

Stack, Queues, Priority Queues & Heaps Lecture 1

Sunday, 4 August 2024 2:03 PM

Stacks

C++
<stack.h>

```
stack<int> s;  
    <T>
```

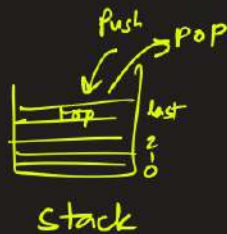
s.push(-) $O(1)$ ✓

s.pop(); $O(1)$ ✓

s.top() → top element $O(1)$ ✓

s.empty() $\begin{cases} \text{True} \\ \text{False} \end{cases}$

s.size() → ✓



Python

```
from collections import deque
```

```
s = deque();
```

✓ s.append(-);

✓ s.pop();

✓ s[-1]; ← top

✓ if s: → True (Not empty)
bool(s) → False

✓ len(s)

()
valid

{ }
valid

{ }
Invalid

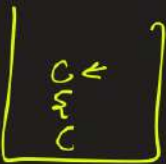
{
Invalid

{, [,], }, {, }

eg: { { { { { { { {
↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑



] Invalid



{ Invalid



{ { { { } } } { }
↑ ↑ ↑ ↑ Invalid

open - push
closing - same type
opening must
be on top
yes / No
pop / Invalid

[] Invalid

[

(Invalid

(Stack

open - push

closing - same type
opening must

be on top

yes/
pop

No
Invalid

end - stack is empty

yes/
Valid

No
Invalid

```
class Solution {
public:
    char cob(char c) {
        if(c == ')') return '(';
        if(c == '}') return '{';
        return '[';
    }
    bool isValid(string s) {
        stack<char> st;
        for(auto c: s) {
            if(c == '(' || c == '{' || c == '[')
                st.push(c);
            else if(!st.empty() && st.top() == cob(c))
                st.pop();
            else
                return false;
        }
        if(st.empty()) return true;
        return false;
    }
};
```

$O(n)$

$O(1)$

$O(n) \rightarrow \text{len}(s)$

Next greater Element

Given an array, find the index/element of next greater element for all elements in the array.

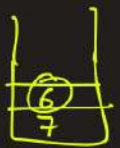
0 1 2 3
[1, 3, 4, 2]
Next gr. elem [3, 4, -1, -1]
next gr index [1, 2, -1, -1]

[5, 2, 3, 4, 6, 7]
[6, 3, 4, 6, 7, -1]

Brute :- $O(n^2)$ ✓

Stacks

[5, 2, 4, 3, 6, 7]
← 6, 4, 6, 6, 7, -1



stack.top()
 $e \rightarrow \begin{cases} t \leq e & \text{pop()} \\ t > e & \leftarrow \underline{\text{ans.}} \end{cases}$

✓ problem | traversal

$e \rightarrow \begin{cases} \text{stack.top()} \\ t \leq e \quad \text{pop()} \\ \underline{t > e} \leftarrow \underline{\text{ans.}} \end{cases}$

✓	problem	traversal	pop	ans
right	greater ✓	reverse	$t \leq e$	$t > e$
right	lesser ✓	reverse	$t \geq e$	$t < e$
left	greater ✓	same	$t \leq e$	$t > e$
left	lesser	same	$t \geq e$	$t < e$

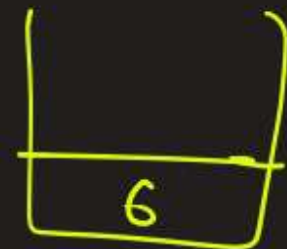
Stacks

[5, 2, 4, 3, 6, 7]

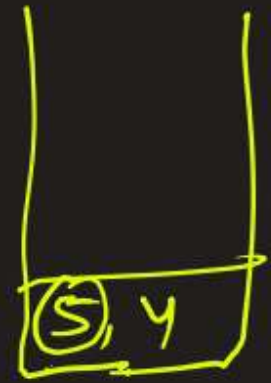
← 6, 4, 6, 6, 7, -1



[3, 6, 2, 5, 1, 4]
[6, -1, 5, -1, 4, -1]



0 1 2 3 4 5 6 7
[4, 2, 1, 3, 5, 4, 3] ⊗
↑ ↑ ↑
elem [5, 3, 3, 5, -1, -1, -1]
index [4, 3, 3, 4, 7, 7, 7]



<https://leetcode.com/problems/next-greater-element-i/>

```
from collections import deque
```

```
class Solution:
```

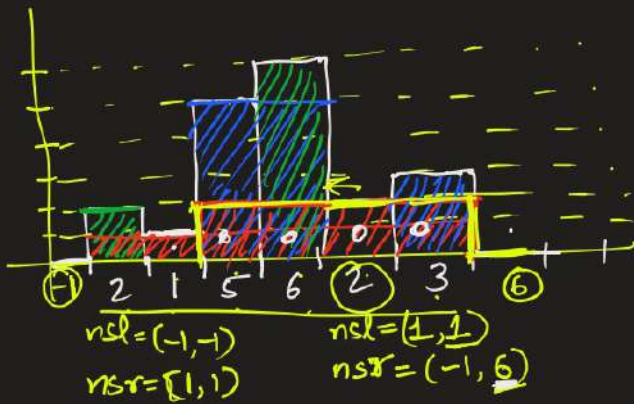
```
    def nextGreaterElement(self, nums1: List[int], nums2: List[int]) -> List[int]:
        s = deque()
        d = {}
        for i in range(len(nums2)-1, -1, -1):
            while s and s[-1] <= nums2[i]:
                s.pop()
            if s:
                d[nums2[i]] = s[-1]
            else:
                d[nums2[i]] = -1
            s.append(nums2[i])
        return [d[n] for n in nums1]
```



Largest Rectangular Area in Histogram

<https://leetcode.com/problems/largest-rectangle-in-histogram/>

eg $[2, 1, 5, 6, 2, 3]$



Rectangle

② $arr[0] :- 2$

① $arr[1] :- 6$

⑤ $arr[2] :- 10$ (10)

⑥ $arr[3] :- 6$

② $arr[4] :- 8$

③ $arr[5] :- 3$

for any index i

↳ Find the rectangle with $arr[i]$ as the height

↳ How far can you go left $O(n)$

↳ nse to the left (indx nsl) ✓

↳ How far can you go right $O(n)$

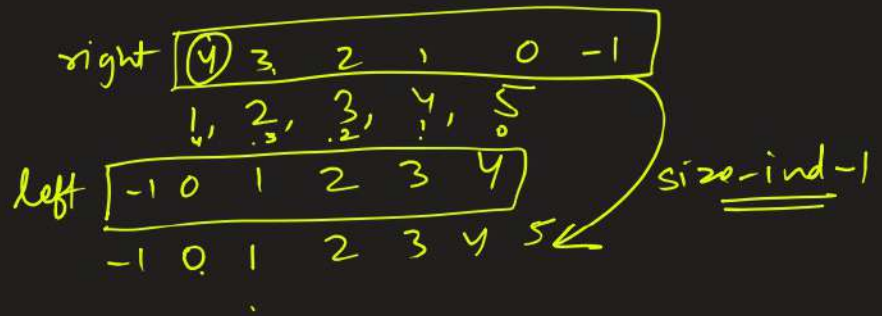
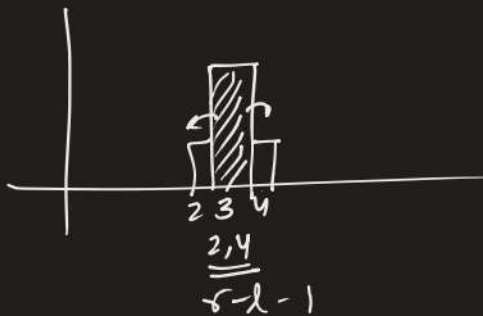
↳ nse to the right (indx nsr) ✓

↳ size of rectangle =

$$\underbrace{arr[i]}_{\text{height}} \times \underbrace{(nsr - nsl - 1)}_{\text{width}}$$

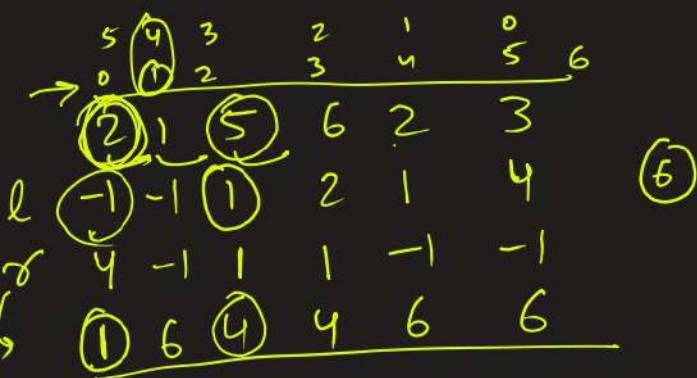
Time:-
 $O(n)$

space:-
 $O(n)$



4 → 0
 3 → 1
 2 → 2
 1 → 3
 0 → 4
 -1 → 5

size-ind-1
 $5-4-1$



$4-1-1$
 $= 2$

$(\text{size} - r[i] - 1 - l[i] - 1)$
 $1 - (-1) - 1 = 1$

```

from collections import deque
def nsel(nums):
    s = deque()
    ans = []
    for i, n in enumerate(nums):
        while s and s[-1][0] >= n:
            s.pop()
        if s:
            ans.append(s[-1])
        else:
            ans.append((-1, -1))
        s.append((n, i))
    return ans
class Solution:
    def largestRectangleArea(self, heights: List[int]) -> int:
        l = nsel(heights)
        r = nsel(heights[::-1])
        r.reverse()
        ans = 0
        for i, h in enumerate(heights):
            val = h * (len(heights) - r[i][1] - l[i][1] - 2)
            ans = max(ans, val)
        return ans

```

```

class Solution {
public:
    vector<pair<int, int>> nsel(vector<int> &nums) {
        vector<pair<int, int>> ans;
        stack<pair<int, int>> s;
        for(int i=0; i<nums.size(); i++) {
            while(!s.empty() && s.top().first >= nums[i]) s.pop();
            if(s.empty()) ans.push_back(make_pair(-1, -1));
            else ans.push_back(s.top());
            s.push(make_pair(nums[i], i));
        }
        return ans;
    }
    int largestRectangleArea(vector<int>& heights) {
        vector<int> rHeights;
        for(int i=heights.size()-1; i>=0; i--) rHeights.push_back(heights[i]);
        vector<pair<int, int>> l = nsel(heights), r=nsel(rHeights);
        reverse(r.begin(), r.end());
        int ans = 0;
        for(int i=0; i<heights.size(); i++) {
            int val = heights[i]*(heights.size()-r[i].second-l[i].second-2);
            ans = max(ans, val);
        }
        return ans;
    }
};

```

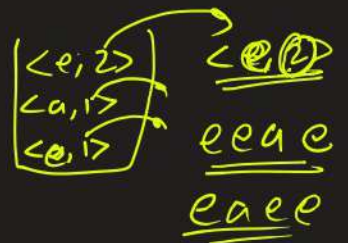
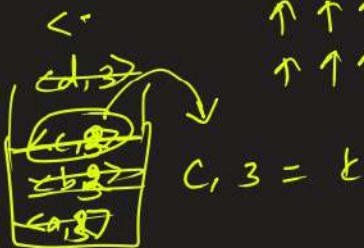
<https://www.geeksforgeeks.org/problems/restrictive-candy-crush--141631/1>

$k=3$

a bb ccc b ddd a e e e
 ↘
abbba e e e e
 ↘
na e e e e
 ↘
e a e e



a b e e e b a d d d a e e e e
 ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑
 ↑ ↑ ↑ ↑ ↑



```
class Solution{
public:
string Reduced_String(int k,string s){
    // Your code goes here
    stack<pair<char, int>> st;
    for(auto c: s) {
        if(!st.empty() && st.top().first == c) {
            pair<char, int> p = st.top();
            p.second++;
            st.pop();
            st.push(p);
        }
        else
            st.push(make_pair(c, 1));
        if(!st.empty() && st.top().second == k)
            st.pop();
    }
    string ans;
    while(!st.empty()) {
        pair<char, int> p = st.top();
        while(p.second-->0) ans += p.first;
        st.pop();
    }
    reverse(ans.begin(), ans.end());
    return ans;
}
};
```