

→ LIS

↓
Longest Inc Subseq

$$(2-1) == (3-2)$$

$$(4-3) == (3-2)$$

[1, 2, 3] 4

① [1, 2, 3, 4]

[1, 2, 3, 4]



(1, 2, 3)

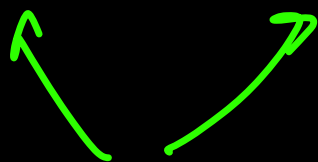
(2, 3, 4)

(1, 2, 3, 4)

at least

3 length

(4, 5, 6)



i

0 1 2 3 4

[1, 2, 3, 4, 5, 6]

1

2 3 4
1+1 1+2 1+3

(2, 3, 4, 5)
(1, 2, 3, 4, 5)

(3, 4, 5)
(2, 3, 4, 5)
(1, 2, 3, 4, 5)

$$arr[i] - arr[i-1] == arr[i-1] - arr[i-2]$$

(i, i-1, i-2)

→ 1, 2, 3, 4, 7, 8, 9
↓ ↓
0 0, 1, 2, 0, 0, 1
↓
0

(1, 2, 3)

(2, 3, 4)

(1, 2, 3, 4)

(7, 8, 9)

$f(i)$
 \downarrow
 no. of
 arithmetic
 subarrays ending
 at i .

Brand new
triplet

$(i, i-1, i-2)$

$$= \begin{cases} 0 \\ 1 + f(i-1) \end{cases}$$

$$\text{if } (a[i] - a[i-1]) = a[i-1] - a[i-2]$$

else

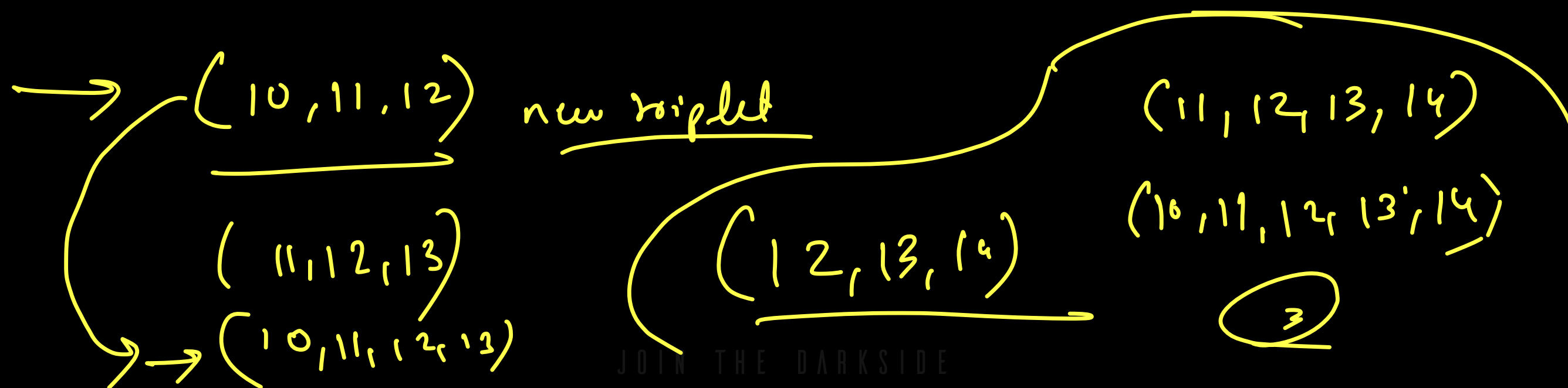
because we can attach i^{th}
 element to all subarrays ending
 at $(i-1)$

$$\text{ans} \rightarrow \sum_{i=0}^{n-1} f(i)$$

↓

| | | | | | |
|---------|-----|-----|-----|----|---|
| 0 | 1 | 2 | 3 | 4 | 5 |
| 10, 11, | 12, | 13, | 14, | 15 | |

$f(i) \rightarrow$ 0 0 1 2 3



$$i=0 \rightarrow f_0$$

$$i=1 \quad f_1$$

$$i=2 \rightarrow f_2$$

$$\downarrow$$

$$f_1$$

$$i=3 \quad f_3$$

$$\downarrow$$

$$f_2$$

$$\downarrow$$

$$f_1$$

$$i=4 \quad f_4$$

$$\downarrow$$

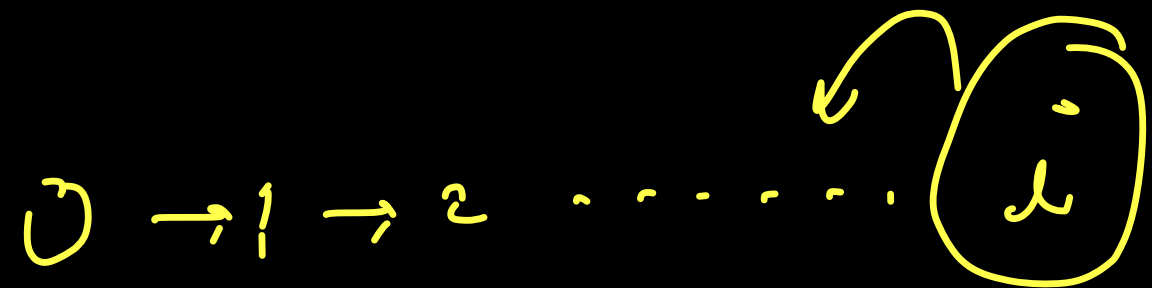
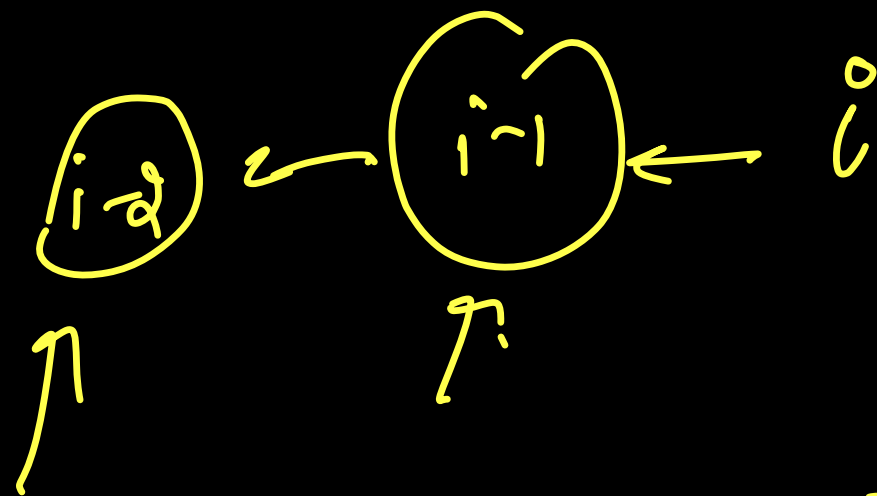
$$f_3$$

$$\downarrow$$

$$f_2$$

$$\downarrow$$

$$f_1$$

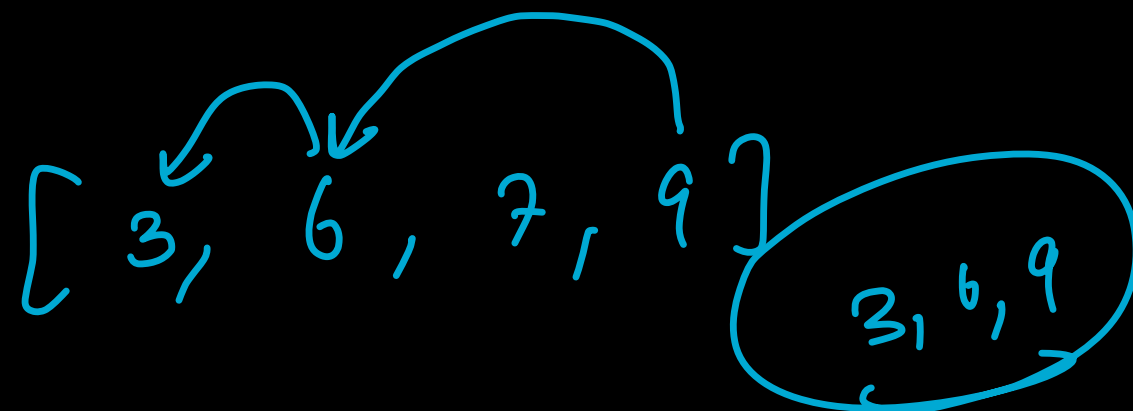


at least 3
elements

ending at i

$[2, 4, 6, 8, 10]$

→ lis



$[2, 4, 6]$

$(4, 6, 8)$ $(2, 4, 6, 8)$

$(10, 8, 6)$ $(2, 4, 6, 8, 10)$

$(10, 6, 2)$

$(4, 6, 8, 10)$

current
subseq &
further
after

(4, 5, 6)
(2, 4, 6)
(4, 5, 6, 7)
(5, 6, 7)
(5, 6, 7, 8)
(6, 7, 8)
(4, 5, 6, 7, 8)

(2, 4, 5, 6, 7, 8, 10)

| | | | | |
|-------|-------|-------|-------|-------|
| (1-1) | (1-2) | (1-3) | (1-4) | (2-4) |
| (3-1) | (2-2) | (2-1) | (2-3) | (4-2) |
| (4-1) | (3-1) | (3-2) | (5-1) | |
| | (5-1) | (4-1) | (6-1) | |
| | | (6-1) | (5-1) | (3-2) |

Ans = 0 + 1 + 1
+ 2 + 3
+ 2 + 1
+ 3 + 1
+ 1 + 1

potential
subseq

well
common
diff &

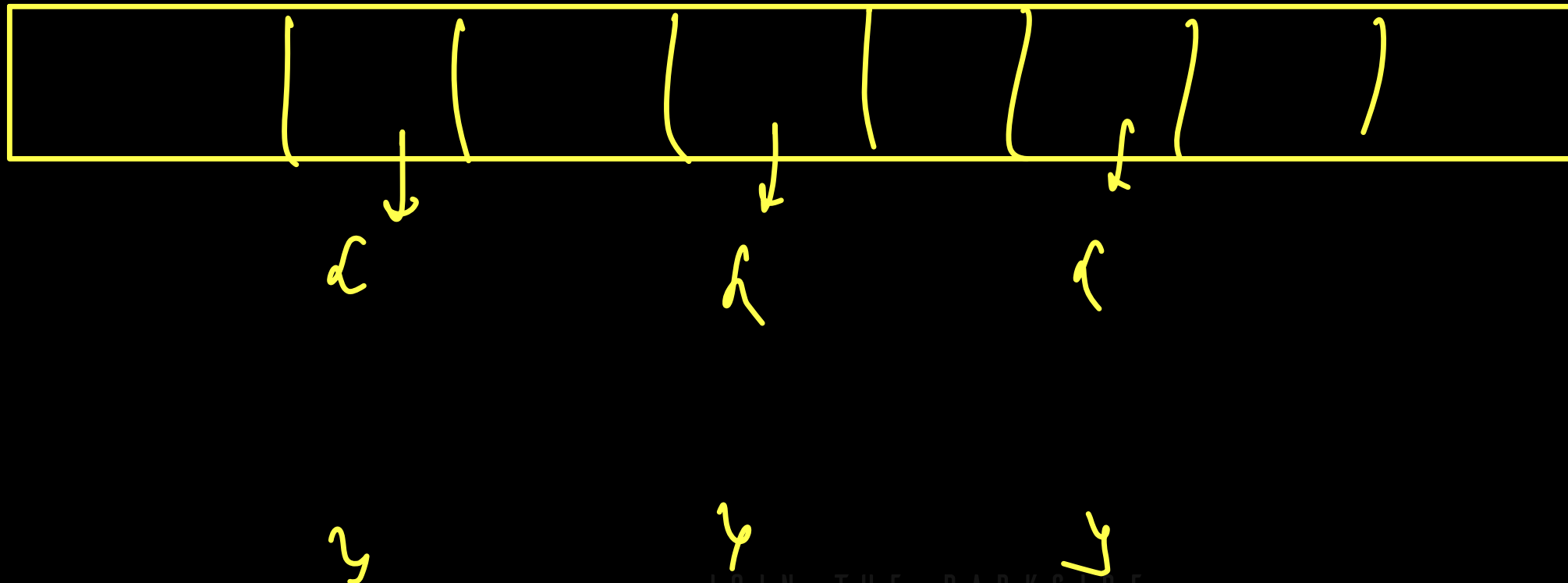
(4, 6, 8)
(2, 4, 6, 8)
(6, 8)

(5, 8)
(4, 5, 8)

dp - dis

ending at every index we store all the subsequences
(arithmetic + non-arithmetic) with a given common
diff

for every value of $i \rightarrow$ $\langle \text{key}, \text{value} \rangle$ diff all poss: 614
subseq



Python → array of dict

JS → array of object

Java → array of hashmap

C++ → array of unordered-map

ans = 0

```
for ( i = 1 ; i < n ; i++) {
```

```
    for ( j = 0 ; j < i ; j++) {
```

```
        diff = arr[i] - arr[j]
```

```
        if ( dp[j].get(diff) ) {
```

```
            ans += dp[j].get(diff) ;
```

```
            dp[i].put( diff, dp[j].get(diff) + 1 )
```

```
        }
```

```
    }
```

```
for ( i = 1 ; i < n ; i++)
```

```
for ( j = 0 ; j < i ; j++)
```

```
diff = arr[i] - arr[j]
```

```
if (dp[j][diff])
```

```
ans += dp[j][diff]
```

```
dp[i][diff] = 1 + dp[j][diff]
```

```
}
```

```
}
```

7, 7, 7, 7, 7
↓ ↓ ↓
13 0-1 0-2

$am = 0 + 1$

| | | | |
|----|----|-----|---|
| 1 | | | |
| 2, | 2, | 3, | 4 |
| ↓ | ↓ | ↓ | |
| { | { | 1+2 | |
| } | } | | |

2