

$\text{Emp}(\text{cid}, \text{sal})$

Q) Retrieve cids who gets minimum salary.

$\pi_{\text{cid}}(\text{emp}) - \pi_{\text{cid}}(\text{Emp} \bowtie_{\substack{\text{Sal} > S \\ I, S}} \text{S}_{\text{Emp}})$

universal set

All employees

not ~~minimum~~ minimum

(\leq -ary)

$\cup - (> \text{some})$

$A = \underline{U} = \overline{A}$

= minimum employee.

Select Eid

From Emp \bar{T}_1

where not exists

False

(Select *
from Emp \bar{T}_2
where $\bar{T}_1.\text{Sal} > \bar{T}_2.\text{Sal}$)

$\bar{T}_1.\text{Sal} > \bar{T}_2.\text{Sal}$
not minian. ✓

$\text{Emp}(\text{cid}, \text{sal}, \text{dno})$

Retrieve eids of employees who gets min salary for each dept

\leq every $\cup - (>)$

$\pi_{\text{cid}} \text{Emp} - \pi_{\text{cid}} \left(\text{Emp} \bowtie \begin{array}{c} S(\text{emp}) \\ \text{sal} > s \\ \wedge \text{dno} = D \end{array} \right)$

for the previous SQL queries just add this condition.

we can use grouping and aggregation function.

Select eid
:
X eid is not present in
group by clause.

Group by dno
Select dno, min(sal)
:
X we want eid
not dno
Group by dno;

we have to use nested queries.

Select \times eid

From

Emp

(Select $\underline{\underline{dno}}$, $\underline{\underline{\min(Sal)}}$ msal

table.

From Emp

Group by $\underline{\underline{dno}}$) temp:

where $\underline{\underline{\text{Emp.dno} = temp.dno}}$

and $\underline{\underline{\text{Sal} = msal}}$

eid	sal	dno
e ₁	40	3
e ₂	70	3
e ₃	50	3
e ₄	30	4
e ₅	60	4

Temp

dno	msal
3	40
4	30

eid	sal	dno	dno	msal
e ₁	40	3	3	40
e ₄	30	4	4	30

SQL query which is equal to division of RA:

Emoll (sid, cid) course (cid, Instructor)
Retrieve Sids who enrolled in every course taught by koth.

RA: $(\pi_{\substack{\text{Sid} \\ \text{=}}} \text{Emoll} \setminus \pi_{\substack{\text{cid} \\ \text{Inst=koth}}} \sigma_{\text{course}})$ \rightarrow we saw this.
we have seen.

How to do division in SQL

enroll(T_1)		
	Sid	Cid
Outer	S_1	$C_1 \checkmark$
	S_1	$C_2 \checkmark$
	S_1	$C_3 \checkmark$
	S_2	C_1
	S_2	C_4
	S_3	C_4

Course

Cid	IM
C_1	K
C_2	K
C_3	K
C_4	N

Sid	Cid
S_1	C_1
S_1	C_2
S_1	C_3
S_2	C_1
S_2	C_4
S_3	C_4

I have taken two instances of enroll.
For nested query.

$S_1 \checkmark$

Retrieve $\underline{T_1 \cdot Sid}$ from $\text{enroll}(T_1)$
if $\{ \text{all cids of } \}$ - $\{ \text{cids of courses} \}$
both $\underline{\text{enrolled by } T_1 \cdot Sid}$ $\underline{\text{from enroll}(T_2)}$

some $\text{enroll}(T_1)$

$= \emptyset \cdot$ $\rightarrow \underline{\text{not exist}} \cdot$
 $(C_1, C_2, C_3) - (C_1, C_2, C_3, C_4) = \emptyset$.

$\underline{S T_1 \cdot Sid} \rightarrow S_1 \Rightarrow (C_1, C_2, C_3) - (C_1, C_2, C_3) = \emptyset \cdot$

$T_1 \cdot Sid \rightarrow S_2 \Rightarrow (C_1, C_2, C_3) - (C_1, C_4) = (C_2, C_3) \checkmark$

$T_1 \cdot Sid \rightarrow S_3 \Rightarrow (C_1, C_2, C_3) - (C_4) = (C_1, C_2, C_3)$

Select distinct sid

From Enroll T₁

where

not exists

= \emptyset

Select eid

From course

where Ins = Kolth

Except

Select cid From

Enroll T₂ where

T₂.sid = T₁.sid

all Kolth Courses.

Courses taken by one student
T₁.sid

y

works for (eid, bid) Project (Pid, name)

Retrieve all eids who works for every project of Pname DB

works for (T_1)

eid	bid
1	1
1	2
1	3
2	1
3	4

Project

Pid	name
1	DB
2	DB
3	DB
4	OS

eid	bid
1	1
1	2
1	3
2	1
3	4

works for (T_2)

$$eid = 1 \quad \{1, 2, 3\} - \{1^2, 3^4\}$$

$$eid = 2 \quad \{1, 2, 3\} - \{1^2\} \neq \emptyset$$

$$2, 3 \neq \emptyset$$

$$eid = 3 \quad \{1, 2, 3\} - \{4\}$$

$$1, 2, 3 \neq \emptyset.$$

Retrieve $T_1.eid$ from works for (T_1)

If $\left(\underbrace{\text{all bids of pname} = DB}_{\cdot} \right) - \left\{ \begin{array}{l} \text{Bids works by} \\ T_1.eid \end{array} \right\} = \emptyset$

Select distinct $T_1.eid$

From works FL (T_1)

where

not exists

Select Pid
from Project
where Pname = DB
except

~~exists~~
 $= \emptyset$ \oplus

Select Pid
from worksfl T2
where $T_2.eid = T_1.eid$

Pids of DB project.

{ 1, 2, 3 }

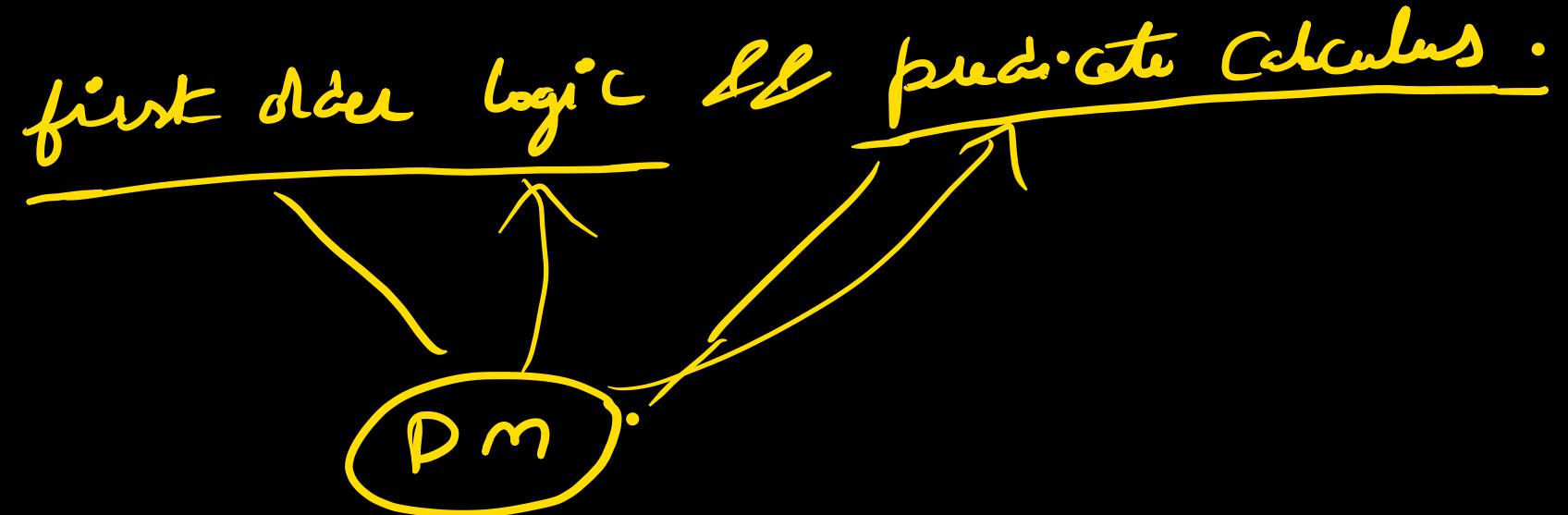
All the project that some
employee is done
{ 1, 2, 3 }

End of SQL.

We have solved all the models.
Exam questions will be from my notes.



Tuple relational calculus (TRC) :

- non procedural query language
 - SQL specifies what we want but not how we want.
 - uses first order logic or predicate Calculus.
- ∴ You will not understand everything.
After Pm is over, you revisit this.

Basic formulae used in TRC:

P, Q are predicates
↳ (statement which can be true/false)

$P \vee Q$

$P \wedge Q$

$\neg P$

$P \rightarrow Q$

$x \in \text{Rel}$

$\exists x \in \text{Rel} (P(x))$
For some x which belongs to Rel s.t. $P(x)$ is TRUE

$\forall x \in \text{Rel} (P(x))$
For every $x \in \text{Rel}$ $P(x)$ is always true.

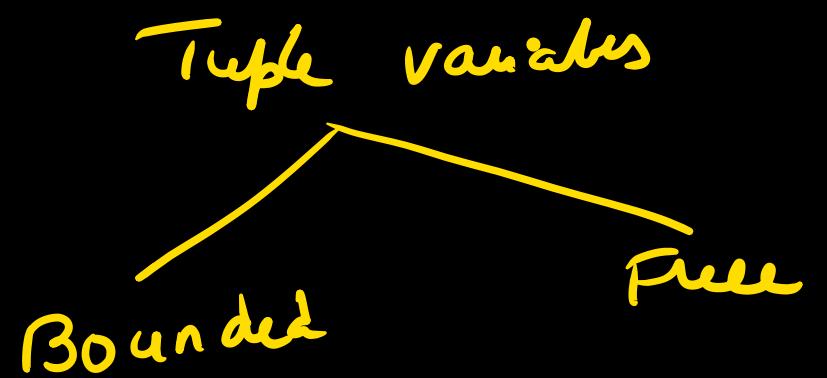
Format of TRC Query :-

$\{\tau / P(\tau)\}$ τ : Tuple variable $P(\tau)$: formula over tuple variable τ .

Returns set of tuples (τ) those satisfy $P(\tau)$

Ex: $\{\tau / \underbrace{\tau \in \text{stud}}_{\text{Bounded}} \wedge \underbrace{\tau.\text{age} > 20}_{\text{Free}}\}$

Retrieves all students whose age is more than 20.



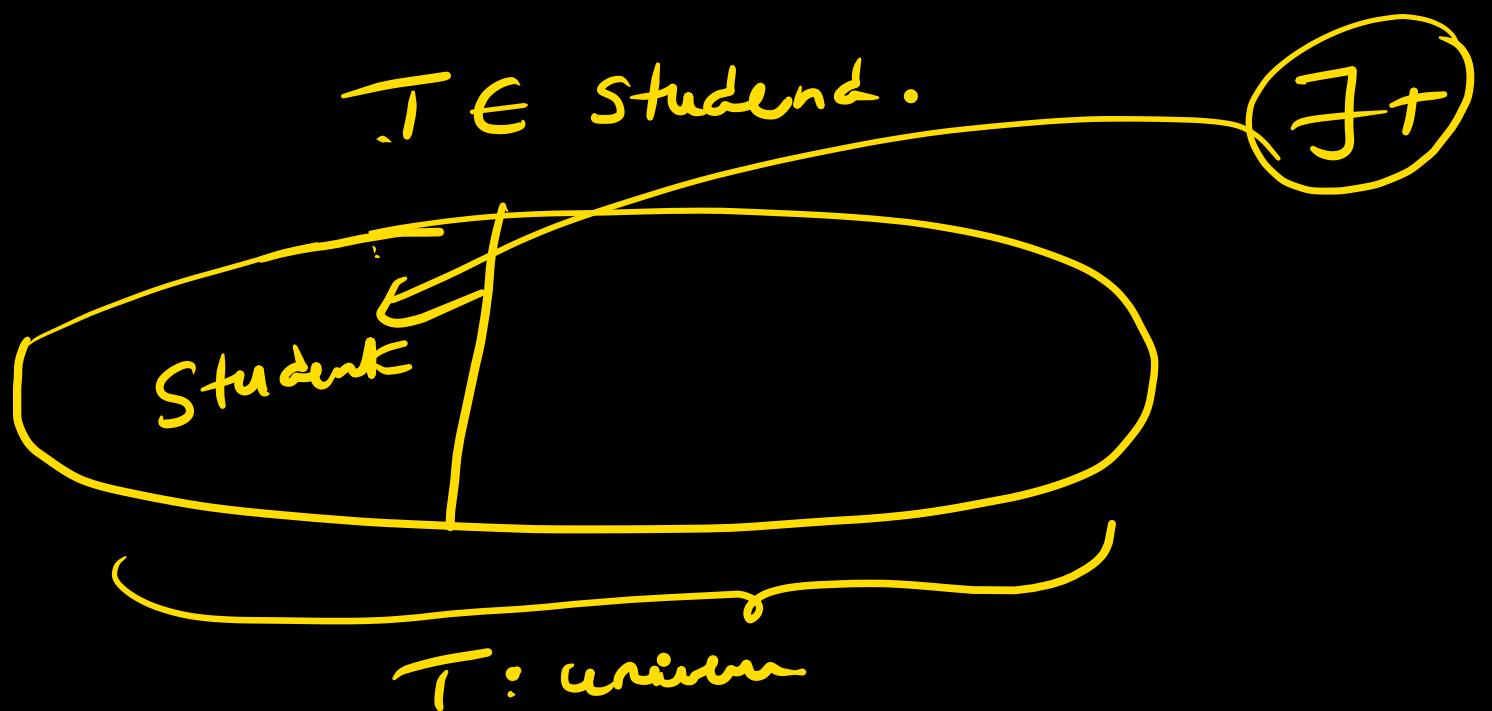
Bounded tuple variables: Variables bounded by quantifier (\exists, \forall)

Ex: $\exists T_1 \in \text{Student} (\dots \dots)$

$\forall T_2 \in \text{Course} (\dots \dots)$

Free variable: not bounded by quantifier

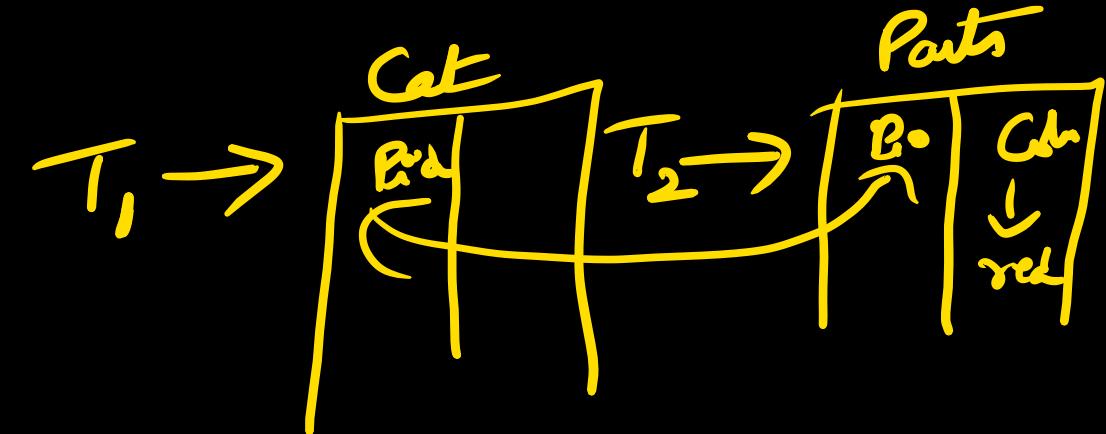
universal variable



Suppliers (Sid, Rating)

Parts (Pid, Price, color)

Catalog (Sid Pid cost)



Retrieve Sid's of suppliers who supplied some red parts.



RA:

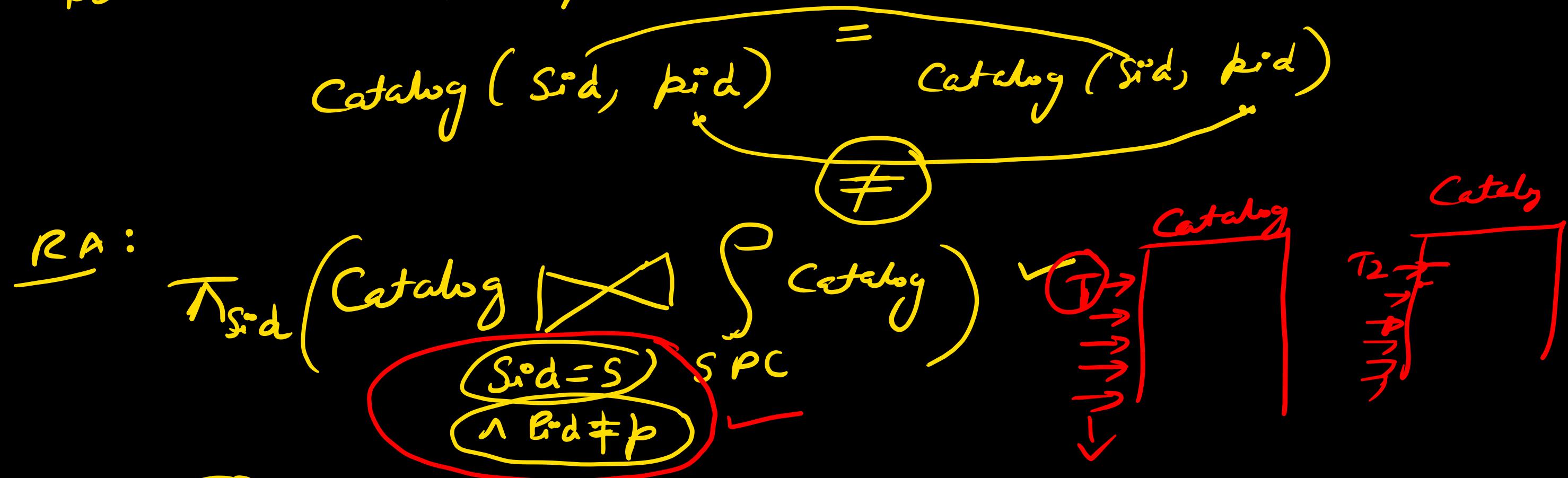
$$\overline{\Delta}_{\text{goal}} \left(\underbrace{\text{Catalog} \times \text{Parts}}_{\text{Cat} = \text{Red}} \right)$$

Catalog.Pid = parts.Pid

$\{ \cap_p (R \times S)$
 $R \bowtie_b S$
 $R \bowtie S \}$ Some
/ any
/ atleast one

In TRC we will use \exists existential quantifier

Retrieve Sids of Suppliers who supplied atleast two parts.



$$\begin{aligned} & \exists T_1 \in \text{Catalog}, \exists T_2 \in \text{Catalog} \\ & (T_1 \cdot \text{Sid} = T_2 \cdot \text{Sid} \wedge \\ & T_2 \cdot \text{pid} \neq T_2 \cdot \text{pid} \wedge \\ & T = T_1 \cdot \text{Sid}) \end{aligned}$$

$$\left\{ \begin{array}{l} R \cup S = \{\tau / \tau \in R \vee \tau \in S\} \\ R \cap S = \{\tau / \tau \in R \wedge \tau \in S\} \\ \underline{\underline{R - S}} = \{\tau / \tau \in R \wedge \tau \not\in S\} \end{array} \right\}$$

$$R - S = R \cap \overline{S}$$

Supplier (sid, rating)

Part (Pno, Pname, Code)

Catalog (sid, Pid, cost)

\geq every

Comb
 $<$ some
↓

Retrieve Supplier ids where rating is maximum.

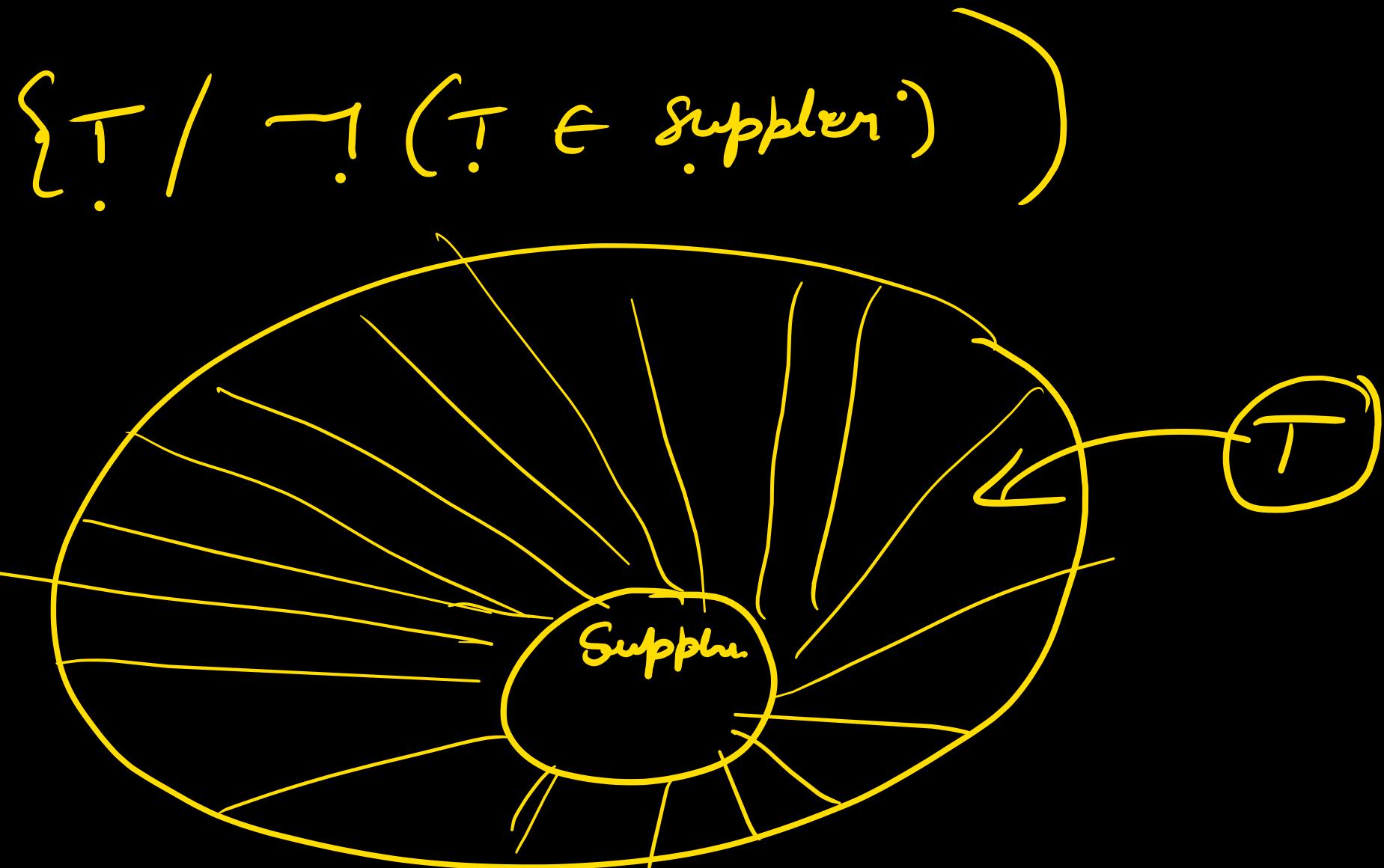
RA: $\pi_{sid}(\text{Supplier}) - \pi_{sid}(\text{Supplier} \bowtie \text{Supplier})$
 $\quad\quad\quad \text{rating} < R^S_R$

TRC: $TRC = \{ T / \exists T_1 \in \text{Supplier} (T = T_1 \cdot sid) \wedge \neg \exists T_1 \in \text{Supplier} \exists T_2 \in \text{Supplier} ((T_1 \cdot \text{rating} < T_2 \cdot \text{rating}) \wedge (T \neq T_2 \cdot sid)) \}$

 unsafe:

Conclusion:

TRC query with infinite results in result is unsafe.



Expressive Power :-

$$\{ \text{Basic RA queries} \quad = \quad \{ \text{Safe TRC queries} \\ \text{expensive power} \} \}$$

TRC can do the following operators of RA

$$\{ \pi, \times, \cap, \setminus, \cup, -, \cap, \bowtie, \bowtie_c, \bowtie_s, \bowtie_e \\ \bowtie_d, / \wedge \% \}$$

Safe TRC / RA cannot do the following:

- a) Count of records / Count of attribute values
- b) Sum of attribute values
- c) Avg of attribute values

RA, SQL, TRC.
99%

ER model :