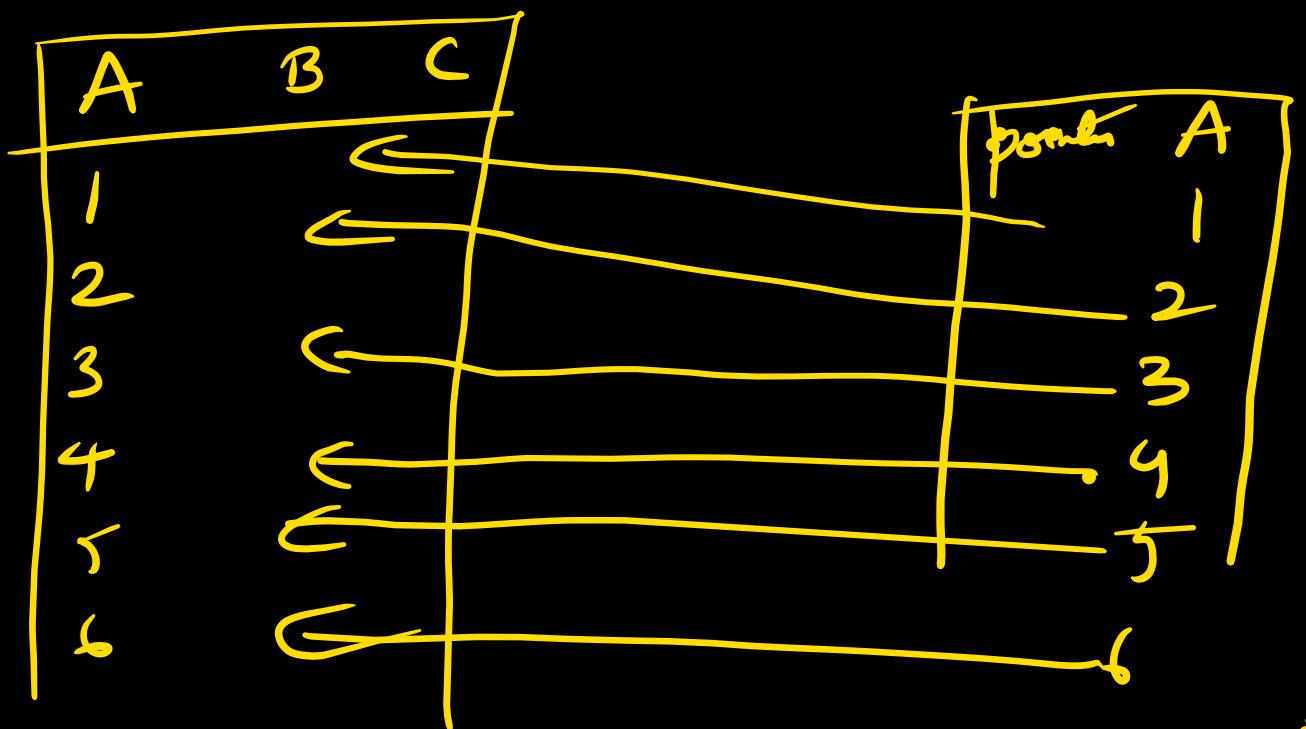
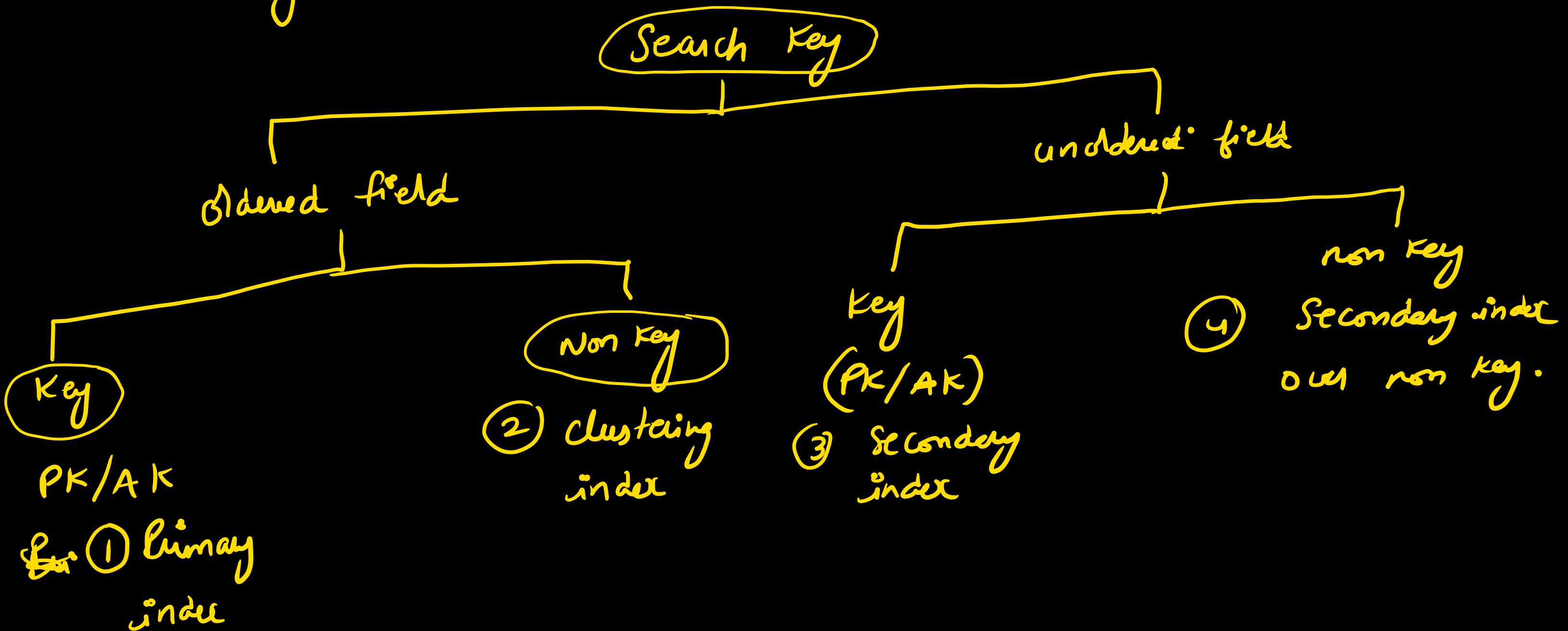


Search Key: fields used for indexing

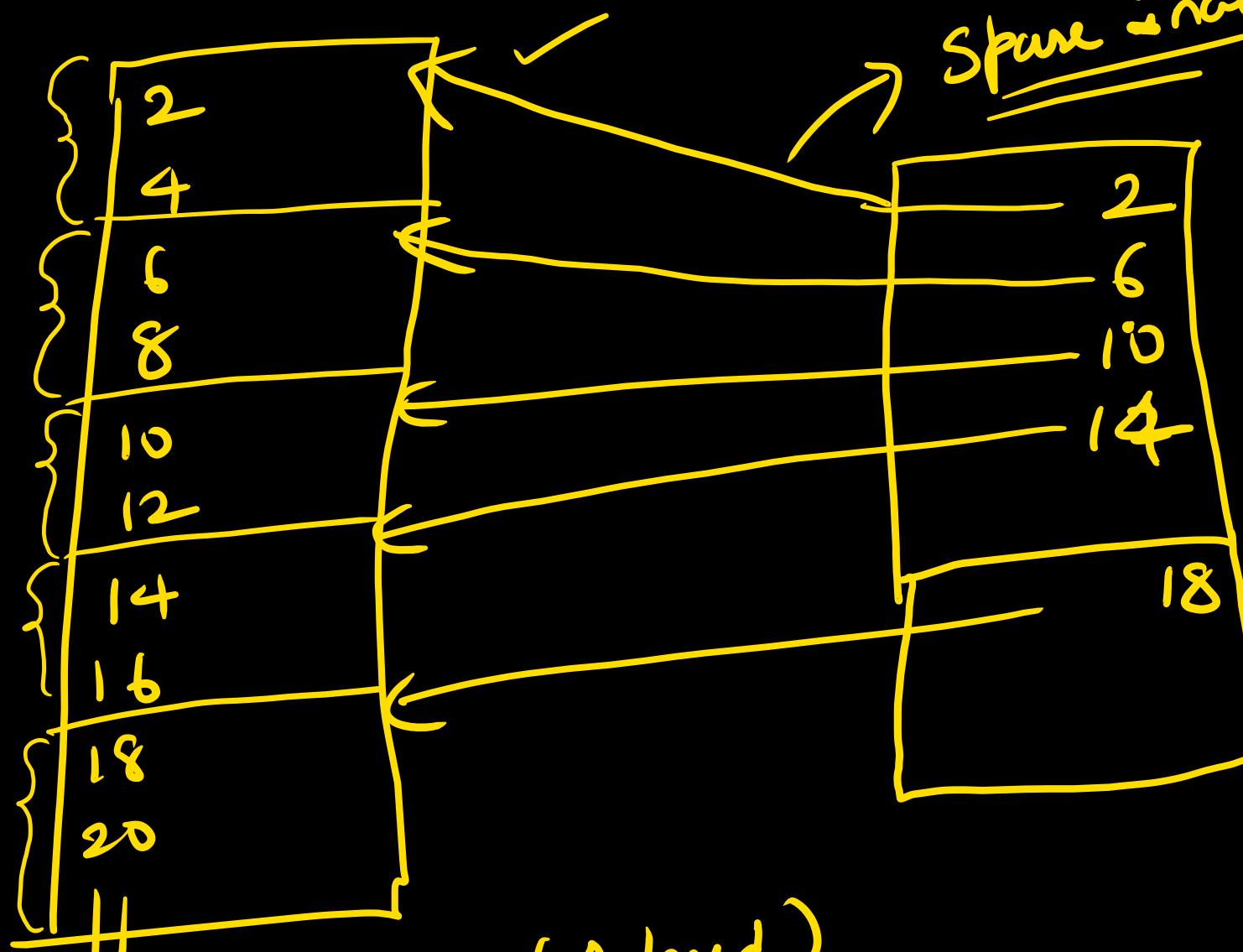


and for this case A is search key.

Search key can be the key of DBT or non key of DBT



Primary key: (Primary field & Key)  
↓  
sorted  
non repetition



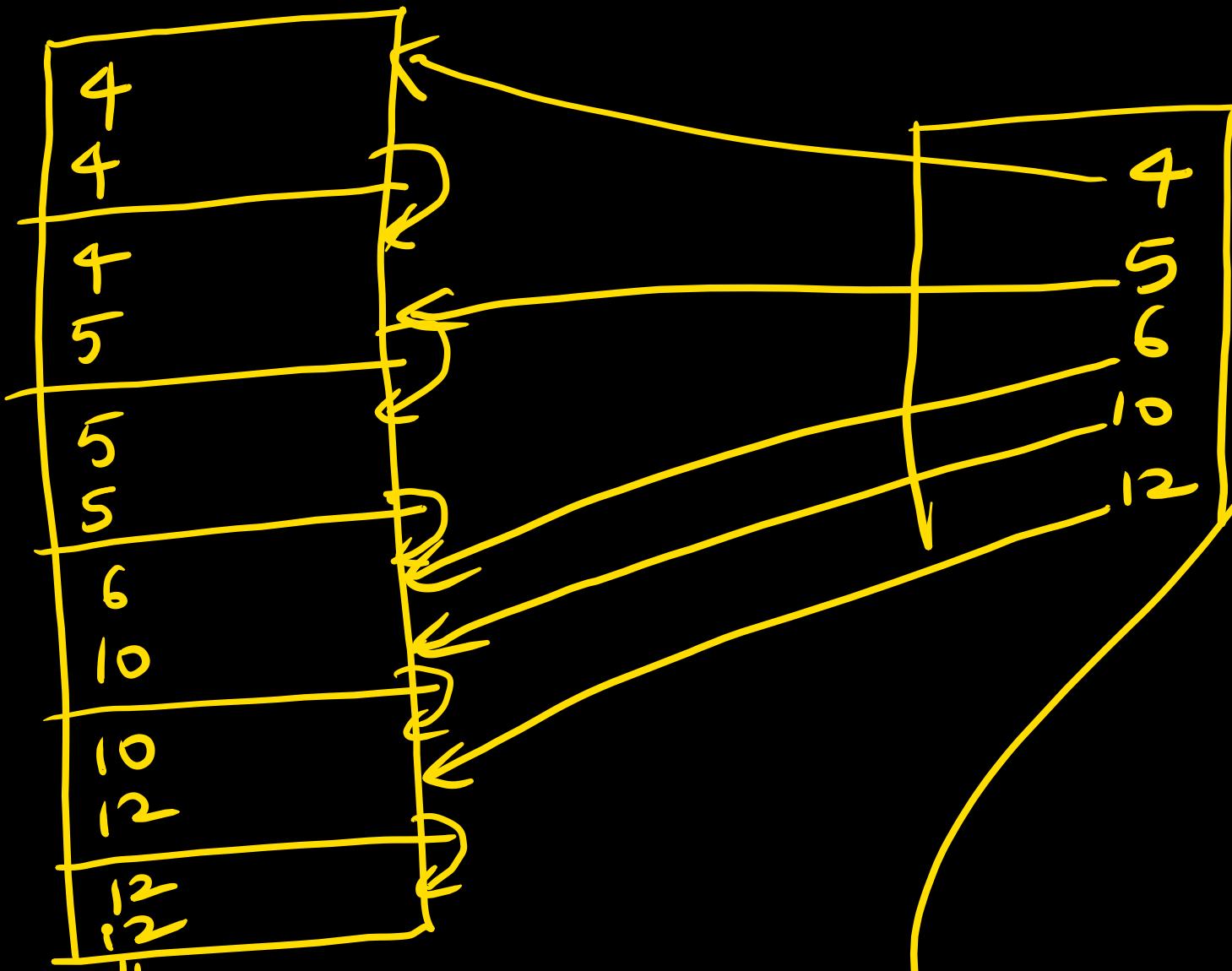
→ For many data records we have  
1 index record

## Important points on Primary index:

- Primary index can be sparse or dense index
- I/O cost PI with multilevel indexing =  $\underbrace{K+1}_{\text{blocks}}$   $K \rightarrow \text{no of levels.}$
- Sorted <img alt="Diagram showing a sorted array [A B C D] with indices 1, 2, 3, 4 below it." data-bbox="58 360 260 540"/>  
[A B C D]  
1 2 3 4
- For a DB Table atmost one PK can be there.  
Because PI is on sorted (sorted) field and we  
can have only one field on which table can  
be sorted.

clustering index: (ordered and not key)

↓  
repetitions



↓  
ordered and non key

I/O cost with CI with next level

indexing =  $K + \frac{one/mode block}{qOBT}$

levels of  
indexing.

4 → 2 blocks  
5 → 2 blocks.

CI

## Clustering index

10

Sparse

Repetition is there.

For every cluster we  
use one index record

dense

Repetition is not there.  
Then for every data record,  
there is a index record

Atmost one clustering index is possible . ( Because CI is on sorted field )

Either primary index or clustering index , only one is possible

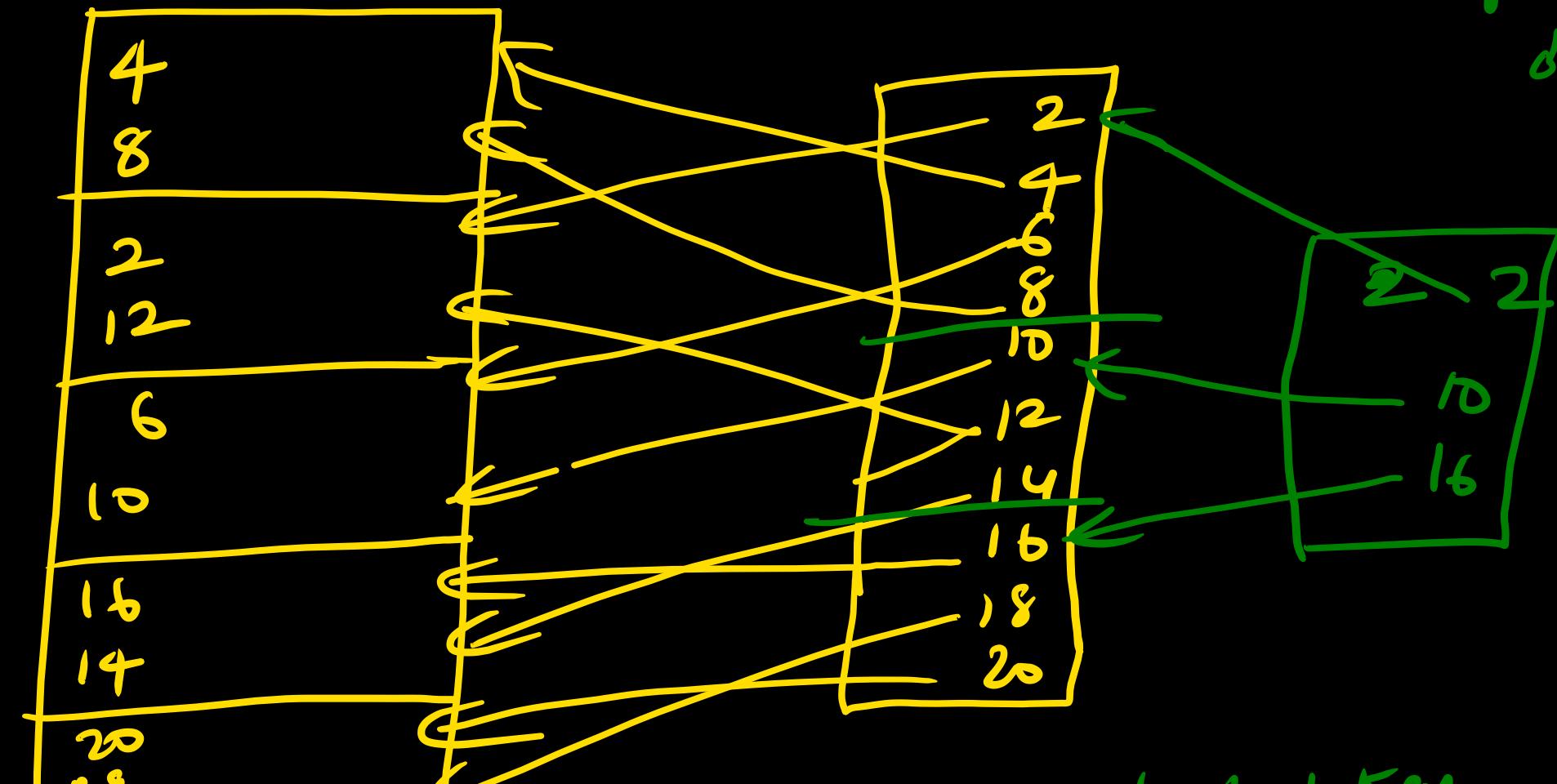
Secondary Index:  $(\text{unordered field} + \text{key})$

many SIs are possible  
in DBT because  
ordering is not required

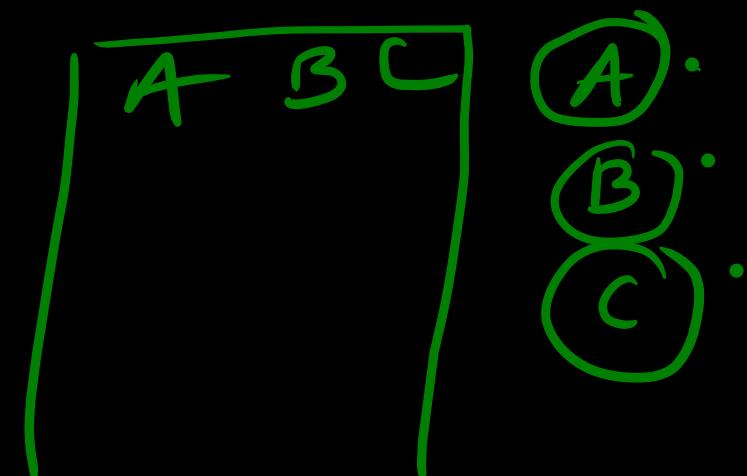
I/O cost  
 $= (K+1)$

no of levels  
of indexing

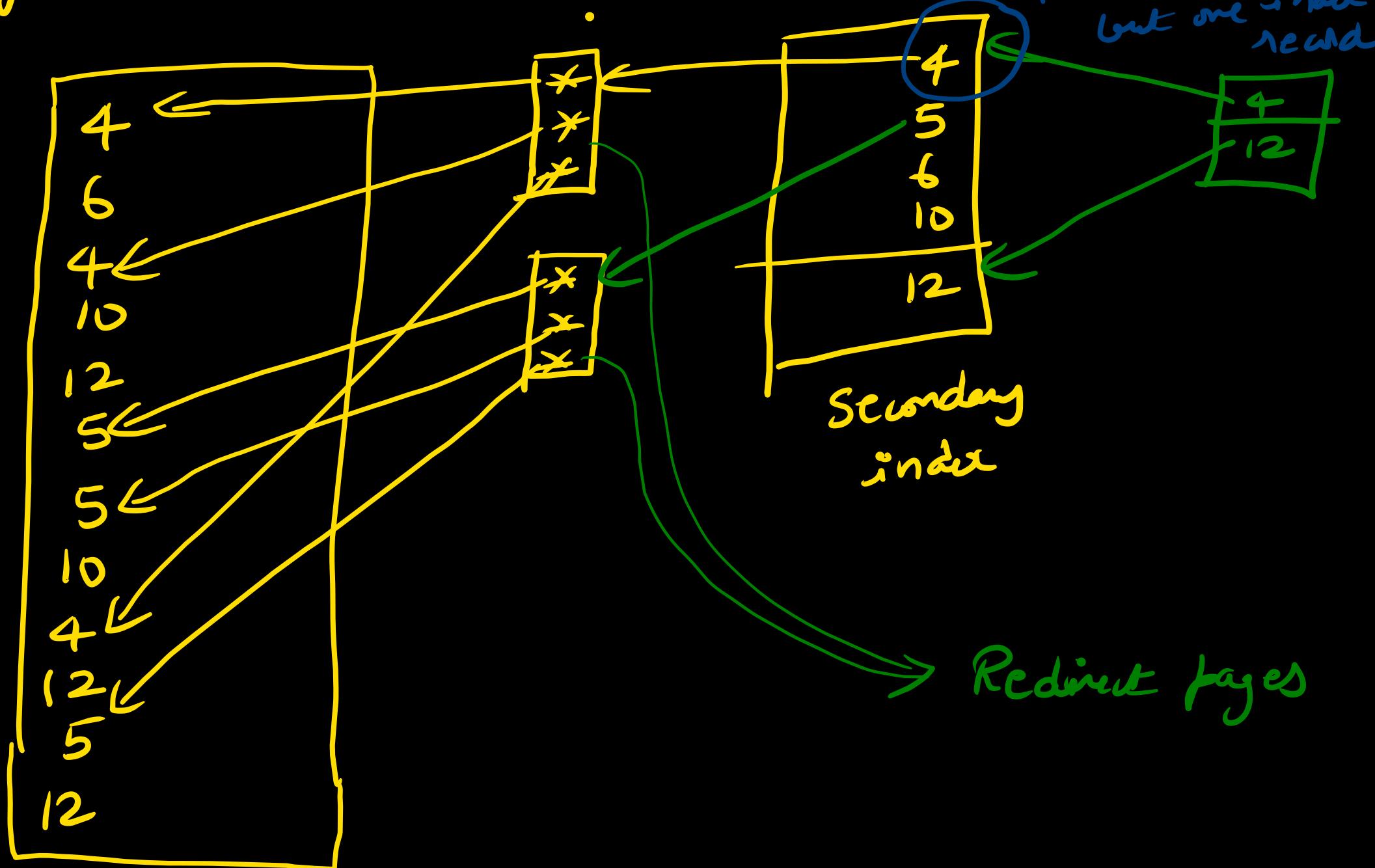
Key  $\rightarrow$  no repetition  
unordered



SI over unordered + key  
is always dense



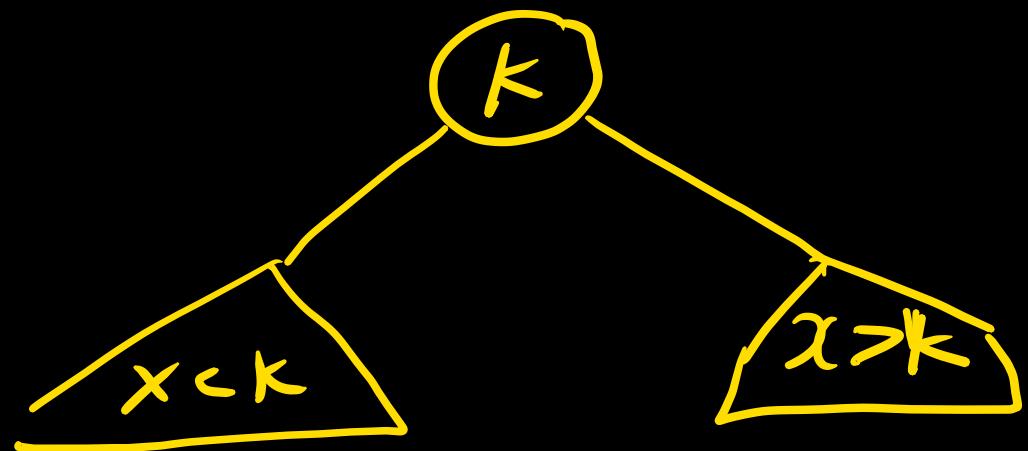
Secondary index over non key (repetitions)

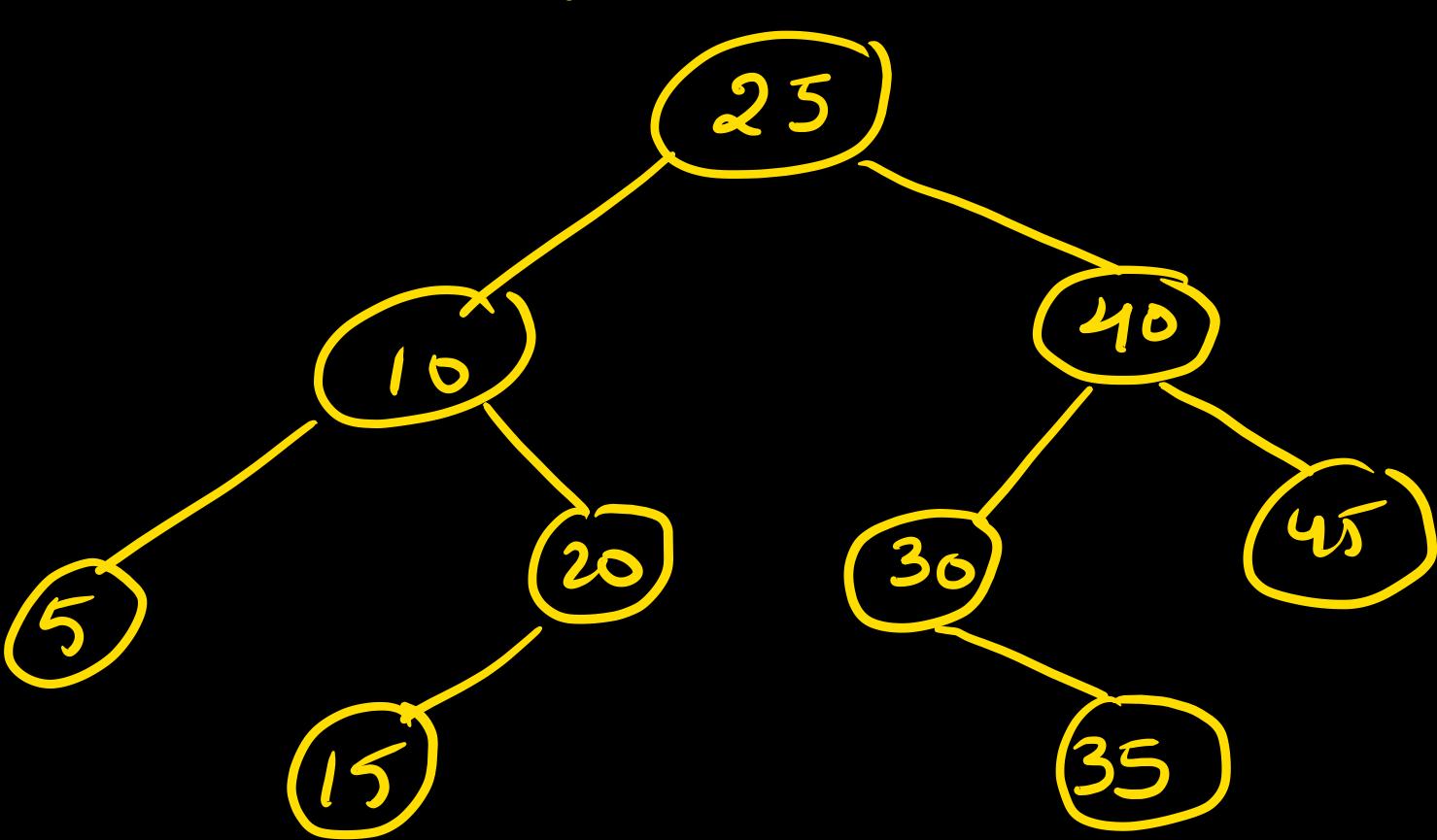


Dynamic multi level index:

B tree }      Balanced search trees.  
 $B^+$  tree }

Search tree: Data structure that organised keys

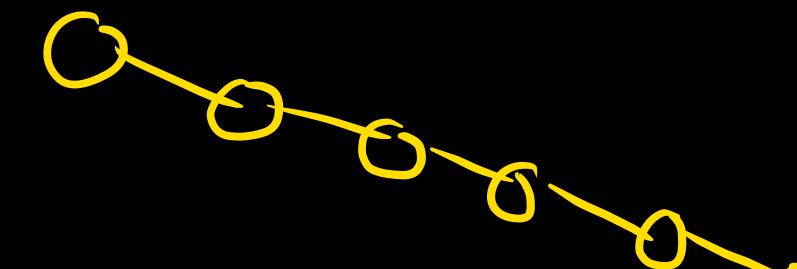




BT BST is optimized for searching.

Disadv if BST :

worst case time complexity  
is  $O(n)$  for search.



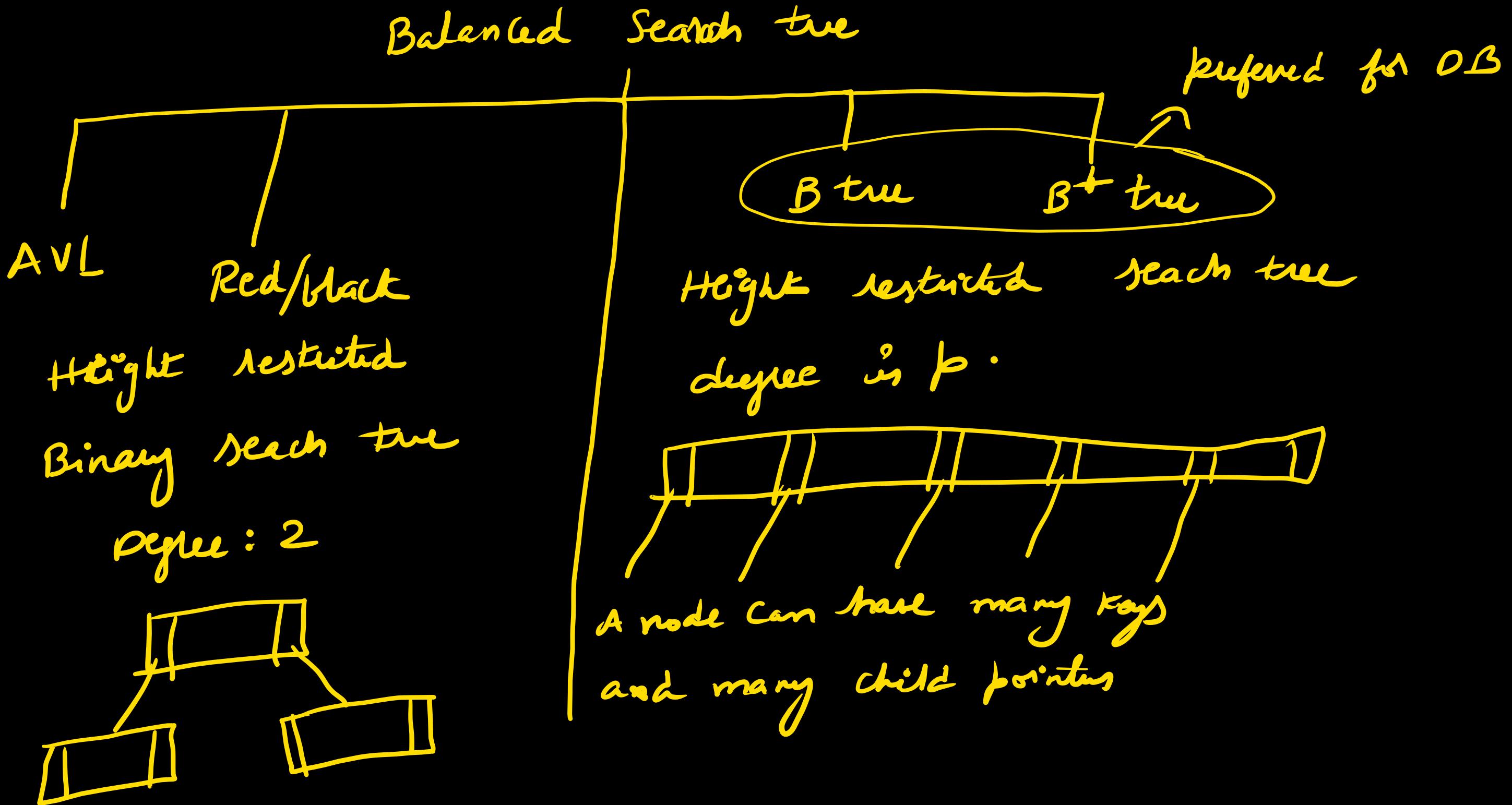
So we need balanced  
search tree which doesn't have  
 $O(n)$  worst case time.

we need balanced search search tree which has ~~worst~~  
worst case time complexity as  $O(\log n)$  not  $O(n)$

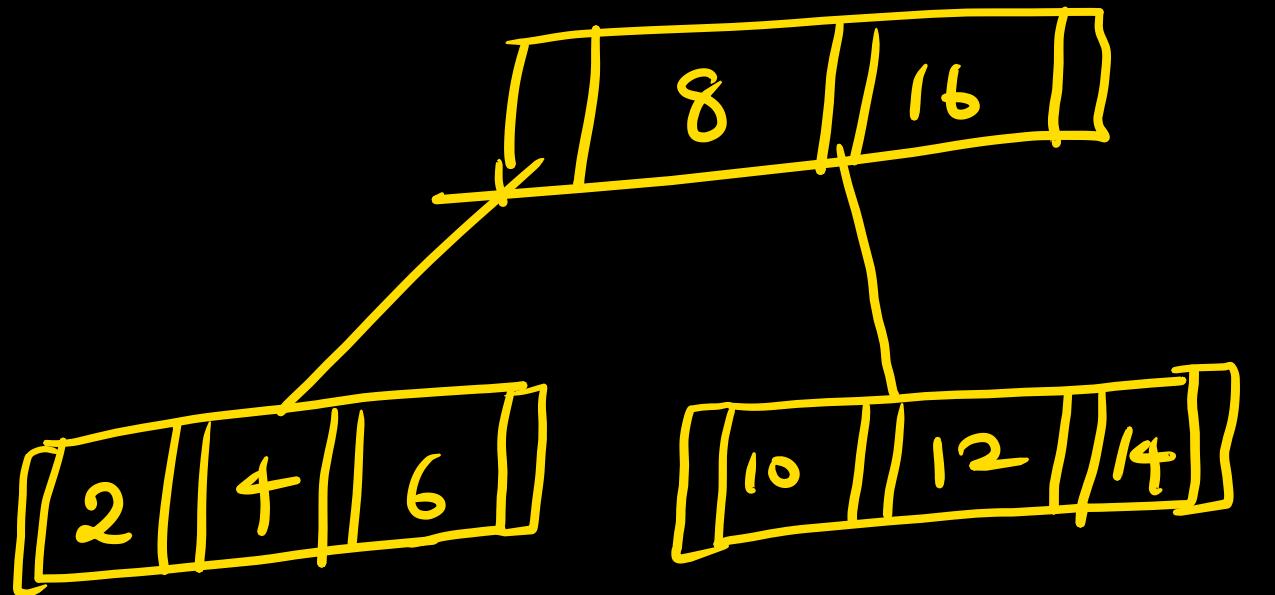
Balanced search tree:

max height of search tree should not exceed  $O(\log n)$  ✓  
for  $n$  distinct key.

worst case search cost doesn't exceed  $O(\log n)$



Ex of B tree :-

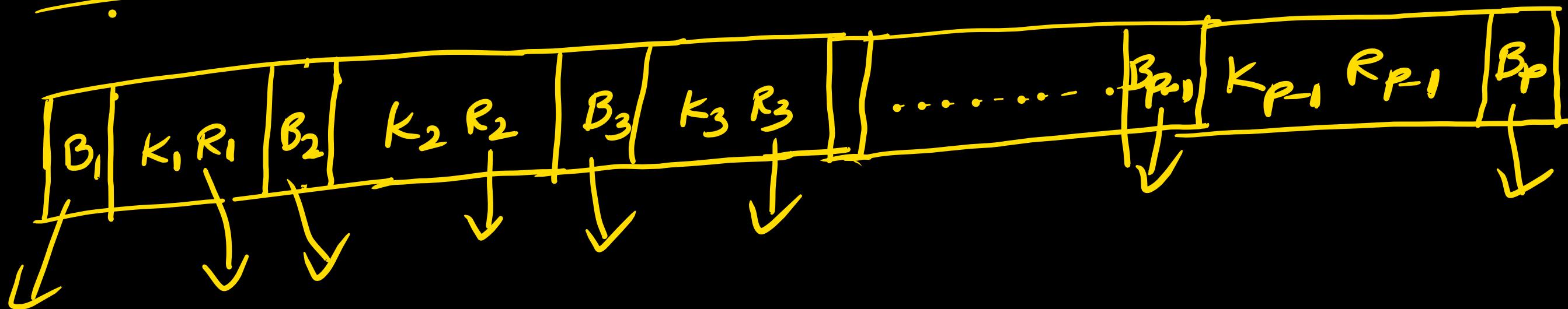


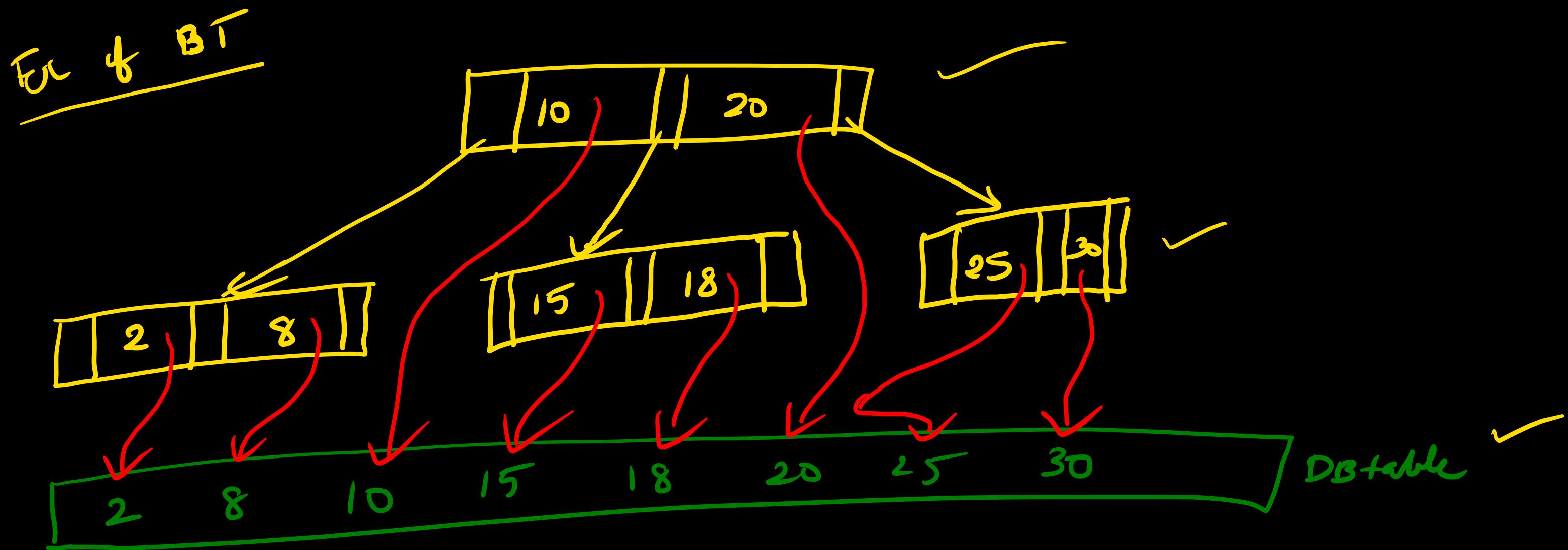
B tree definition :-

what is order P?

maximum possible block pointers which can be present in B tree node

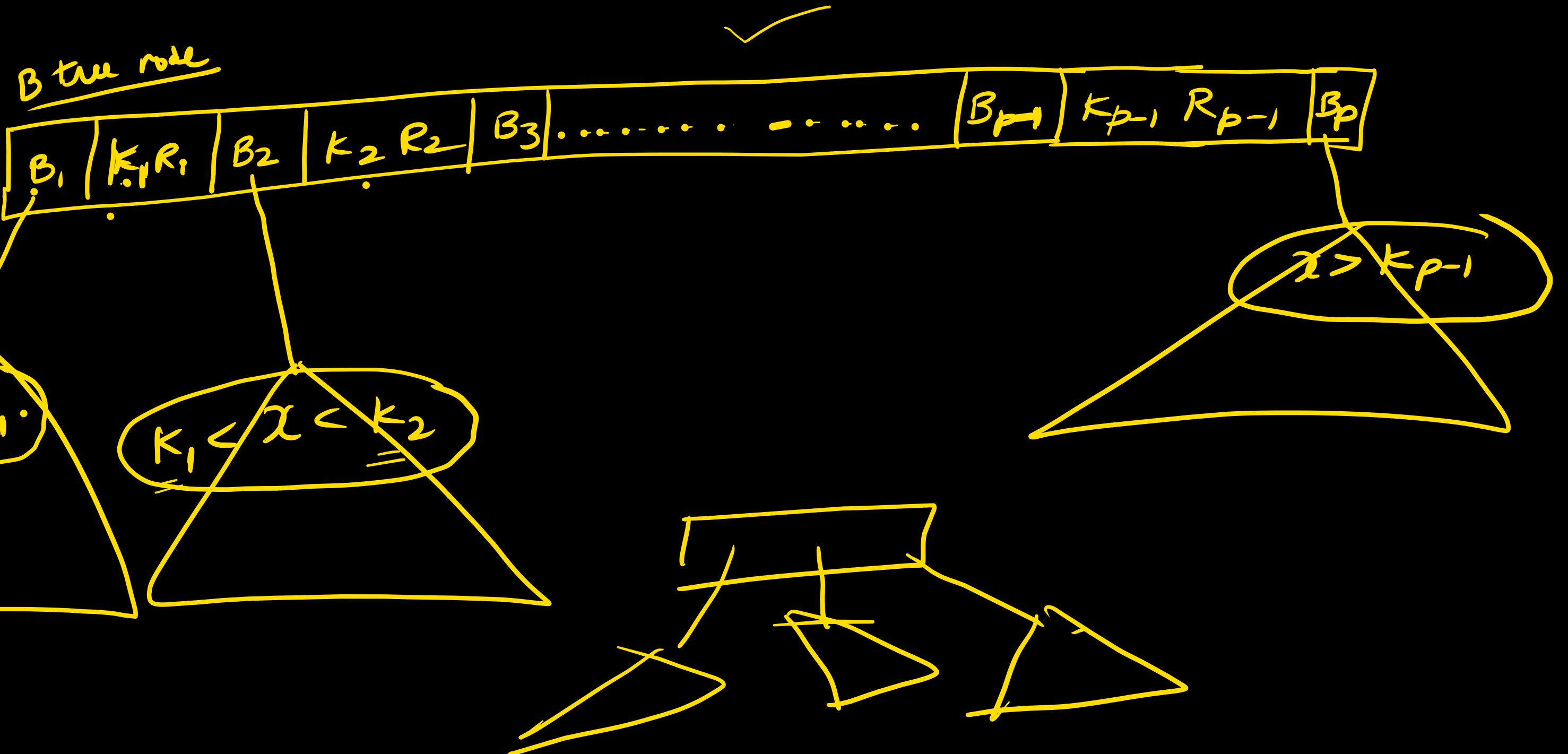
i) node structure: ✓





Yellow arrows are block pointers

Red arrows are read pointers

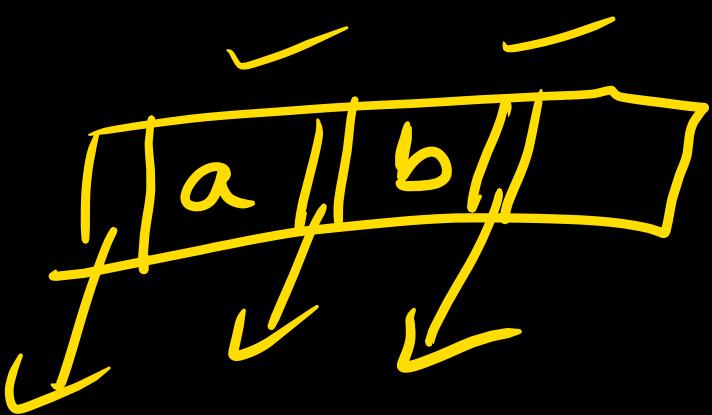


2) Every internal node except Root must be atleast  $\lceil \frac{p}{2} \rceil$   
block pointers with  $\lceil \frac{p}{2} \rceil - 1$  keys.

Assume  $p = 5$

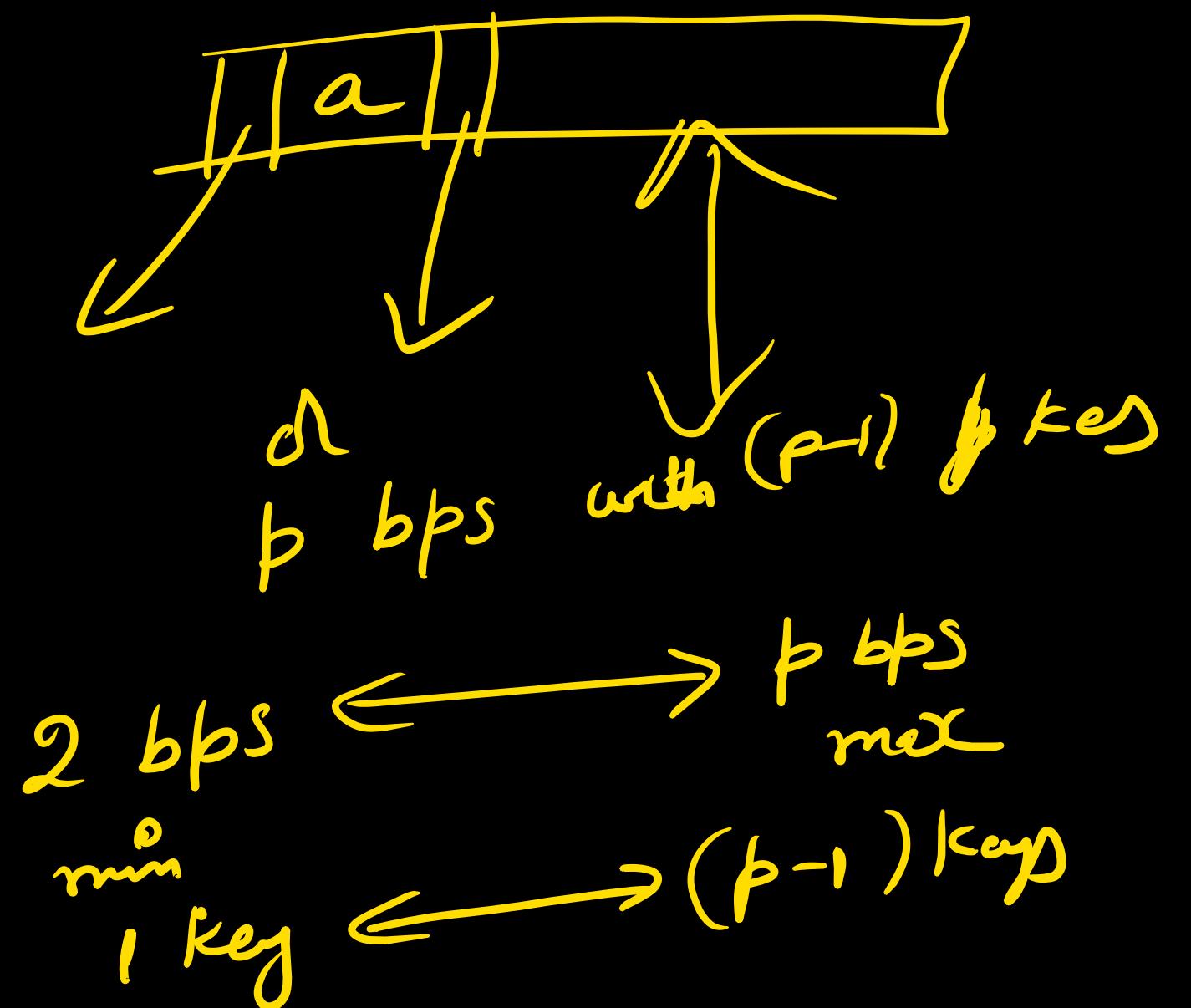
$$\lceil \frac{p}{2} \rceil = \lceil 2.5 \rceil = 3$$

$$\lceil \frac{p}{2} \rceil - 1 = 2$$



Every internal node can have at most 'p' block  
pointers and  $(p-1)$  keys

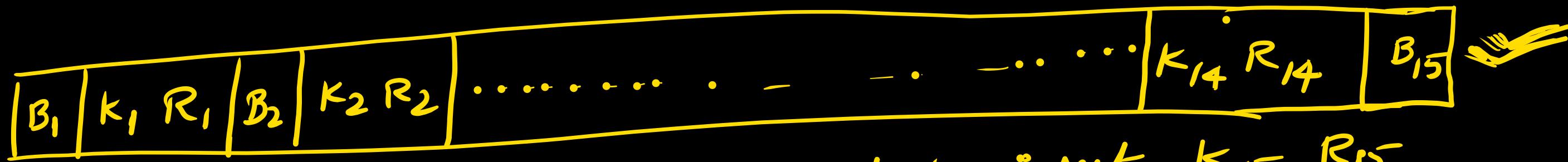
3) Root node can have atleast 2 bps with 1 key  
and atmost  $p$  bps with  $p-1$  keys



4) Every leaf node must be at the same level.

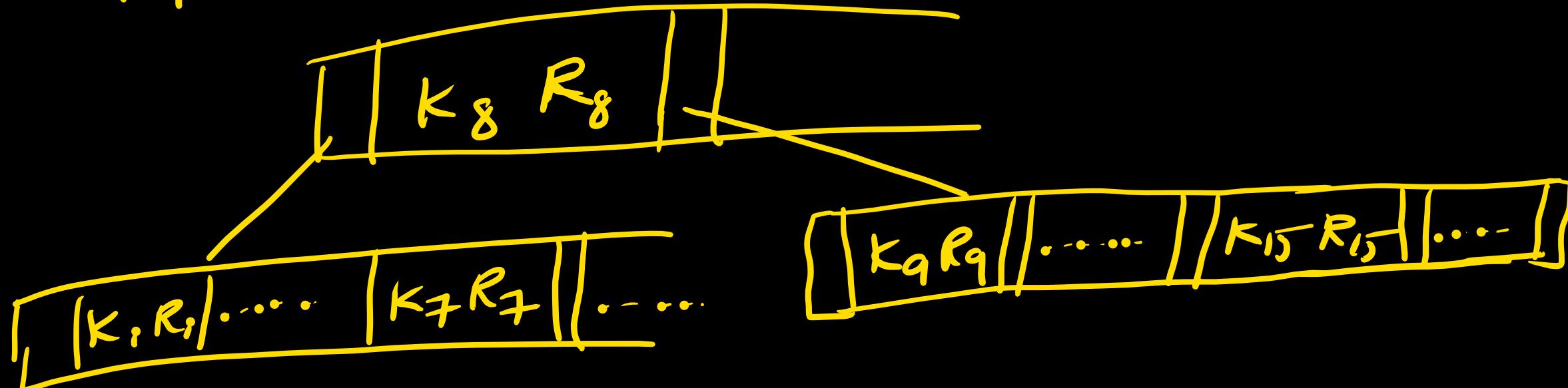
② ③ ④ are called balancing conditions

EC: older P:15 (max bp's = 15)



The node is full. we want to insert  $K_{15} R_{15}$

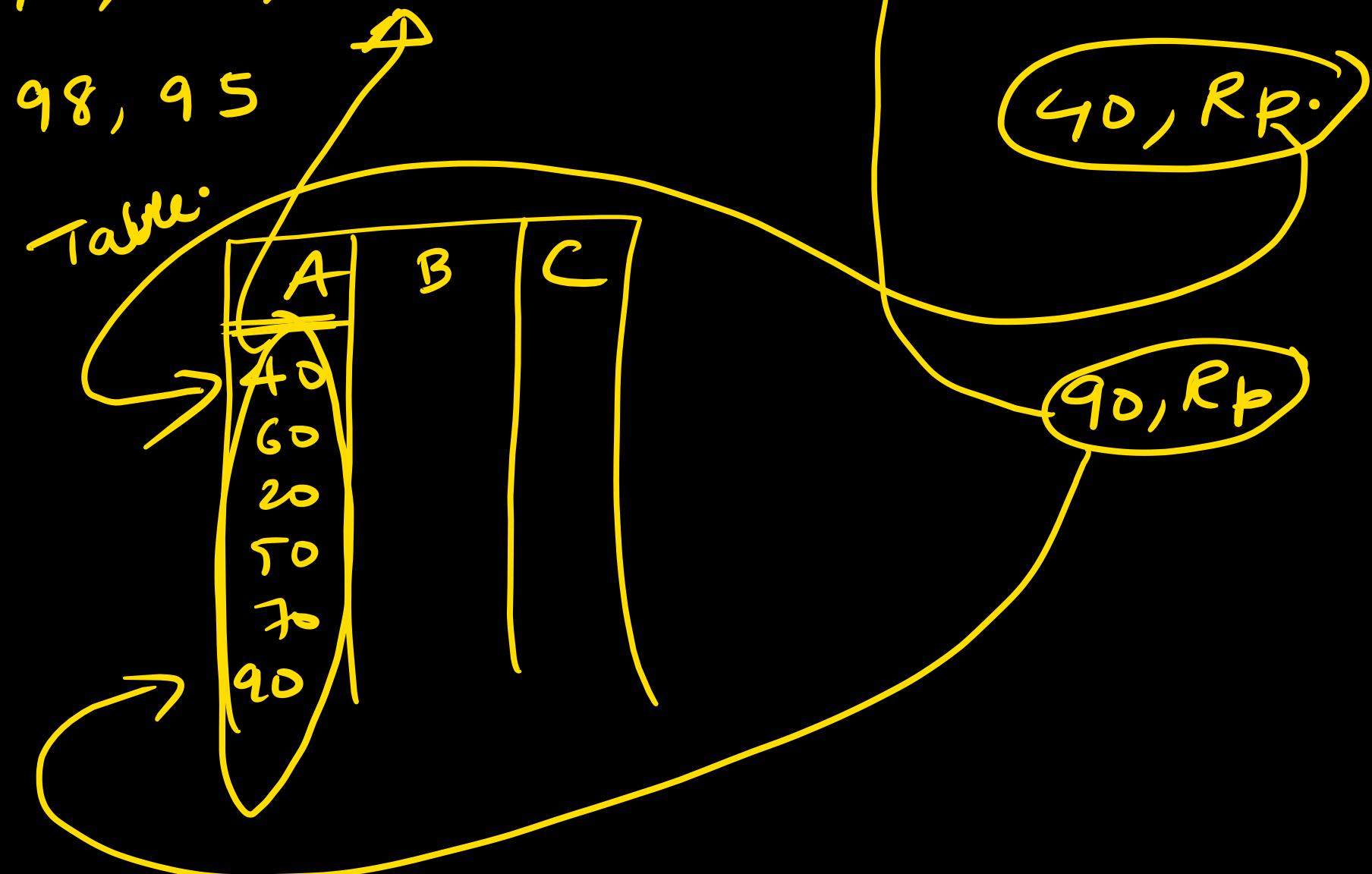
$K_1 < K_2 < K_3 \dots < K_8 < \dots < K_{15}$



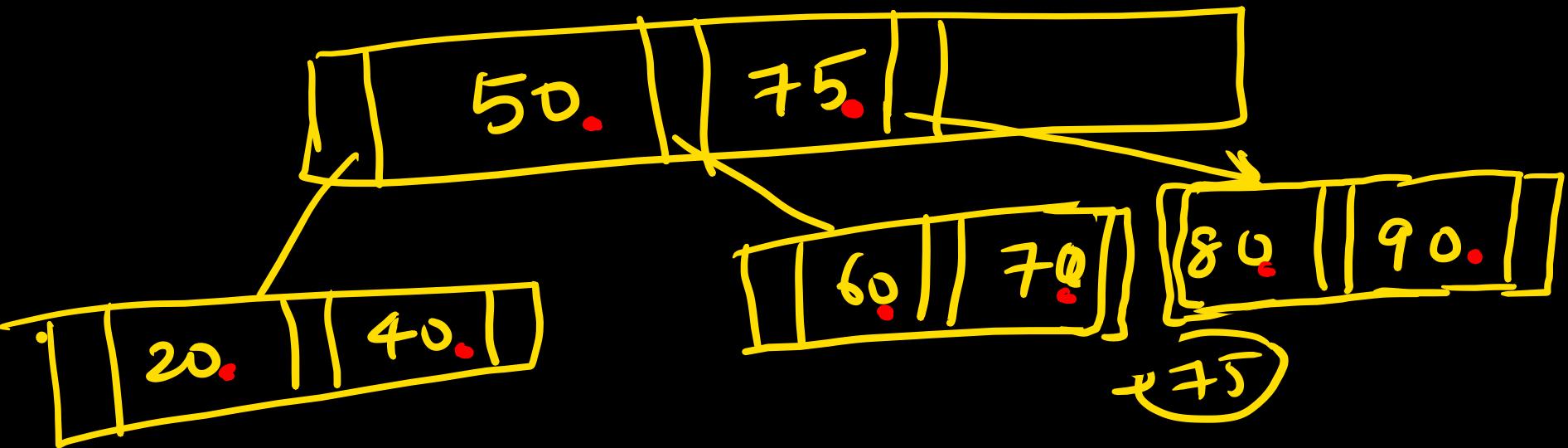
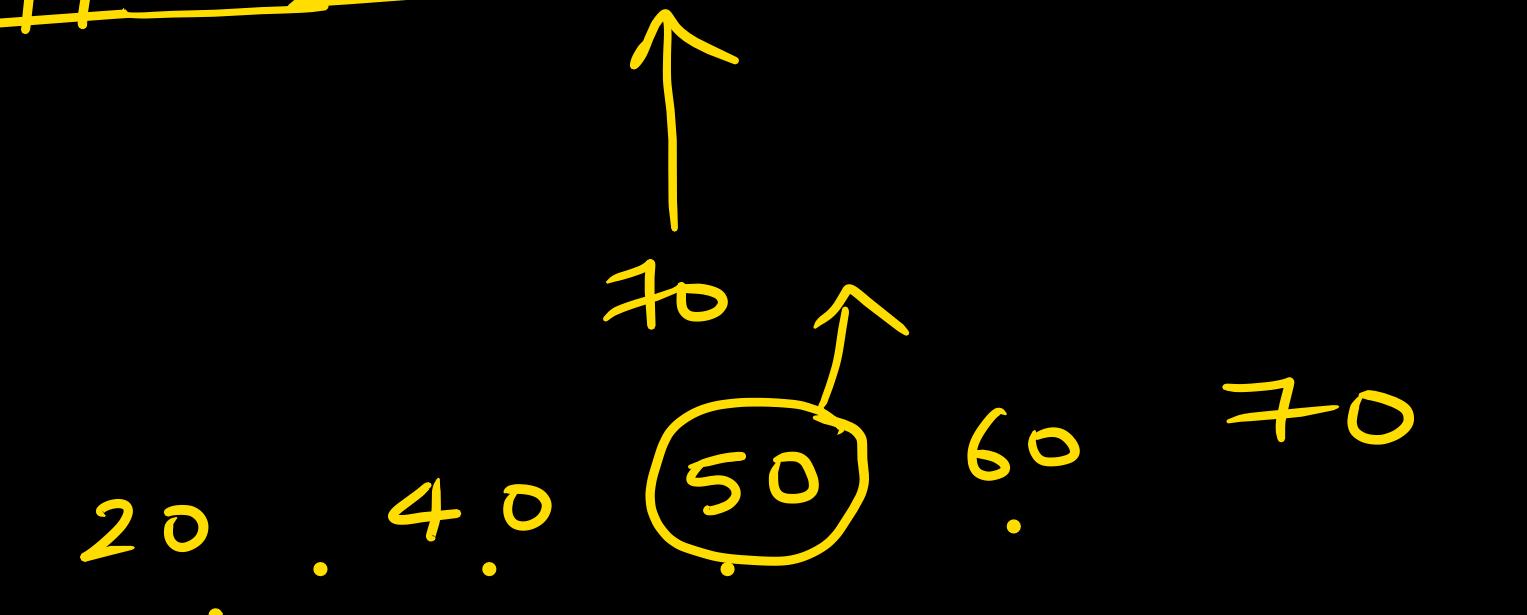
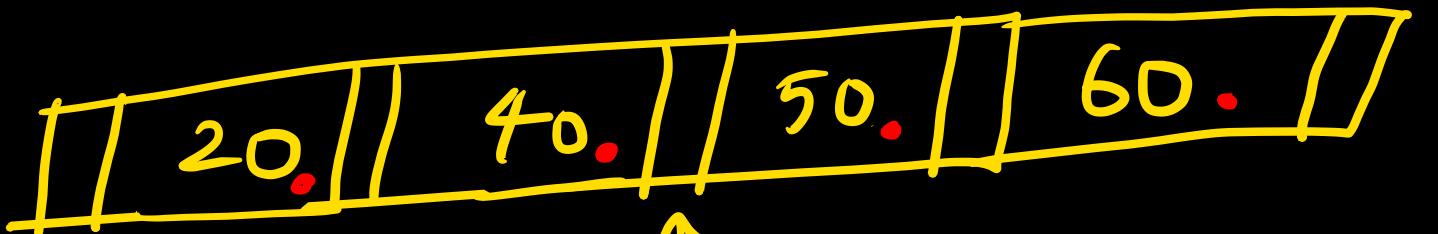
In B trees except Root node , all the nodes are atleast 50% occupied .

Construct a B tree order 5:  $\rightarrow$  (max BPs are 5, max keys = 4)

Keys: 40, 60, 20, 50, 70, 90, 80, 75, 10, 15, 25, 55, 65, 68, 85

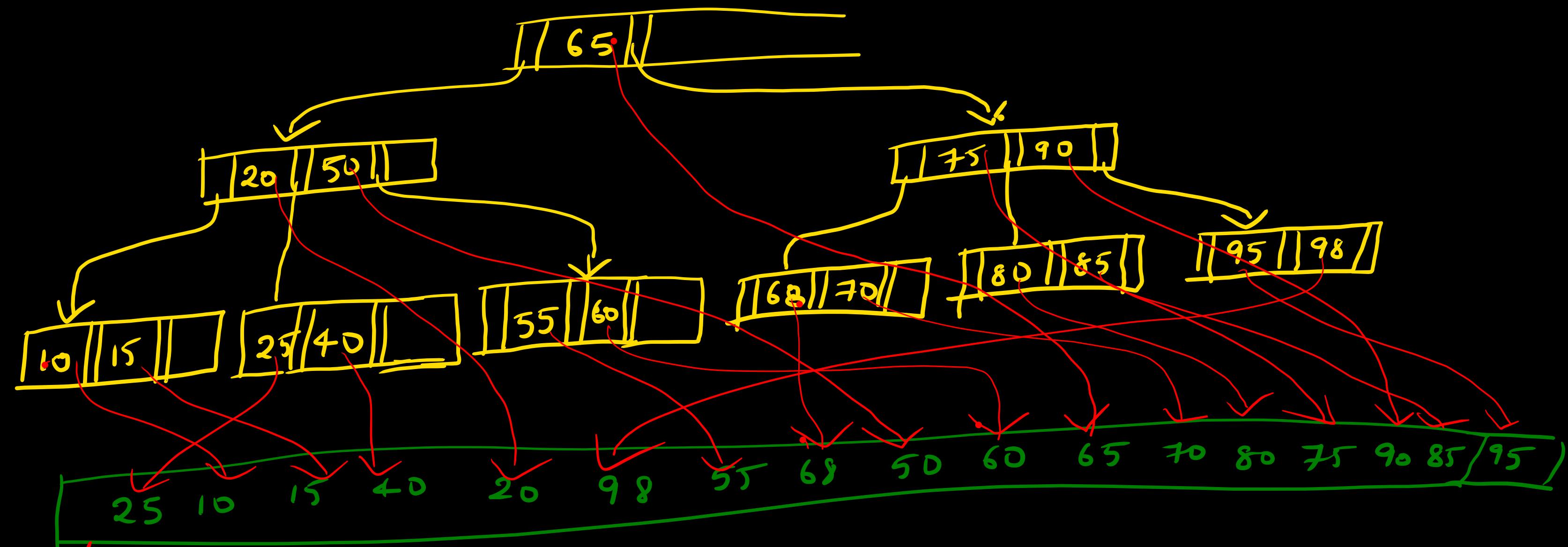


40, 60, 20, 50, 70, 90, 80, 75



60 70 75 80 90

$p \rightarrow 5 \rightarrow$  5.  
kg - 4.



Btree index can be dense & sparse  
 In this example, it is dense

- If the indexing is done on ordered field, then we get sparse index and we need only one key ~~per~~ per block.
- If the indexing is done on un ordered field, then we get dense index. one key per record.

① B trees are suitable for random access of one record

Ex: Select \* from R

where A = 40;

I/O cost :  $K + ①$

/  
levels of B tree

② B tree is not suitable for sequential access of a range queries. Select \* from R where  $A \geq 68$  and  $A \leq 85$

$68 - K+1$

$69 - K+1$

$\vdots$   
 $85 - K+1$

we go for  $B^+$  trees where random access is possible and also  
large queries also possible in less time.

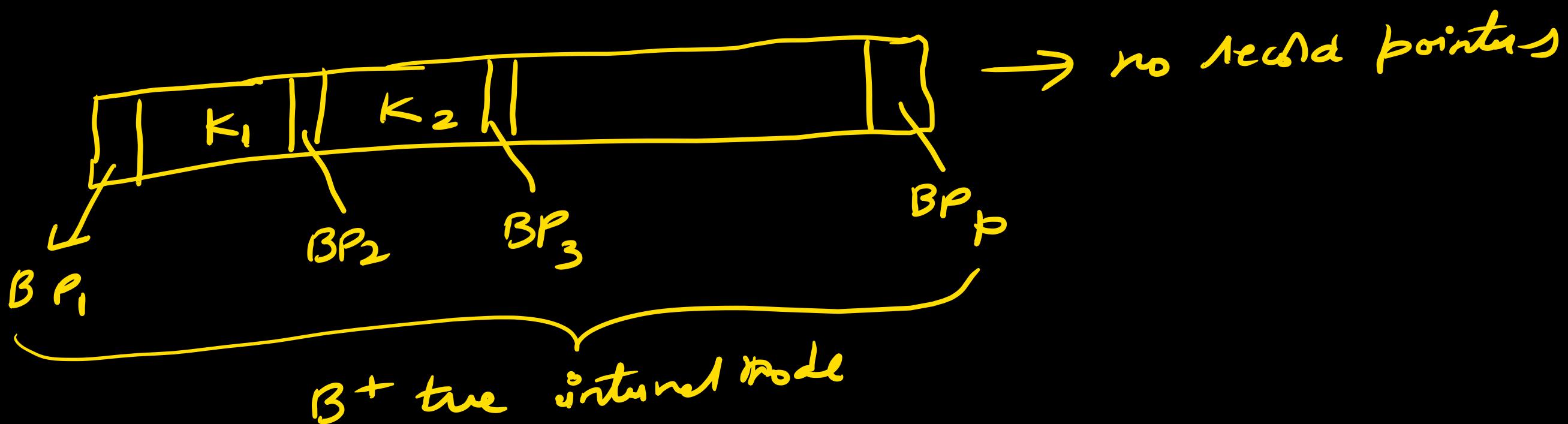
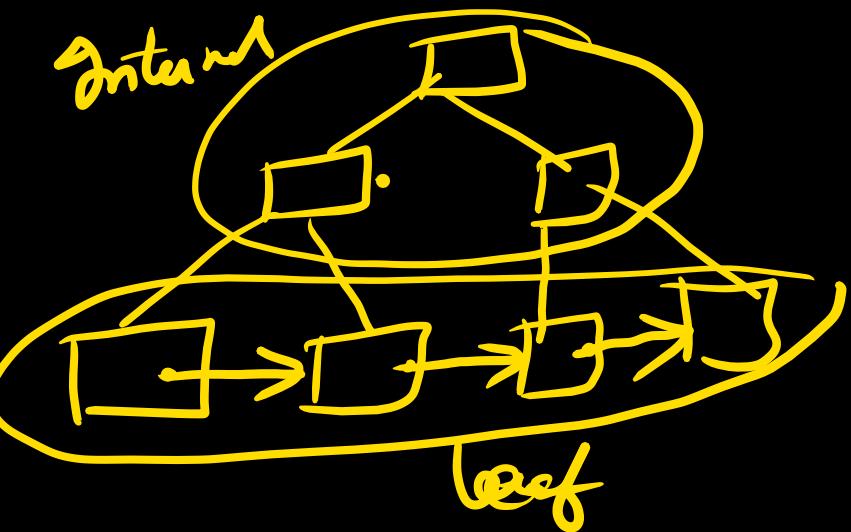
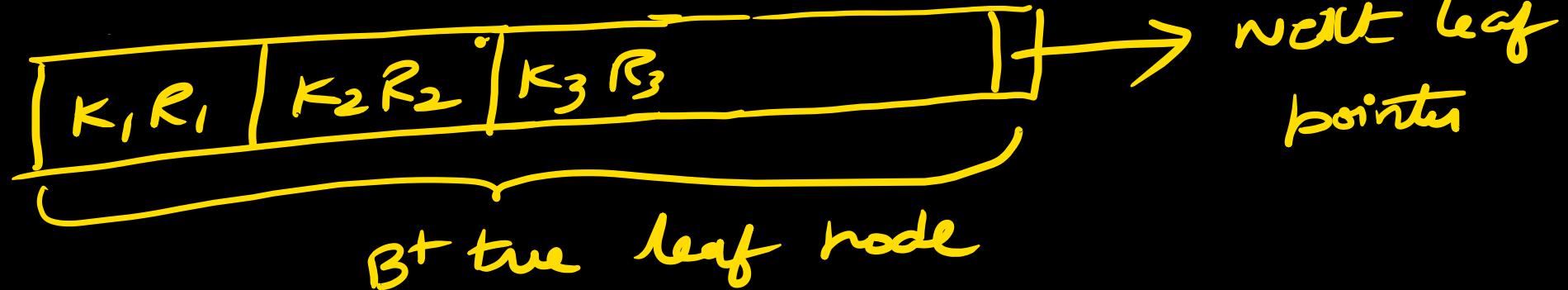
B<sup>+</sup> tree:

what is order P?

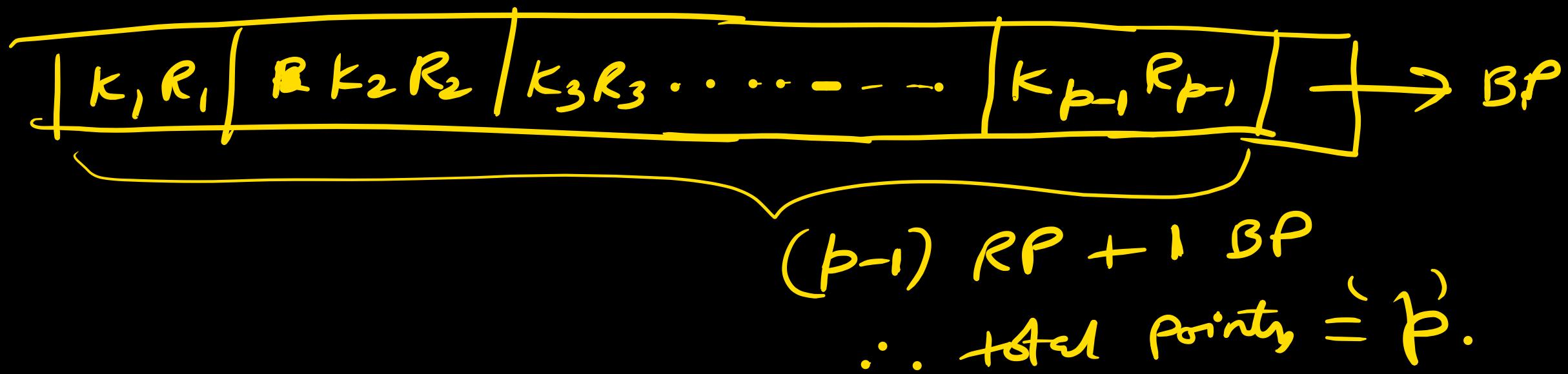
P is maximum possible pointers that can be stored in B<sup>+</sup> tree node.

1)

# 1) node structure



leaf node: Set of  $(\text{key}, R_p)$  pairs and one block pointer  
which points to next leaf.



Internal nodes:

only keys and block pointers

