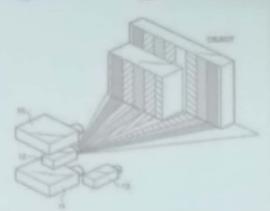
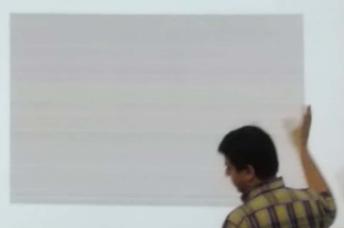
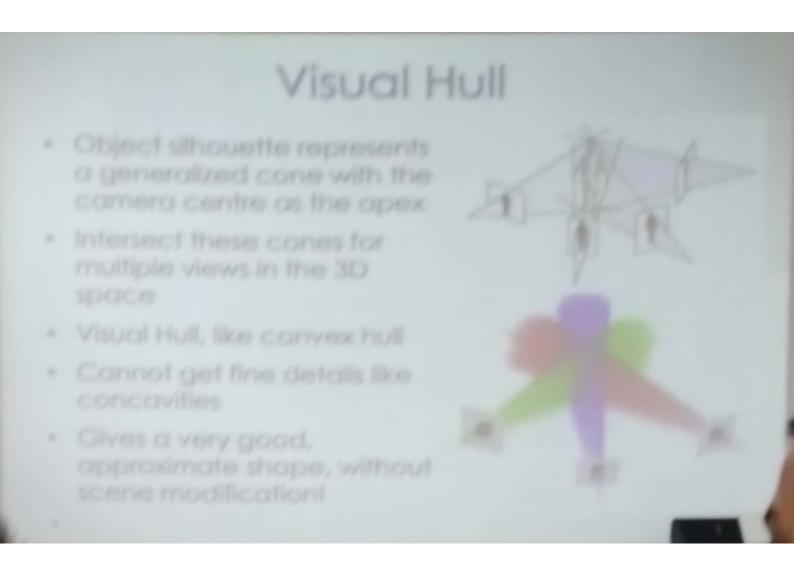
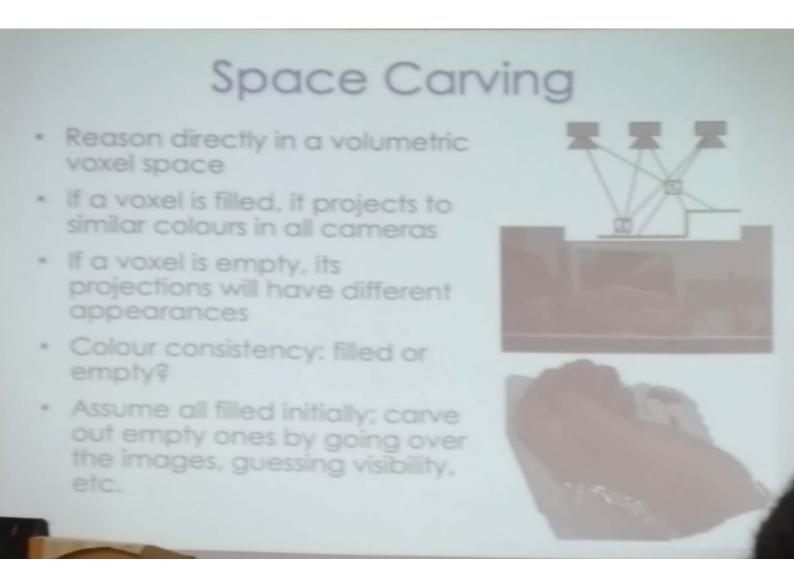
Structured Lighting

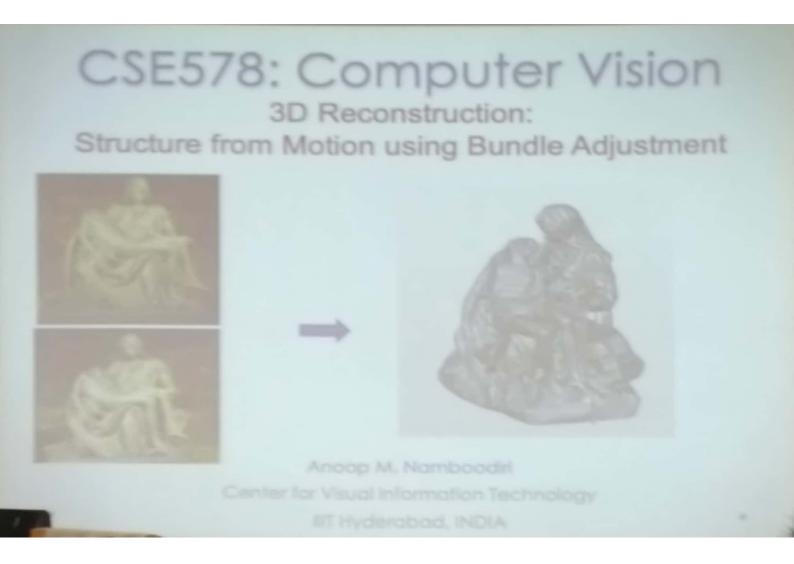
- Finding correspondences is hard by itself
- Can we help it by projecting patterns onto the world?
- Structured Lights!
- Lightstrip range finders, etc.
- Combination of sinusoids sometimes to get dense matches
- Active vision, as it changes the appearance
- The light projected need not be in the visible spectrum

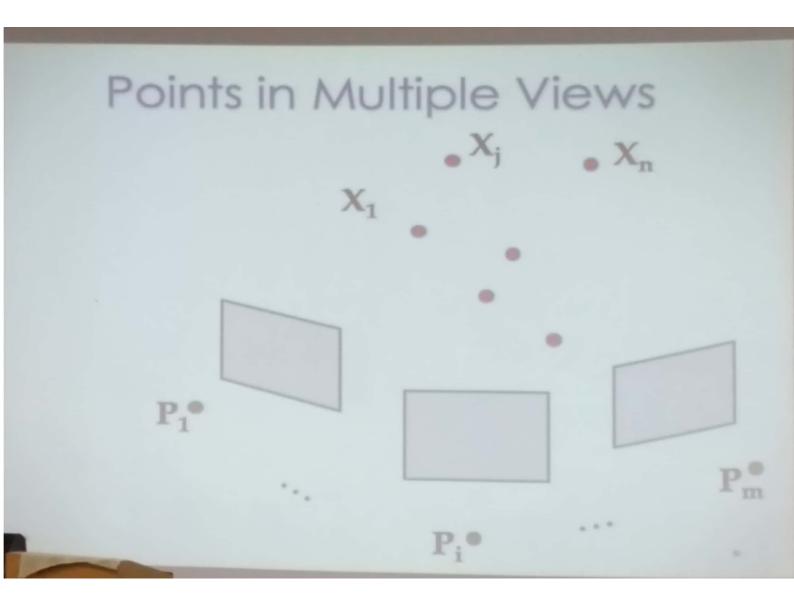


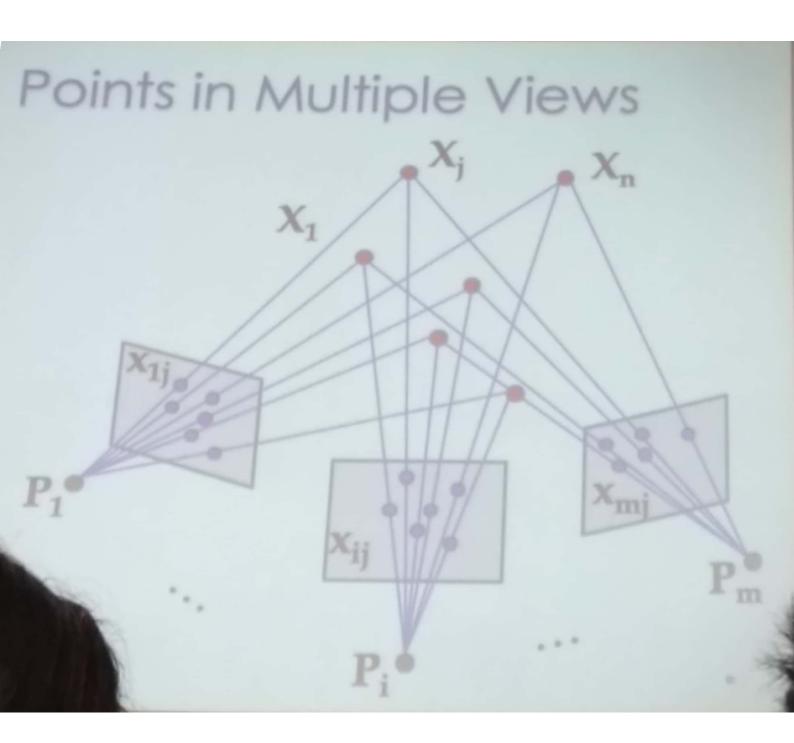


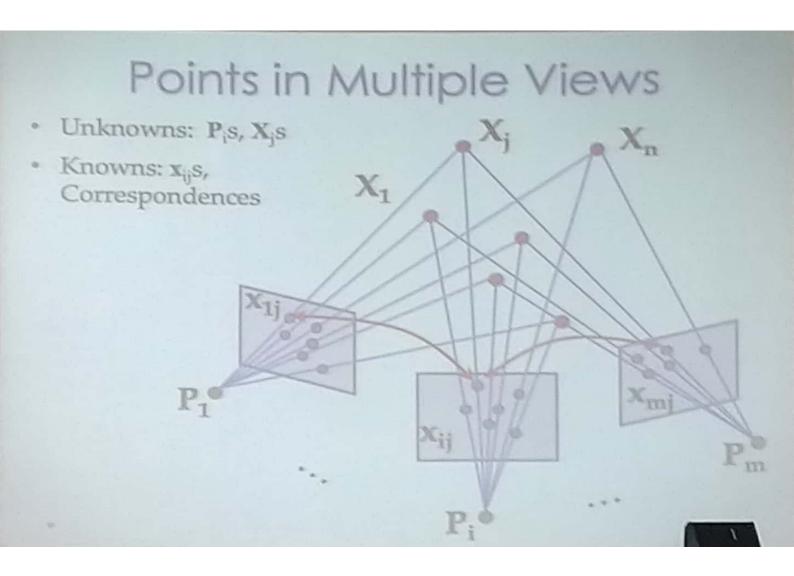












Structure from Motion

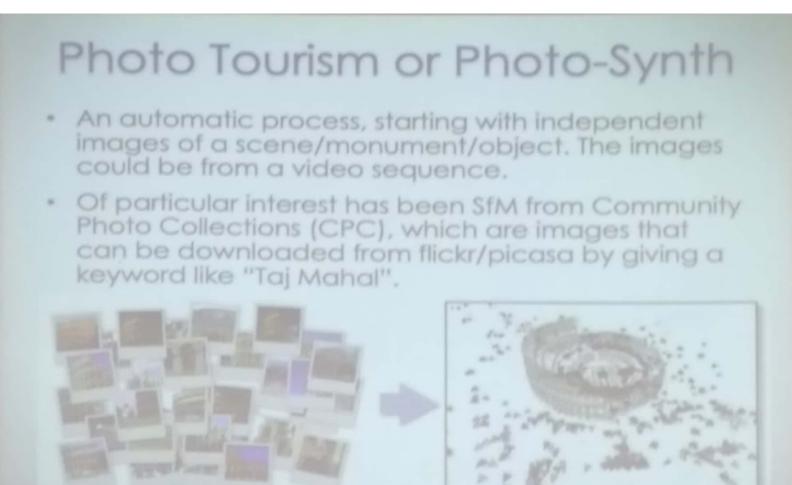
- * m cameras and n points, with correspondences
- Unknown: m matrices P_i and n coordinates, X_j
- * We have: $x_{ij} = P_i X_j$, $1 \le i \le m$, $1 \le j \le n$
- 2mm equations in total (2 for each visible point)
- Can be solved if 2mn > 11m + 3n
- However, under projective, PX = (PQ)(Q-1X), a projective ambiguity will remain
- Projective structure if 2mn > 11m + 3n 15
- Affine structure if 2mn > 11m + 3n 12
- Metric structure if 2mn > 11m + 3n 7
- Affine/Metric structure only by enforcing affine/metric constraints

Bundle Adjustment

- * Given m views of n 3D points, with unknown P_i and X_j . Ideally, $\mathbf{x}_{ij} = \mathbf{P}_i \mathbf{X}_j$
- Minimize the re-projection error over all cameras/views:

$$\min_{P_i X_j} \sum_{i=1}^m \sum_{i=1}^n dist(X_{ij}, P_i X_j)^2$$

- A non-linear optimization problem. Can be solved using the Levenberg-Marquardt procedure directly.
- Called bundle adjustment. Known to photogrammetry community for a long time
- Needs good initialization as the complex non-linear optimization problem can get stuck in local minima



SfM Steps

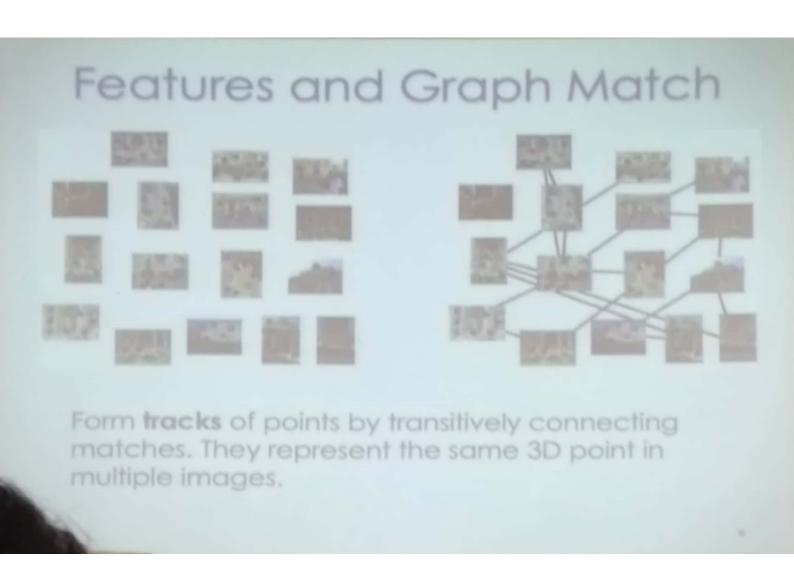
- 1. Download images for the place of interest!!
- 2. Extract descriptors from interest points on all images
- 3. Match points in pairs of images using Approximate Nearest Neighbours
- Refine matches using Geometric Verification: Epipolar relationship, etc.
- Form tracks of points across images. Transitively connect matches to get long matching "tracks"
- 6. Build image connectivity graph based on common points
- 7. Perform incremental SfM using the image connectivity graph and bundle adjustment

Matching Points across Images

- * Extract interest points p_{ij} in each image I_i and descriptors s_{ij} for it. SIFT is popular. A few thousand in a typical image.
- Match interest points in image pairs. An approximate nearest neighbour approach is used, with a ratio test
- Point p_{ij} matches point p_{kl} iff:
 - 1. $dist(s_{ij}, s_{kl})$ is minimum over all points in I_k and
 - 2. $dist(s_{ij}, s_{kl}) < r \times dist(s_{ij}, s_{km})$ where p_{km} is the second closest point in I_k . r is typically 0.6
- Discard all points involved in case of multiple matches

Geometric Verification and Tracks

- Find fundamental matrix between pairs of cameras using RANSAC
- Refine matches by eliminating those not satisfying epipolar relation
- Propagate matches using transitivity to generate tracks, which represent the same world point in multiple images
- Form image connectivity graph. Two images have an edge if they share a point
- Densely connected regions represent parts of the scene visible to a large number of views. Sparse, leaf regions denote low sampling of parts of the scene



Track Statistics

- For a typical large data set with approx 3000 images:
 - o 1.5 million tracks
 - o 75-80% with of length 2
 - o 98% of length less than 10
 - o A few tracks of length more than 100
- Remember: Only 2D feature matching and verification has been done so far, but we seem to have come far!!

Structure from Motion

- 11m + 3n parameters for m cameras and n points. 2mn equations mapping each point in each camera
- Recover camera and structure. Minimize reprojection error across all of them using a non-linear minimization step. This needs good initialization
- Not possible to do them all together. So, start with one pair of cameras and incrementally add more cameras
- Adjust points and cameras to reduce global reprojection error after new cameras are added

Modern digital cameras store a lot of metadata in the images as EXIF tags, including the focal length!

Assume: Only focal length is the unknown intrinsic parameter!

Incremental SfM

- Find a strong starting pair of cameras. These should have a large number of points in common and a large baseline
- Find a pair with a large number of matches. Compute a planar homography from the matches. The pair is good if the error from the homography is high!
- Select the pair with the lowest percentage of inliers to homography using RANSAC
- Estimate the essential matrix for the camera pair
- Reconstruct cameras and common points using the essential matrix
- Perform bundle adjustment to minimize reprojection error

Adding Views

- While there are more connected cameras
 - o Pick an image that sees most number of 3D points so far
 - Estimate pose of the camera using DLT and known 3D points. Perform a local bundle adjustment to correct new camera pose
 - o Triangulate new points (if any) and add to the collection
 - Perform a global bundle adjustment on all cameras and points, using a non-linear optimization step
- Can remove outlier tracks altogether
- Can add a small group of camera views together, instead of one at a time

Bundle Adjustment

Find P, X that minimizes (with visibility indicator w_{ij})

$$g(P,X) = \sum_{i}^{m} \sum_{j}^{n} w_{ij} ||p_{ij} - P_{i}X_{j}||^{2}$$

- Write it as $g(P,X) = ||A P(P,X)||^2$, where P is the non-linear camera projection function
- Linearize
- Iterative solution using Levenberg-Marquardt method
- A sparse problem as the indicator w_{ij} of point j being visible in camera/image i is sparse.

Practical Aspects

- Heavy computations. Several days to reconstruct 500 images. About half of that time is for the bundle adjustment step
- Several optimizations have been worked on recently.
- Typical papers:
 - o "Building Rome in a Day", ICCV 2009 (U of W)
 - o "Building Rome on a Cloudless Day", ECCV 2010 (UNC)
- Combinatorics of pairwise matching is also huge.
 Use image search approaches to reduce the potential numbers

Building Rome in a Day

Agarwal, Simon, Seitz, Szeliski. ICCV 2009

- o Over a million images of the city of Rome
- o Pair-wise matching can take 15 years at 2 pairs/sec
- o Find 40 most similar words (fast matching)
- o Query expansion to increase graph density
- o Full bundle adjustment may run till end of time (nearly!)
- Use skeletal graphs to capture overall structure; perform bundle adjustment in local clusters
- o Reconstructed Rome in 24 hours on a 1000-node cluster!
- A local experiment on a 400-image Hampi dataset:
 - o Extracting SIFT: 54 minutes,
 - o Image matching: 17.2 hrs
 - o Bundle adjustment: 12.6 hrs!!



Structure Recovery: Conclusions

- A problem that has been solved somewhat well
- Many challenges remain, but many have been tackled
- Next generation movies: Watch it from a viewpoint of your choice, decided at view time!!

