

void A(struct node *t)

{ if (t)

{ 1. Pf ("%c", t->data)

2. B (t->left)

3. B (t->right)

}

}

Void B(struct node *t)

{ if (t)

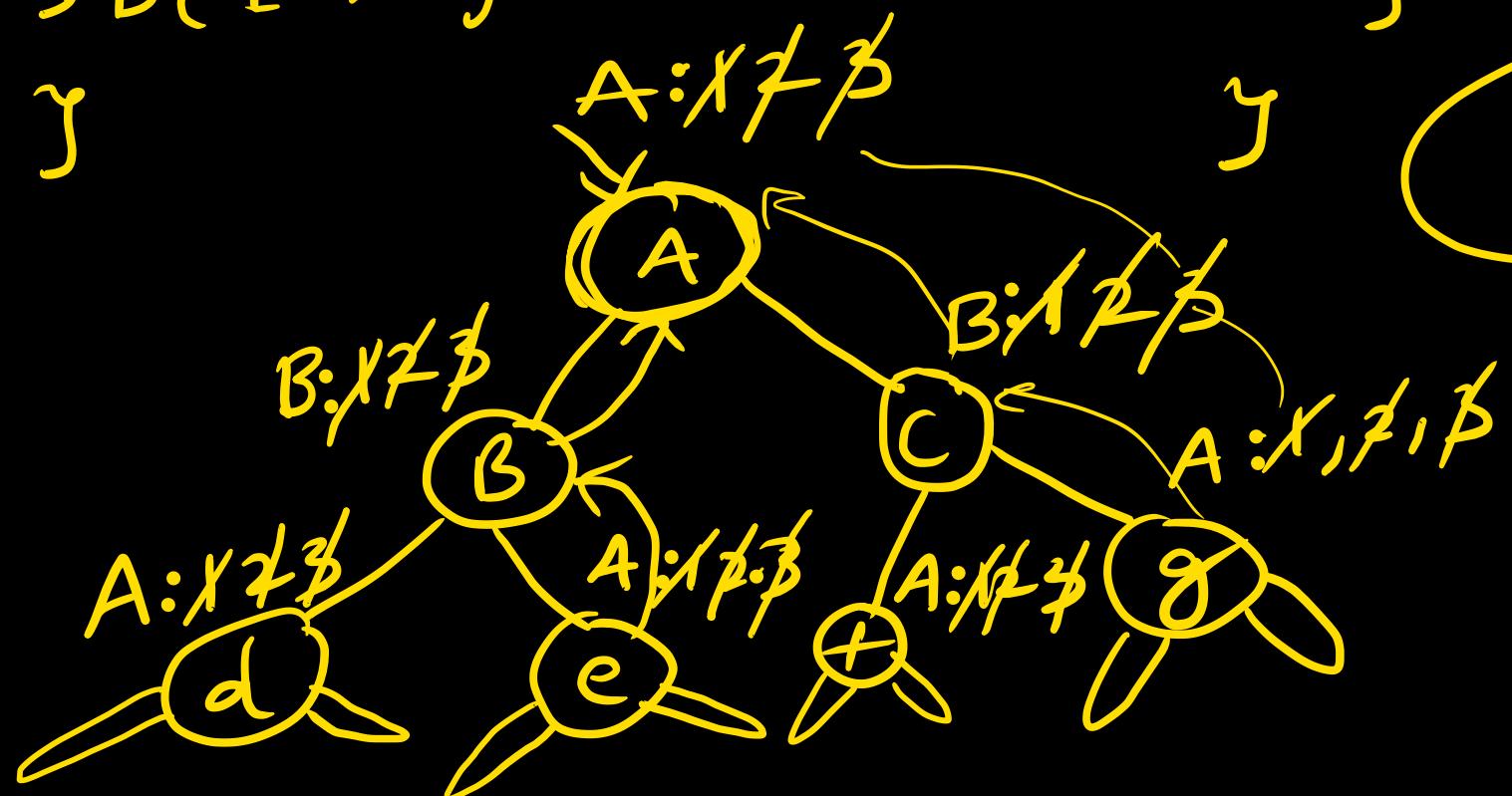
{ 1. A (t->left)

2. Pf ("%c", data)

3. A (t->right)

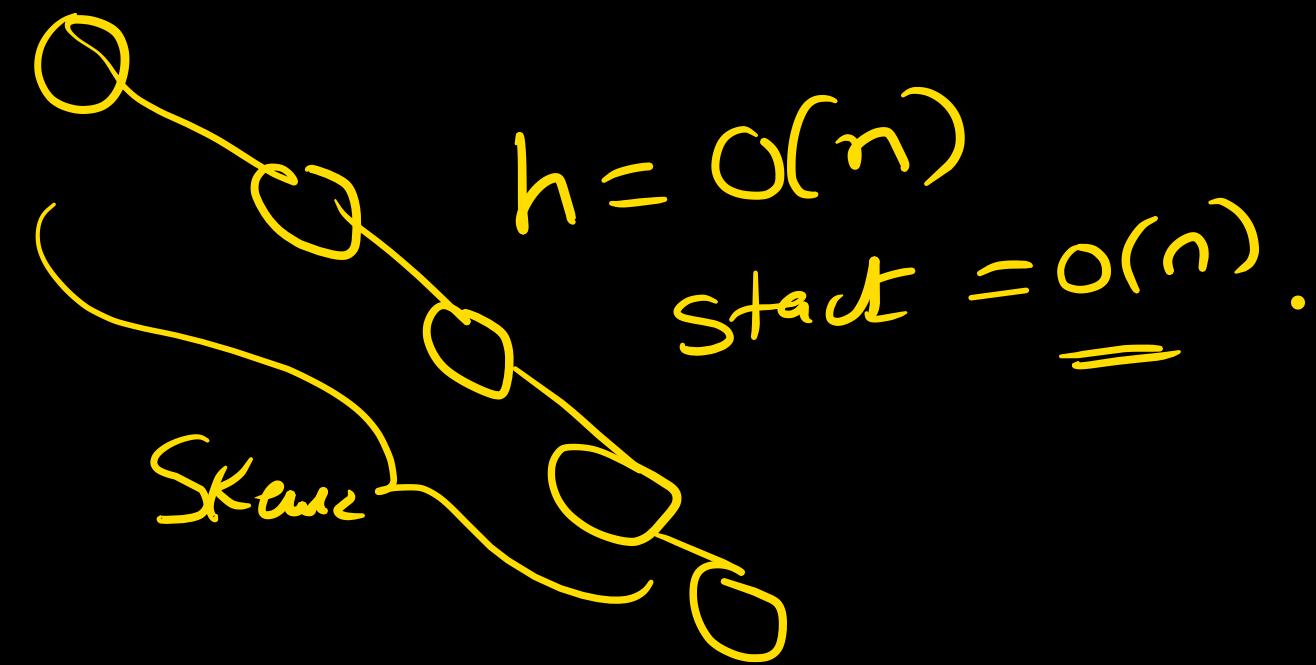
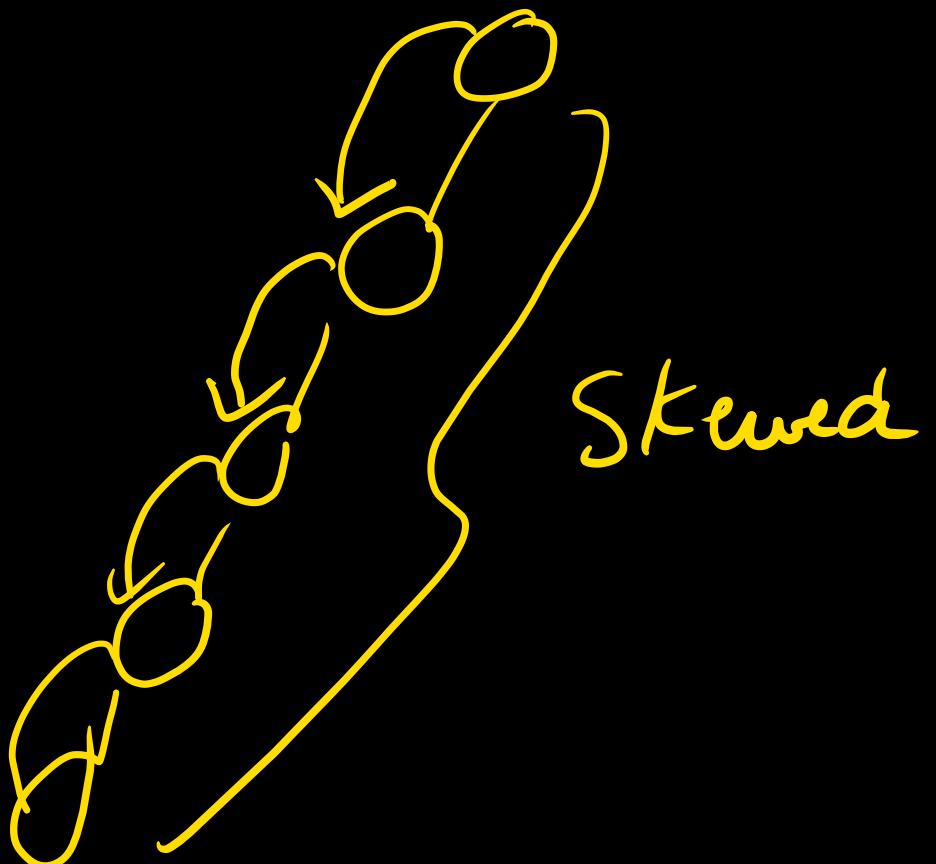
}

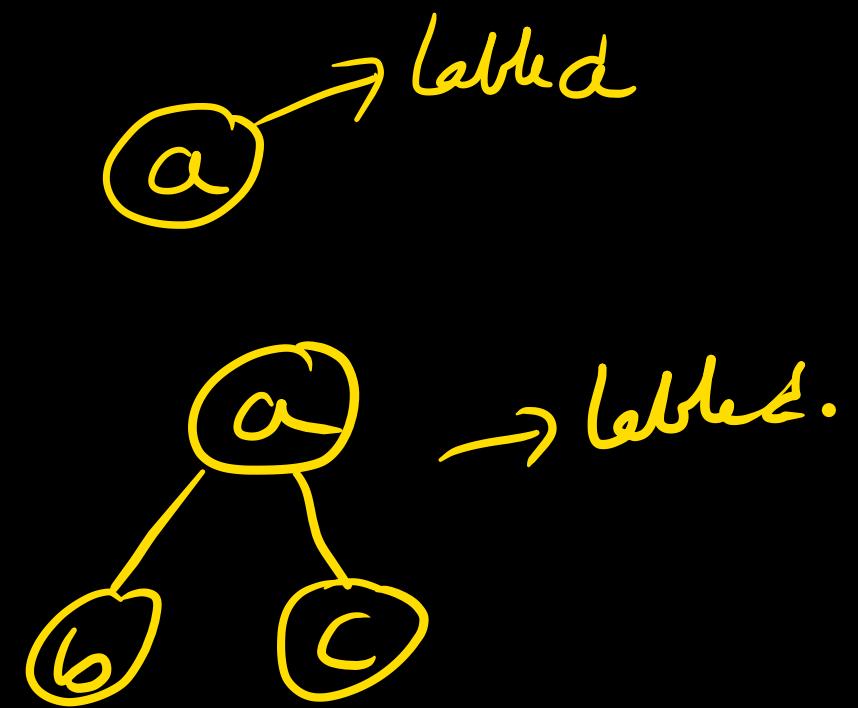
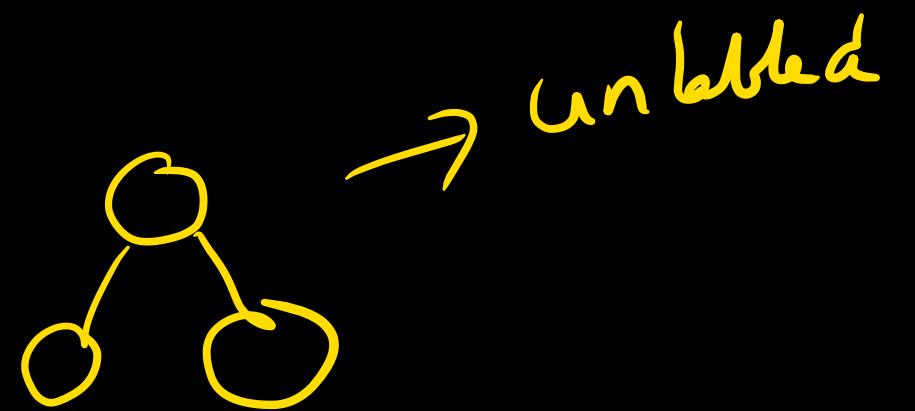
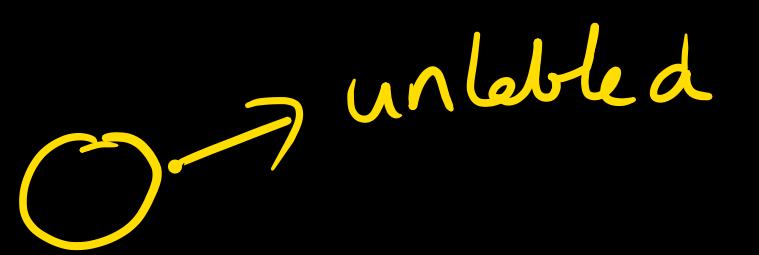
Similar to inorder.



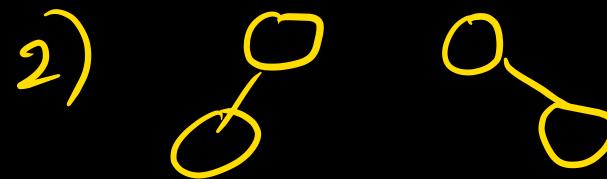
A d B e f g

	TC	SC
Pre	$O(n)$	$O(n) \checkmark$
Ind	$O(n)$	$O(n) \checkmark$
post	$O(n)$	$O(n) \checkmark$





number of unlabeled binary trees:



GATE 2007

- III year

B.Tech.

80

IV

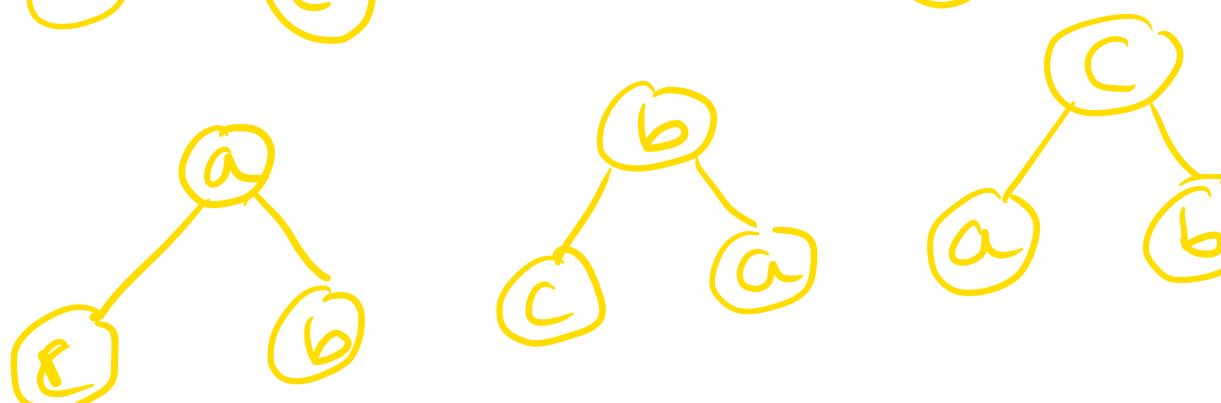
13

50

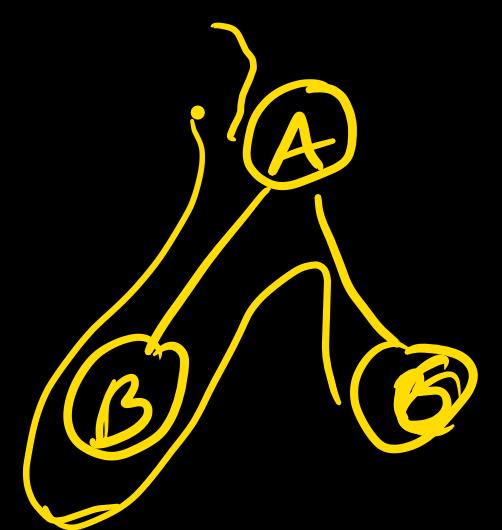
$$\frac{2^{n_c} n}{n+1}$$

labeled =

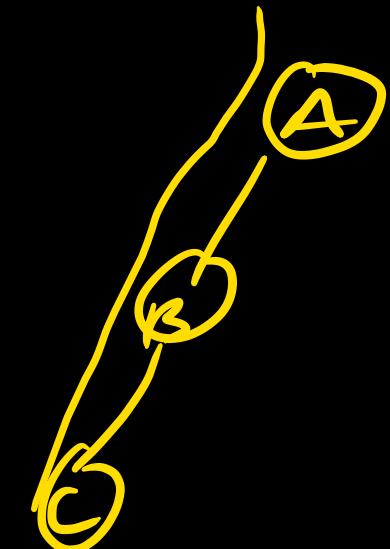
$$\left(\frac{2^{n_c} n}{n+1} \right) * n!$$



Construct a BT Given a pre order \rightarrow uniquely



ABC

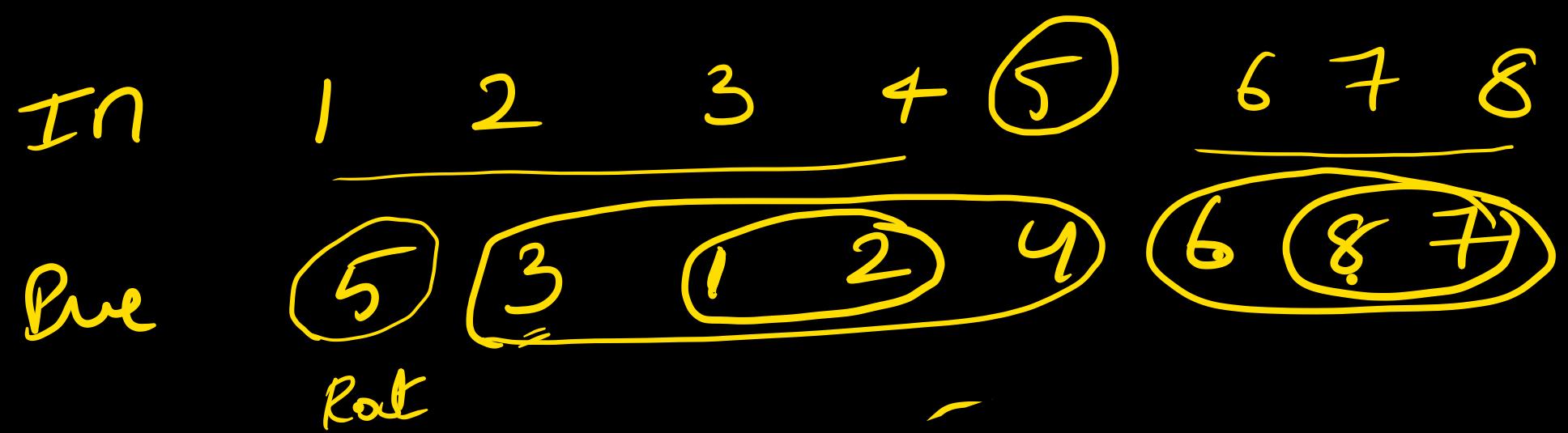


A B C.

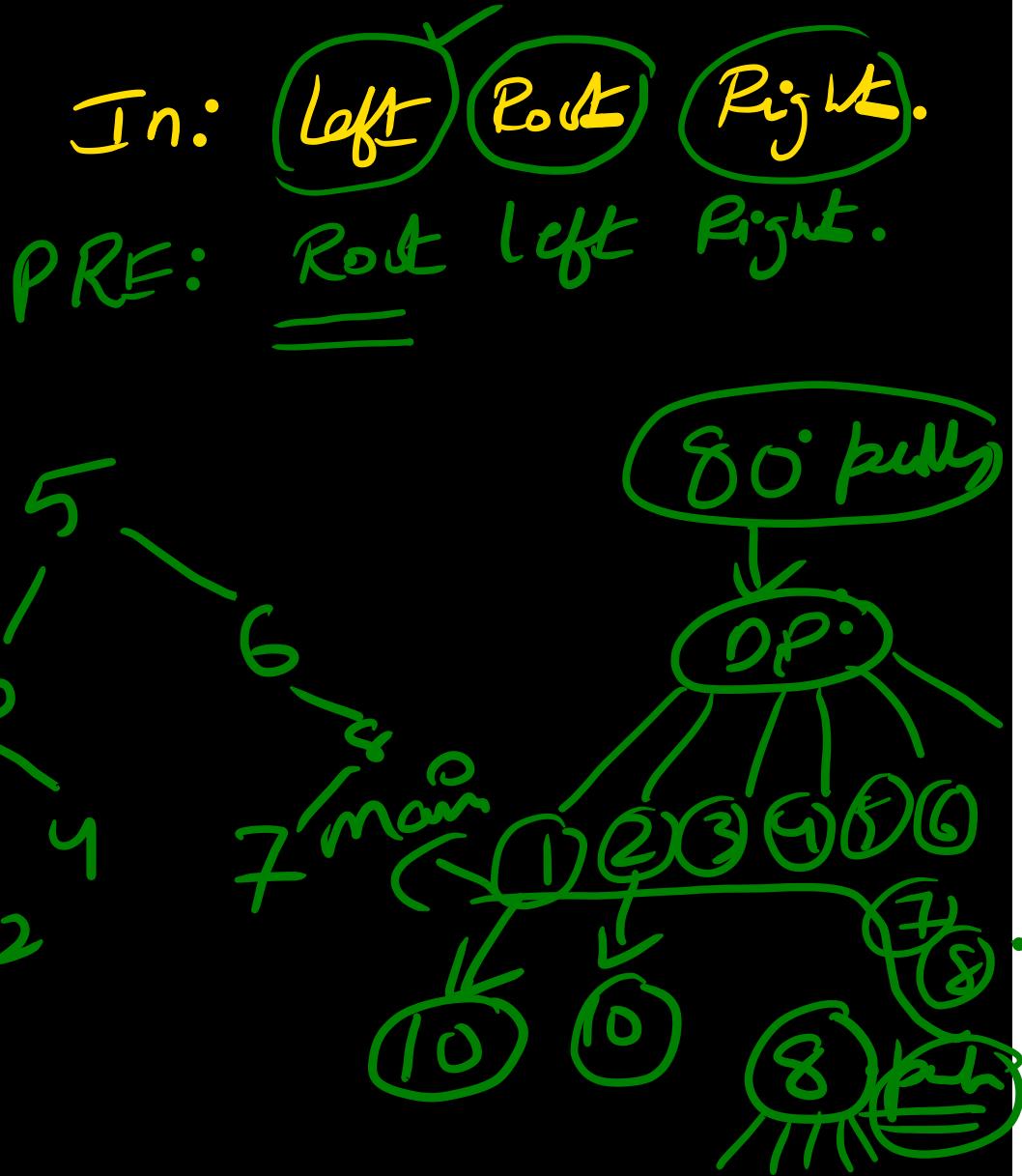
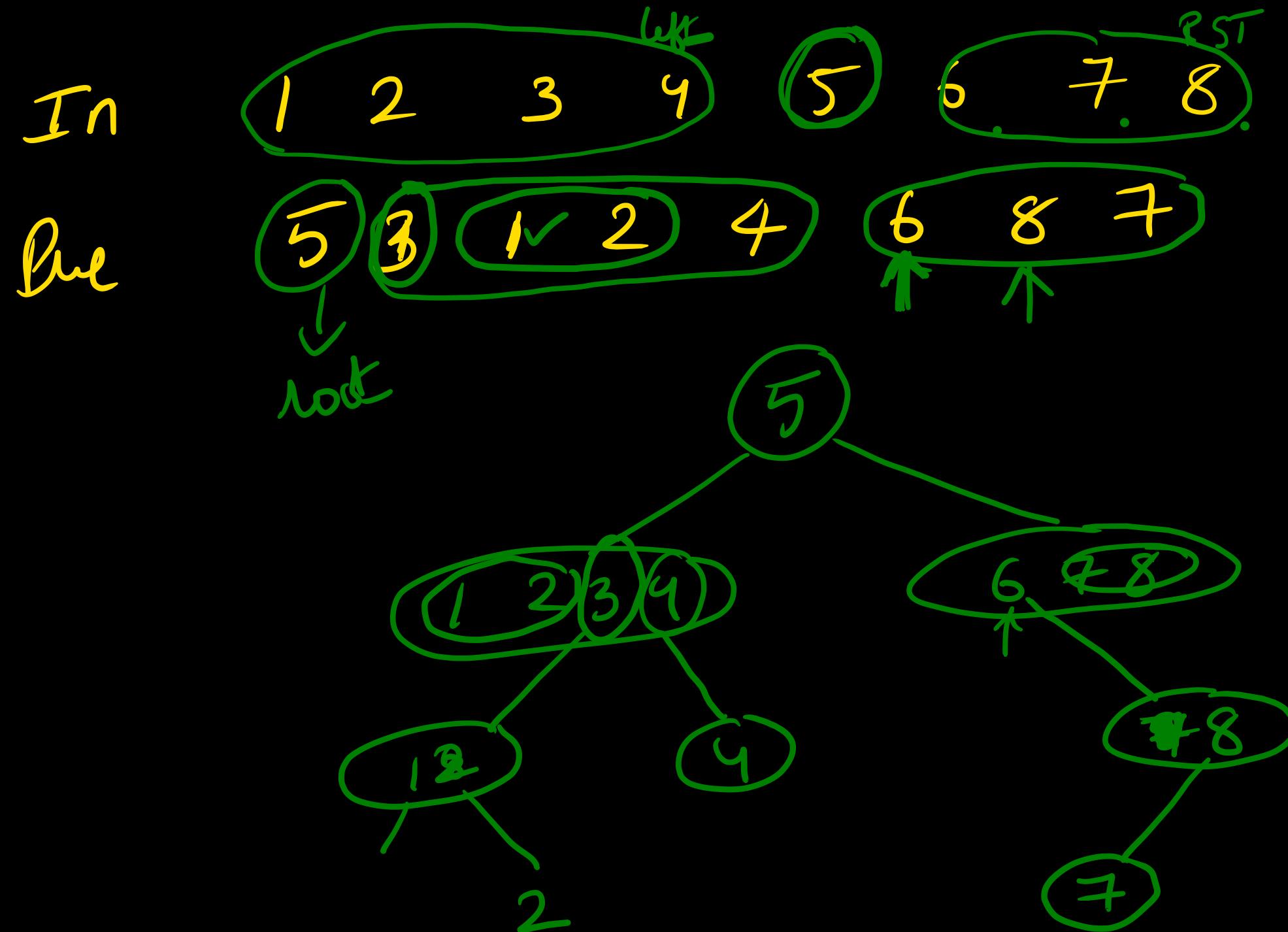
Given a preorder we cannot construct a BST uniquely
" pre-order " " "
" post-order " " "
" in-order " "

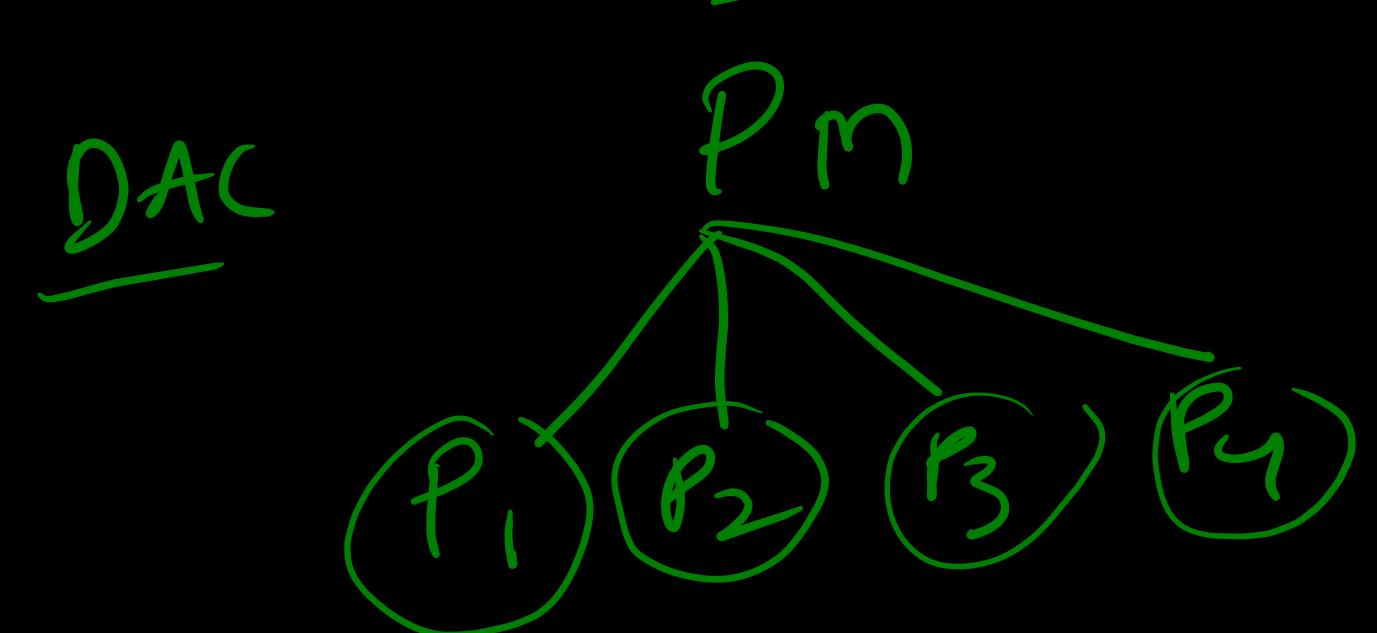
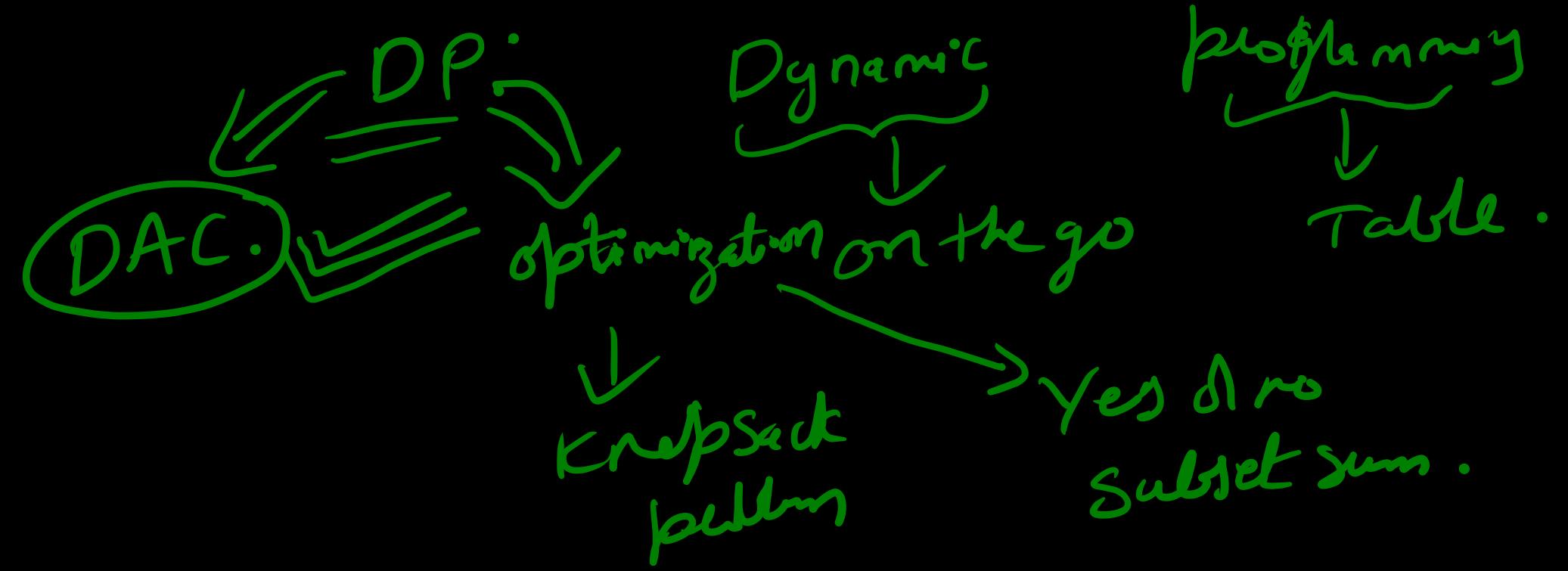
Given In and pre }
In and post } \Rightarrow uniquely.

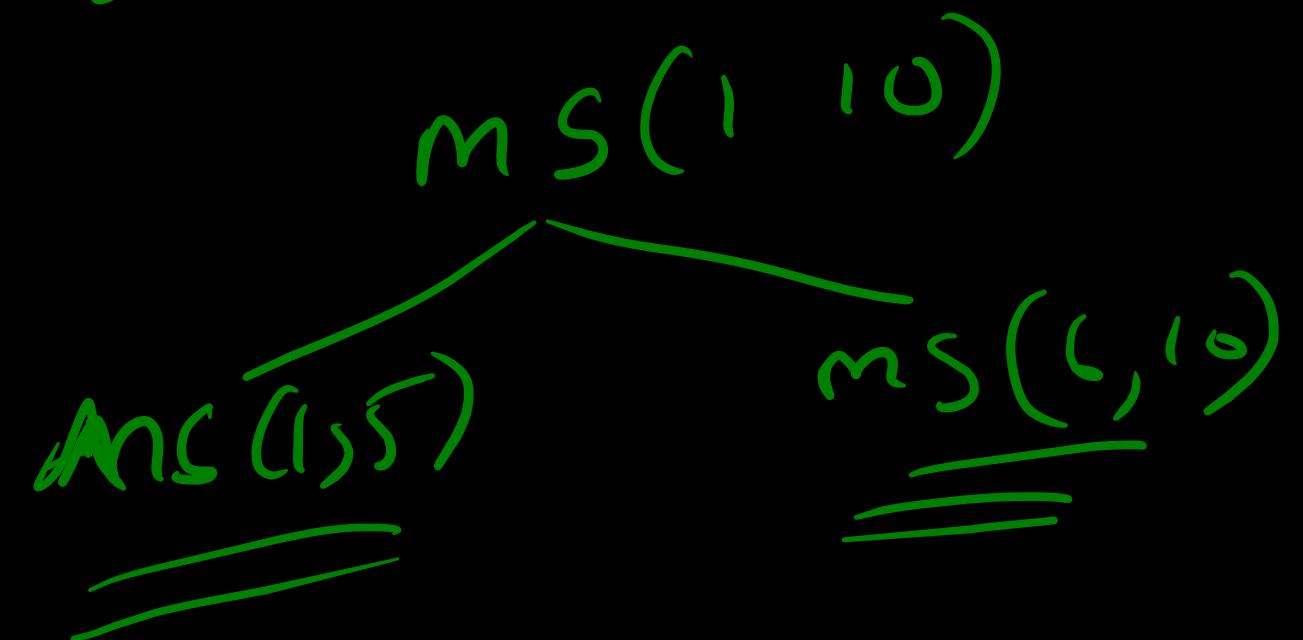
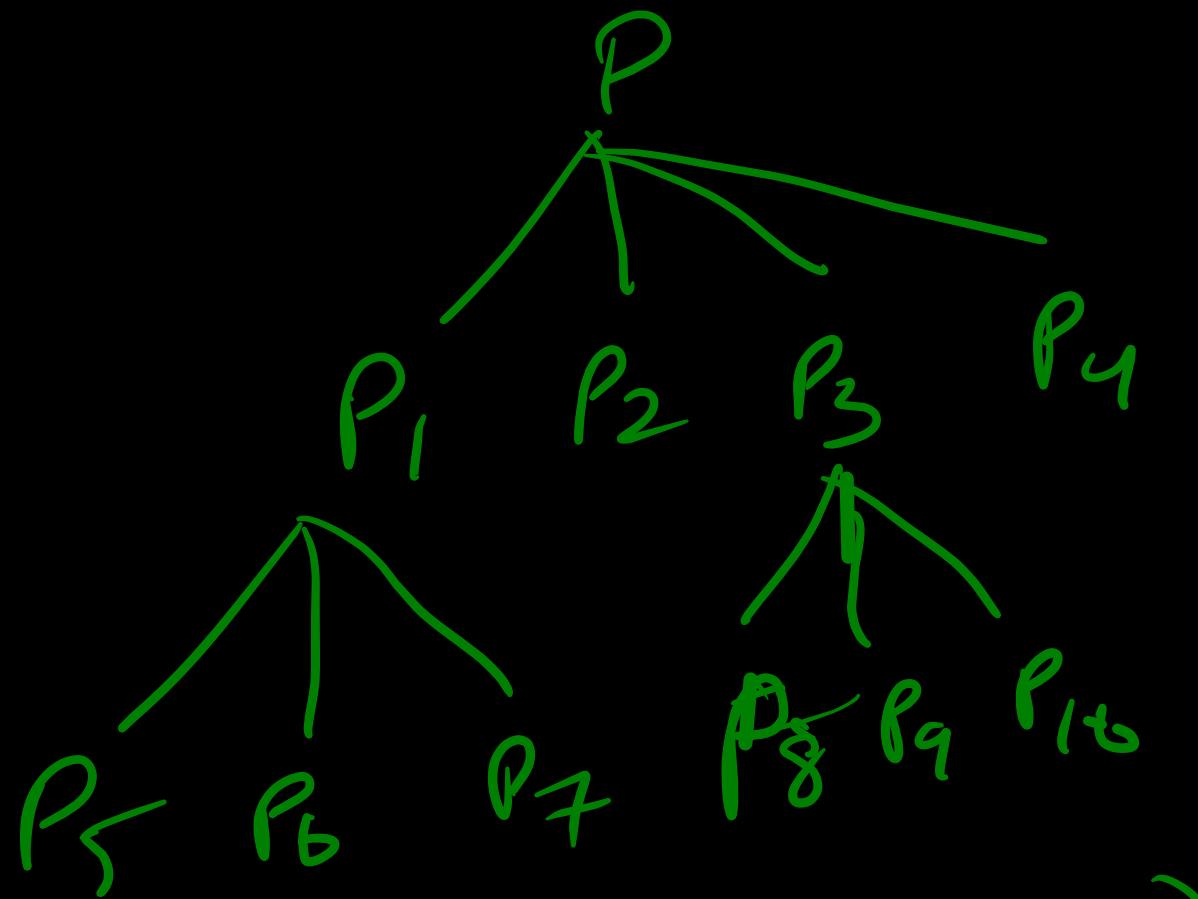
Given pre and post } \Rightarrow we cannot construct
a BT uniquely.



In: Left Root Right
Pre: Root Left Right

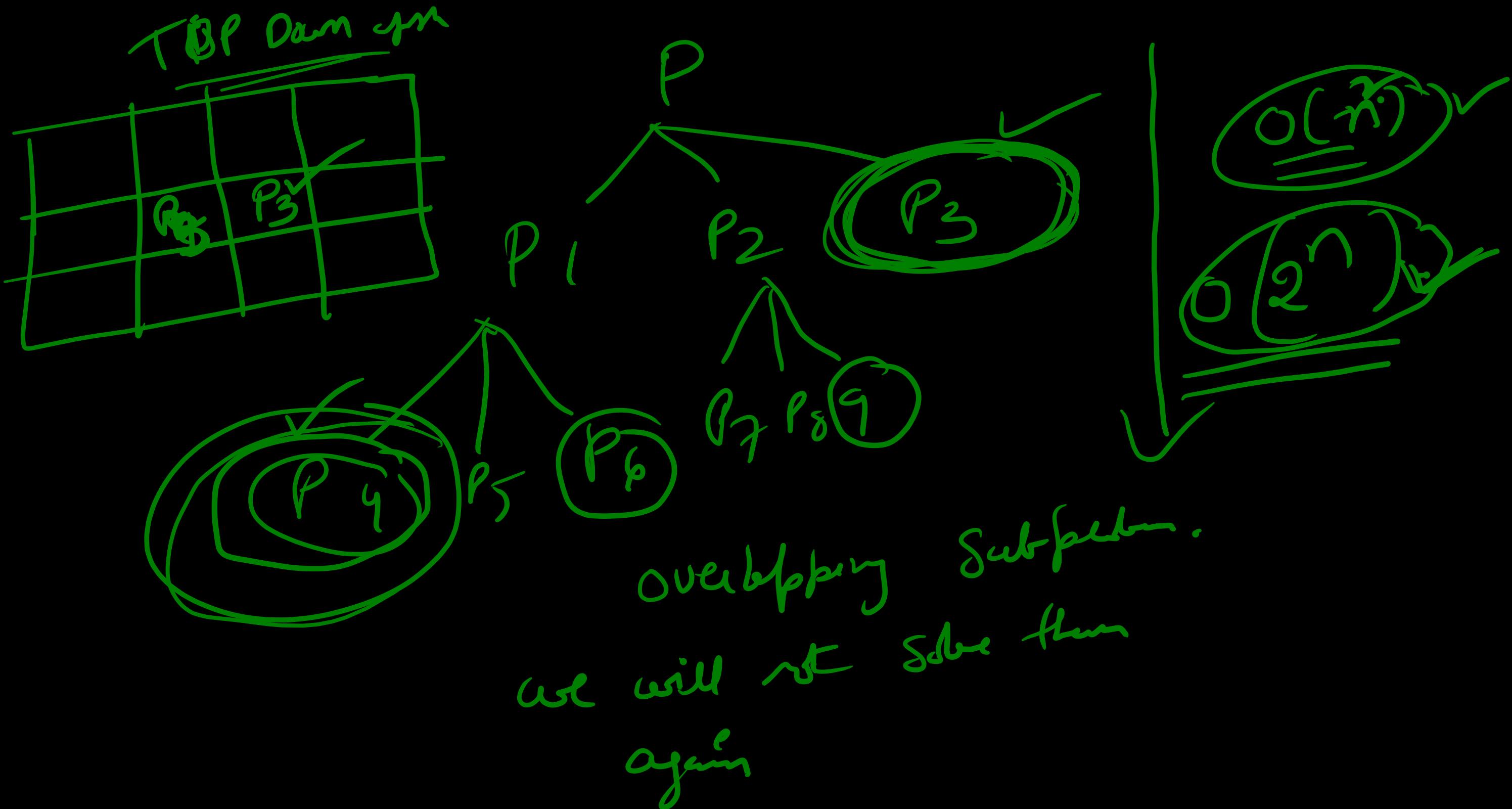


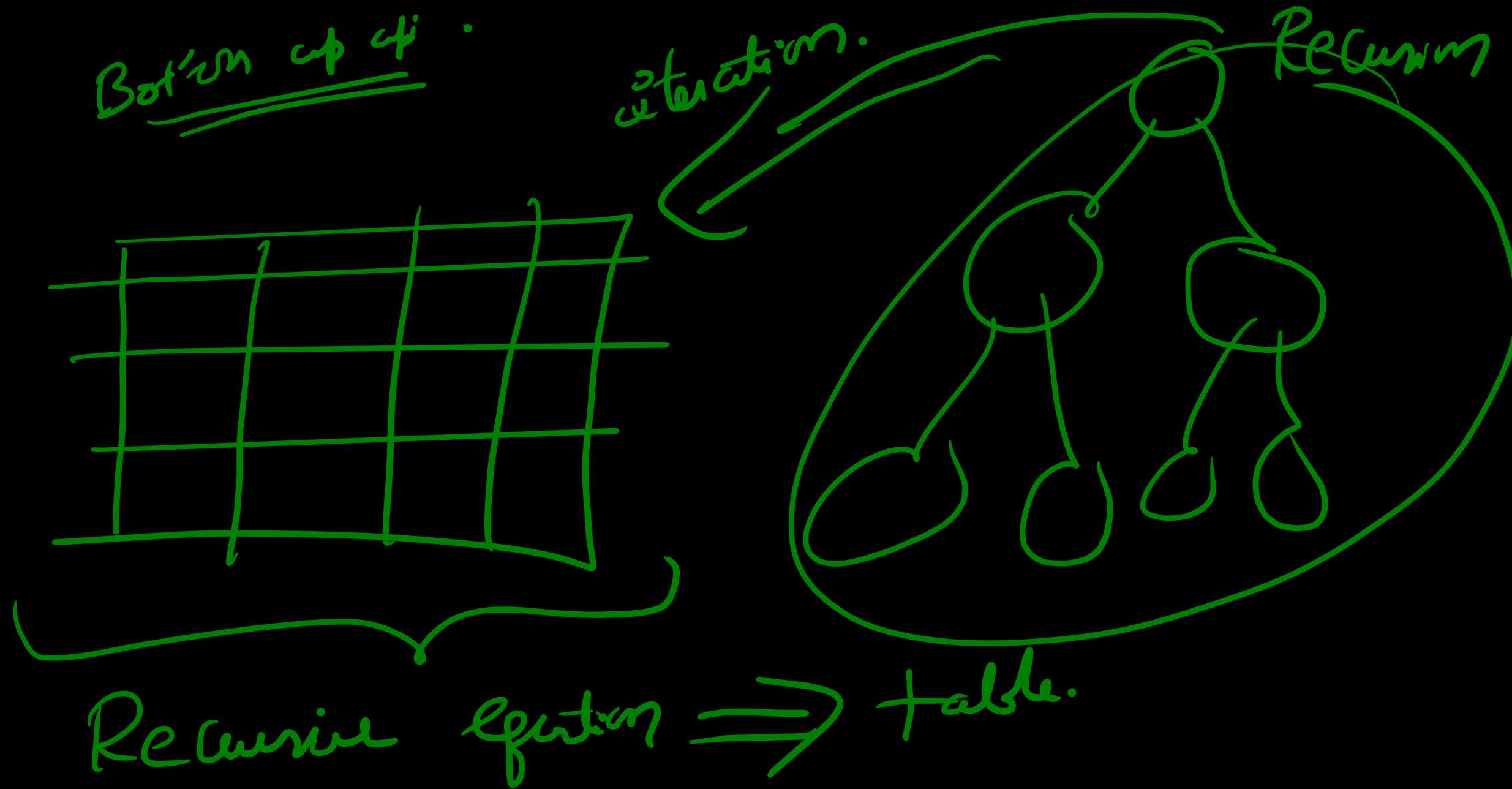


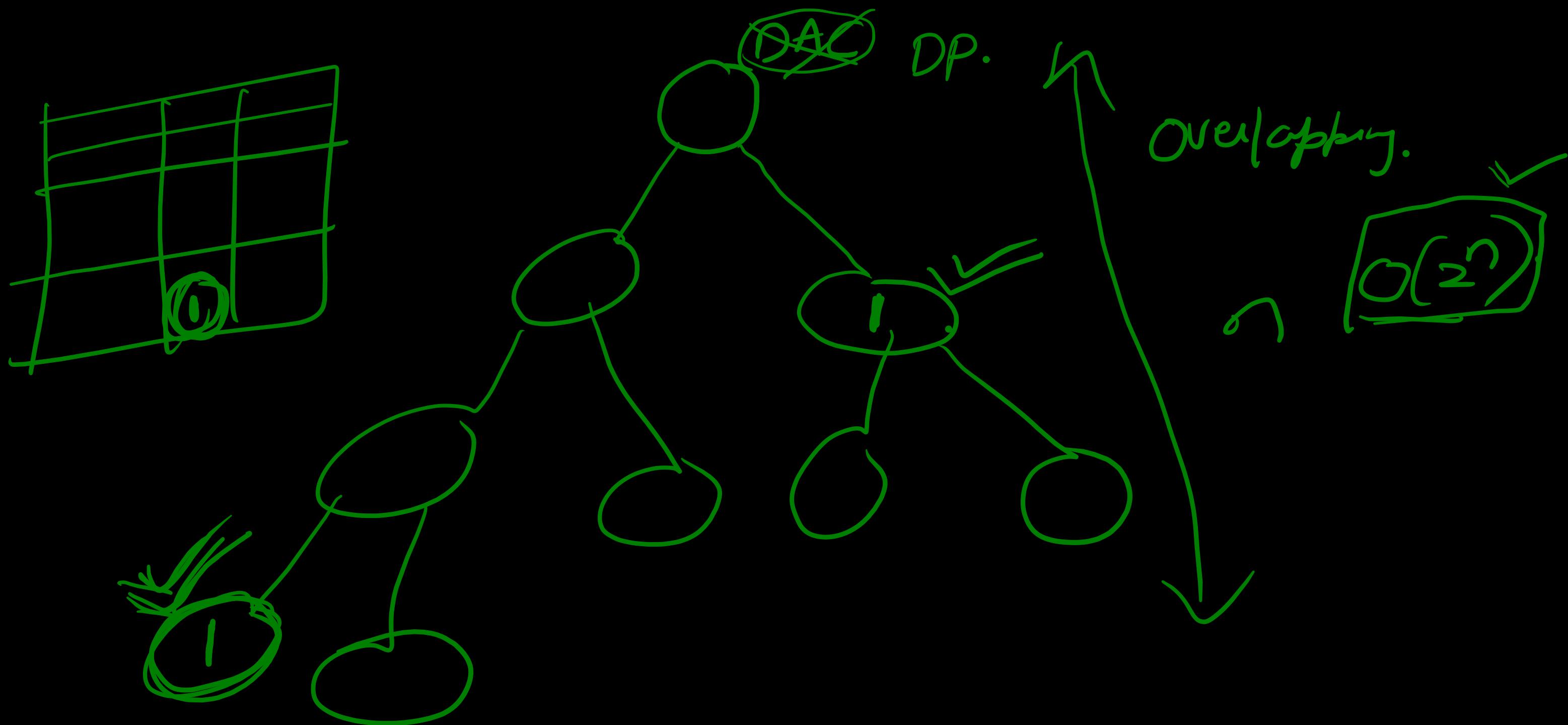


DAC

all at the bottom
are unique.







→ { ~~(Code)~~ Algo → who does this algo do .
They will say the algo → Fill in the blanks . }

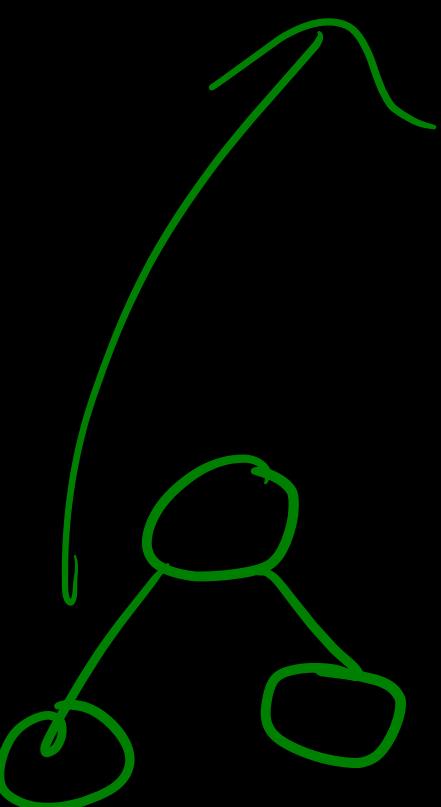
able to write algo → Fill in the blanks
trace the algo and find out what it does.

- ① write algo ✓
- ② trace them ✓

Gate :

formula

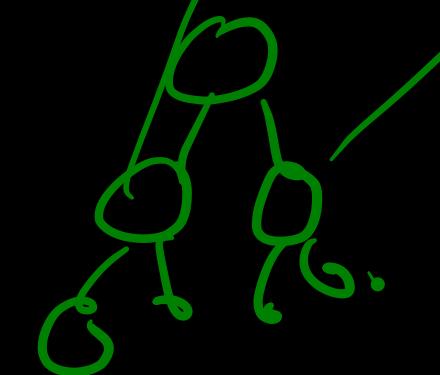
a) $n+1$



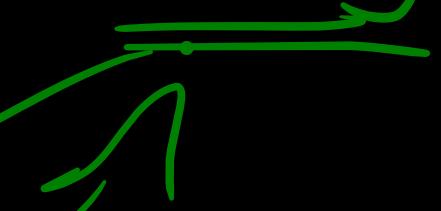
b) $n-1$



c) $\lceil \frac{n}{2} \rceil$



c) $\lfloor \frac{n}{2} \rfloor$



Don't derive formula.

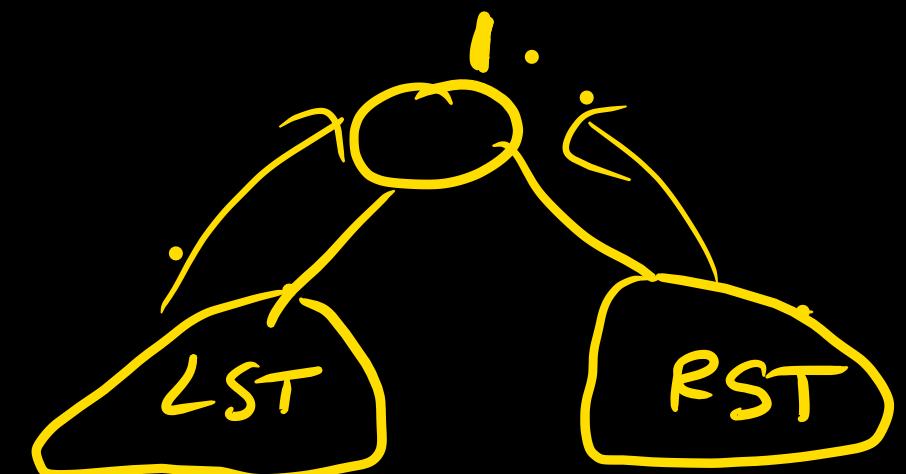
Write an algo to count no of nodes in a BT.

Recursive equations: \Rightarrow RA \Rightarrow Trace.

99% recursive

1%

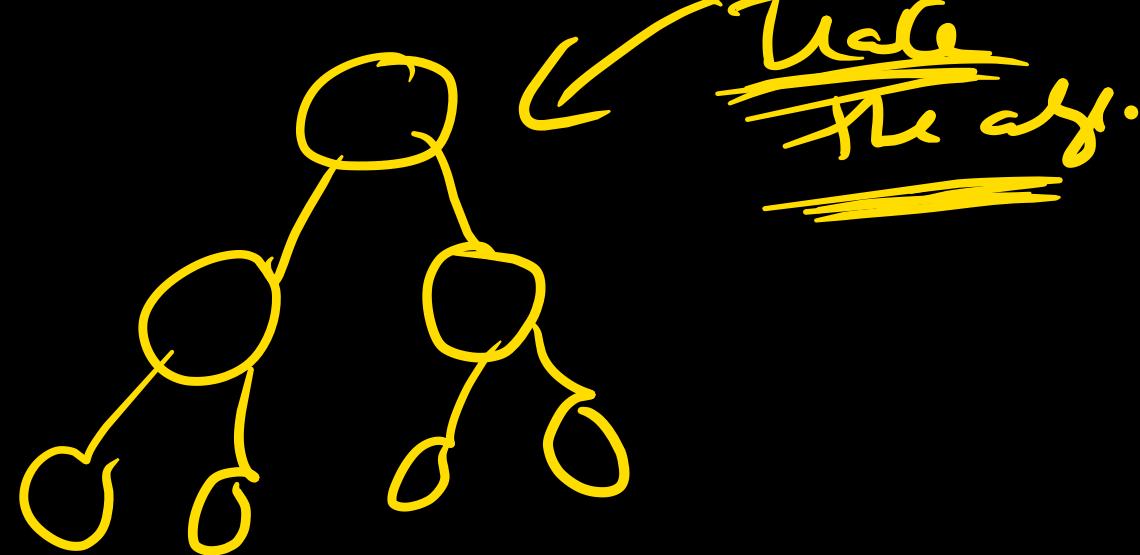
$$NN(T) = \begin{cases} 1 + NN(LST) + NN(RST); & \text{if } T \neq \text{null} \\ 0; & \text{T is null} \end{cases}$$



```

int NN( Struct Node *t) Tree
{
    if(t)
    {
        return 1 + NN(t->left) + NN(t->right); Random algo → what does it do
    }
    else
        return 0
}

```

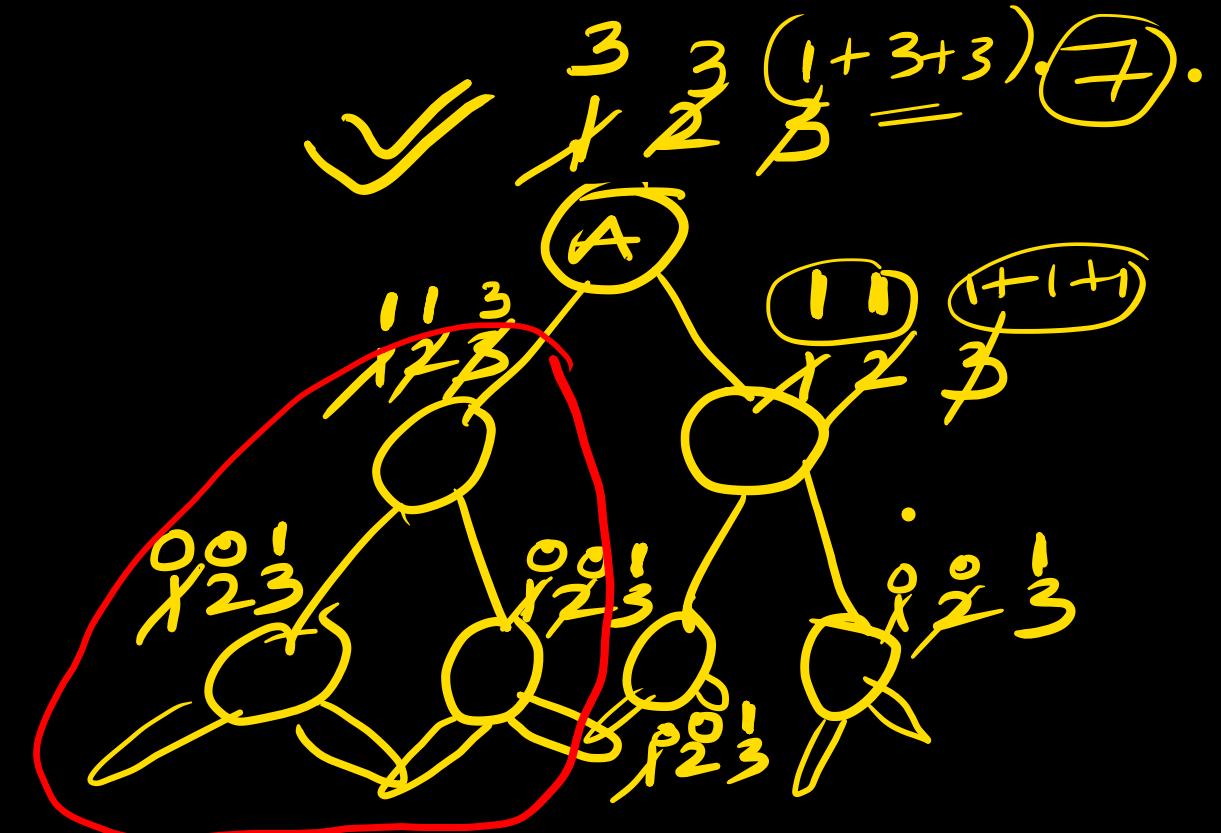


```

int nn( struct node *t)
{
    if (t)
    {
        1 l = nn(t->left)
        2 r = nn(t->right)
        3 return (1 + l + r)
    }
    else
        return 0
}

```

Count the tree non leaf



- a) —
 - b) —
 - c) —
 - d) —
- to count the full tree.

RE
↓

Recursive tree.
lous.

BT & Rec.

DP Rec.
lous.

BT
↓

meant fd recuse.

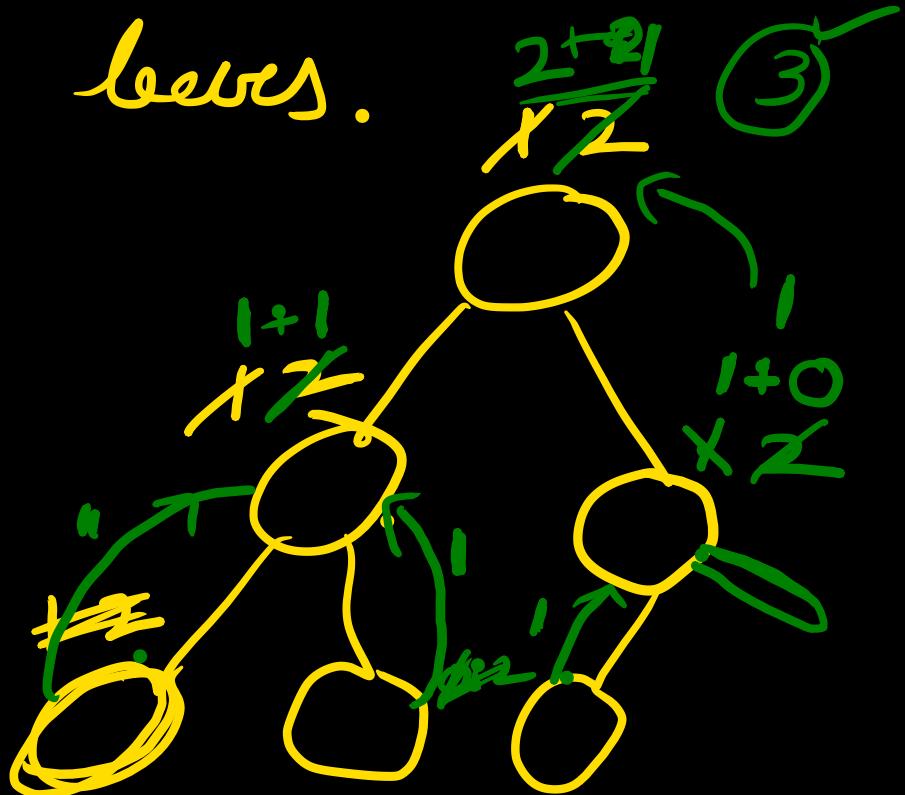
To write an algo to find the no of leaves.

NL(Start node t)

{
 if ($t == \text{null}$) return 0;

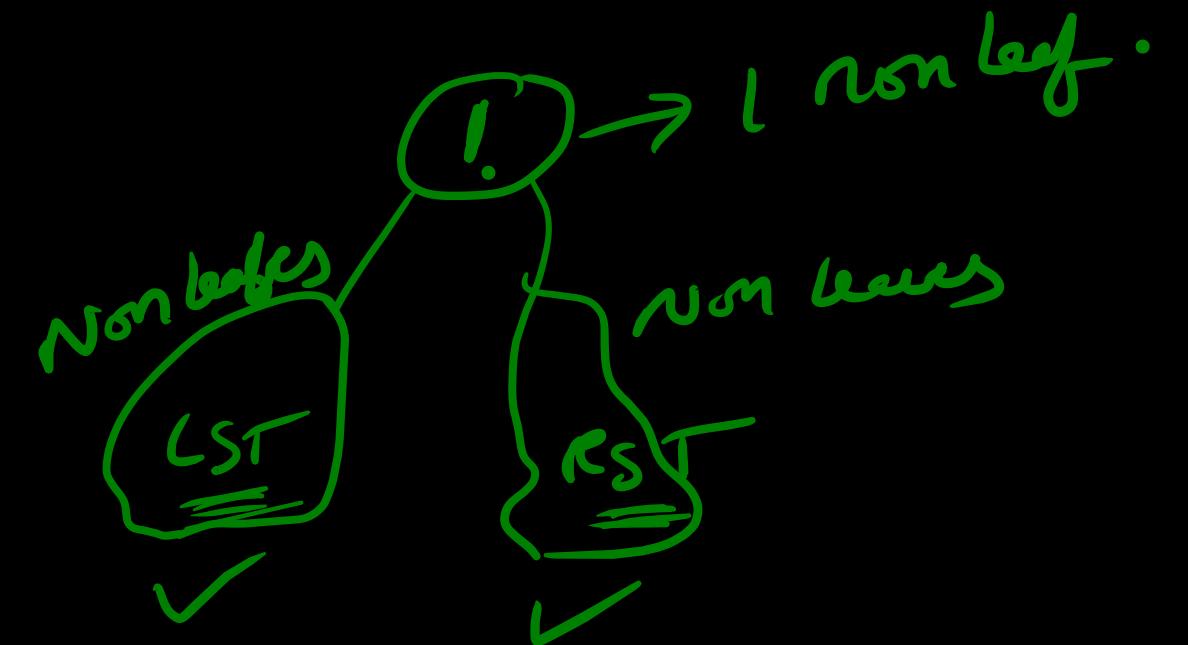
=
 if ($t \rightarrow \text{left} == \text{null}$ && $t \rightarrow \text{right} == \text{null}$)
 return 1;
 else
 return (NL($t \rightarrow \text{left}$) + NL($t \rightarrow \text{right}$));

}



Write an algo to find no of non leaves

$$NL(T) = \begin{cases} 0 & \text{if } T \text{ is a leaf.} \\ 1 + NL(\cancel{LST}) + NL(RST) & \text{otherwise.} \end{cases}$$



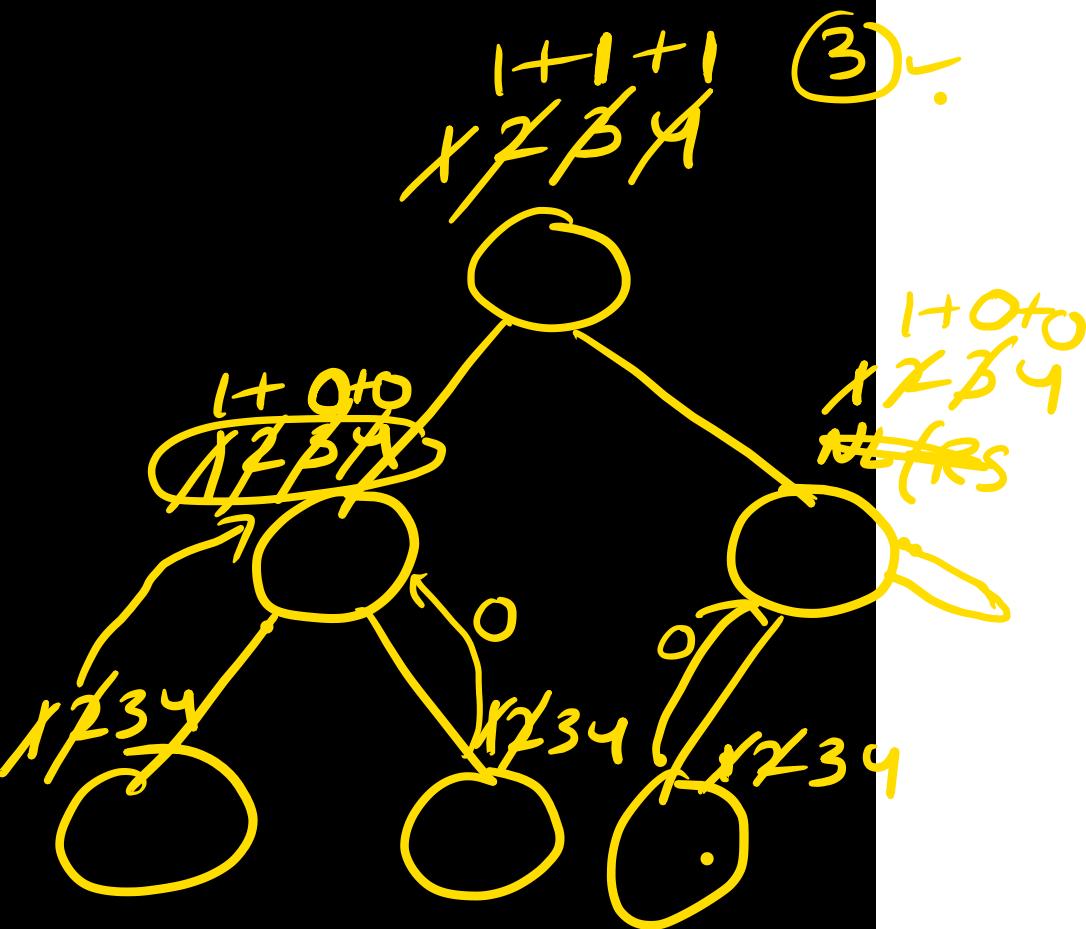
```
int NL (struct node *t)
```

```
{ ① if (t == null) return 0;
```

```
② if (t->left == null && t->right == null)
```

```
return 0;
```

```
else return (1 + NL(t->left) + NL(t->right))
```



1+0+0

x2pA

#trs

x234

x234

x234

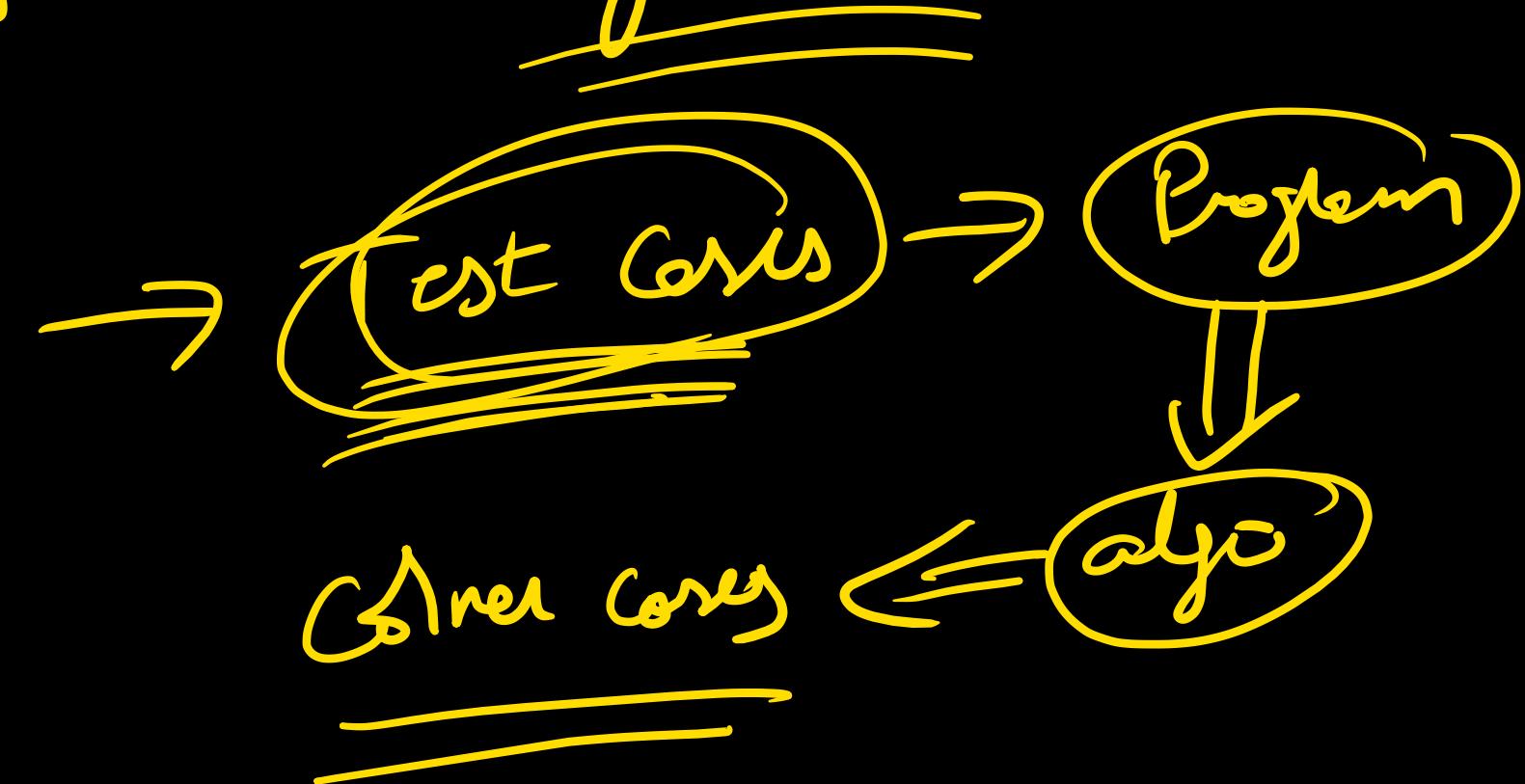
.

Show

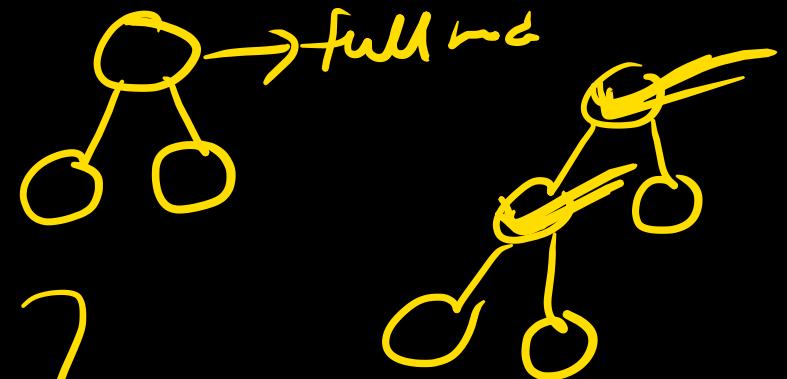
write the algo.

Answer costs and dry run.

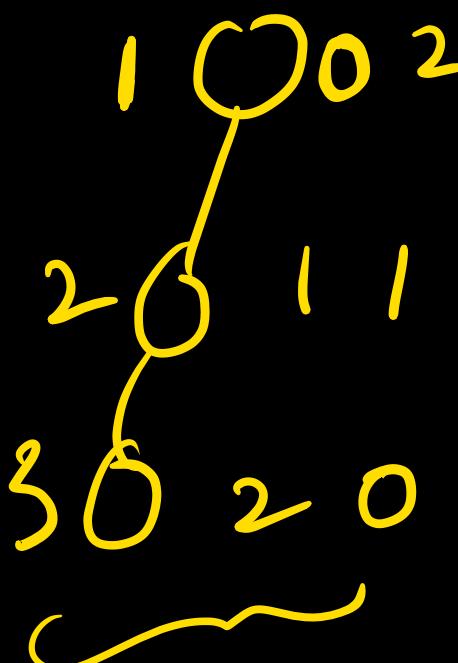
Interviews



In a binary tree if a node has two children, then it is called full node.



level:



Complete tree \rightarrow multiple definition

Full tree \leftrightarrow multiple definition

Strict tree \rightarrow multiple defn

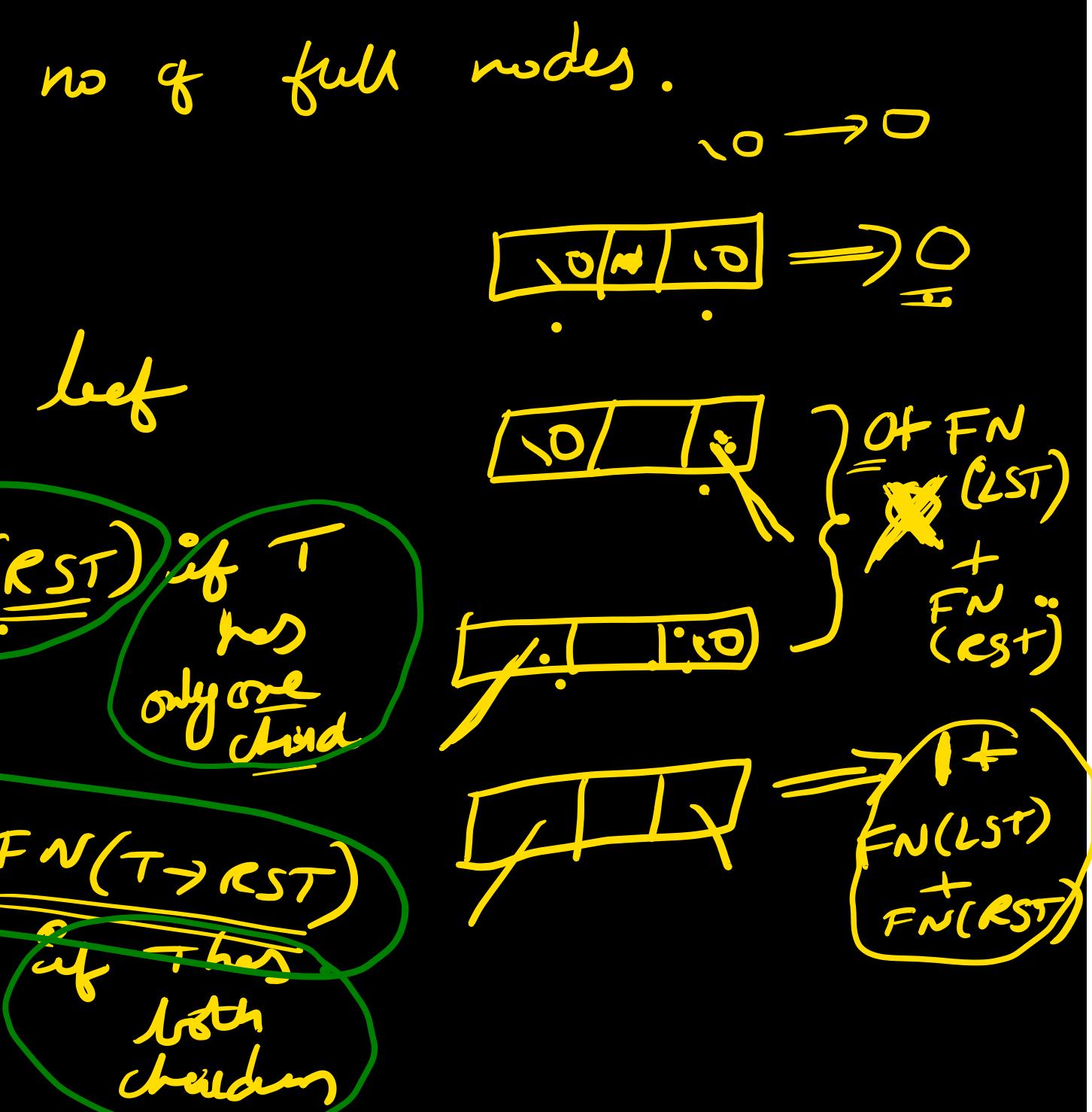
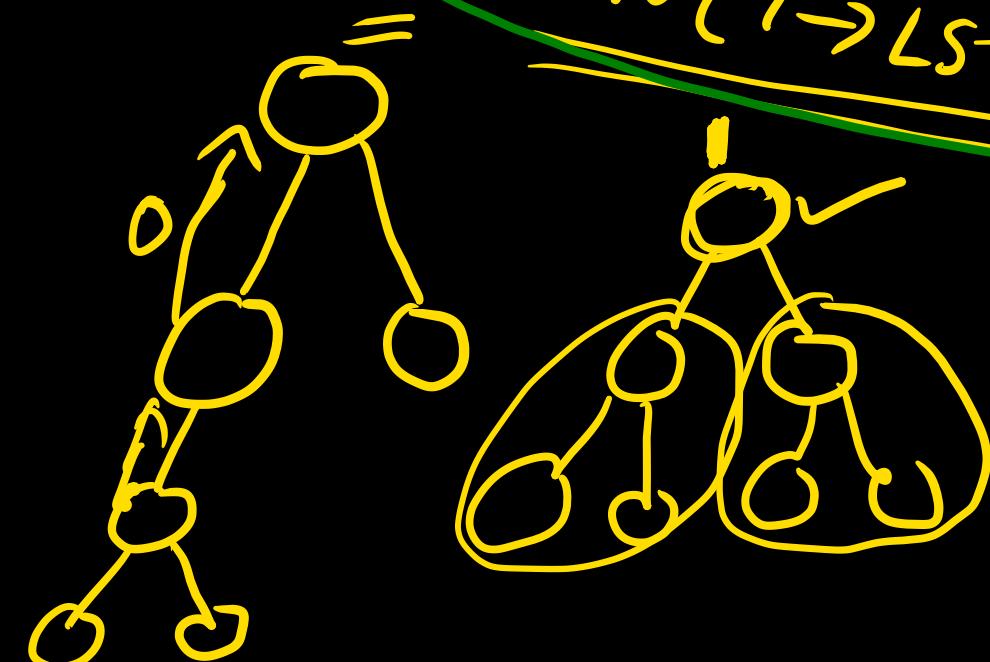
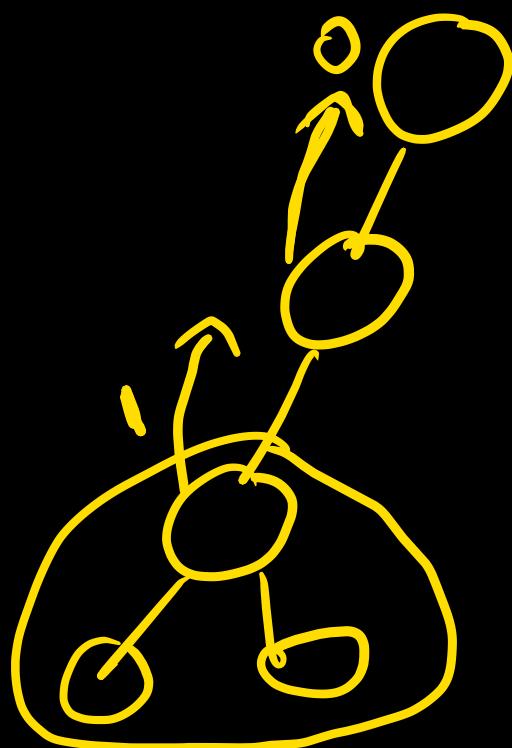
many books
no ~~no~~ many
def.

In the exam they will give you
defn.

Write an algorithm to find no of full nodes.

$$10 \rightarrow 0$$

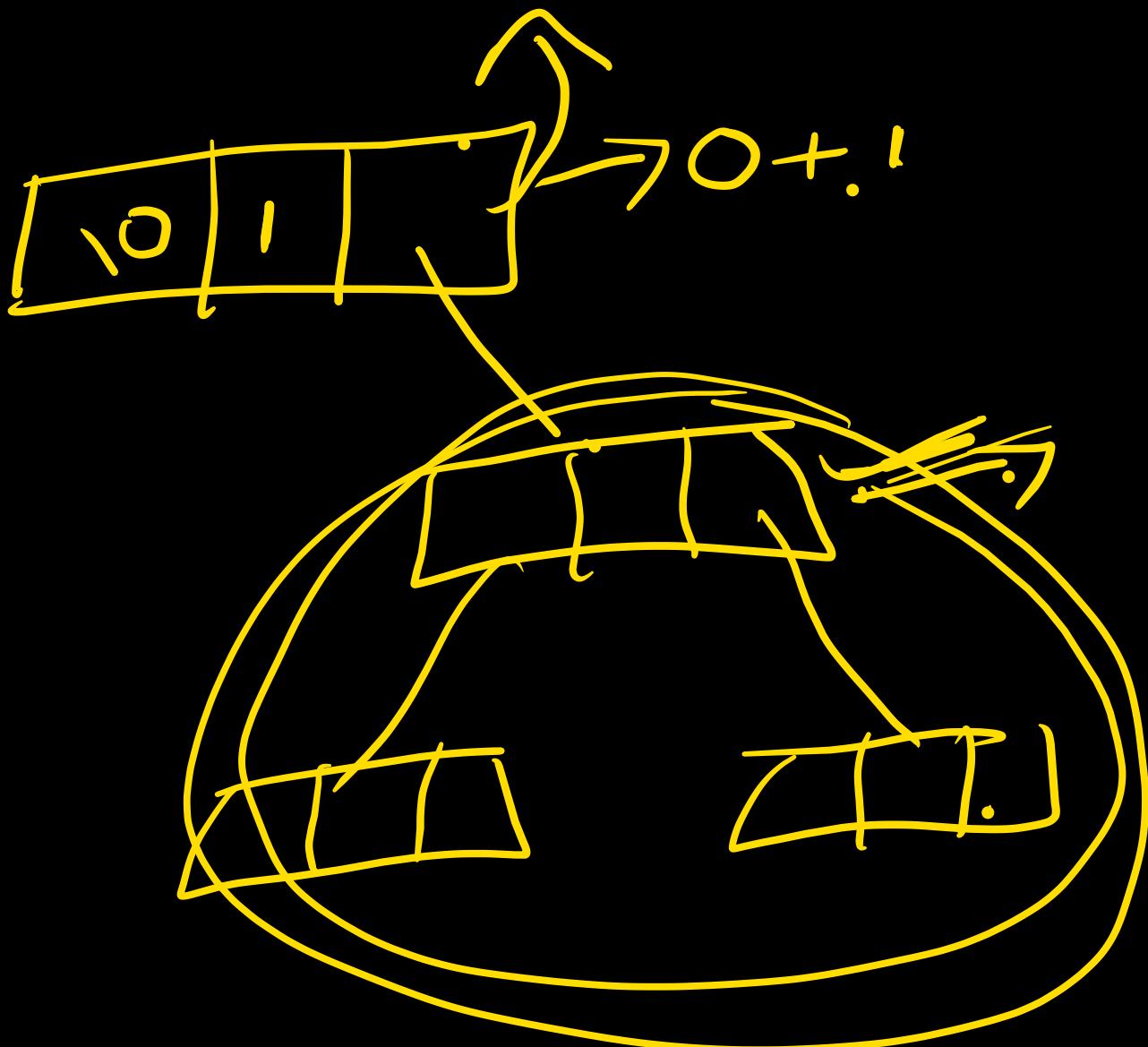
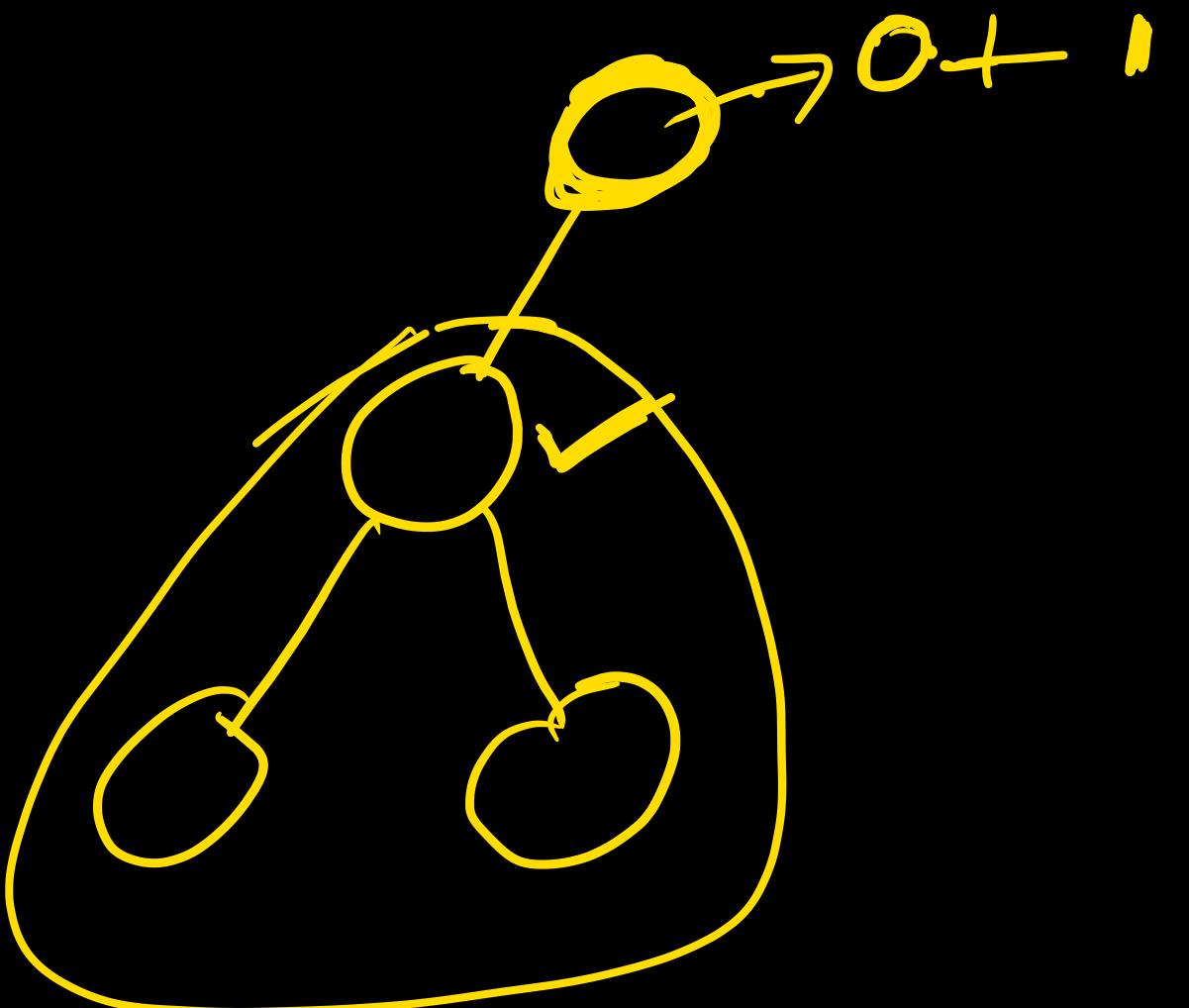
$$FN(T) = \begin{cases} \underline{0}; T = \text{null} \\ 0; T \text{ is a leaf} \\ 0 + FN(T \rightarrow LST) + FN(T \rightarrow RST) \text{ if } T \text{ has only one child} \\ 1 + FN(T \rightarrow LST) + FN(T \rightarrow RST) \text{ if } T \text{ has both children} \end{cases}$$



$$\begin{array}{|c|c|c|} \hline \cdot & 0 & \cdot \\ \hline \end{array} \Rightarrow 0$$

$$\begin{array}{|c|c|c|} \hline \cdot & 0 & \cdot \\ \hline \end{array} \quad \left. \begin{array}{l} = 0 + FN(LST) \\ + FN(RST) \end{array} \right\} \Rightarrow 0$$

$$\begin{array}{|c|c|c|} \hline \cdot & 1 & 0 \\ \hline \end{array} \Rightarrow 1 + FN(LST) + FN(RST)$$

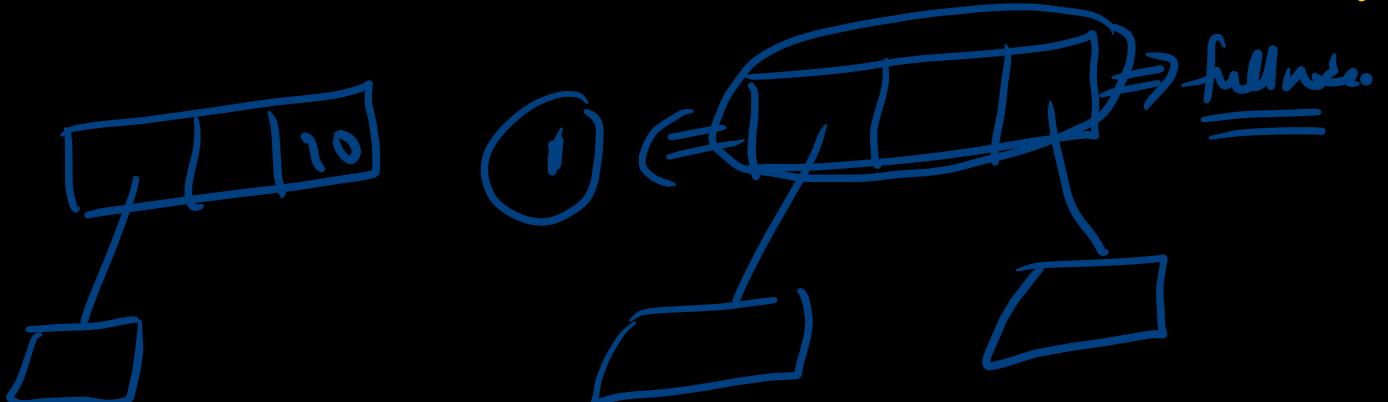


```

int FN( Struct node *t )
{
    if (!t) return 0;
    if (!t->left && !t->right)
        return 0;

```

$$\text{return } (\text{FN}(t \rightarrow \text{left}) + \text{FN}(t \rightarrow \text{right})) + (\text{t} \rightarrow \text{left} \& \& \text{t} \rightarrow \text{right})? 1 : 0;$$



\downarrow
 not null
 null be not null

