QUIZ 6 - Amanjit Gill - Dec 6, 2022

Calculations for Question 1

K=6, p=4

Probabilities: K-1 5

means: Kp 24 λ (size): K A (shape): K(p-1) 18 P (orientation): $\binom{p}{2}$

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```
library(mclust)
## Package 'mclust' version 6.0.0
## Type 'citation("mclust")' for citing this R package in publications.
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
library(GGally)
## Loading required package: ggplot2
## Registered S3 method overwritten by 'GGally':
     method from
##
     +.gg
            ggplot2
library(copula)
# QUESTION 6 - PART A
X <- read.csv("X.csv")</pre>
ans_a_fit <- Mclust(X)</pre>
ans_a_K \leftarrow 6
# QUESTION 6 - PART B
ans_b_fit <- Mclust(X, G=2)</pre>
ans_b_o <- TRUE
# QUESTION 7 - PART A
X \leftarrow \text{matrix}(c(1.35, -0.53, 0.73, 7.72, 1.86, 0.19, 0.54, 2.07, 0.92, 1.76,
               1.18, -0.65, 1.9, 0.17, 1.58, 0.23, 0.5, 0.96, 1.97, 1.79,
```

```
2.06, 1.17, 0.93, -3.41, 0.96, -1.02, 0.84, 1, 0.63, -1.42,
              1.96, -2.15, 1.23, 5.11, 0.15, 2.18, 1.2, -1.8, 0.56, 0.04),
            20, 2, byrow=TRUE)
XU <- pobs(X)
e_fit <- fitCopula(normalCopula(dim=2), XU, method="irho")</pre>
ans_a_r \leftarrow -0.1965
# QUESTION 7 - PART B
normGNc <- mvdc(normalCopula(dim=2), margins=c("gamma","norm"),</pre>
                paramMargins = list(list(shape=1, rate=1),
                                     list(mean=0, sd=1)))
gn_fit \leftarrow fitMvdc(as.matrix(X), normGNc, start = c(1,1, 0,1, 0))
summary(gn_fit)
## Call: fitMvdc(data = as.matrix(X), mvdc = normGNc, start = c(1, 1,
       0, 1, 0)
## Maximum Likelihood estimation based on 20 2-dimensional observations.
## Copula: normalCopula
## Margin 1 :
            Estimate Std. Error
               3.358
                           1.014
## m1.shape
## m1.rate
               2.914
                           0.949
## Margin 2 :
           Estimate Std. Error
             0.6731
                          0.545
## m2.mean
## m2.sd
             2.4363
                          0.385
## Normal copula, dim. d = 2
        Estimate Std. Error
## rho.1 -0.2033
                       0.214
## The maximized loglikelihood is -62.73
## Optimization converged
## Number of loglikelihood evaluations:
## function gradient
##
         59
                  21
ans b r <--0.2033
ans_b_mean <- 0.6731
ans_b_sd \leftarrow 2.4363
ans_b_shape <- 3.358
ans_b_rate <- 2.914
```