

Practical No. 1

Title: Random Variable

Q.1] find the mean and variance for the following

|    |        |     |     |     |     |
|----|--------|-----|-----|-----|-----|
| a] | $X$    | -1  | 0   | 1   | 2   |
|    | $P(X)$ | 0.1 | 0.2 | 0.3 | 0.4 |

Solution:

| $x$   | $P(x)$          | $x \cdot P(x)$          | $E(x)^2$             | $[E(x)]^2$             |
|-------|-----------------|-------------------------|----------------------|------------------------|
| -1    | 0.1             | -0.1                    | 0.1                  | 0.01                   |
| 0     | 0.2             | 0                       | 0                    | 0                      |
| 1     | 0.3             | 0.3                     | 0.3                  | 0.09                   |
| 2     | 0.4             | 0.8                     | 0                    | 0.64                   |
| TOTAL | $\sum P(x) = 1$ | $\sum x \cdot P(x) = 1$ | $\sum E(x)^2 = 0.20$ | $\sum [E(x)]^2 = 0.74$ |

$$\therefore \text{Mean} = E(x) = \sum x_i \cdot p(x) = 1$$

$$\text{Variance} = V(x) = \sum E(x)^2 - [E(x)]^2$$

$$= 0.74 - 0.20 = 0.54$$

~~$$\therefore \text{Mean } E(x) = 1 \text{ & Variance } V(x) = 0.54$$~~

|    |        |                |                |                |                |
|----|--------|----------------|----------------|----------------|----------------|
| b) | $X$    | -1             | 0              | 1              | 2              |
|    | $P(X)$ | <del>1/8</del> | <del>1/8</del> | <del>1/4</del> | <del>1/2</del> |

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| x     | P(x)          | XP(x)                | $E(x)^2$              | $[E(x)]^2$             |
|-------|---------------|----------------------|-----------------------|------------------------|
| -1    | $\frac{1}{8}$ | - $\frac{1}{8}$      | $\frac{1}{8}$         | $\frac{1}{64}$         |
| 0     | $\frac{1}{8}$ | 0                    | 0                     | 0                      |
| 1     | $\frac{1}{4}$ | $\frac{1}{4}$        | $\frac{1}{4}$         | $\frac{1}{16}$         |
| 2     | $\frac{1}{2}$ | 1                    | 2                     | 1                      |
| Total | $\sum = 1$    | $\sum = \frac{9}{8}$ | $\sum = \frac{19}{8}$ | $\sum = \frac{69}{64}$ |

$$\therefore \text{Mean } = E(x) = \sum x P(x) = \frac{9}{8}$$

$$\therefore \text{Variance } = V(x) = \sum E(x)^2 - [E(x)]^2$$

$$\begin{aligned}
 &= \frac{19}{8} - \frac{69}{64} \\
 &= \frac{152 - 69}{64} \\
 &= \frac{83}{64}
 \end{aligned}$$

Mean  $E(x) = \frac{9}{8}$  and Variance  $V(x) = \frac{83}{64}$

| x    | -3  | 10   | 15   |
|------|-----|------|------|
| P(x) | 0.4 | 0.35 | 0.25 |

| x     | P(x)       | XP(x)         | $E(x)^2$      | $[E(x)]^2$       |
|-------|------------|---------------|---------------|------------------|
| -3    | 0.4        | -1.2          | -3.6          | 1.44             |
| 10    | 0.35       | 3.5           | 35            | 12.25            |
| 15    | 0.25       | 3.75          | 56.25         | 14.0625          |
| Total | $\sum = 1$ | $\sum = 6.05$ | $\sum = 94.8$ | $\sum = 27.7525$ |

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$$\therefore \text{Mean} = E(x) = P(x) = 6.05$$

$$\therefore \text{Variance} = V(x) = \sum E(x)^2 - [E(x)]^2$$

$$= 94.85 - 27 \cdot 75.25$$

$$= 67.0975$$

$$\text{Mean } E(x) = 6.05$$

$$\text{Variance } V(x) = 67.0975$$

2) If  $P(x)$  is pmf of a random variable  
 If  $P(x)$  represents pmf for random variable  $x$ .

Find value of  $k$ . Then evaluate mean & variance

→ As  $P(x_i)$  is a part it showed satisfy the properties of pmf which are

a)  $P(x_i) \geq 0$  for all sample space.

$$\text{b) } \sum P(x_i) = 1$$

|        |                  |                |                |                  |
|--------|------------------|----------------|----------------|------------------|
| $x$    | -1               | 0              | 1              | 2                |
| $P(x)$ | $\frac{k+1}{13}$ | $\frac{k}{13}$ | $\frac{1}{13}$ | $\frac{k-4}{13}$ |

$$\sum P(x_i) = \frac{k+1}{13} + \frac{k}{13} + \frac{1}{13} + \frac{k-4}{13}$$

$$1 = \frac{k+1+k+1+k-4}{13}$$

$$13 = 3k - 12$$

$$15 = 3k$$

| $x$   | $P(x)$     | $x \cdot P(x)$ | $E(x)^2$       | $[E(x)]^2$      |  |
|-------|------------|----------------|----------------|-----------------|--|
| -1    | $6/13$     | $-6/13$        | $6/13$         | $36/169$        |  |
| 0     | $5/13$     | 0              | 0              |                 |  |
| 1     | $1/13$     | $1/13$         | $1/13$         | $1/169$         |  |
| 2     | $1/13$     | $2/13$         | $4/13$         | $4/169$         |  |
| TOTAL | $\sum = 1$ | $\sum = -3/13$ | $\sum = 11/13$ | $\sum = 41/169$ |  |

$$\therefore \text{Mean} = E(x) = \sum x \cdot P(x) = \frac{-3}{13}$$

$$\begin{aligned}\text{Variance } V(x) &= \sum E(x)^2 - [E(x)]^2 \\ &= \frac{11}{13} - \frac{41}{169} \\ &= \frac{143 - 41}{169} \\ &= \frac{102}{169}\end{aligned}$$

mean =  $-3/13$  & variance =  $102/169$

Q.3) ~~find the PMF of random variable  $x$  is given by~~

| $x$    | -3  | -1  | 0    | 1   | 2   | 3    | 5    | 8    |
|--------|-----|-----|------|-----|-----|------|------|------|
| $P(x)$ | 0.1 | 0.2 | 0.15 | 0.2 | 0.1 | 0.15 | 0.05 | 0.03 |

- obtain cdf find 1)  $P(-1 \leq x \leq 2)$   
 2)  $P(1 \leq x \leq 5)$   
 3)  $P(x \leq 2)$

| <del>x</del> | -3  | -1  | 0    | 1    | 2    | 3    | 5    | 8    |
|--------------|-----|-----|------|------|------|------|------|------|
| $P(x)$       | 0.1 | 0.2 | 0.15 | 0.2  | 0.1  | 0.15 | 0.05 | 0.05 |
| $F(x)$       | 0.1 | 0.3 | 0.45 | 0.65 | 0.75 | 0.90 | 0.95 | 0.95 |

$$\begin{aligned}
 \textcircled{1} P(-1 \leq x \leq 2) &= P(x \leq 2) - P(x \leq -1) + P(x = -1) \\
 &= F(2) - F(-1) + P(-1) \\
 &= 0.75 - 0.3 + 0.2 \\
 &= 0.25
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{2} P(1 \leq x \leq 5) &= E(x_b) - E(x_a) + P(a) \\
 &= F(5) - F(1) + P(1) \\
 &= 0.95 - 0.65 + 0.2
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{3} P(x \leq 2) &= P(x = -3) + P(x = -1) + P(x = 0) + \\
 &\quad P(x = 1) + P(x = 2) \\
 &= 0.1 + 0.2 + 0.15 + 0.2 + 0.1 \\
 &= 0.75
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{4} P(x > 0) &= 1 - F(0) + P(0) \\
 &= 1 - 0.4 + 0.15 \\
 &= 0.40
 \end{aligned}$$

4) Let  $f$  be continuous random variable with pdj

$$f(x) = \frac{x+1}{2} \quad -1 < x < 1$$

Obtain cdf of  $x$  otherwise

→ By definition of cdf we have.

$$f(x) = \int_{-\infty}^x t dt$$

$$= \int_{-1}^x \frac{x+1}{2} dx$$

$$= \frac{1}{2} (\frac{1}{2} x^2 + x) \text{ for } -1 \leq x \leq 1$$

Hence the cdf is

$$F(x) = 0 \text{ for } x \leq -1$$

$$\frac{1}{2} x^2 + \frac{1}{2} x \text{ for } -1 < x \leq 1$$

Let  $f$  be Continuous

random variable with pdj

$$f(x) = \frac{x+2}{18} \quad -2 \leq x \leq 4$$

$$= 0 \quad \text{otherwise.}$$

calculate cdf

→ By definition of cdf we have

$$f(x) = \int_2^4 t dt$$

$$= \int_2^4 \frac{x+2}{18} dx$$

$$= \frac{1}{18} (\frac{1}{2} x^2 + 2x)$$

Ex

for  $-2 \leq x \leq 4$

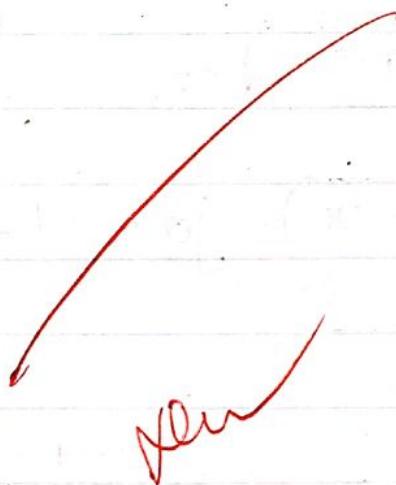
Hence cdf is

$$f(x) = 0 \quad \text{for } x < -2$$

$$= \frac{1}{18} \left( \frac{1}{2}x^2 + 2x \right)$$

for  $-2 < x < 4$

$$= 0 \quad \text{for } x \geq 4$$



## Practical No.2

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### Title : Binomial Distribution

Q.1) An unbiased coin is tossed 4 times calculate the probability of obtaining no head, at least one head and more than one tail.

> abinom(0, 4, 0.5)

[1] 0.0625

AT LEAST ONE HEAD

> 1 - abinom(0, 4, 0.5)

[1] 0.9375

MORE THAN ONE TAIL:

> pbinom(1, 4, 0.5, lower.tail = F)

[1] 0.9375

Q.2) The probability that student is accepted to a prestigious college is 0.3. If 5 students apply, what's the probability of at most 2 are accepted?

> pbinom(2, 5, 0.3)

[1] 0.83632

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3) An unbiased coin is tossed 6 times. The probability of head at any toss = 0.3  
 Let  $x$  be no. of heads that comes up. Calculate  $P(x=2)$ ,  $P(x=3)$ ,  $P(1 \leq x \leq 5)$

> abinom(2, 6, 0.3)

[1] 0.324135

> abinom(3, 6, 0.3)

[1] 0.18522

> abinom(2, 6, 0.3) + abinom(3, 6, 0.3)

+ abinom(4, 6, 0.3)

[1] 0.74373

4) For  $n = 10$ ,  $p = 0.6$ , evaluate binomial probabilities and plot the graphs of pmf & cdf.

> x = seq(0, 10)

> y = abinom(x, 10, 0.6)

> y

[1] 0.0001048576  
0.0424673280

0.0015728640 0.0168632

0.114767360 0.20066892

0.2508226560

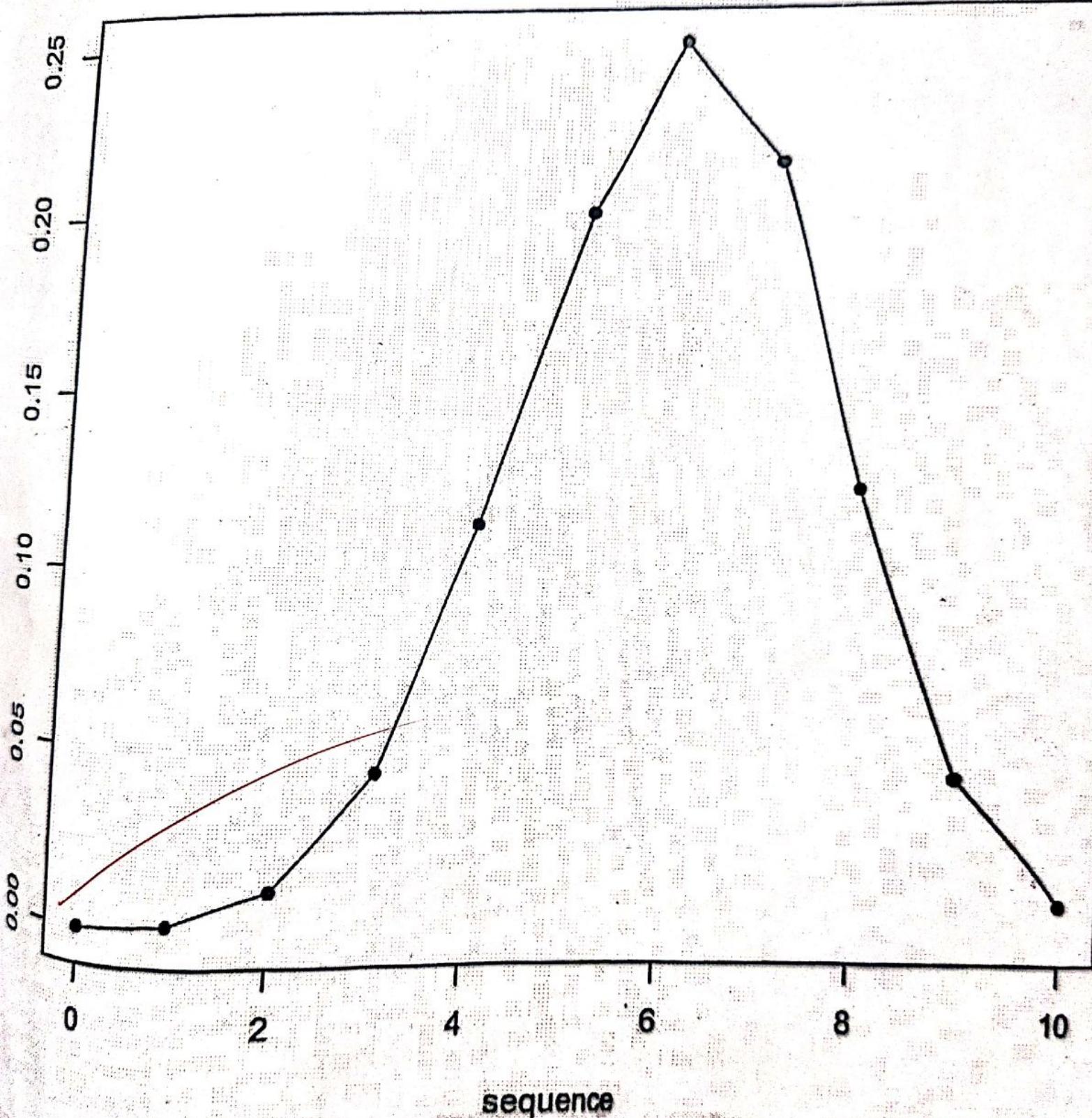
0.2149908480 0.120932

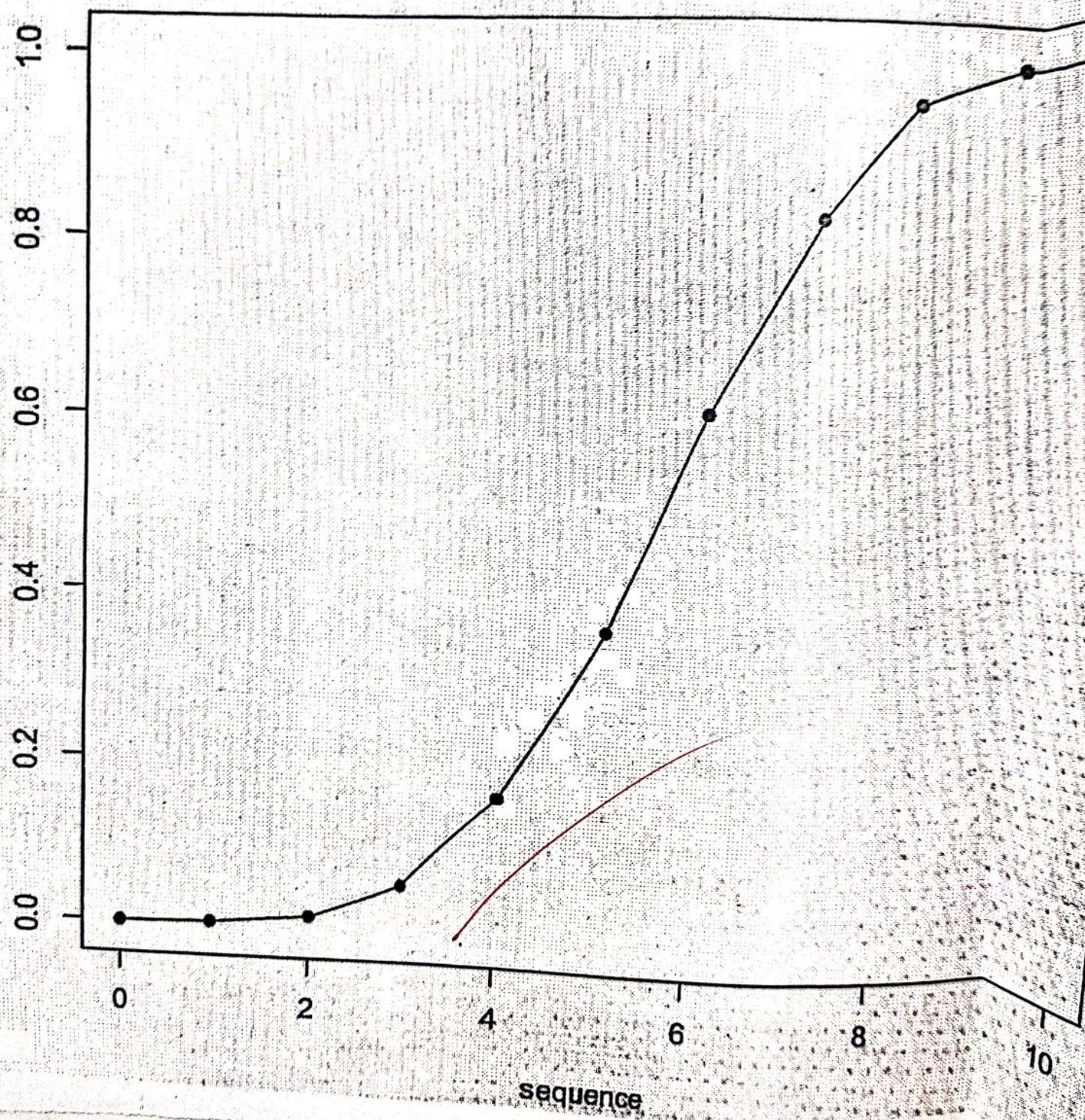
0.0403107840

0.0060466176

> plot(x, y)

"probabilities" "sequence", "a", "pch=16")





```

> x = seq(0, 10)
> y = pbinom(x, 10, 0.6)
> plot(x, y, xlab = "Sequence", ylab =
  "Probability", "0!", pch = 16,

```

5) Generate a random sample of size 10 for a B.D  $\rightarrow$  B(0.3). Find the mean & the variance of the sample

```

> rbinom(9, 10, 0.3)
[1] 2 2 3 4 3 4 2 3
> mean(rbinom(8, 10, 0.3))
[1] 2.375
> var(rbinom(8, 10, 0.3))

```

6) The probability of men hitting the target is  $\frac{1}{4}$ . If the shoots 10 times what is the probability that he hits the target at least one.

```

> abinom(3, 10, 0.25)
[1] 0.2502823
> 1 - abinom(1, 10, 0.25)
[1] 0.8122883

```

back up.

→  $\text{Ibrom} \quad [2] \\ 0.340 \quad \text{O}_2 = =$

"methyl"



## Practical No. 3.

### [TITLE]: NORMAL DISTRIBUTION.

- A normal distribution of 100 students with mean marks 40 & deviation 15  
 Find the no. of students whose marks are
- (1) less than 80
  - (2) 40 & 70
  - (3) 25 & 35
  - (4) more than 60.

→ mean = 40

s.d = 15

$$0.5 - \text{pnorm}(50, 40, 15)$$

$$0.2524725$$

$$\text{pnorm}(10, 40, 15) - \text{pnorm}(40, 40, 15)$$

$$0.4839377$$

$$\text{pnorm}(35, 40, 15) - \text{pnorm}(25, 40, 15)$$

$$0.210786$$

more than 60

$$\text{pnorm}(60, 40, 15, \text{lower.tail} = \text{F})$$

$$0.0912122$$

If the random variable ' $x$ ' follows a normal distribution with mean 50 & variance 100, S standard deviation

$$\text{Find } (1) P(x < 70) \quad (2) P(x > 65) \quad (3) P(x \leq 30)$$

$$(4) P(-35 < x < 60) \quad (5) P(20 < x < 32)$$

$$\text{Pnorm}(34, 50, 10) - \text{Pnorm}(20, 50, 10) \\ = 0.05482180$$

3) Let  $x \sim (60, 400)$  find let  $k_2$   
such that  $P(x < k_1) = 0.6$   
 $P(x > k_2) = 0.8$

$$\rightarrow \text{qnorm}(0.6, 160, 20) \\ + 65.0669$$

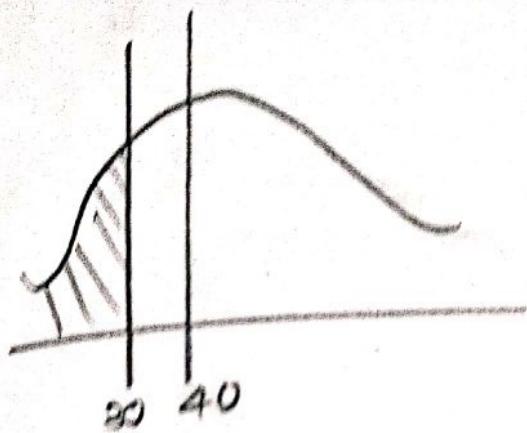
$$\text{qnorm}(0.2, 160, 20) \\ 143.1676$$

4) A random variable  $x$  follows normal distribution with  $\mu = 10, \sigma^2 = 2$ .  
Generally 100 observations and  
find mean, median & variable

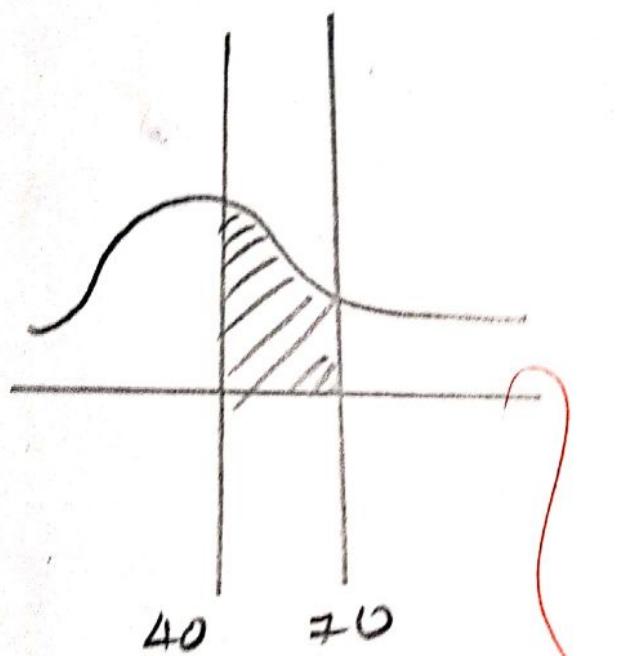
$$\rightarrow \text{pnorm}(100, 10, 2) \\ \text{mean} = 9.911 \\ \text{median} = 9.928 \\ \text{variable} = 4.13785$$

5) write a command to generate  
to standard deviation  $s.d.$   
deviation  $s.d.$  for  $s.d.$   
find the median.  
Sample mean

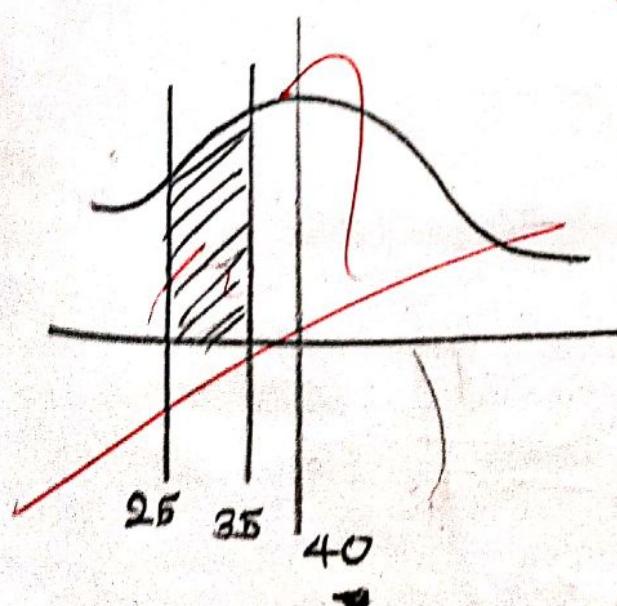
$$\rightarrow \text{pnorm}(10, 50, 10) \\ \text{mean} = 51.455 \\ \text{median} = 51.455$$



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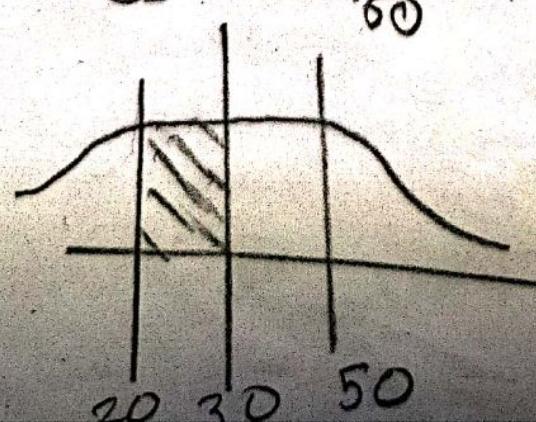
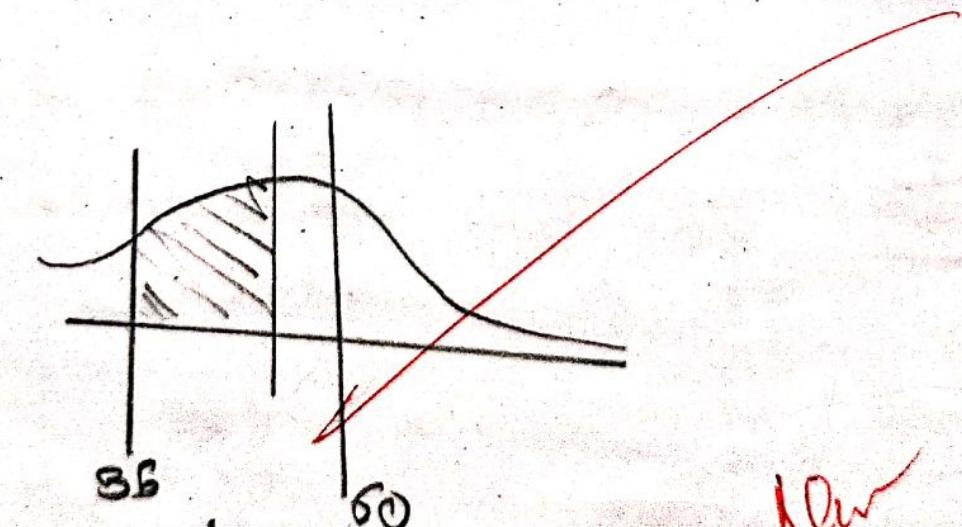
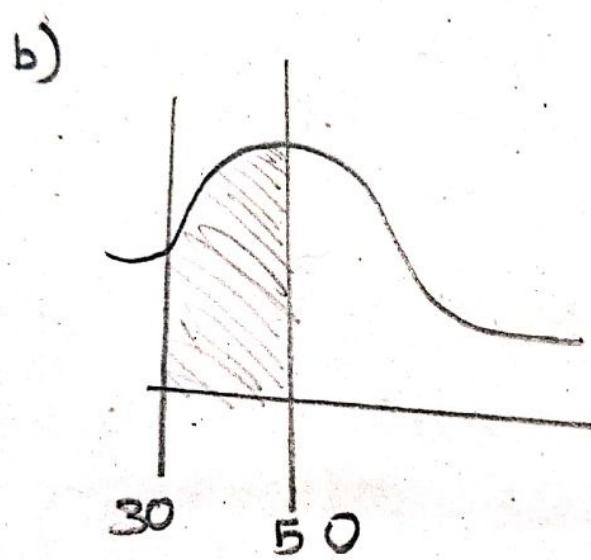
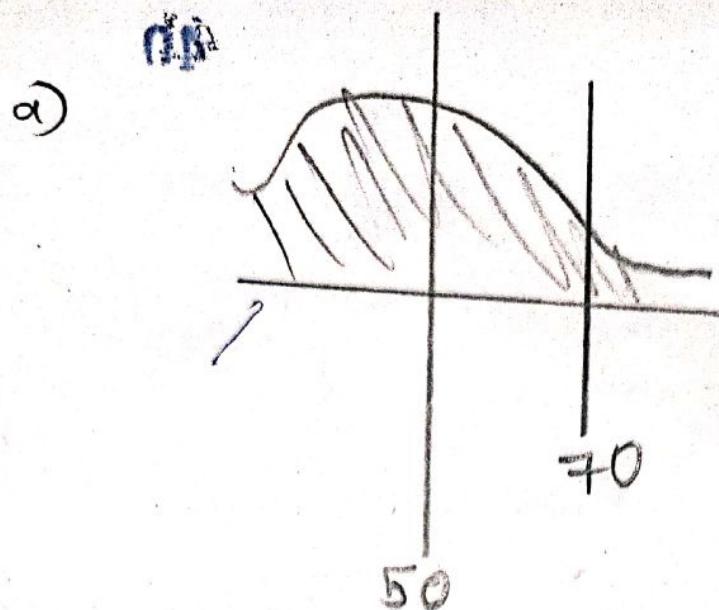


40 70



25 35 40





### Practical No. 4

Aim: Sample mean & deviation given single population.

- i) Suppose the food level on the cookie bag that it has almost of seaweed salt in a single cookie. In a sample of 35 cookies it was found that mean and average of seaweed salt is 21g. Assume the S.D is 0.3 (5% level of significance)

$$\Rightarrow \sigma = 0.3$$

$$n = 35$$

$$\bar{x} = 21$$

$$\alpha = 2$$

$$x_0 = (\text{null hypothesis}) = \mu < 2$$

$$x_1 = (\text{alt hypothesis}) = \mu > 2$$

$$z = \frac{\bar{x} - \alpha}{\frac{\sigma}{\sqrt{n}}}$$

$$z = \frac{21 - 2}{\frac{0.3}{\sqrt{35}}} = 1.8720.21$$

$$p\text{-value} = 1 - \text{prob}(z) \\ = 0.0243$$

∴ Reject the null hypothesis ∵ p value  
∴ Accepted alternate hypothesis  $< 0.05$

Q2

A sample of 100 customers was randomly selected & it was found that already was 275%. the  $SD = 30$  using 0.05 level of significance, would you conclude that the amount spent by the customer is more than 250% whereas the rest want claim that it is not = 250%.

$$\Rightarrow \bar{x} = 275, u = 250, \sigma = 30, n = 100$$

$$x_0 = u \leq 250$$

$$x_1 = u > 250$$

$$z = \frac{\bar{x} - u}{\frac{\sigma}{\sqrt{n}}} = \frac{275 - 250}{\frac{30}{\sqrt{100}}} = 8.33$$

$$\Rightarrow pt(z \geq 8.33, \text{ lower tail}) = F$$

$$\therefore P\text{-value} = 2 \cdot 305 + 36 \cdot e^{-13}$$

$\Rightarrow$  Reject the null hypothesis p-value  $< 0.05$   
Accept the alternate hypothesis ( $-u > 250$ )

Q3] A quality control engineer finds that sample of 100 have average life 470 hours. Assuming population test whether the population mean is 480 hours vs population means  $> 480$  hours at 1.05  $\rightarrow 0.05$ .

$$n = 100, \bar{x} = 420, u < 480, \sigma = 25$$

$$u = 480$$

$$\rightarrow z = \frac{\bar{x} - u}{\frac{\sigma}{\sqrt{n}}} = -4$$

$$P\{t(7, 99) \text{ lower tail} = T\}$$

$$= \underline{\underline{1.112576e-05}}$$

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Reject the null hypothesis

$$\underline{\underline{P > 0.08}}$$

accept the alternative hypothesis.

$$m_1 < +80.$$

- Q.4) A principal at school claims that the IQ is 100 of the students. A random sample of 20 students whose IQ was found to be 112. The SD of population is 15. Test the claim of principal.

> method 1 : 1 tail test

$$\bar{x}_0 = u = 100$$

$$x_1 = e = 100$$

$$\bar{x} = 112, 5 \cdot D = 15 \quad u = 100 ; n = 20$$

$$Z = \frac{\bar{x} - u}{\sigma}$$

$$= \frac{112 - 100}{\frac{15}{\sqrt{20}}} = 4.38118$$

$$P \text{ value} = 8 - 8856 \cdot e^{-0.6}$$

$\Rightarrow$  Reject the null hypothesis claims of principal  
( $u = 100$ )

method 2 : 2 tail test

$$\bar{x}_0 = e = 100$$

$$x_1 = u = 100$$

$P\text{ value} = 2 \times (1 - \text{pnorm}(\text{abs}(2))) = 1.77134$

→ Reject the null hypothesis.  $\therefore P\text{ value} = 0.05$

SP2

\* Single population proportion.

- Q.4) It is believed that coin is fair. The coin is tossed 40 times. 125 times head occurs. Indicate whether the coin is fair or not at 1% c.o.c

$$\Rightarrow Z = \frac{p - p_0}{\sqrt{\frac{p_0 q_0}{n}}}$$

$$p_0 = 0.5 \quad q_0 = 1 - p_0 = 0.5 \quad p = \frac{28}{40} = 0.7$$

$$n = 40$$

$$Z = \frac{0.7 - 0.5}{\sqrt{\frac{0.5 \times 0.5}{40}}}$$

$$z_0 = u = 0.5$$

$$z_1 = u \neq 0.5$$

$$\rightarrow P\text{ value} = 2 \times (1 - \text{pnorm}(\text{abs}(2)))$$

$$\therefore P\text{ value} = 0.01141209$$

→ Reject the null hypothesis.  $\therefore P < 0.05$

Accept the alternate hypothesis.

## Equality of 2 population proportion.

In an early election campaign, a telephone poll of 800 registered voters shows favour 460. In second poll opinion 520 of 1000 registered voters favoured the Credit Candidate at 5% level of confidence is there sufficient evidence that popularity has decreased?

$$H_0 = P_1 \neq P_2$$

$$H_1 = P_1 \neq P_2$$

$$> p = (460 * 800 + 520 * 1000) / (520 + 1000)$$

$$> p$$

$$> [1] 0.544$$

$$> 1 - 0.544$$

$$> 0.456$$

$$> z = \text{sqrt} [0.544 * 0.456 * (1/520 + 1/1000)]$$

$$> * (1 - \text{Prnorm}(\text{abs}(z)))$$

$$[1] 0.5444$$

Accept  $H_0$ .

From a consignment 200 articles are drawn and 44 was found defective from consignment B. 200 sample test whether the proportion of defective items in consignment are significantly.

$H_0 = P_1 = P_2$  non significant at 10% ptile up to

$H_1 = P_1 \neq P_2$

$$> (0.22 * 200 + 0.15 * 200) / (1 * 200, 11/200)$$

$$> 0.185$$

$$> 1 - 0.185$$

$$> Z = (0.185 * 0.815 * (1/200 + 1/200))$$

$$> Z * (1 - \text{norm}(\text{abs}(Z)))$$

$$[+] 0.9969018$$

Accept  $H_0$ .

$$\text{At } P < 0.05$$

$$Z = 1.96$$

$$Z = 1.96$$

$$Z = 1.96$$

$$Z = 1.96$$

## Practical No.5

41.

### Aim: Chi square test

Use the following data to test whether the attribute condition of home and child are independent.

| Condition of child | Clean & cleanliness |       | Condition of Homes |       |
|--------------------|---------------------|-------|--------------------|-------|
|                    | clean               | dirty | clean              | dirty |
|                    | 70                  | 50    |                    |       |
|                    | 80                  | 20    |                    |       |
|                    | 35                  | 45    |                    |       |

$H_0$  = Both are independent,  $H_1$  = Both are dependent.

>  $x = c(70, 80, 35)$

>  $y = c(50, 20, 45)$

>  $z = \text{data.frame}(x, y)$

|   | $x$ | $y$ |
|---|-----|-----|
| 1 | 70  | 50  |
| 2 | 80  | 20  |
| 3 | 35  | 45  |

> chisquaretest  $\rightarrow$  chisqtest(z)  
Pearson's chi squared test

data : 2  
 $\chi^2$  - squared = 25.646, df = 2, p-value = 2.698e-06

∴ Reject the null hypothesis.

∴ Both are dependent.

Q.2] A dice is tossed 120 times and following 100 rolls are obtained

| NO. of terms | frequency |
|--------------|-----------|
| 1            | 30        |
| 2            | 25        |
| 3            | 18        |
| 4            | 10        |
| 5            | 22        |
| 6            | 15        |

Test the hypothesis that dice is unbiased

$\therefore H_0$  = dice is biased

$\therefore H_1$  = dice is unbiased

$$\text{> obs} = ((30, 25, 18, 10, 22, 15))$$

$$\text{> exp} = \text{sum (obs)} / \text{length (obs)}$$

$$\text{> exp} = 20$$

$$\text{> z} = \text{sum} ((\text{obs} - \text{exp})^2 / \text{exp})$$

$$\text{> Pchisq (z, d = length (obs) - 1)}$$

$$[1] 0.956659$$

$\therefore$  Accept the null hypothesis

$\therefore$  dice is biased.

Q.3) An IQ test was conducted and the students were observed before and after training the result are following.

| <u>before</u> | <u>after</u> |
|---------------|--------------|
| 110           | 120          |
| 120           | 118          |
| 123           | 125          |
| 132           | 126          |
| 125           |              |

Test whether there is change in the IQ after the training.

$\therefore H_1$  = No change in IQ

$\therefore H_0$  = IQ increased after training.

$> a = c(120, 118, 125, 136, 121)$

$> b = c(110, 120, 123, 132, 125)$

$> z = \text{sum}((b-a)^2 / a)$

$> pchisq(z, df = \text{length}(b) - 1)$

[1] 0.1135959

Accept the null hypothesis

$\therefore$  There is no change in IQ after training.

|              | Graduate | undergraduate |
|--------------|----------|---------------|
| Online       | .20      | 25            |
| face to face | 40       | 5             |

Is there any association between students's preference for type of education and method.

$\therefore H_0$  = Independent

$H_1$  : Dependent

$> x = c(20, 40, 25, 5)$

$> z = \text{matrix}(x, \text{ncol} = 2)$

$> \text{chisq.test}(z)$

Pearson's chisquared test with 9 d.f

data : z

$x^2$  : squared = 18.06, df = 1, P-value = 2.157e-05

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- ∴ Reject null hypothesis
- ∴ Both are dependent

A dice is tossed 180 times

| No. of terms | frequency |
|--------------|-----------|
| 1            | 20        |
| 2            | 30        |
| 3            | 35        |
| 4            | 40        |
| 5            | 12        |
| 6            | 43        |

Test the hypothesis that dice is unbiased

$H_0$  = dice is biased

$H_1$  = dice unbiased

$\chi^2 = c(20, 30, 35, 40, 12, 43)$

chi sq. test ( $\chi^2$ )

chi squared test for given probabilities

data: 2

$\chi^2$ -squared = 23.933, df = 5, pvalue

= 0.0002236

∴ Reject null hypothesis

∴ dice is unbiased

## Practical No.6

46

Title : T test.

Q.1] Let  $x = 3366, 3337, 3361, 3410, 3316, 3357, 3338,$   
 $3356, 3876, 3388, 3377, 3355, 3408,$   
 $3409, 3388, 3424, 3328, 3374, 3384,$   
 $3374.$

write the R command for following to test

$$\textcircled{1} \quad H_0: \mu = 3400, H_1: \mu \neq 3400$$

$$H_1: \mu > 3400.$$

$$\textcircled{2} \quad H_0: \mu = 3400, H_1: \mu < 3400$$

$$\textcircled{3} \quad H_0: \mu = 3400$$

at 95% level of confidence also check  
 at 97% level of confidence

$$\text{Ans: } H_0: \mu = 3400$$

$$H_1: \mu \neq 3400$$

> to test ( $x, \text{mu} = 3400, \text{alter} = -1 \text{ one.sided}$ )  
 config.level = 0.45)  
 one sample test

data: x

$t = -4.4865, df = 19, \text{Pvalue} = 0.0002528$   
 alternative hypothesis true mean is not  
 equal to 3400

95 percent confidence level

3366(0.759) 3386.103

Sample Estimate:

mean of x : 3373.95.

Sample Estimate:

mean of  $x$ :

3373.95

∴ Reject  $H_0$

∴ Accept  $H_1$

> t-test ( $x, m_0 = 3400$ , alter = "two-sided", conf.level = 0.95)

one sample % test

data:  $x$

$x = -4.4865$ ,  $df = 19$ , p-value = 0.002528

alternative hypothesis : true mean is not equal to 340

3360.33 3387.57

Sample Estimate

mean of  $x$ : 3373.95

∴ Reject  $H_0$

∴ Accept  $H_1$

2)  $H_0: \mu = u = 3400$

$H_1: \mu > 3400$

> t-test ( $x, m_0 = 3400$ , alter = "greater", conf.level = 0.95 ! one sample test)

data:  $x$

$t = -4.4865$ , df = 19, p value =

95 percent confidence  
sample estimate  
mean  $\bar{x} = 3383.95$

alternative hypothesis true mean is greater than  
3400

3363.91 Inf.

$$H_0 \neq \mu_1 = 3400$$

$$\mu_1 = \mu < 3400$$

>t.test(x, mu = 3400, alter = "less", conf.level = 0.95)  
one sided t-test

data : x

→ -4.9866, df = 19, P.value = 0.0001264

alternative hypothesis true mean is less than  
3400

95 percent level as Confidence hf 3383.99

Sample Estimate

mean of x :

3373.95

∴ Reject  $H_0$  ; Accept  $H_1$

>t.test(x, mu = 3400, alter = "less", conf.level = 0.97)  
one sample t-test

delta : x

t = -4.4866, df = 19, p-value = 0.0001264

alternative hypothesis : True mean is less

then 3400

97 percent of confidence

inf 33.55.563

Sample Estimate :

mean of  $\bar{x}$

3373.95

$\therefore$  Reject  $H_0$   $\therefore$  Accept  $H_1$

Below are the data of gain in weight on 2 different diets A & B

Diet A : 25, 32, 30, 43, 24, 24, 14, 32, 24, 31, 35, 25

Diet B = 99, 84, 22, 10, 47, 31, 40, 30, 30, 32, 35, 18, 21

Ans:  $\therefore H_0 = a - b = 0$   $H_1 = a - b \neq 0$

$\gt a = c(25, 32, 30, 43, 24, 24, 14, 32, 24, 31, 35, 18, 21)$

$\gt b) = f(99, 84, 22, 10, 47, 31, 40, 30, 32, 24, 31, 31, 18, 21)$

t-test (a, b, paired config level = 0.095) = t.alter = "Two sided"

Paired t-test

data : A & B

there is difference in  
value in different conditions  
2000, 20950, 4974, 10036  
60430, 55850, 49336, 3727  
+ 3552  
 $\mu_0 = S_1 = 52$   
 $\mu_0 = S_2 = 52$   
20026 9,490, 58850, 43435, 32200  
20026 15,3490, 58850, 43425  
7.8% test (ca. C<sub>D</sub>, paired = T, after  
confi level = 0.95)

pained to see

part of  
data + ea and ch

Family  
data + co and cb  
+ met (ca, cb) found  
family (ca) + o.s.

alternative hypothesis : true difference in means is less than 99 percent confidence interval:

$$-1 < F < 0.863333$$

Sample estimate:

mean of the difference:

$$-1$$

Accept  $H_0$

a. 4) Two drugs for BP was given & data was collected.

$$D_1: 0.7, -1.6, -0.2, -1.2, -0.11, 3.4, 3.7, 0.8, 0.2$$

$$D_2: 0.1, 0.8, 1.1, 0.1, -0.1, 4.4, 5.5, 1.6, 4.6, 3.4$$

>t.test(d1, d2, alter = "two-sided", paired = TRUE, conf.level = 0.95)

Paired t test

data: d1 and d2

$$t = -4.062, df = 4, p\text{ value} = 0.002833$$

alternative hypothesis: two difference in means is not equal to 0.

95 percent confidence intervals

mean as

the

difference: -1.58

Reject  $H_0 \rightarrow$  Accept  $H_1$ .

Q5) If there is difference in salaries for the same job in 2 different countries.

CA : 53000, 49958, 41974, 44366, 30470,

CB : 62490, 58850, 49995, 52263, 47674, 43552.

$$\therefore H_0 : S_1 = S_2$$

$$\therefore H_1 : S_1 \neq S_2$$

> CA : (63490, 58850, 49495, 52263, 47674, 43552)

> CB : {6.3490, 58850, 49495, 52263, 47674, 43552}

> t-test (ca, cb, paired = T, alter = "two sided", confi level = 0.95)

Paired test

data = ca and cb

t-test (ca, cb, paired) = T, alter = "two sided",  
confi . level = 0.95)

Paired test

data = ca and cb

t = 4.456, df = 5, p-value = 0.00666,

alternative hypothesis : true difference in mean  
is not equal to 0.

45 percent confidence interval:  
- 104.04, 821

Sample estimates:

mean of the difference

$\therefore$  Reject  $H_0$

$\therefore$  Accept  $H_1$

## Practical No. 3

### F Test

D) The variancy in D region of India in 1980 and 2000 are given below test wether the variances at the 2 times are same:

1980 : 22, 23, 28, 26, 42, 45, 38, 46, 43, 50, 51,  
2000 : 44, 48, 49, 48, 42, 43, 50, 41, 43, 50,  
42, 52, 53

$$z = c(22, 23, 28, 26, 42, 45, 38, 46, 43, 50, 51)$$

$$y = c(44, 48, 49, 48, 42, 43, 50, 41, 43, 52, 53)$$

var.test(z,y)

F test to compare two variance  
data: z and y

F = 1.0343, num df = 9, denom df = 11, p-value = 0.491  
alternative hypothesis: Hence section of variance  
is not equal to 33 percent confidence  
(interval).

0.2822877 4.1265887

Sample estimates:  
ratio of variances

1.089826

i) Accept H<sub>0</sub>

ii) Variances of 2 times are same

Q.2) I 25 28 26 22 22 29 31 31 26 31  
 II 30 25 31 32 23 25 36 26 31 32 27 31 28 24

50

at 95% of confidence level check the ratio of the population variance.

$$\bar{x} = c \quad \therefore H_0 = \sigma_1^2 = \sigma_2^2$$

$$H_1 = \sigma_1^2 \neq \sigma_2^2$$

$$\bar{x} = c (25, 28, 26, 22, 27, 31, 26, 31)$$

$$\bar{y} = c (30, 25, 31, 32, 23, 25, 36, 25, 25, 31, 32, 32, 27, 31, 38, 24)$$

$\rightarrow$  var. test ( $x, y$ )

$\rightarrow$  F-test to compare two variance

$$P\text{value} = 0.4535$$

Accept the  $H_0$

$\therefore$  Variance of I and II are same

Q.3) For the following data test the hypothesis for.

1) Equality of 2 population mean  $\rightarrow$  t-test

2) Equality of proportion variance  $\rightarrow$  F-test

2) Equality of proportion variance  $\rightarrow$  F-test

Sample 1: 175, 168, 145, 140, 190, 181, 185, 185, 200.

Sample 2: 180, 170, 153, 180, 183, 199, 183, 187, 205

$$\textcircled{1} \quad H_0 = \mu_1 = \mu_2$$

$$H_0 = \mu_1 \neq \mu_2$$

$$\bar{x} = c (175, 168, 145, 190, 181, 185, 175, 200)$$

$$\bar{y} = c (180, 170, 153, 180, 179, 183, 187, 205)$$

$\rightarrow$  t-test  $E(x, y, \text{alter} = \text{"two sided"})$ , conf.level = 0.951.

$\rightarrow$  t-test  $E(x, y, \text{alter} = \text{"two sided"})$

watch two sample t-test

$$P\text{-value} = 0.777$$

11) Accept  $H_0$

∴ equality of 2 population mean are same.

Q) equality of proportion variance

> val-test (x, y)

F-test to compare two variances

R-value = 0.7759

∴ Accept  $H_0$

∴ equality of proportion variance are same.

Q.4) The following are the price of commodity in the sample of shops selected at random from different city.

City A: 79.10, 77.70, 75.35, 74, 73.80,  
79.30, 75.80, 76.80, 77.10, 79.40

City B: 70.80, 74.90, 76.20, 72.80, 78.10,  
74.90, 69.80, 81.20

$\therefore H_0: \sigma_1^2 = \sigma_2^2$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

>  $x = C (74.80, 77.10, 75.3), 74, 73.80, 79.30,$   
 $75.80, 79.80, 76.80, 77.10, 76.04)$

>  $C (70.80, 74.90, 76.20, 72.80, 78.10, 74.90,$   
~~69.80, 81.20)~~

⇒ var.test(x, y)

t-test to compare two variance

$$\text{P-value} = 0.02756$$

Reject  $H_0$

∴ equality of 2 population mean not same.

⇒ t-test (x, y), var.equal = F, paired = F

welch two sample t-test.

$$\text{P-value} = 0.8244$$

Accept  $H_0$

mean of two population is same.

(Q5) Prepare a CSV file in excel-import the file in R and apply the test to check the equality of variance of 2 data.

observed 1: 10, 15, 11, 16, 20

observed 2: 15, 19, 17, 19, 11, 12, 19

$$\therefore H_0: \sigma_1^2 = \sigma_2^2$$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

Save the above observation in excel

file CSU(ms - HOS) format.

⇒ at data = read.csv(file, choose(), header=)

OB1

|   |    |
|---|----|
| 1 | 10 |
| 2 | 15 |
| 3 | 17 |
| 4 | 11 |
| 5 | 16 |
| 6 | 20 |

OB2

|    |
|----|
| 15 |
| 19 |
| 10 |
| 11 |
| 12 |
| 19 |

attach(data)

var.test(OB1, OB2)

NC

T-test to compare two variance

P-value = 0.5717 suggests H<sub>0</sub> is true.

- Accept H<sub>0</sub>

- The variance at 2 ats are same

~~Practical No. 8~~

Topic: Non param test

d-1) The times of failures in hours after 10 randomly selected 9 volt battery of a certain company is as follows:-  
(28.9, 1.2, 28.9, 72.5, 48.5, 52.4, 39.6, 49.5, 62.1, 154.5)

test the hypothesis that the population median is 63 against alternative is than 63 at 5% (level of significance).

Solution: H<sub>0</sub> = median = 63

H<sub>1</sub> = median > 63

## Practical No. 8

52

Topic : The times of failures in hours after 10 randomly selected 9 volt battery of a certain company is as follows:-

(28.9, 15.2, 28.9, 72.5, 48.5, 52.4, 37.6, 49.5  
62.1, 54.5)

Solution :  $H_0 = \text{median} = 63$   
 $H_1 = \text{median} = 63$

$\rightarrow x = c (28.9, 15.2, 28.9, 72.5, 48.5, 52.4, 37.6,$   
 $49.5, 62.1, 54.5)$

$\gg S_p = \text{len} (\text{which } (x < 63))$

$\gg S_p = \text{len} (\text{which } (x = 63))$

$\gg n = S_n + SD$

$\gg \text{abinom} = (0.05, n, 0.5)$

2

$\gg S_n$

9

$\gg p\text{binom}(S_n, n, 0.5)$

0.9990204

$\rightarrow H_0$  is accepted.

Q.2] The following data gives the weight of 40 students in random samples:-

46, 49, 57, 64, 46, 67, 54, 48, 69, 61, 57, 54, 50, 48, 65, 61, 66, 54, 50, 48, 49, 63, 47, 49, 47, 55, 59, 63, 53, 56, 67, 49, 60, 69, 53, 50, 48, 51, 52, 54

Use the sign test to test whether the mean weight of population is 80 kg's against the alternative that it is greater than 80 kg's.

Solution:  $H_0 = \text{median} = 50$

$H_1 = \text{median} \neq 50$

>>  $x = c(46, 49, 57, 64, 46, 67, 54, 48, 69, 61, 57, 54, 50, 48, 65, 61, 66, 54, 50, 48, 49, 63, 42, 49, 47, 54, 59, 63, 63, 67, 56, 49, 56, 49, 60, 46, 64, 53, 50, 48, 51, 52, 54)$

>>  $S_n = \text{length}(x[x < 50])$

$S_p = \text{length}(x[x < 250])$

$n = S_p + S_n$

>> abinom(0.05, n, 0.5)  
14

>>  $S_n$

13

$S_o, S_A$  is rejected  $H_0$   
 $H_0$  is Rejected

Q.3] The median age of tourist visiting the certain place is claimed to be 41 years. A random sample of 17 tourist have the age 25, 29, 52, 48, 57, 39, 43, 36, 30, 49, 28, 39, 44, 63.

Solution:  $H_0 = \text{median} = 41$

$H_1 = \text{median} \neq 41$

$\gg s = c(25, 29, 52, 48, 57, 39, 43, 36, 60, 30, 49, 28, 39, 44, 63, 32, 65, 42)$

$\gg S_n = \text{len}(\text{which}(s > 41))$

$\gg S_n = \text{len}(\text{which}(s < 41))$

$\text{qneqbinom}(0.05, n, 0.5)$

$\gg n$

$\gg S_n$

$\rightarrow \text{qbinom} = < S_n \ H_0 \text{ is accepted}$   
 $\text{median} = 41 \text{ is Accepted}$

82

The time in minute, that a patient has to wait for consultant is recorded as follows  
 15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 66  
 will use wilcox test to check whether the median wait in time is more than 20 minutes at 5% level of significance

Solution:  $H_0 = \text{median} \geq 20$

$H_1 = \text{median} < 20$

$\Rightarrow x = c(15, 17, 24, 25, 20, 21, 32, 72, 12, 25, 24, 66)$

$\Rightarrow \text{wilcox.test}(x, \text{alternative} = \text{'less'})$

0.999

Accept  $H_0$

5) The weight in kg's of the person before and after he stop smoking.

Before

65

75

75

62

72

After

72

82

72

66

73

Use the wilcoxon test to check whether the weight of person increases after stopping smoking at the 5% level of significance.

Solution:  $H_0$  = weight increased

$H_1$  = weight don't change

$\gg a = c(65, 75, 75, 62, 72)$

$\gg b = c(72, 82, 72, 66, 73)$

$\gg a - b$

$\gg x = [-7, -7, 3, -4, -1]$

$\gg \text{wilcox.test}(x, mu = 0)$

$\gg a - b$

$\gg x$

$-7, -7, 3, -4, -1$

$\gg \text{wilcox.test}(x, mu = 0)$

$\gg p\text{-value} = 0.1756$

$\gg \text{wilcox.test}(x, mu = 0)$

Pair value 70.05

→ Accept  $H_0$

## Practical No. 9

### ANOVA

- 1) The following data given the effect of treatments test the hypothesis that they have the raw effect.

Solution:

$H_0$  : Treatment are equally effective

$H_1$  : Treatment are not equally effective

> a = c(2, 3, 7, 2, 6)

> b = c(10, 8, 7, 5, 10)

> c = c(10, 13, 14, 13, 15)

> d = data.frame(a, b, c)

> e = stack(d)

> oneway.test(values ~ ind, data = e)

P value = 0.0006232

∴ This is enough evidence to reject  $H_0$ .

2) The lifecycle of different brands of types in given

Test whether the driving life of all the type is same.

$H_0$  = life all brands of tyres is same.  
 $H_1$  = life of all brands of tyres is not same.

$$a = c(20, 23, 18, 11, 21, 17, 22, 24)$$

$$b = c(19, 15, 11, 20, 16, 17)$$

$$c = c(21, 29, 22, 11, 17, 20)$$

$$d = c(15, 14, 16, 18, 14, 16)$$

$$m = \text{list}(a, b, c, d)$$

$$n = \text{stack}(m)$$

$$m = \text{list}(p=a, q=b, r=c, d=d)$$

$$e = \text{stack}(m)$$

e

one-way-test(value.ind, data=e, var.equal=True)

$$p\text{-value} = 0.0000$$

Reject  $H_0$

Q) There are types of mask is applied for the protection of case and no. of days of protection were noted test whether there are equally effective.

$H_0$ : equally effective

$H_1$ : not equally effective

$\neq a = c (99, 45, 46, 47, 48, 49)$

$b = c (90, 92, 51, 52, 55)$

$c = c (50, 53, 58, 59)$

$m = \text{list} \cdot (R=a, a=b, a=c)$

$m$

$e = \text{stack}(m)$

$e$

one way test (values = int, rdata = e)

P-value = 0.08225

reject  $H_0$

4) An experiment was conducted 8 person and observation were noted. Test the hypothesis that all groups have equal results on their health. 56

$H_0$  = equal results on their health

$H_1$  = not equal results

$$a = c(23, 26, 51, 48, 58, 37, 29, 44)$$

$$b = c(22, 27, 29, 39, 46, 48, 49, 65)$$

$$c = c(59, 66, 38, 49, 56, 62)$$

d = data.frame(a, b, c)

a = as.matrix(a)

e = stack(e)

e

qov(value ~ int, data = e)

one way: list(value ~ ind data = e)

F value = 0.01683

Reject  $H_0$ .