

(EXERCISE - J-ADVANCED)

Solution-1 (Ans - A, D)

(A) $T_1 = T_2$
(Isothermal path)

(B) $T_3 < T_2 (=T_1)$

final temperature (for
same volume expansion, from same
initial state) of adiabatic expansion is
less than isothermal expansion

i.e. $T_1 = T_2$ (Isothermal expansion)

$T_3 < T_1$ (Adiabatic expansion)

(C)

Area under P-V curve for

$$A_{\text{isothermal}} > A_{\text{adiabatic}}$$

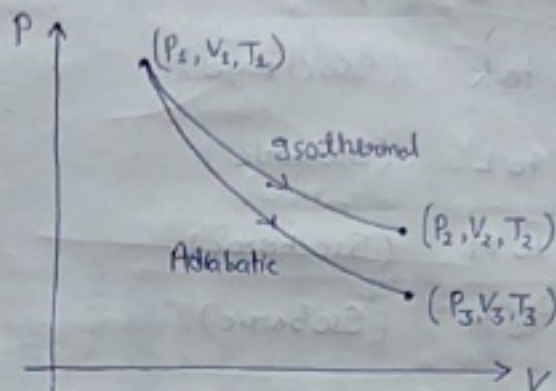
$$W_{\text{isothermal}} < W_{\text{adiabatic}} \quad [W = -A \text{ expansion}]$$

(D) $\Delta U = n C_{vm} \Delta T$ (ideal gas)

$$\Delta T_{\text{isothermal}} = 0$$

$$\Delta T_{\text{adiabatic}} < 0 \quad (T_3 < T_1)$$

So $\Delta U_{\text{isothermal}} > \Delta U_{\text{adiabatic}}$



Solution-2 (Ans-B)

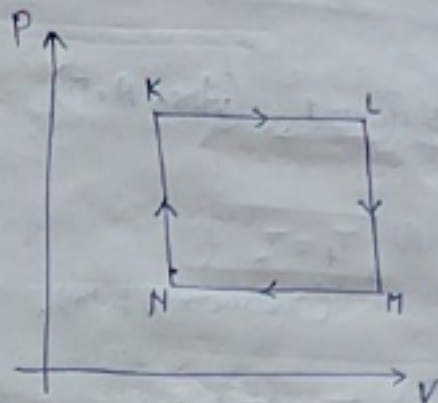
From P-V graph

N to K (Isochoric)

K to L (Isobaric)

L to M (Isochoric)

M to N (Isobaric)



So pair of Isochoric path ($V: \text{Constant}$) is L to M and N to K

Solution-3 (Ans-C)

K to L (Isobaric)

$P: \text{Constant}$

$V \propto T$

V is increasing so Heating

L to M (Isochoric)

$V: \text{Constant}$

$P \propto T$

P is decreasing so cooling

M to N (Isobaric)

$P: \text{Constant}$

$V \propto T$

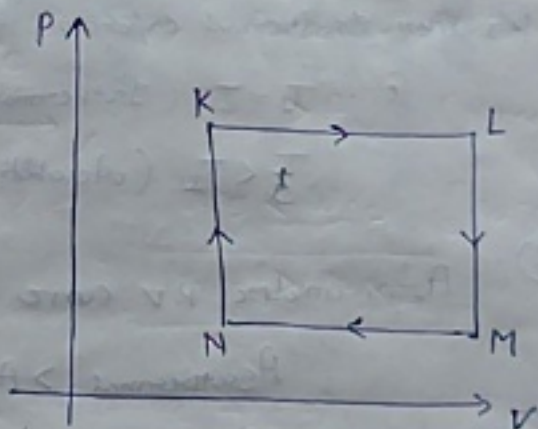
V is decreasing so cooling

N to K (Isochoric)

$V: \text{Constant}$

$P \propto T$

P is increasing so Heating



So option is

Heating, cooling, cooling, Heating

Solution-4 - (Ans. A, B, C)

(A) $q = 0$

(Insulated vessel)

(B) $w = 0$ ($p_{ext} = 0$)

$$\Delta U = \underbrace{q}_0 + \underbrace{w}_0$$

$$\Delta U = 0$$

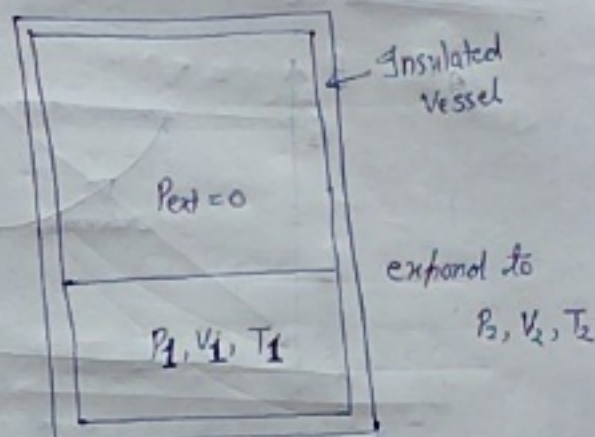
$$\Rightarrow n C_{vm} \Delta T = 0 \quad (\text{Ideal gas})$$

$$\Rightarrow \Delta T = 0$$

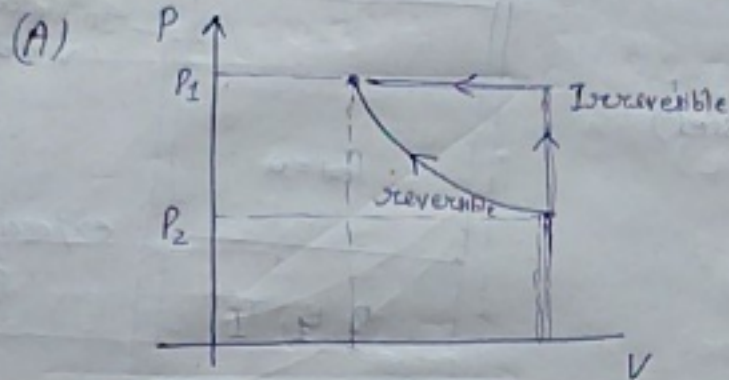
$$\Rightarrow \boxed{T_1 = T_2}$$

(C) $\boxed{P_1 V_1 = P_2 V_2}$ ($T_1 = T_2$)

(D) $\text{so } P_1 V_1^\gamma \neq P_2 V_2^\gamma$ (Irreversible, $p_{ext} = 0$, $p_{ext} \neq p_{gas}$)



Question-5, (Ans - A, B, D)

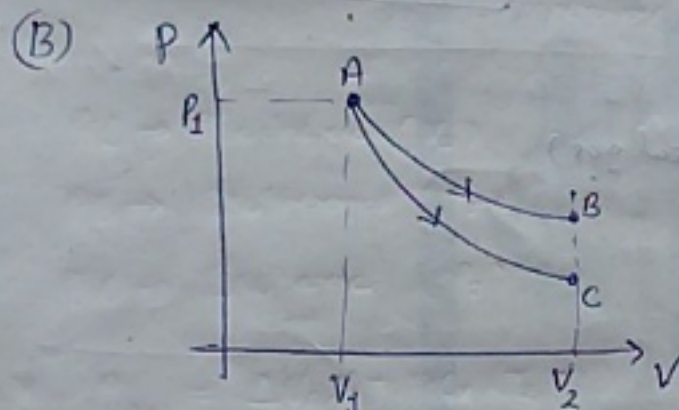


Area under P-V curve

$$A_{irr} > A_{rev}$$

$$W = +A \text{ (Compression)}$$

$$|W_{irr}| > |W_{rev}|$$



AB: Reversible Isothermal

AC: Reversible Adiabatic

$$A_{AB} > A_{AC} \text{ (Area)}$$

$$W_{AB} < W_{AC} \text{ [} W = -A \text{ expansion]}$$

$$|W_{AB}| > |W_{AC}|$$

(i) $\Delta U = n C_{vm} \Delta T = 0$ (Isothermal $\Delta T = 0$)

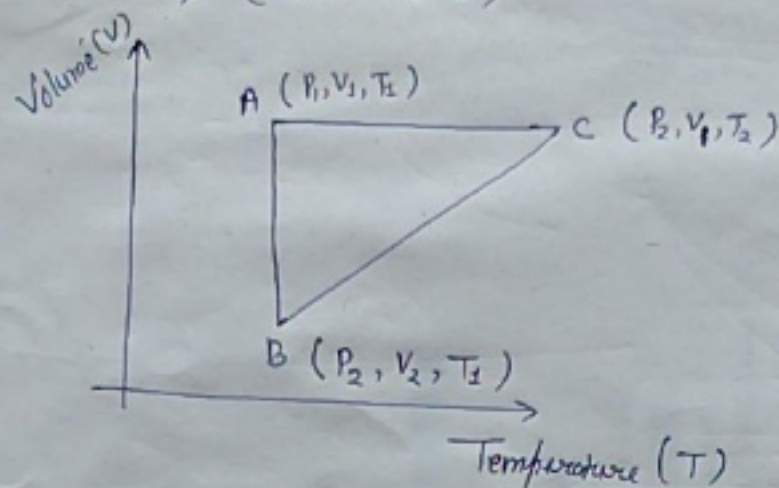
(ii) $\Delta U = q + w = -ve$ ($q = 0, w < 0$)

So $\Delta U = n C_{vm} \Delta T \Rightarrow \Delta T < 0$

D) $q = 0$ (adiabatic), $w = 0$ (free expansion)

$$\Delta U = 0 \Rightarrow \Delta T = 0 \text{ (Isothermal)}$$

Solution-6 → (Ans - B, C)



AC → Isochoric (V_1)

AB → Isothermal (T_1)

BC → Isobaric (P_2)

(A)* $q_{AC} = \Delta U_{BC} = nC_V (T_2 - T_1)$ $[q_{AC} = \Delta U_{AC} = \overset{\text{Isothermal}}{\Delta U_{AB}} + \Delta U_{BC} = \Delta U_{BC}]$

$w_{AB} = -nRT_1 \ln\left(\frac{V_2}{V_1}\right)$
 But given $w_{AB} = P_2(V_2 - V_1)$ → (A wrong)

(B)* $q_{BC} = \Delta H_{BC} = \underset{\text{Isothermal}}{\Delta H_{BA}} + \Delta H_{AC} = \Delta H_{AC}$

$q_{BC} = \Delta H_{AC} = nC_P (T_2 - T_1)$

$w_{BC} = -P_2(V_1 - V_2)$ → (B - correct)

(C)* $nC_P(T_1 - T_2) < nC_V(T_1 - T_2)$

$\Delta H_{CA} < \Delta U_{CA}$

(C - correct)

(D)* $\Delta H_{CA} < \Delta U_{CA}$

(D - wrong)