

Towers of Hanoi Trace:

I have print statements throughout the function to help trace:

```
def moves(n, left):  
    print("here " + str(n))  
    if n == 0:  
        return  
    moves(n-1, not left)  
    print("here1 " + str(n))  
    if left:  
        print(str(n) + ' left')  
    else:  
        print(str(n) + ' right')  
    print("here2 " + str(n))  
    moves(n-1, not left)  
print(moves(3, True))
```

says here 3, 2, 1, then 0

that means it goes through the function and adds to the stack:

moves(3, True) moves(2, False) moves(1, True) → first in stack, last to be added

here 1 → now after the recursion part

1 left → executes if left: n=1

here 2 1 → n is still 1

here 0 → n is 0, goes through stack again (n=1 function has already happened, so it goes to n=2)

here 1 2 → n is now 2 (going through the stack)
prints "2 right" because it is move(2, False) ← not true

here 2 $2 \rightarrow$ goes past print statement for 2 right
now it calls moves($n-1$, not left)

n is now 1 and moves(1, True) is added to the stack
here 1 $\rightarrow n$ is now 1

here 0 $\rightarrow n$ is now 0 again

stack: moves(1, True), moves(3, True)
 \hookrightarrow last to be added, so this is what will be called

prints here 1 $1 \rightarrow$ means it's starting after where it left off
 $n = 1$

prints "1 left" \rightarrow if True statement is followed through

prints here 2 $1 \rightarrow n$ is still = 1

calls moves($n-1$, not left) $\rightarrow n = 0$, left is False

stack just has moves(3, True) now

here 0 \rightarrow now returns so it goes to functions in stack

here 1 $3 \rightarrow n$ is now = 3

prints 3 left because the boolean is True

calls moves($n-1$, not left) \rightarrow moves(2, False) is added to stack

here	2	} calls moves(1, True) and then goes to $n=0$
here	1	
here	0	

Stack: moves(1, True), moves(2, False)
 [&]
 at the top

here $1 \rightarrow n=1$

prints 1 left because left = True

moves (n-1, not left) \rightarrow n = 0, goes back to stack because of return

moves(2, False) is now called so $h=2$

goes to else statement \neg prints "2 right"

$\text{moves}(h-1, \text{not left})$ is called $\rightarrow \text{Stack: moves}(1, \text{True})$

n resets to 0 after first move($n-1$, not left) is called

moves (1, True) is called from where it left off

$n=1$, left = true so it prints "1 left"

calls moves($n-1$, not left) so $n=0$.

Stack = empty, return is None.

Recursion ended!