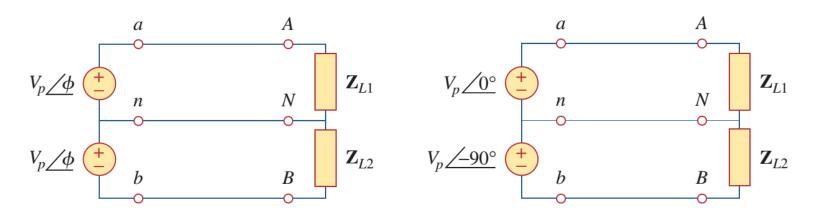
## Lecture 10

- Three-Phase Circuits



## Single phase vs. Polyphase

- Single-phase power supply
  - For example, two 120V sources with the same phase are connected in series.
  - This allows for appliances to use either 120 or 240V
- Circuits that operate with multiple sources, at the same frequency but *at different phases* are called <u>polyphase</u>.

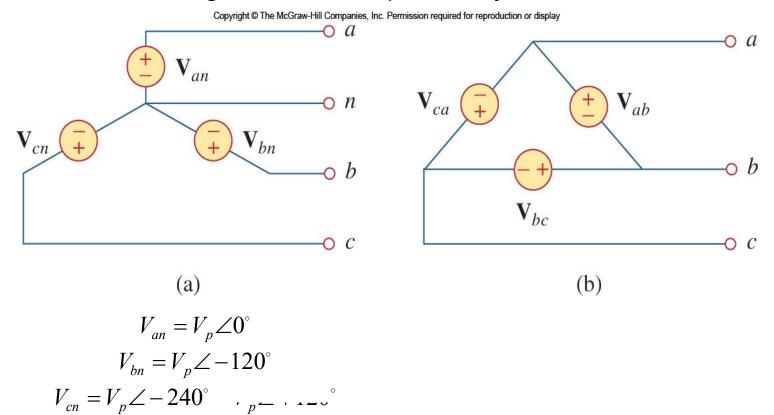


#### **Outline--Three-Phase Circuits**

- Balanced Three-Phase System
  - Balanced sources
  - Balanced loads
- Circuit analysis
  - Phase voltage/current
  - Line voltage/current

# Balanced Three-Phase Sources Connecting the Sources

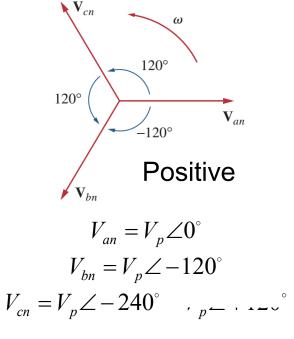
- Three phase voltage sources can be connected by either four or three wire configurations.
  - Four-wire system accomplished using a Y(Wye) connected source.
  - Three-wire configuration accomplished by Delta connected source.

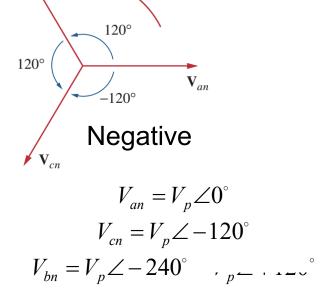




#### **Balanced Three-Phase Sources**

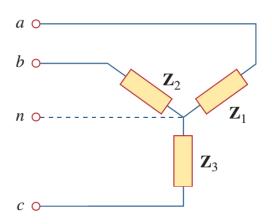
- Balanced phase voltage are equal in magnitude and are out of phase with each other by 120deg
- It's easy to know  $V_{an} + V_{bn} + V_{cn} = 0$
- Two sequences for the phases:

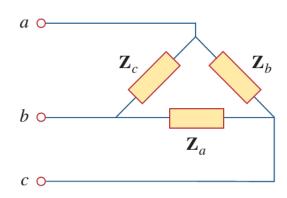




### **Balanced Loads**

- A <u>balanced</u> load means the same impedance for each load.
- -- Impedance are equal in magnitude and in phase
- They may also be connected in either Delta or wye
  - For a balanced wye connected load:  $Z_1 = Z_2 = Z_3 = Z_Y$
  - For a balanced delta connected load:  $Z_a = Z_b = Z_c = Z_\Delta$

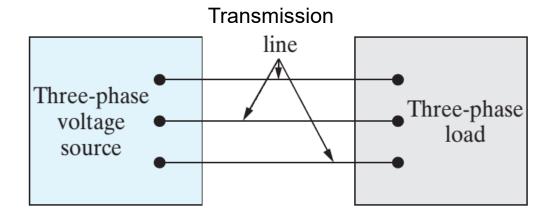




The load impedance per phase for the above configurations can be interchanged.

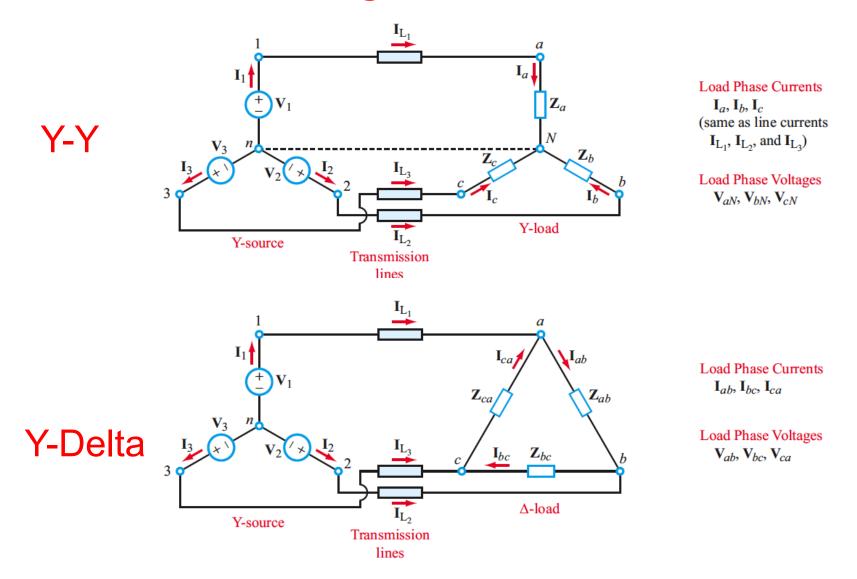


## **Source-Load configurations**

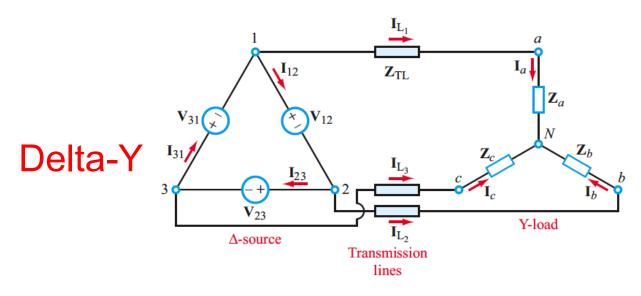


Source	Load
Y	Y
Y	$\Delta$
$\Delta$	Y
$\Delta$	$\Delta$

### **Source-Load Configurations**



## **Source-Load Configurations**

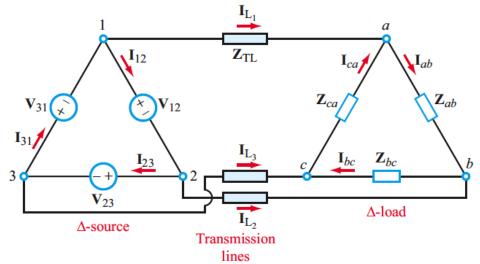


Load Phase Currents

 $\mathbf{I}_a$ ,  $\mathbf{I}_b$ ,  $\mathbf{I}_c$ (same as line currents  $\mathbf{I}_{L_1}$ ,  $\mathbf{I}_{L_2}$ , and  $\mathbf{I}_{L_3}$ )

Load Phase Voltages  $V_{aN}$ ,  $V_{bN}$ ,  $V_{cN}$ 

Delta-Delta



Load Phase Currents  $I_{ab}$ ,  $I_{bc}$ ,  $I_{ca}$ 

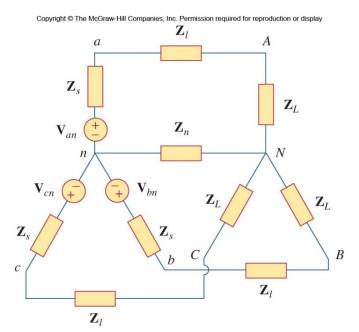
Load Phase Voltages  $V_{ab}$ ,  $V_{bc}$ ,  $V_{ca}$  (same as source voltages if  $Z_{TL}$  is negligible)

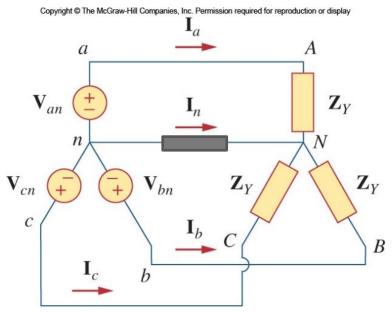


#### **Balanced Y-Y connection**

- The load impedances Z<sub>Y</sub> will be assumed to be balanced.
  - This can be the source  $Z_s$ , line  $Z_l$  and load  $Z_L$  together.

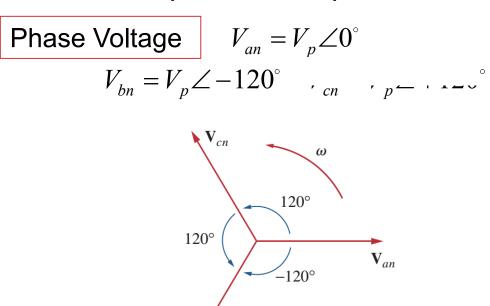
$$\mathbf{Z}_Y = \mathbf{Z}_s + \mathbf{Z}_\ell + \mathbf{Z}_L$$

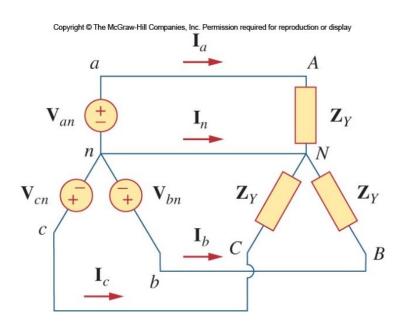




#### Phase Voltage & Line-to-Line Voltage

Use the positive sequence:

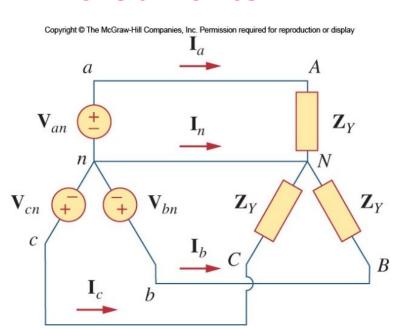




• The line to line voltages (or just line voltages in short):



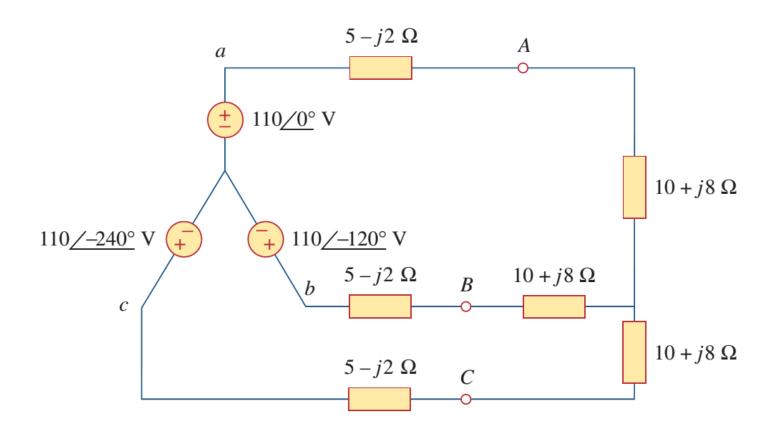
#### **Line Currents**





## **Example**

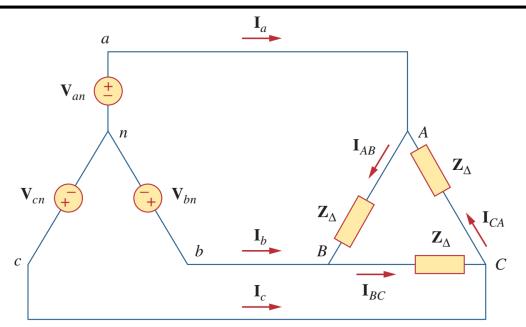
Calculate the line currents.





## Wye-∆

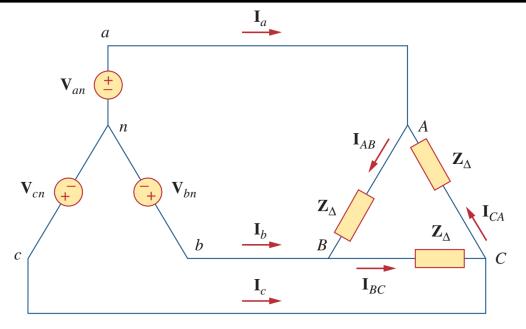
Find load phase current and line current





## Wye-∆

Find load phase current and line current



Assume positive sequence:

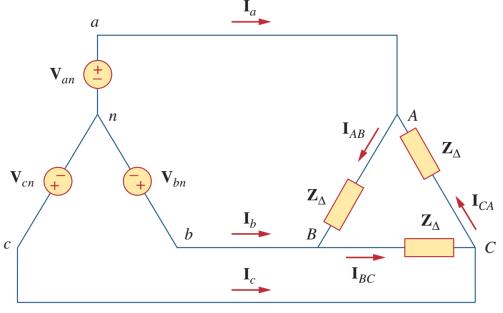
ve 
$$\mathbf{V}_{an} = V_p \underline{/0^{\circ}}$$
  
 $\mathbf{V}_{bn} = V_p \underline{/-120^{\circ}}, \quad \mathbf{V}_{cn} = V_p \underline{/+120^{\circ}}$ 

$$\mathbf{V}_{ab} = \sqrt{3}V_p / 30^{\circ} = \mathbf{V}_{AB}, \qquad \mathbf{V}_{bc} = \sqrt{3}V_p / -90^{\circ} = \mathbf{V}_{BC}$$

$$\mathbf{V}_{ca} = \sqrt{3}V_p / -150^{\circ} = \mathbf{V}_{CA}$$

$$\mathbf{I}_{AB} = \frac{\mathbf{V}_{AB}}{\mathbf{Z}_{\Delta}}, \qquad \mathbf{I}_{BC} = \frac{\mathbf{V}_{BC}}{\mathbf{Z}_{\Delta}}, \qquad \mathbf{I}_{CA} = \frac{\mathbf{V}_{CA}}{\mathbf{Z}_{\Delta}}$$

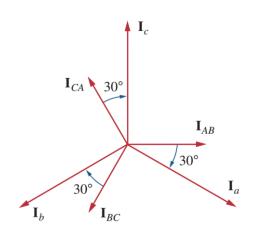
## Wye-∆



$$\mathbf{I}_a = \mathbf{I}_{AB} - \mathbf{I}_{CA}, \qquad \mathbf{I}_b = \mathbf{I}_{BC} - \mathbf{I}_{AB}, \qquad \mathbf{I}_c = \mathbf{I}_{CA} - \mathbf{I}_{BC}$$

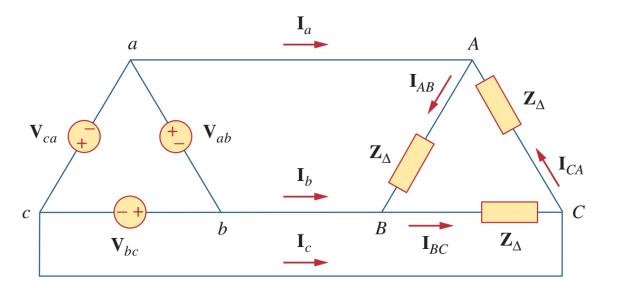
Since 
$$\mathbf{I}_{CA} = \mathbf{I}_{AB} / -240^{\circ}$$
,

$$\mathbf{I}_{a} = \mathbf{I}_{AB} - \mathbf{I}_{CA} = \mathbf{I}_{AB}(1 - 1/240^{\circ})$$
  
=  $\mathbf{I}_{AB}(1 + 0.5 - j0.866) = \mathbf{I}_{AB}\sqrt{3}/-30^{\circ}$ 



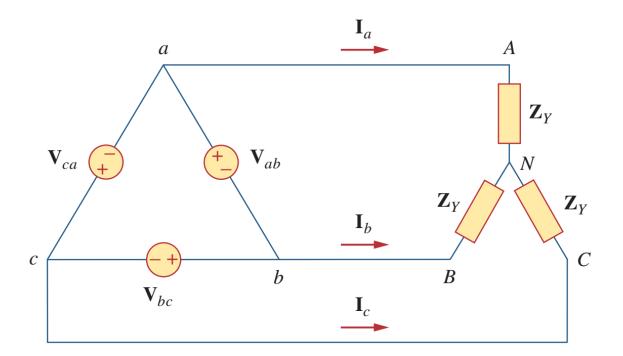
#### Electric Circuits (Fall 2023)





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Δ**-**Wye



Lecture 11 24