

Block size is 1024, BP is 8 bytes, RP: 9 bytes, search key 10 bytes.

Order p: max possible pointers which can be stored in B^+ tree node.

What is the best possible order of B^+ tree?

- (i) Internal node
- (ii) Leaf node

→ Block size is $\approx 512B$, $K = 5$ bytes, $BP = RP = 10B$.

Order P : max possible keys which can be stored in a B^+ tree node.

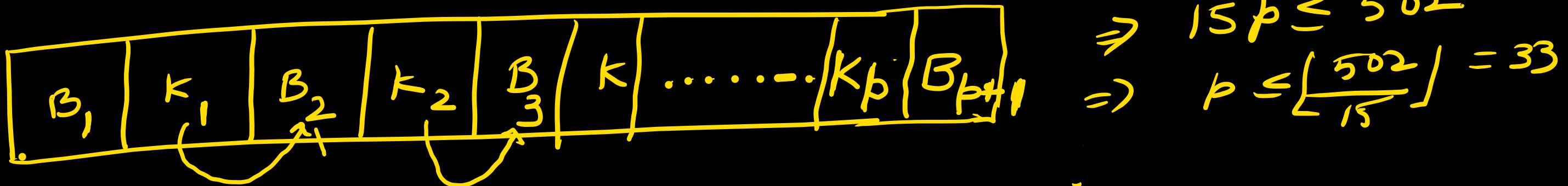
what is the best possible order of B^+ tree node.

$$(p+1)BP + p(K) \leq \underline{\text{Block}}$$

$$(p+1)10 + p(5) \leq 512$$

~~15~~

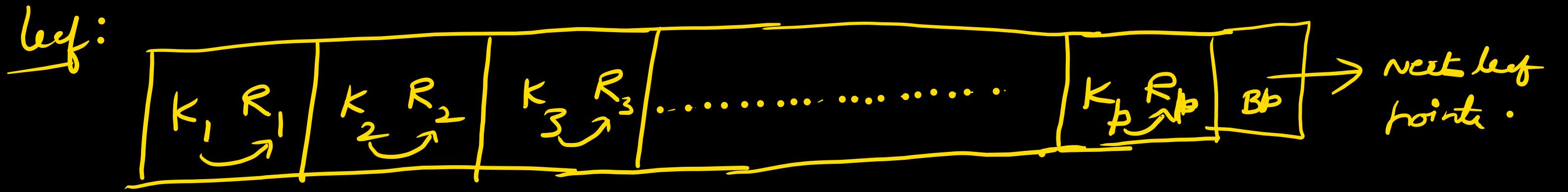
internal node structure:



$$15p \leq 502$$

$$\Rightarrow p \leq \left\lfloor \frac{502}{15} \right\rfloor = 33$$

Key $K_1, K_2, \dots, K_{\text{max}}$



(P) \rightarrow total no of ~~pointer~~ keys.

$$p(K+R) + BP \leq \text{Block size}.$$

$$p = 33 \quad \checkmark$$

In this case, Δ_{de} is some ~~for~~ block leaf and
internal node becomes $BP = RP$ size.

$B: 1024$

$K: 10B$, $R_p = 9B$, $BP = 8 \text{ bytes}$.

B tree node

order $P: 38$

max bps

B^+ tree node

Internal node order = 57

Leaf node order = 54

- B^+ tree node can accommodate more no of keys than Btree.
- If block size of B tree node is same as BS & B^+ tree node, then order $\neq P$ of Btree node $<$ order p of B^+ tree node
- The number of leaves in B^+ tree is less than that of nodes in Btree. $\therefore B^+$ tree I/O cost is less than B tree I/O cost.
- $\therefore B^+$ tree is preferred for DB indices

→ How many min/max keys and nodes in B/B^+ tree with
order $P \leq S$ & leafs $\leq ?$

order p : b/w ② to P bps for root node

$\lceil \frac{S}{2} \rceil = 3$ b/w $\lceil \frac{P}{2} \rceil$ to P bps in other nodes

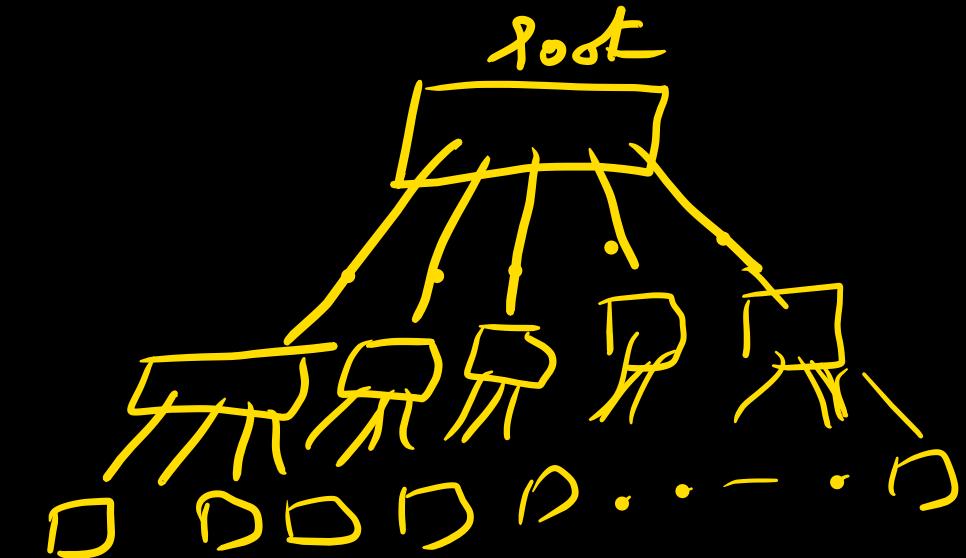
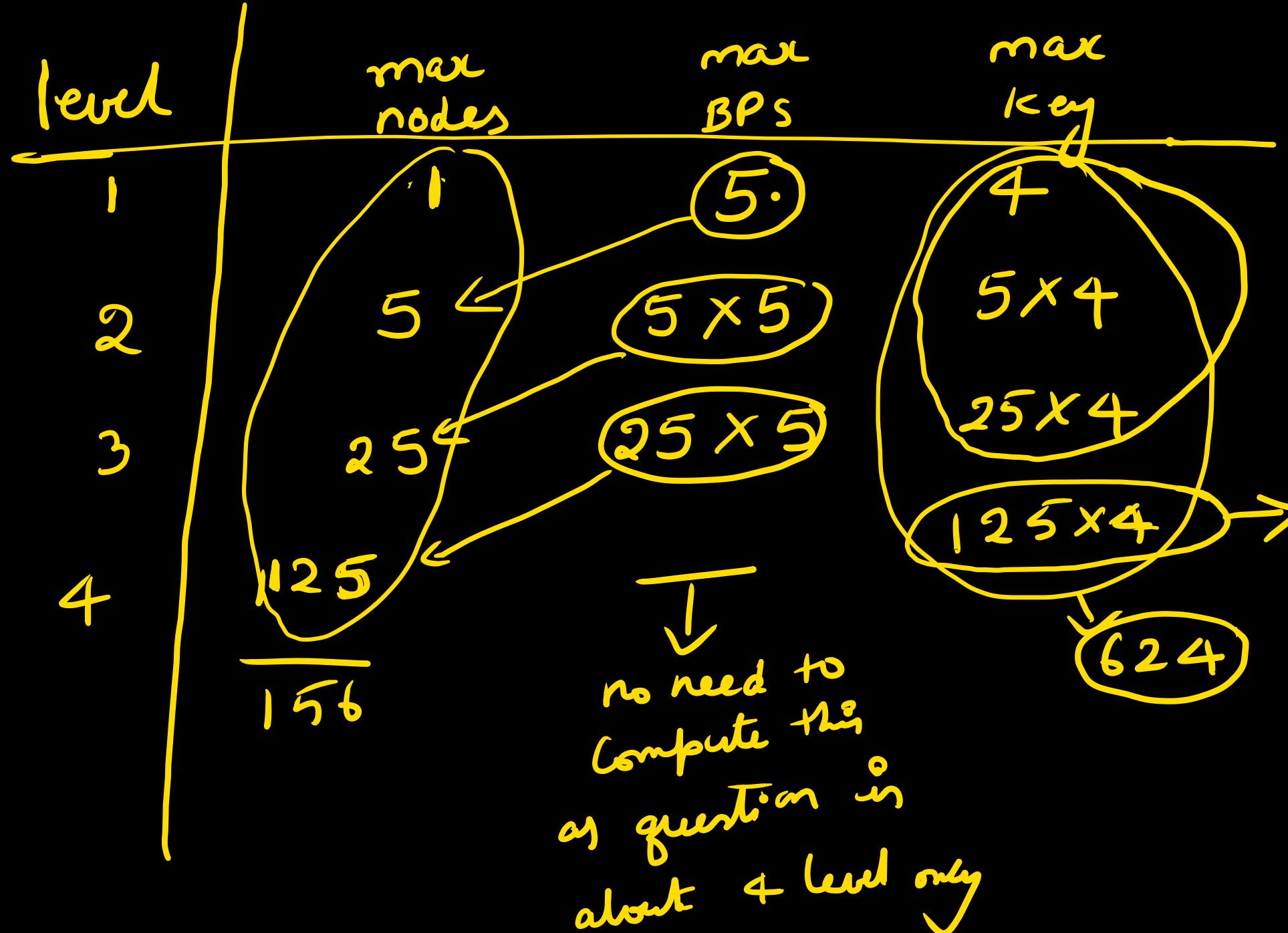
b/w $\lceil \frac{P}{2} \rceil - 1$ to $p-1$ keys in leaf node.

Root : 2 → $\textcircled{P} \textcircled{5}$
min b/p
max b/s

other : $\lceil \frac{p}{2} \rceil$
↓
min bps

$\textcircled{P} \textcircled{5}$
↓
max bps

leaf : $\lceil \frac{p}{2} \rceil - 1$ $p-1$
min max
keys keys

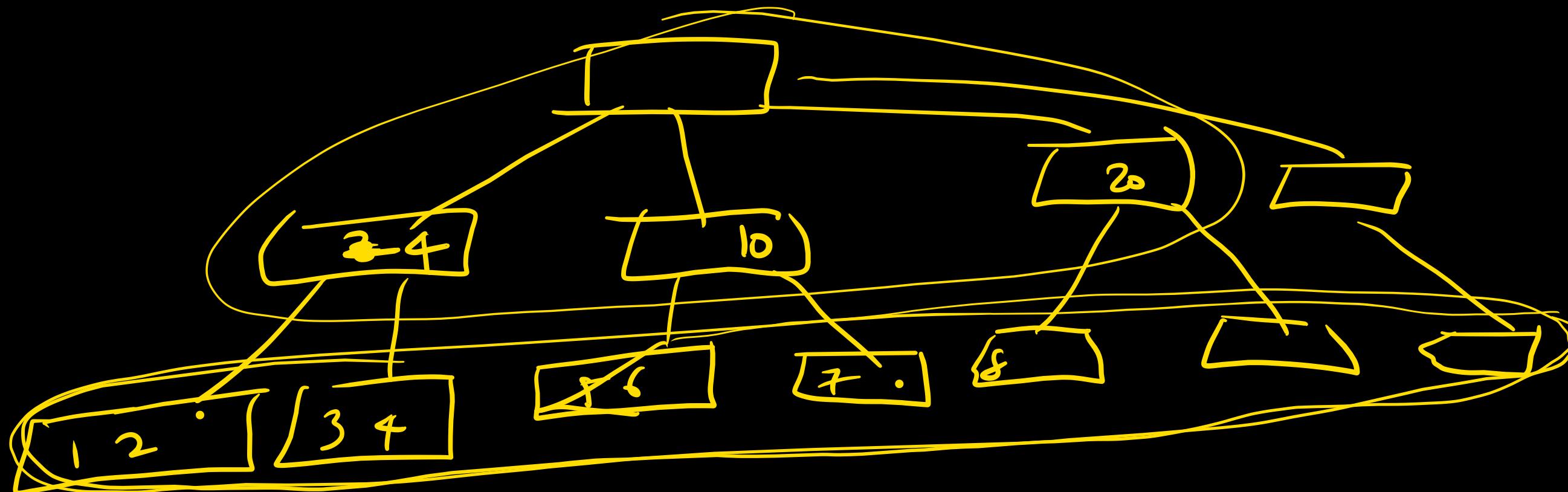


+ actual no keys
 $125 \times 4 = 500$

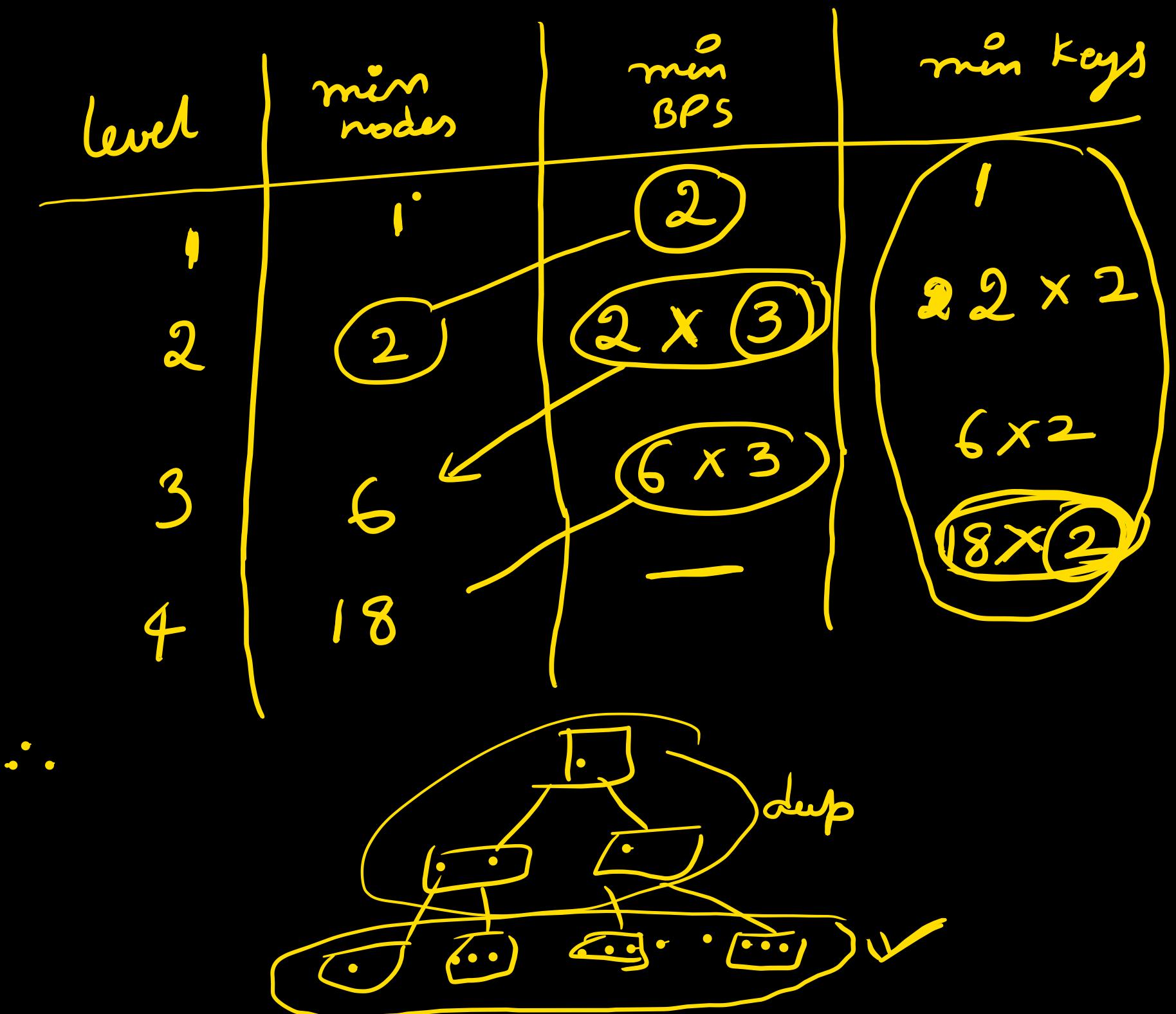
max nodes in B/B⁺ trees = 156 in this question.

max no of key in B tree = 624

In B⁺ trees. ~~no~~ keys = 500



all key are present in leaf



\therefore min nodes in B/B^+ trees
in this example $L_5 = 1+2+6+18 = 27$
no of keys in B tree = 53
no of key in B^+ tree = 36.

→ How many min/max keys & nodes in BTree/B+tree with order p :

$p: 5$ at levels 4:

Assume order P : between $\sqrt{1} \text{ to } \sqrt{2P}$ keys for root
b/w $\frac{P}{2} \text{ to } \frac{2P}{2}$ keys for no other nodes

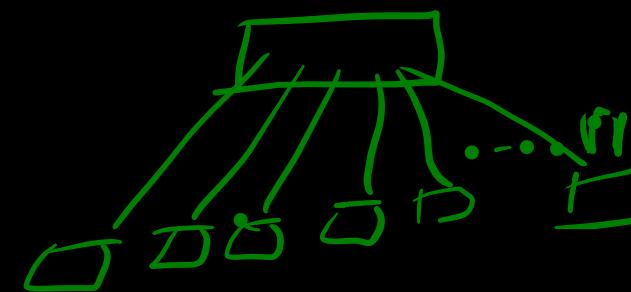
$1, 2, 3, \dots, 10$

	min	max	BP min	BP max
Root order p :	1 key	10 keys	2	11
other nodes order p :	5 key	10 keys	6	11

Order is never a fixed thing.

It changes from question to question.

level	max nodes	max BPS	max key
1	1		
2	11	11	
3	11x11	11x11	10
4	1331	11x11x11	11x10 1331x10



max no of nodes in B/B^+ tree = 1464

max no of keys in B tree = 14640

max no of keys in B^+ tree = 1331x10.

level	min nodes	min OPS	min Keys
1	1	2	1
2	2	2×6	2×5
3	12	12×6	12×5
4	72	—	72×5

$\therefore \text{min no of } \beta/\beta^+ \text{ tree nodes} = 87 \quad (1+2+12+72)$

min key of β tree with $= 4^{31}$

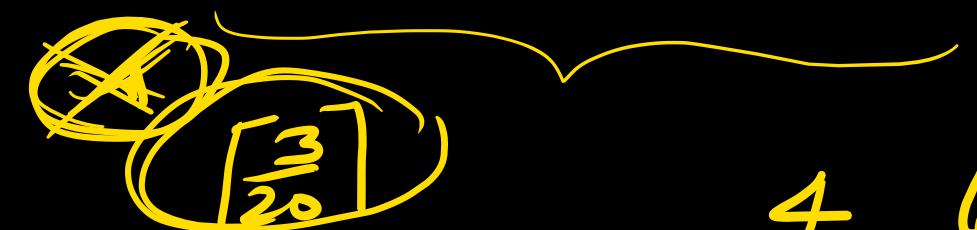
min keys in β^+ tree $= 72 \times 5 = 360.$

→ No of keys used for B^+ index : 20000. Order of p: 20 (max pointers per node)

How many min levels / min nodes of B^+ tree are required?

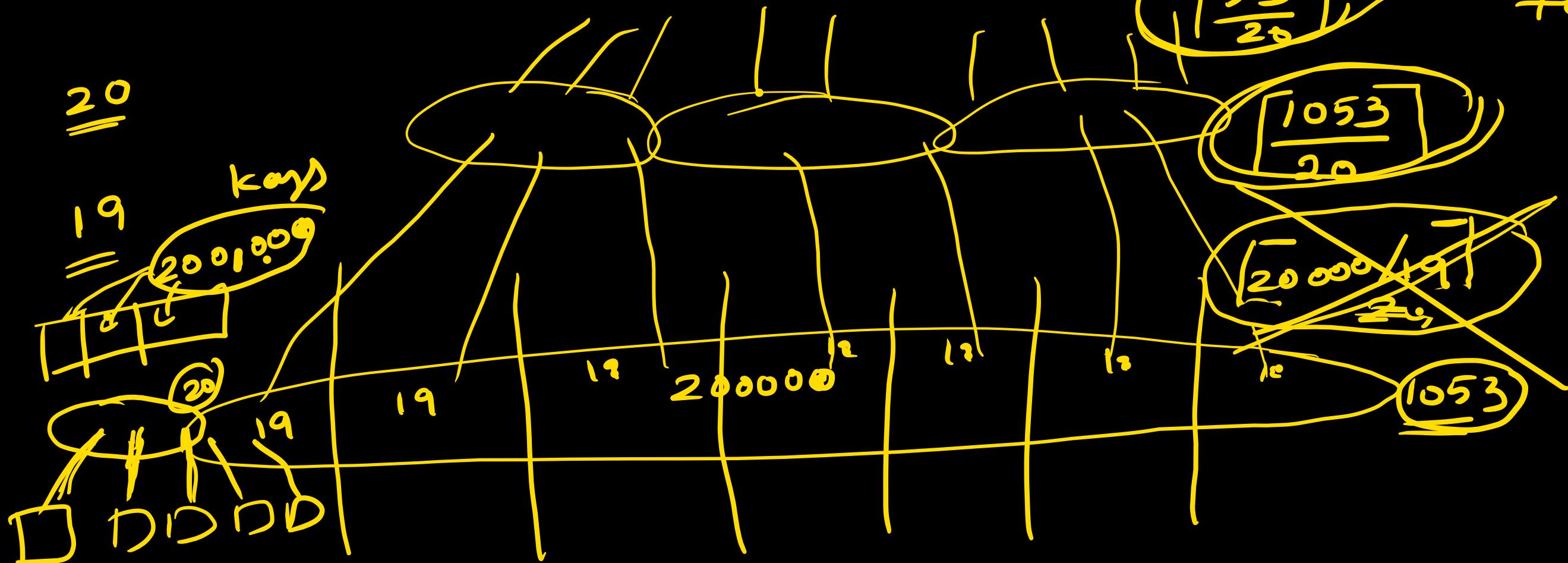
max pointers are 20

max keys are 19.



4 levels

$$\begin{aligned} \text{total} &= 1053 + \\ &53 + 3 + 1. \\ &= \underline{\underline{1110}} \end{aligned}$$



Gate DA is over:

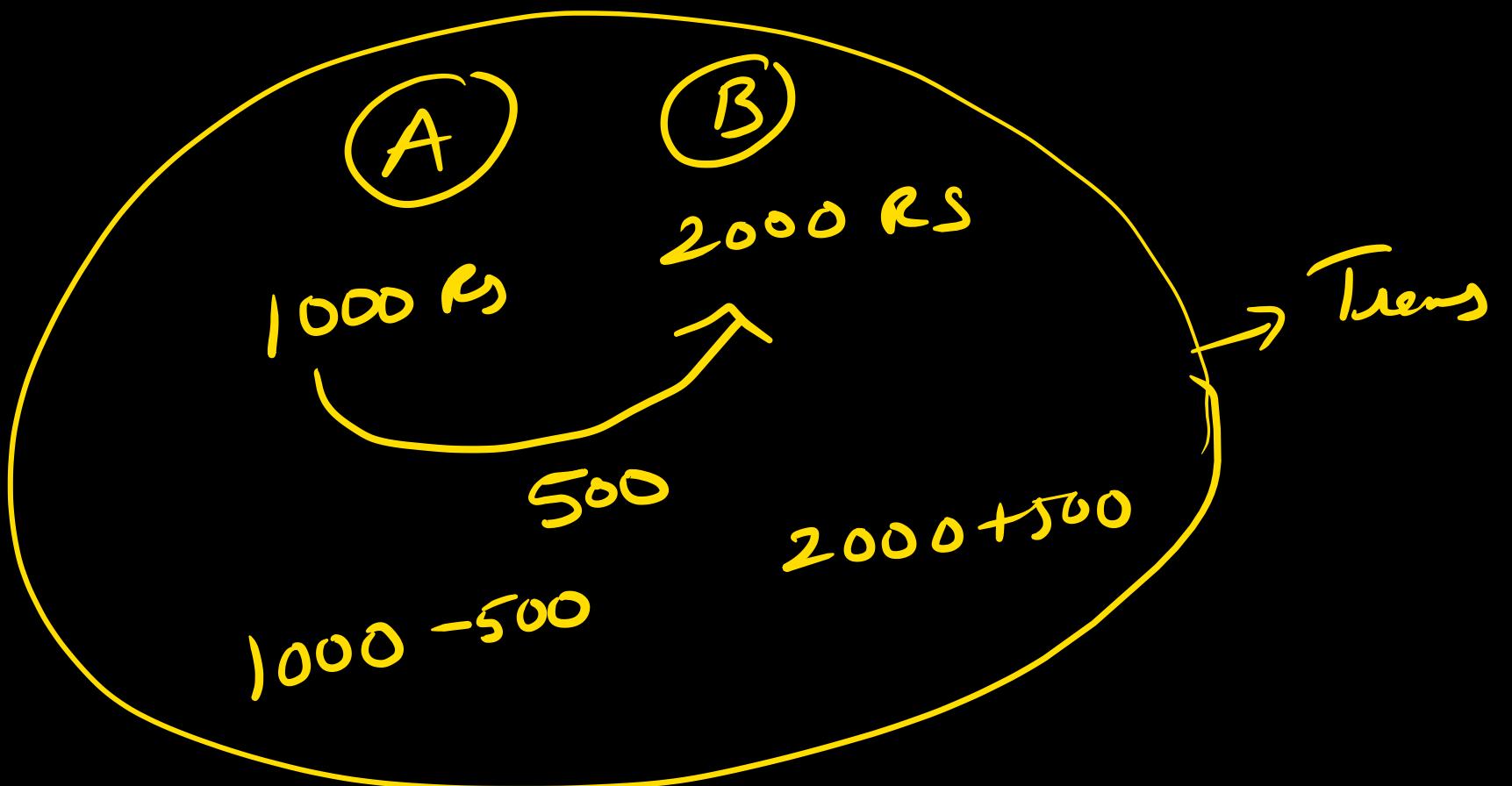
DW → Starts soon:

Transaction and Concurrency Control:

5 min break

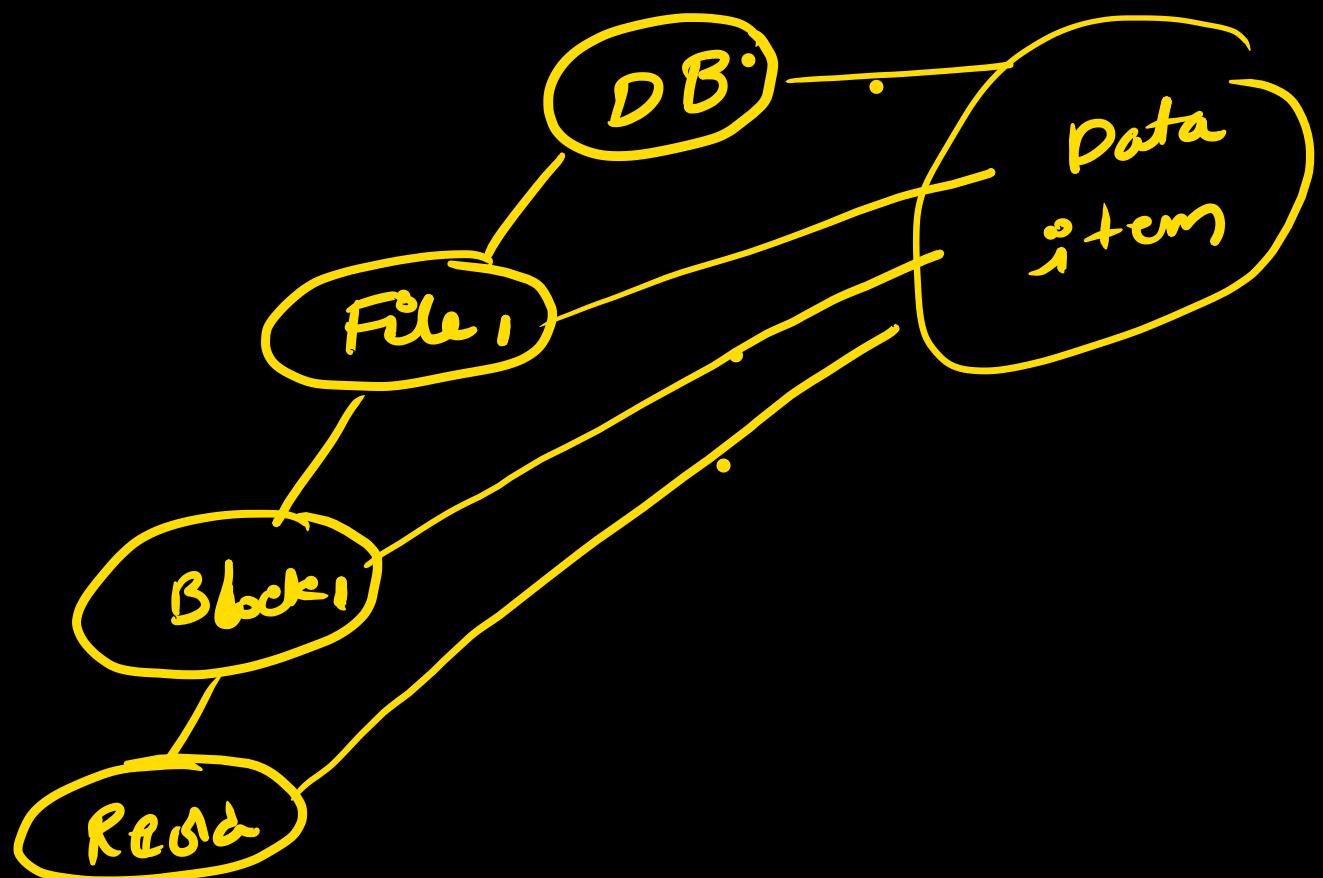
Transaction and Concurrency Control:

Transaction: Set of logically related operations to perform a unit of work.



Data item:-

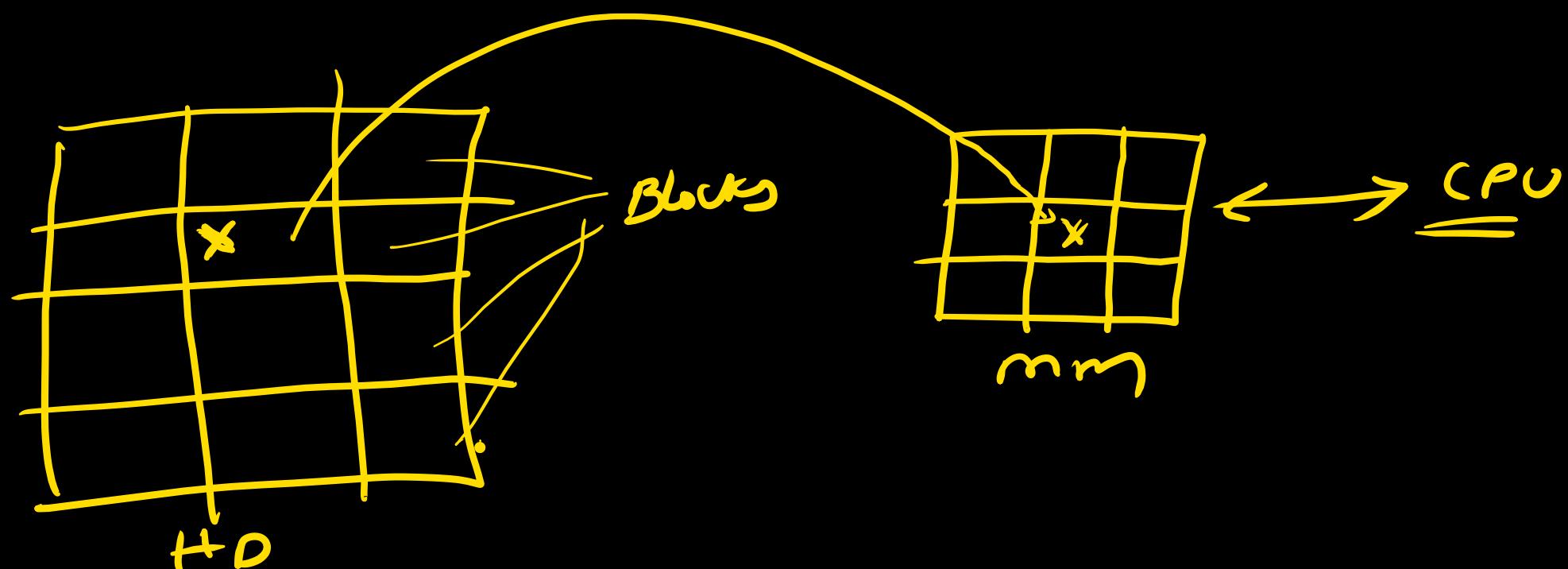
DB element which is needed to be often accessed by many
done in many transactions.



Main operations in transaction :-

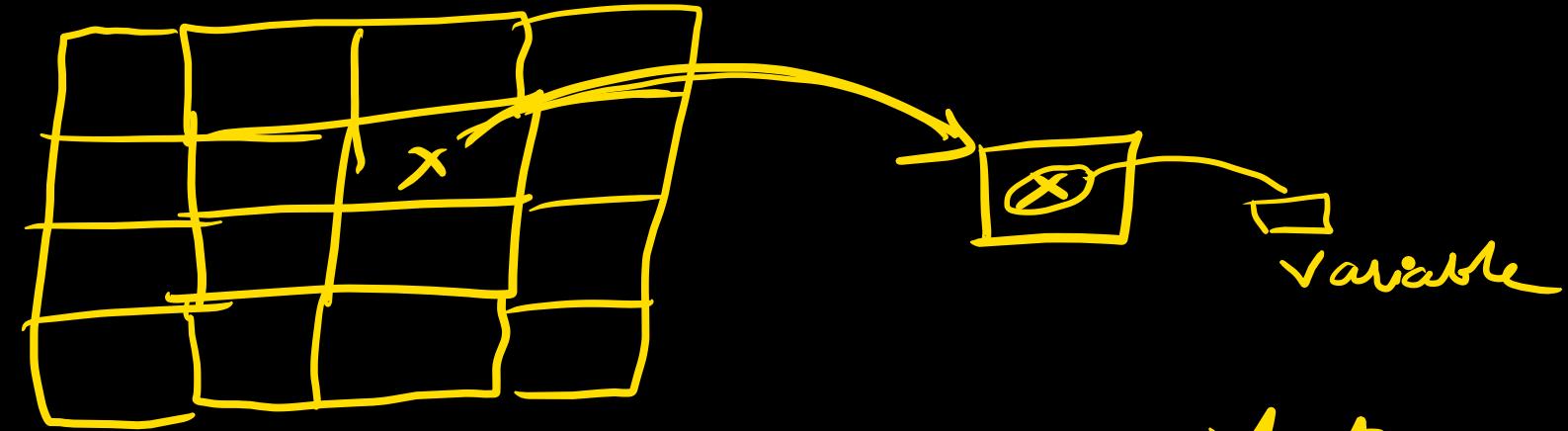
1) Read (x) x: data item

Access data item x from DB file (Disk) to main memory
to use value of x in transaction logic.



Read x :

- 1) Find block from DB file which consist of data item x.
- 2) Transfer entire block from HO to MM



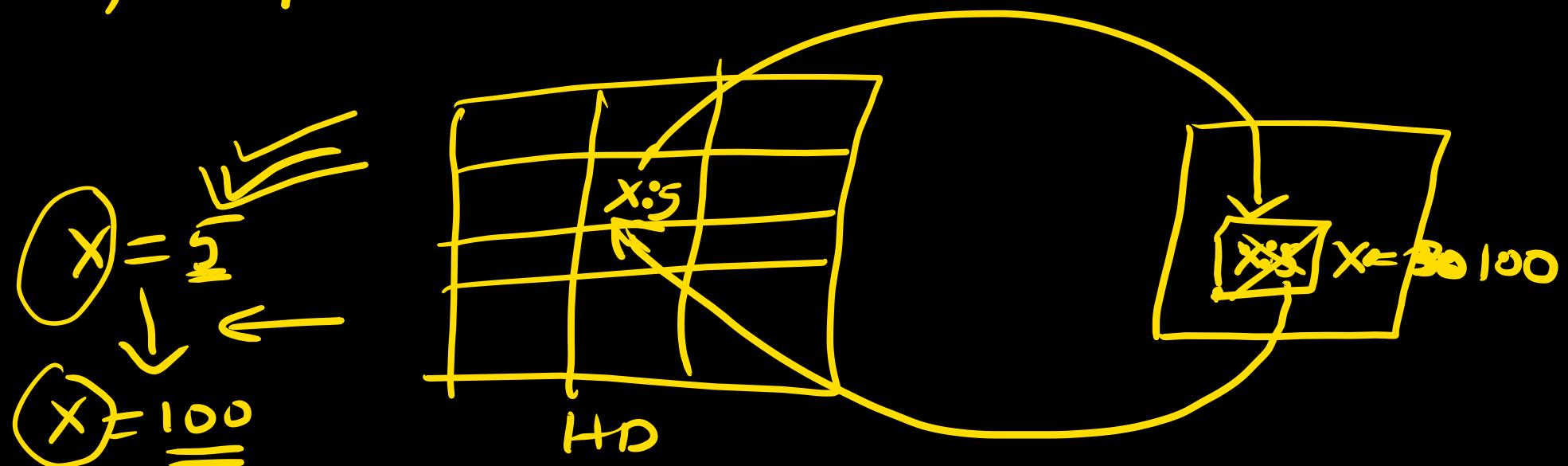
- 3) Find the add of x in mm block
and copy value of 'x' in programmed value variable.

(1, 2, 3) \rightarrow atomic. ~~all of node~~
123, ~~-1~~ ~~x~~

Write(x) :

update of data item in DB file (disk)

- 1) Find block from DB file which consists of data item 'x'.
- 2) Transfer block to mm
- 3) Find add of ' x ' in mm and update x in mm.
- 4) Replace updated block ~~rest~~ in the disk.



Account (cid, bal)

transaction:

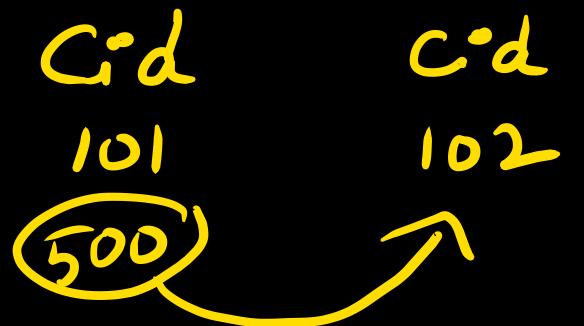
{ begin transaction

update Account

update Account

end transaction

high level



Set $\underline{bal} = \underline{bal} - 500$ where $\underline{cid} = 101$;

Set $bal = bal + 500$ where $cid = 102$;

low level of transaction

Begin transaction T_1

✓ Read (bal of Cid: 101)

$$\text{bal} = \text{bal} - 500;$$

✓ write (bal);

✓ Read (bal of Cid: 102)

$$\text{bal} = \text{bal} + 500;$$

✓ write bal

✓ Commit

end transaction

R, W, Commit