit with *n* nodes, the nodal analysis is accomplished via three steps:
 - 1. <u>Select a node as the reference (i.e., ground) node</u>. Assign the node voltages to the remaining *(n-1)* nodes. Voltages are relative to the reference node.
 - 2. Apply KCL to the *(n-1)* nodes, expressing branch current in terms of the node voltages (using the *I-V* relationships of branch elements).
 - 3. <u>Solve the resulting simultaneous equations</u> to obtain the unknown node voltages.

[Source: Berkeley]



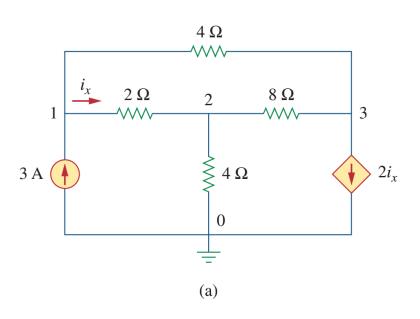
Nodal Analysis: Example #1

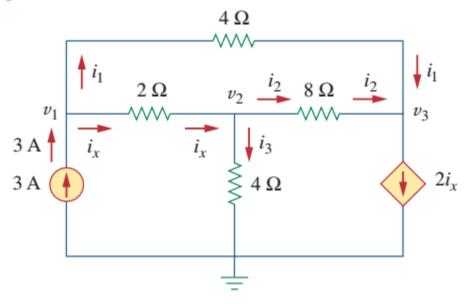


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Nodal Analysis: Example #1



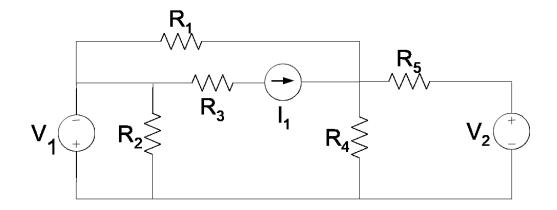


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Nodal Analysis with Voltage Sources

Case I:

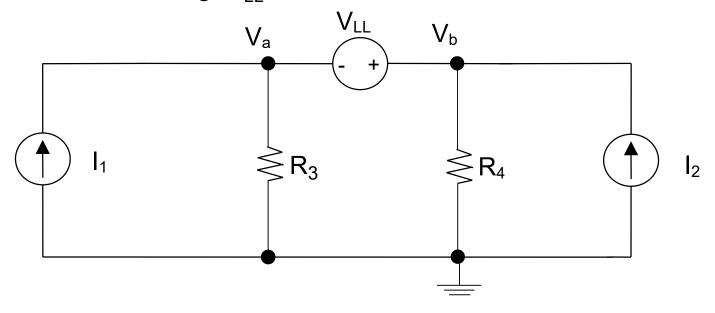




Nodal Analysis: Supernode

Case II

A "floating" voltage source is one for which neither side is connected to the reference node, e.g. V_{LL} in the circuit below:



A supernode is formed by enclosing a (dependent or independent) voltage source connected between two nonreference nodes and any elements connected in parallel with it.

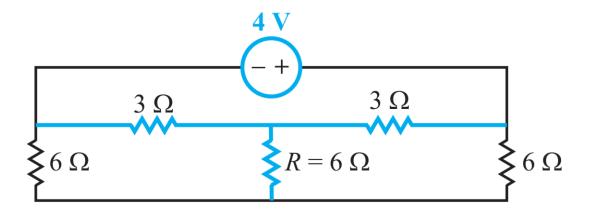
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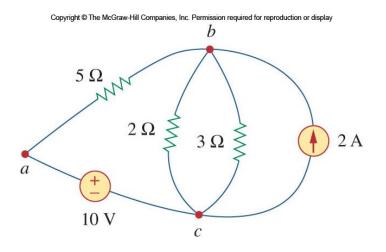
Exercise

• Find the power supplied by the voltage source.



Mesh Analysis--Loop, Independent Loop, Mesh

- A loop is a closed path.
- A loop is <u>independent</u> if it contains at least one branch which is <u>not a</u> <u>part of any other independent loop</u>.
- A mesh is a loop that does not contain any other loop within it.



Mesh = Independent loop?

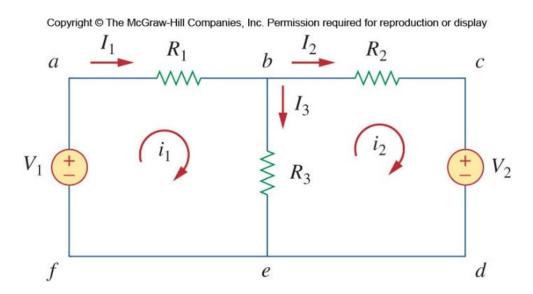
- *b* number of branches
- *n* number of nodes
- l_{ind} number of ind. loops

$$l_{ind} = b - (n-1)$$



Mesh Analysis

 Another general procedure for analyzing circuits is to use the mesh currents as the circuit variables.

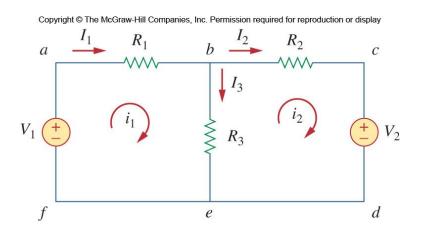


Mesh analysis uses KVL to find unknown currents.



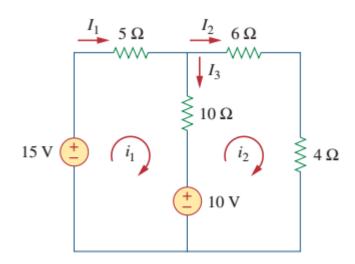
Mesh Analysis Steps

- Mesh analysis follows these steps:
 - 1. Assign mesh currents $i_1, i_2, ... i_x$ to the x meshes
 - 2. Apply KVL to each of the *x* mesh currents.
 - 3. Solve the resulting *x* simultaneous equations to get the mesh currents.





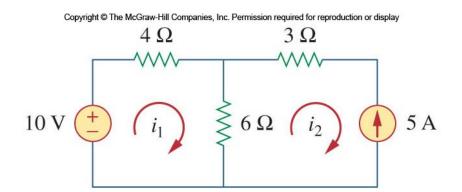
Example





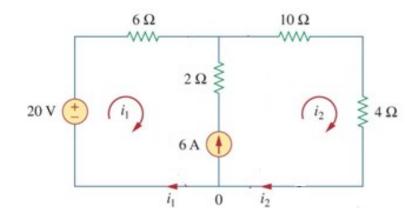
Mesh Analysis with Current Sources

- The presence of a current source makes the mesh analysis simpler in that it reduces the number of equations.
 - If the current source is located on only one mesh, the current for that mesh is defined by the source. For example:



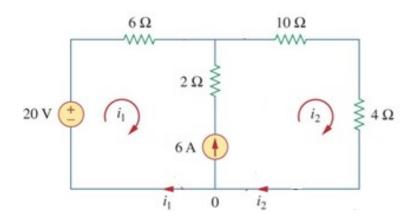


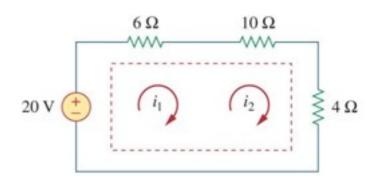
If the current source is located...





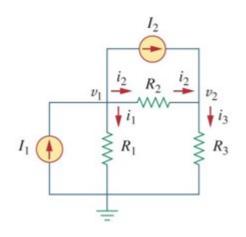
Supermesh





Summary

- Node Analysis
 - Node voltage is the unknown
 - Solve by KCL
 - Special case: Floating voltage source



- Mesh Analysis
 - Mesh current is the unknown
 - Solve by KVL
 - Special case: Current source

