

$$f(n e^t - x) = 1/n(1 + e^{-x})$$