

Query optimization:

$$R \left(\begin{array}{c} R.B = S.B \\ \wedge R.A > 10 \\ \wedge S.C > 5 \end{array} \right) \times S$$

~~Big to apply comparison before δ & δX_C .~~

$$R \left(\begin{array}{c} R.A \neq 10 \\ \wedge R.B = S.B \\ \wedge S.C > 5 \end{array} \right) \times S$$

$I \times$ will be applied
then 3 condition.

$$R \times S = \left| \begin{array}{c} (m \times n) \\ \hline \end{array} \right| \text{ rows}$$

3 conditions (comparisons)

$3 \times m \times n$ comparisons

$\times \delta \propto \delta X_C$.



$$\sigma_{\{R \bowtie S\}} \Leftrightarrow \\ \underbrace{R.A > 10}_{}$$

$$\underbrace{\sigma_R}_{A > 10} \bowtie S = .$$

$$\sigma_{\{R \bowtie S\}} \Leftrightarrow \\ \underbrace{R.A > 10}_{\wedge S.C > 5} \quad \downarrow \\ \text{more no of rows to join} \quad \left(\begin{array}{c} \sigma_R \\ A > 10 \end{array} \bowtie \begin{array}{c} \sigma_S \\ C > 5 \end{array} \right) \\ \downarrow \\ \text{less no of rows to join}$$

$\rightarrow \text{enroll}(\text{sid}, \text{cid})$

{
10000 rows}

course (cid, Insti)

{
100 rows}

$\sim (\text{Enroll} \bowtie \text{Course}) \Rightarrow \approx$

Insti = kath

$\sim (\text{Enroll} \times \text{Course})$
 $E.\text{cid} = C.\text{cid}$
Insti = kath

10000

(enroll) X

$E.\text{cid} = C.\text{cid}$

enroll course

ex: 5 row
n found ✓

size inst = 100M

50000 rows.
50,000 + 100

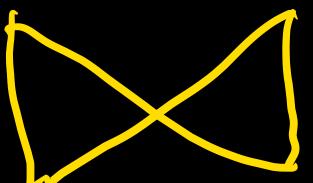
2 Comparisons of conditions

$100000 \times 100 = 10 \text{ letkhs}$
 $= 20 \text{ batch comp.}$

$\text{Emp}(e\text{id}, \text{gen}, \text{sal})$

$\pi_{e\text{id}}(\text{Emp} \bowtie \sigma(\text{gen} = \text{female} \wedge G = \text{male} \wedge \text{Sal} > S) \text{ IGS})$

σ_{Emp}
 $\text{gen} = \text{female}$



$\text{Sal} > S.$

$\sigma_{G = \text{male} \text{ IGS}}$

Queries related to atleast / only / atmost :

Ex.	Size of students who took	at least 2 courses
"	"	only 2 courses
"	"	at most 2 courses
"	"	at least 100 courses
"	"	only 100
		at most 100

$\text{enroll}(\text{Sid}, \text{Cid})$ Retrieve Sid's who enrolled for at least two courses.

Enroll	Sid	Cid	enroll	Sid	Cid
	S_1	C_1		S_1	C_1
	S_1	C_2		S_1	C_2
	S_1	C_3		S_1	C_3
	S_2	C_1		S_2	C_1
	S_2	C_2		S_2	C_2
	S_3	C_1		S_3	C_1

which mean S_1 has taken 2 courses.

$\text{enroll} \bowtie \text{enroll}$: course is diff
 $S_1, C_1 \quad S_1, C_2$
sid are equal \equiv same student

$$\pi_{T_1 \cdot \text{sid}} \left(\wp(T_1, \text{enroll}) \bowtie \wp(T_2, \text{enroll}) \right)$$

$T_1 \cdot \text{sid} = T_2 \cdot \text{sid} \rightarrow \text{Same student}$

$T_1 \cdot \text{cid} \neq T_2 \cdot \text{cid} \rightarrow \text{Two courses}$

(d)

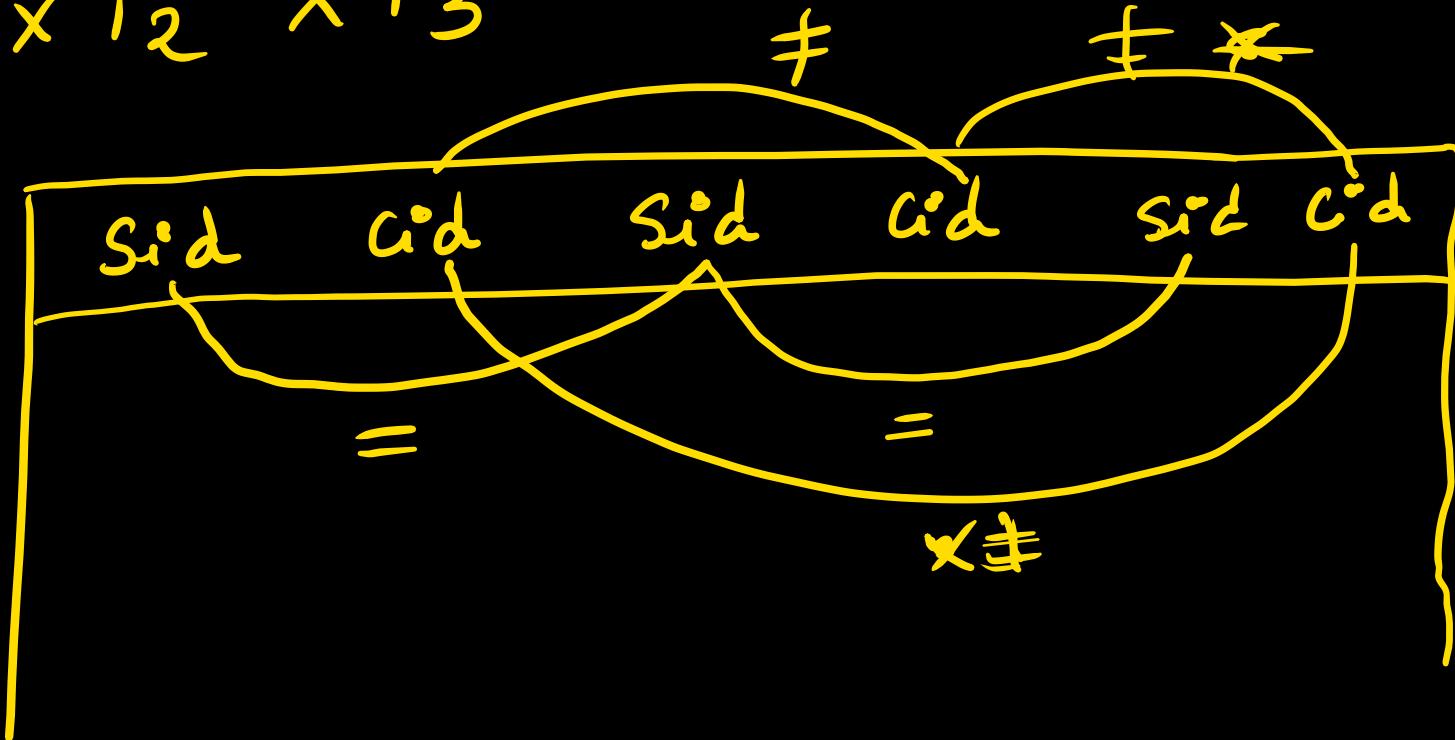
$$\pi_{\text{sid}} \left(\text{enroll} \bowtie \begin{array}{c} \wp(\text{enroll}) \\ \text{sid} = S \\ \wedge \text{cid} \neq C \end{array} \right)$$

Enroll (Sid, Cid)

Sids of enrolled students who enrolled atleast 3 courses.

$T_1, T_2, T_3 \rightarrow \underline{\underline{enroll}}$.

$T_1 \times T_2 \times T_3$



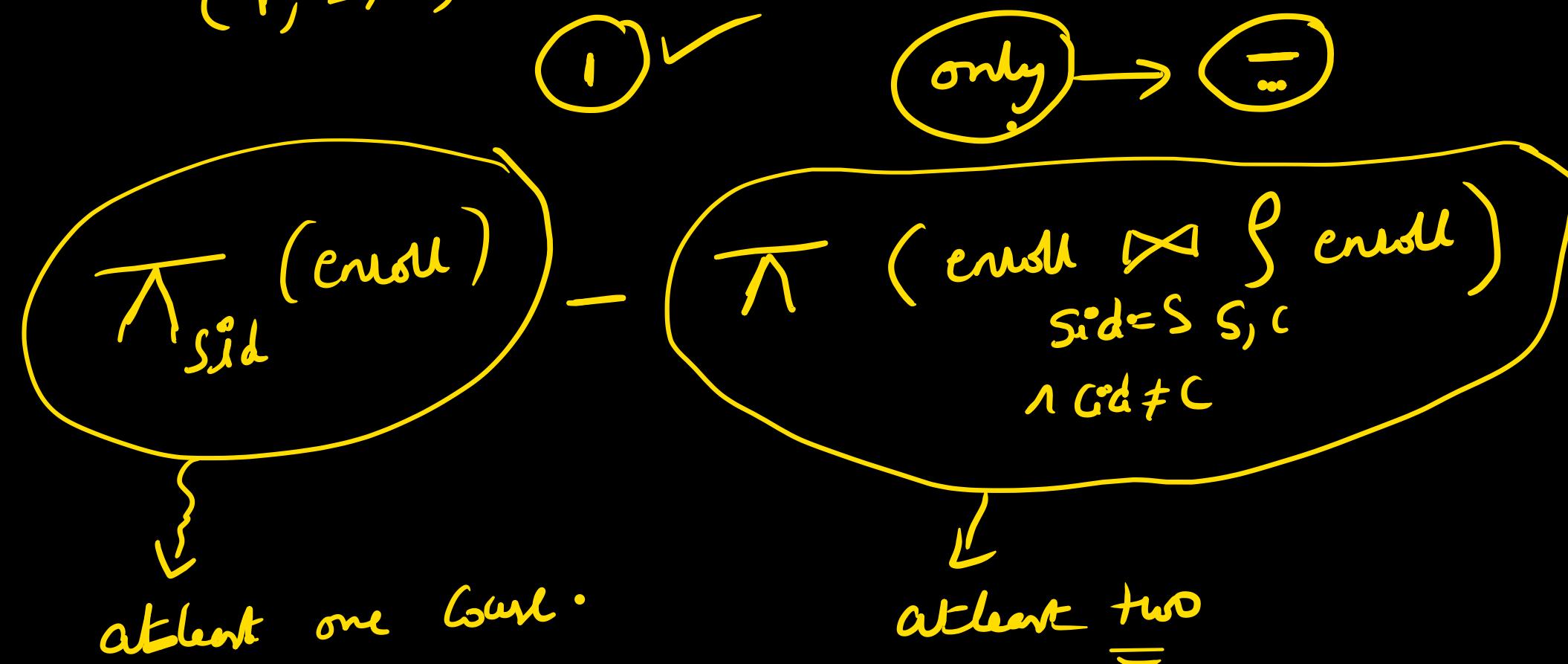
S1 C1 C2 C3
S1 having (3) Courses.

≥ 3 .
=

Sids enrolled only one course. & exactly 1 course.

{ Sids enroll at least one course } - { Sids enrolled at least two courses }

(1, 2, 3, 4, 5, ...) - (2, 3, 4, 5, 6, ...)



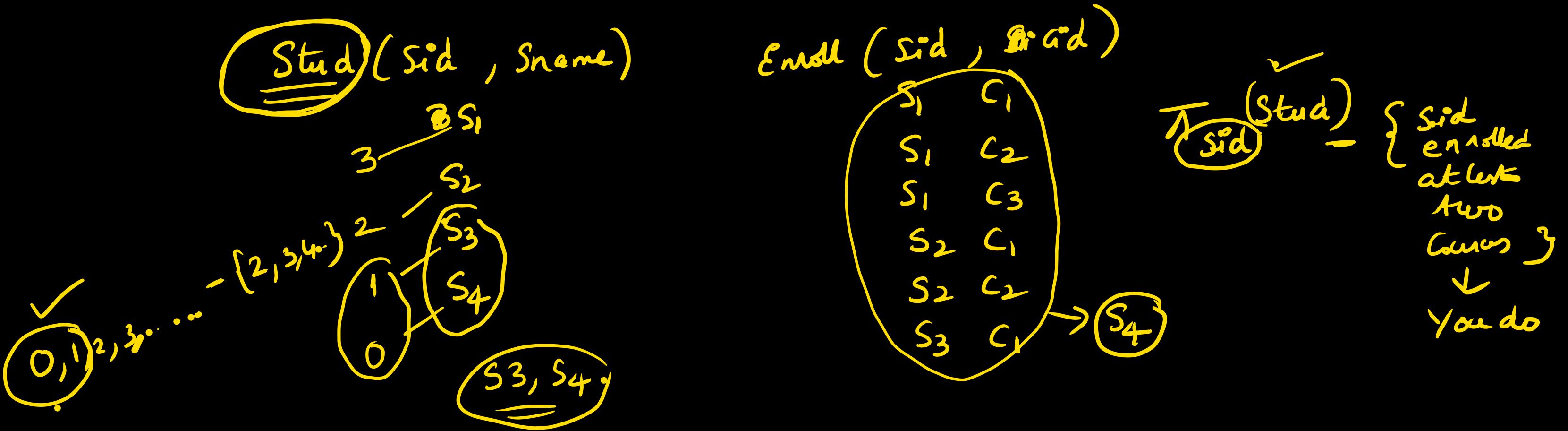
- Sids enrolled in atleast 10 courses.
we need to put cross product on 10 tables.
But there is no other solution
But in SQL we can write it in simple way because
of extra features like groupby , having etc.

Sid enrolled "only two" courses

$$\left(\begin{array}{l} \text{Sids enrolled} \\ \text{in atleast} \\ 2 \text{ courses} \end{array} \right) - \left(\begin{array}{l} \text{Sids enrolled} \\ \text{in atleast} \\ 3 \text{ courses} \end{array} \right)$$

You do it as assignment.

Sid enrolled in at-most one course



$\{ \text{all students} \} - \{ \text{sid's enrolled atleast two course} \}$

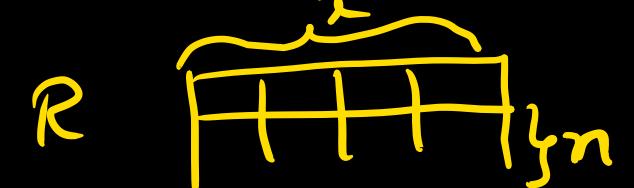
Sids enrolled at most two courses:

{ all students } - { sids enrolled at least three courses }

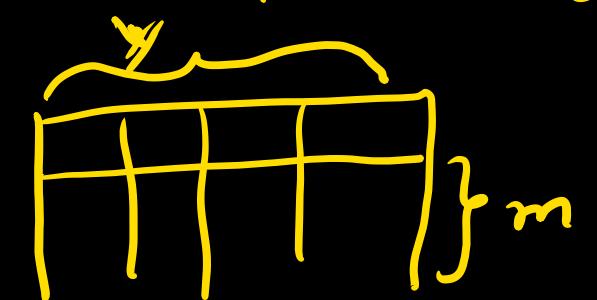


Some theory questions related to division:

→ Rel R with X set of attributes & n distinct tuples.



→ Relation S with Y set of attributes & m distinct tuples.



1) Condition required for R/S is $X \supseteq Y$

2) Resulting attribute set of R/S is $X - Y$

3) Cardinality of R/S
 min = 0
 max = $\left\lfloor \frac{n}{m} \right\rfloor$

$$\pi_{AB}^{(R)} / \pi_B(S)$$

a_1, b_1
 a_1, b_2
 a_1, b_3

b_1
 b_2
 b_3

a_2, b_1
 a_2, b_2
 a_2, b_3

outputs (a_1, a_2)

$$\left[\frac{n}{m} \right]$$

$$\frac{6}{3} = 2 \checkmark$$

$$\left[\frac{7}{3} \right] = 2 \checkmark$$

③ ✓

$\text{Rel } R$ with n distinct tuples, $\text{Rel } S$ with m distinct tuples

RA expression

① $\pi_A(R)$

Cardinality ($n \cdot 1, \text{ max}$)

Atmost $n = \max$
 $1 = \min$

Commutative

NO

② $\sigma_C(R)$

min 0, max - n

Yes

3) $R \times S$

$n \times m$

Yes

4) $R \bowtie S, R \bowtie_C S$

min = 0, max $n \times m$

Yes

5) $R \bowtie_S S$

min = n , max = $\underline{n \times m}$

No

6) $R \bowtie_C S$

min = m max: $n \times m$

No

$\begin{array}{ c c c c } \hline & 1 & 2 & 1 \\ \hline 1 & & & \\ \hline 2 & & & \\ \hline 3 & & & \\ \hline \end{array}$
① $\sigma_{\leq}(R)$

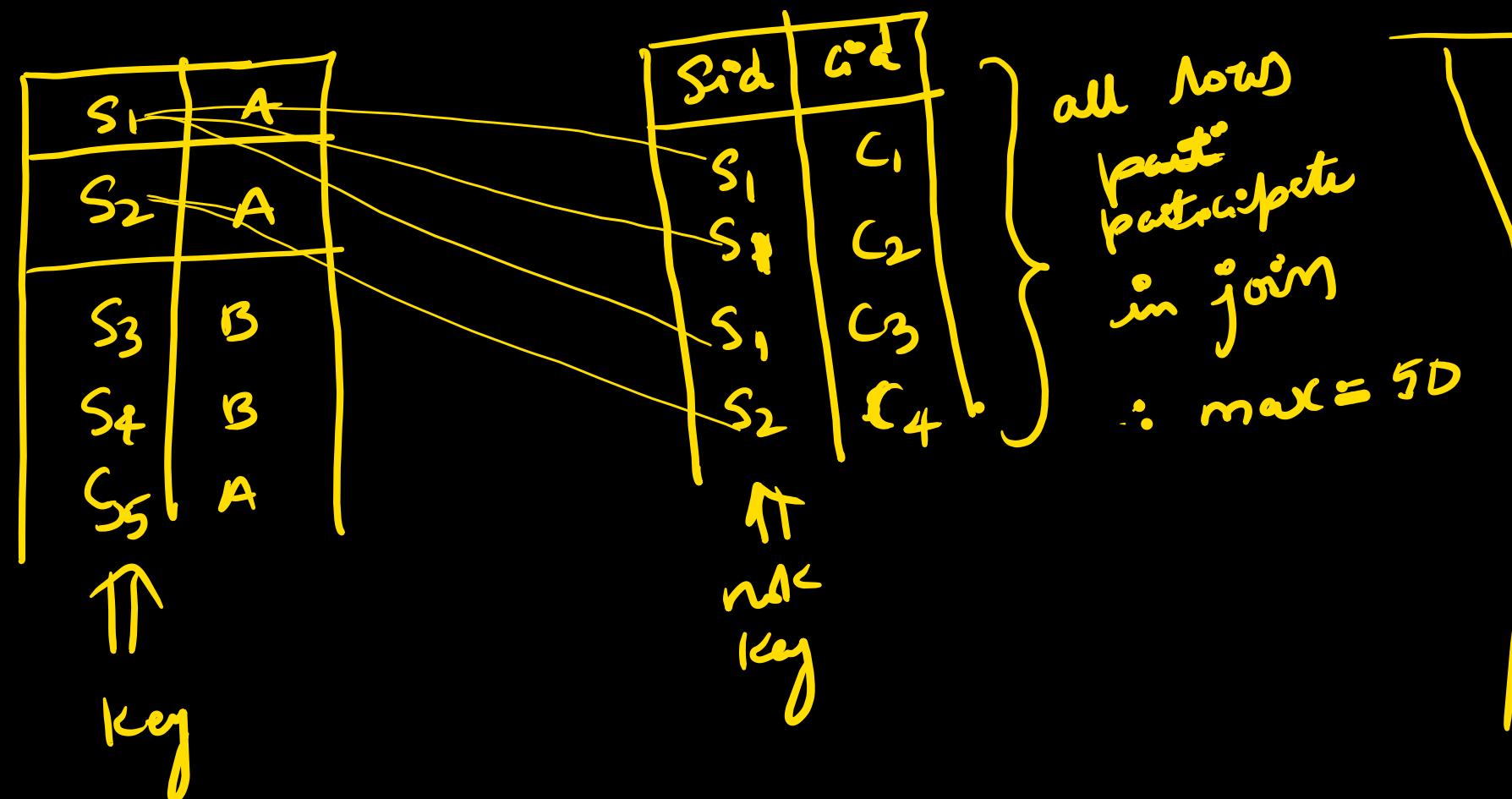
① $\sigma_{\leq}(R)$

7	$R \setminus S$	$\max(n, m)$ to $m \times n$	yes	
8)	$R \cup S$	$\max(n, m)$ to $m+n$ min	yes	
9	$R \cap S$	0 to $\min(n, m)$ max	yes	
10	$R - S$	0 to n	no	
11	R/S	0 to $[n/m]$	no.	

Stud (Sid, sname), Sid is primary key with ≤ 100 tuples, Enroll (Sid, Cid)

Sid Cid primary key with ≤ 50 tuples. How many (max, min) tuples

in result of $\text{Stud} \bowtie \text{Enroll}$.



all rows
participate
in join
 $\therefore \text{max} = 50$

min = no row matches

= '0'

If Sid is fK, all the
Sid's in enroll are
present in Stud.
 $\therefore \text{min} = 50$

RA ✓

SQL, ER, Trns, Index. ✓.