

## BST - Add Node

**//1. create a newnode with given data**

**//2. if tree is empty**

**// add newnode into root itself**

**//3. if tree is not empty**

**//3.1 create trav pointer and start at root**

**//3.2 if value is less than current node data**

**//3.2.1 if left of current node is empty**

**// add newnode into left of current node**

**//3.2.2 if left of current node is not empty**

**// go to left of current node**

**//3.3 if value is greater than current node data**

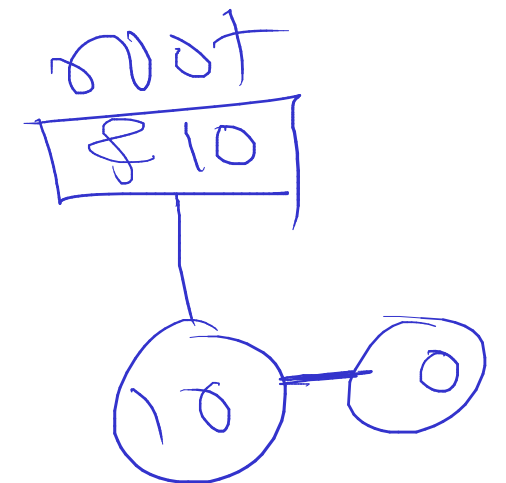
**//3.3.1 if right of current node is empty**

**// add newnode into right of current node**

**//3.3.2 if right of current node is not empty**

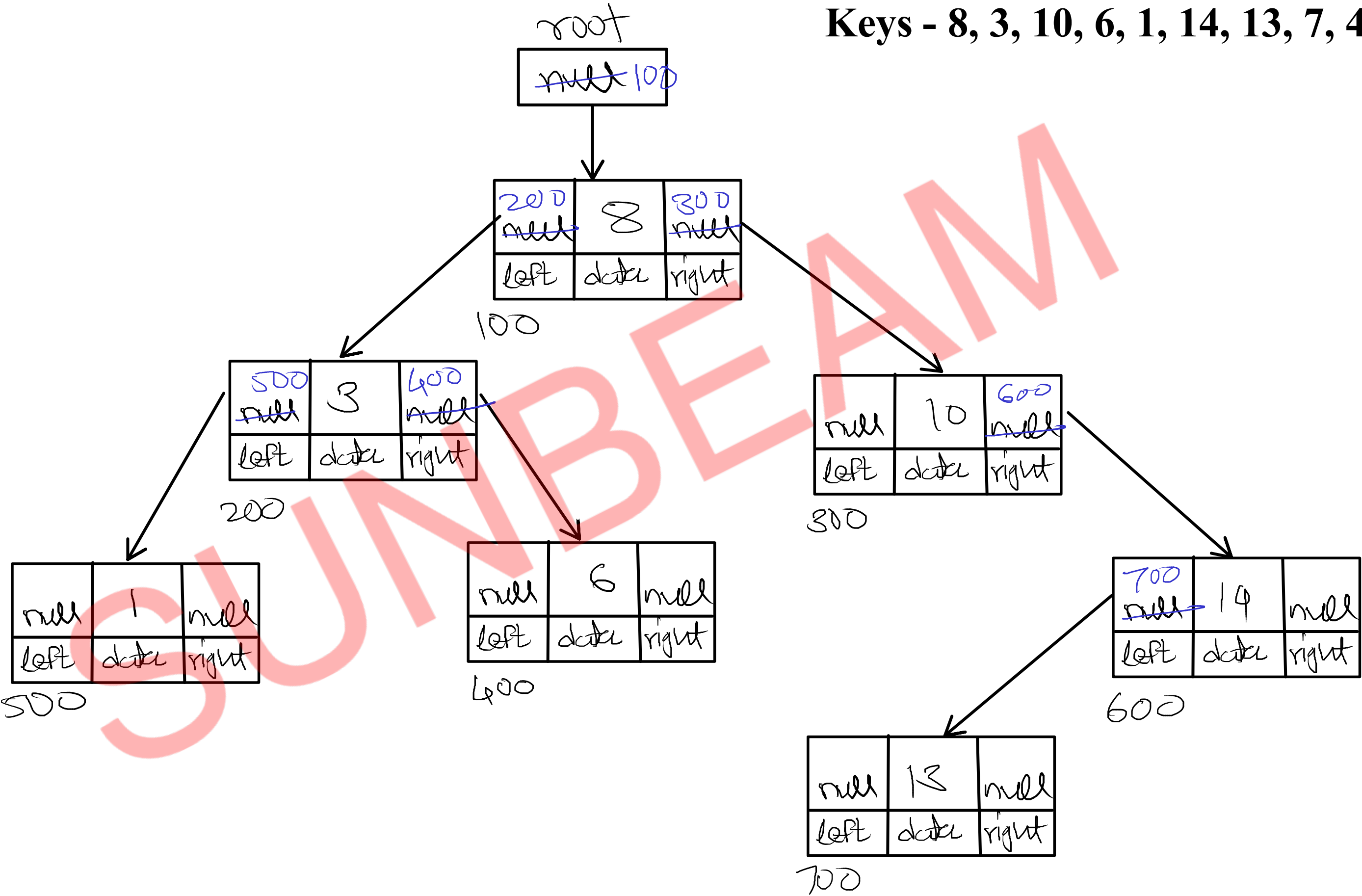
**// go to right of current node**

**//3.4 repeat step 3.2 and 3.3 till node is not added into BST**

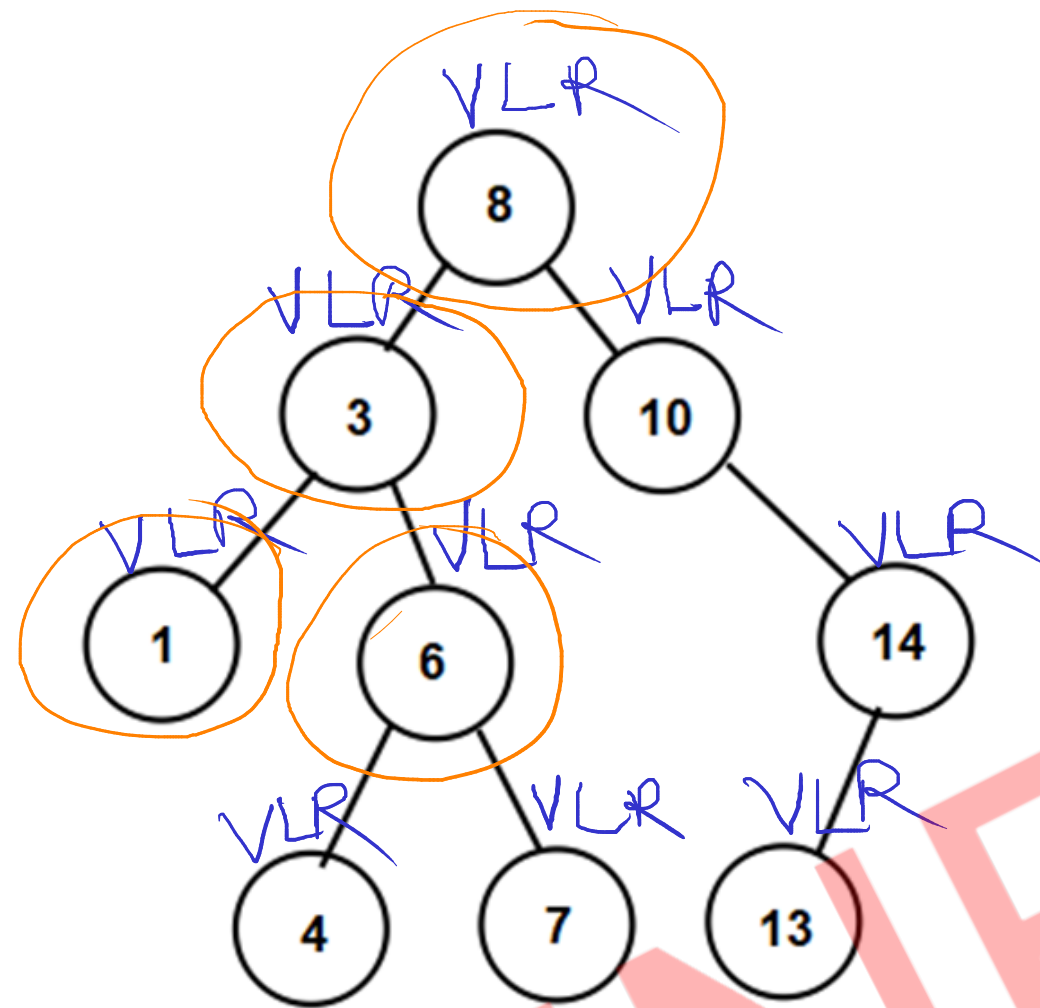


BST - Add Node

Keys - 8, 3, 10, 6, 1, 14, 13, 7, 4



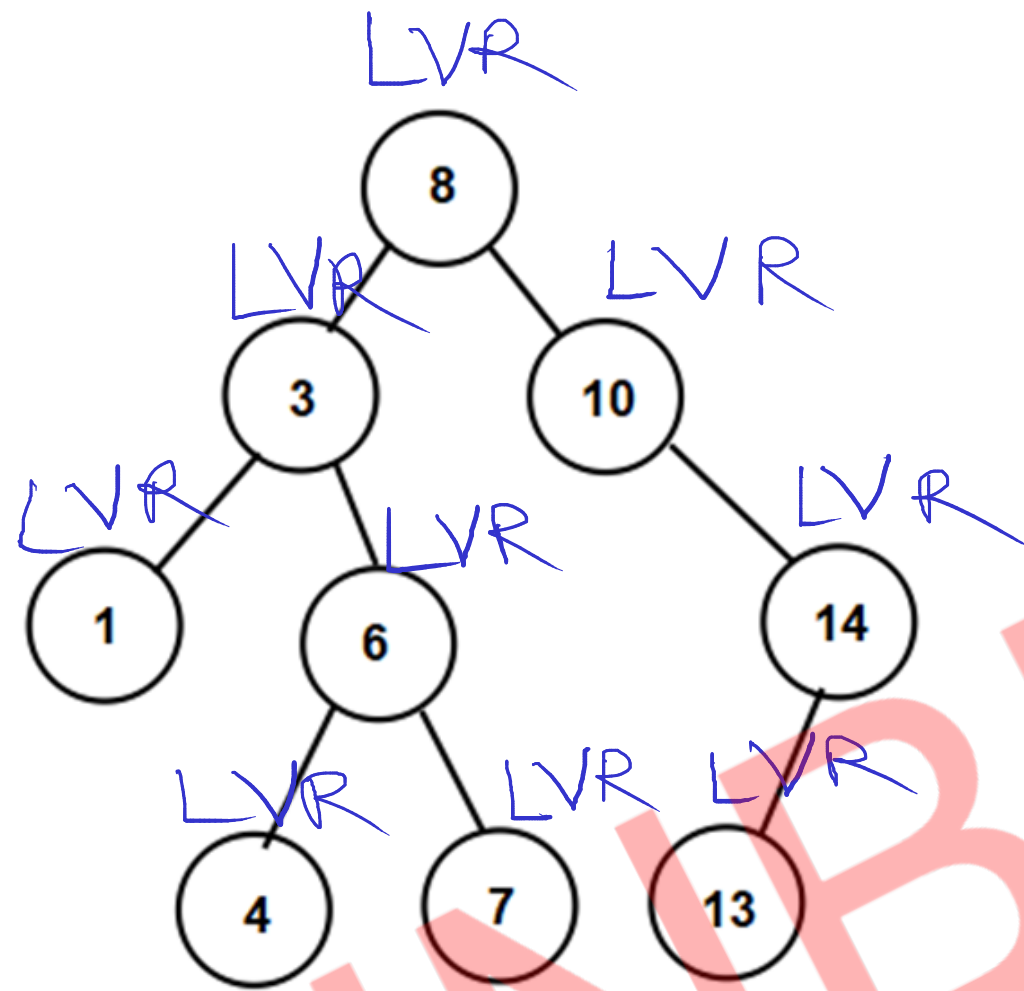
## BST - Preorder Traversal



VLR

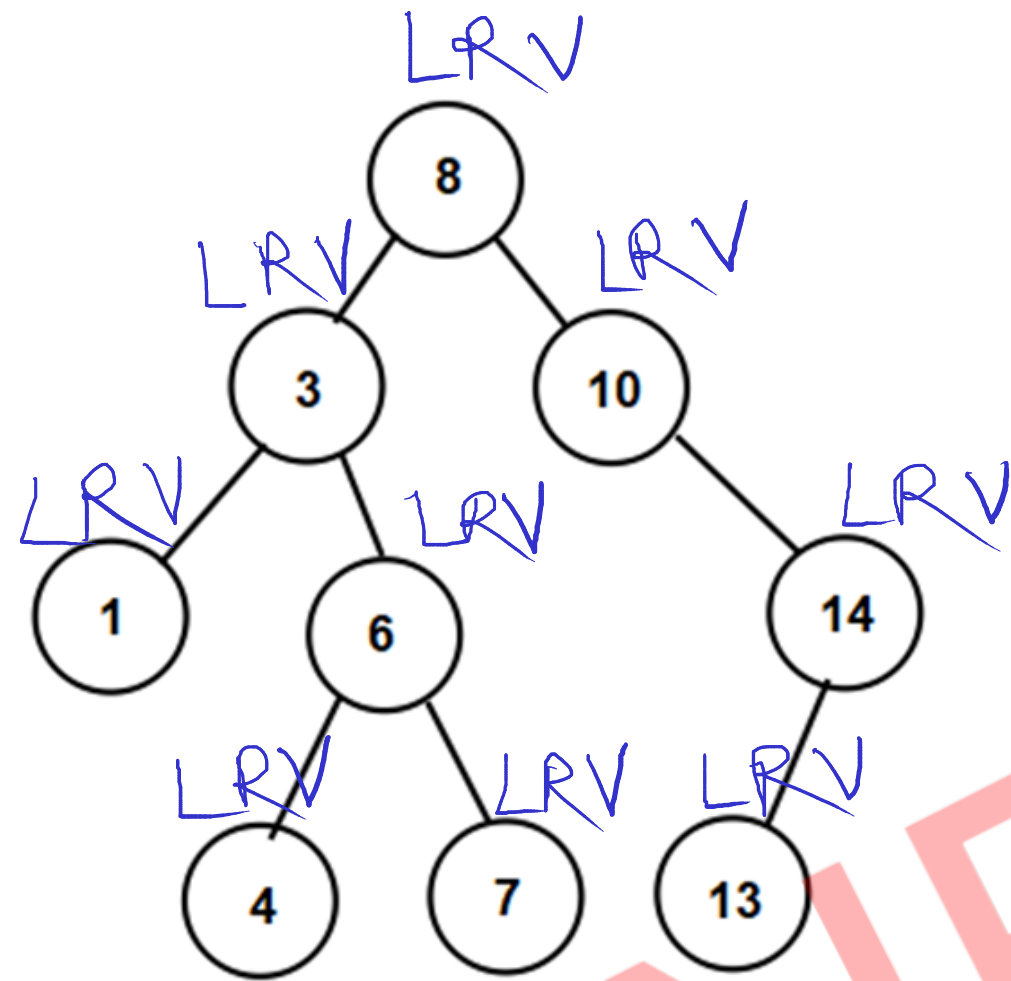
Traversal: 8, 3, 1, 6, 4, 7, 10, 14, 13

## BST - Inorder Traversal



Traversal: 1, 3, 4, 6, 7, 8, 10, 13, 14

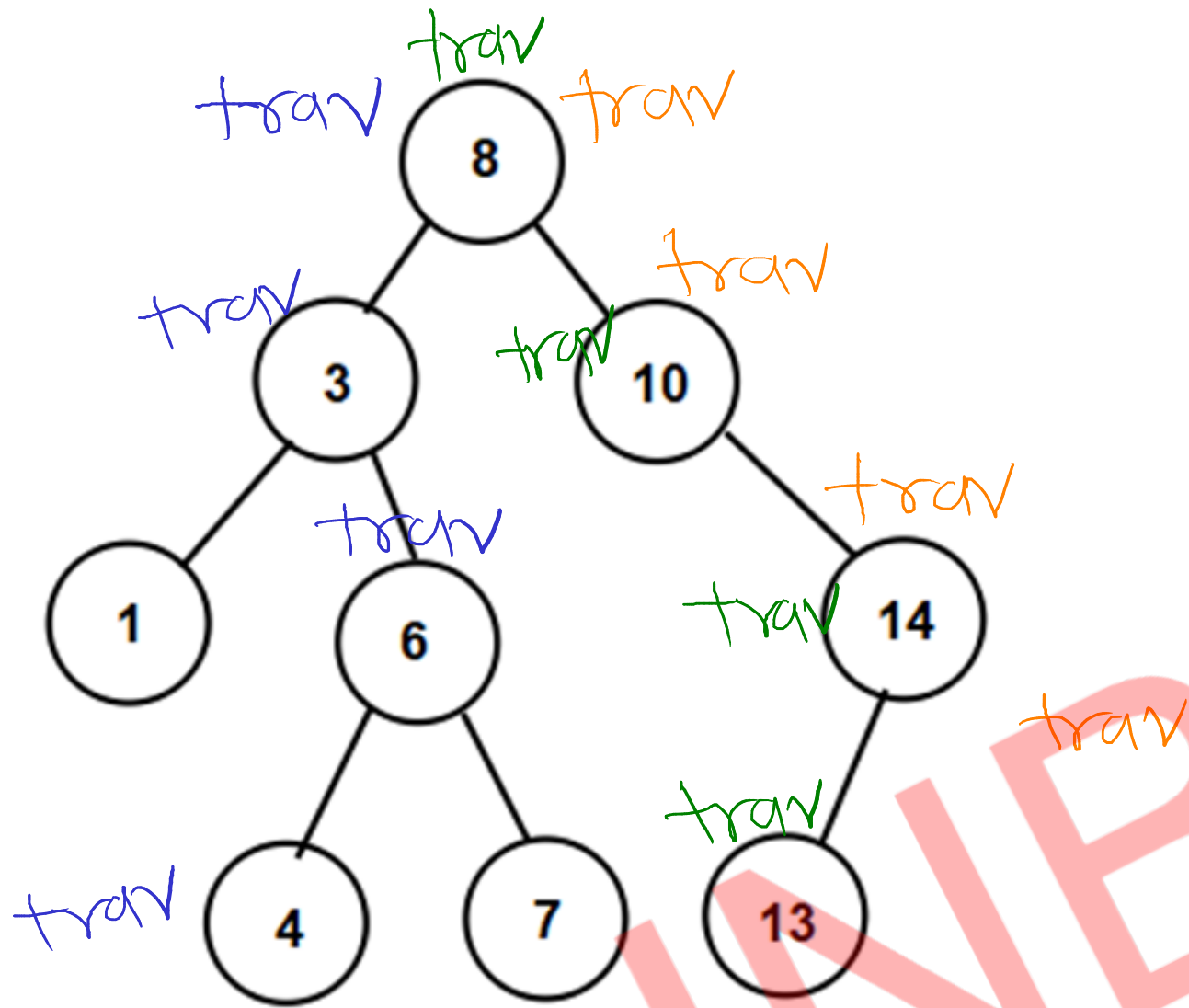
## BST - Postorder Traversal



LRV

Traversal: 1, 4, 7, 6, 3, 13, 14, 10, 8

## BST - Binary Search



//1. start from root

//2. if key is equal to current data

//return current node

//3. if key is less than current data

// search key into left of current node

//4. if key is greater than current data

// search key into right of current node

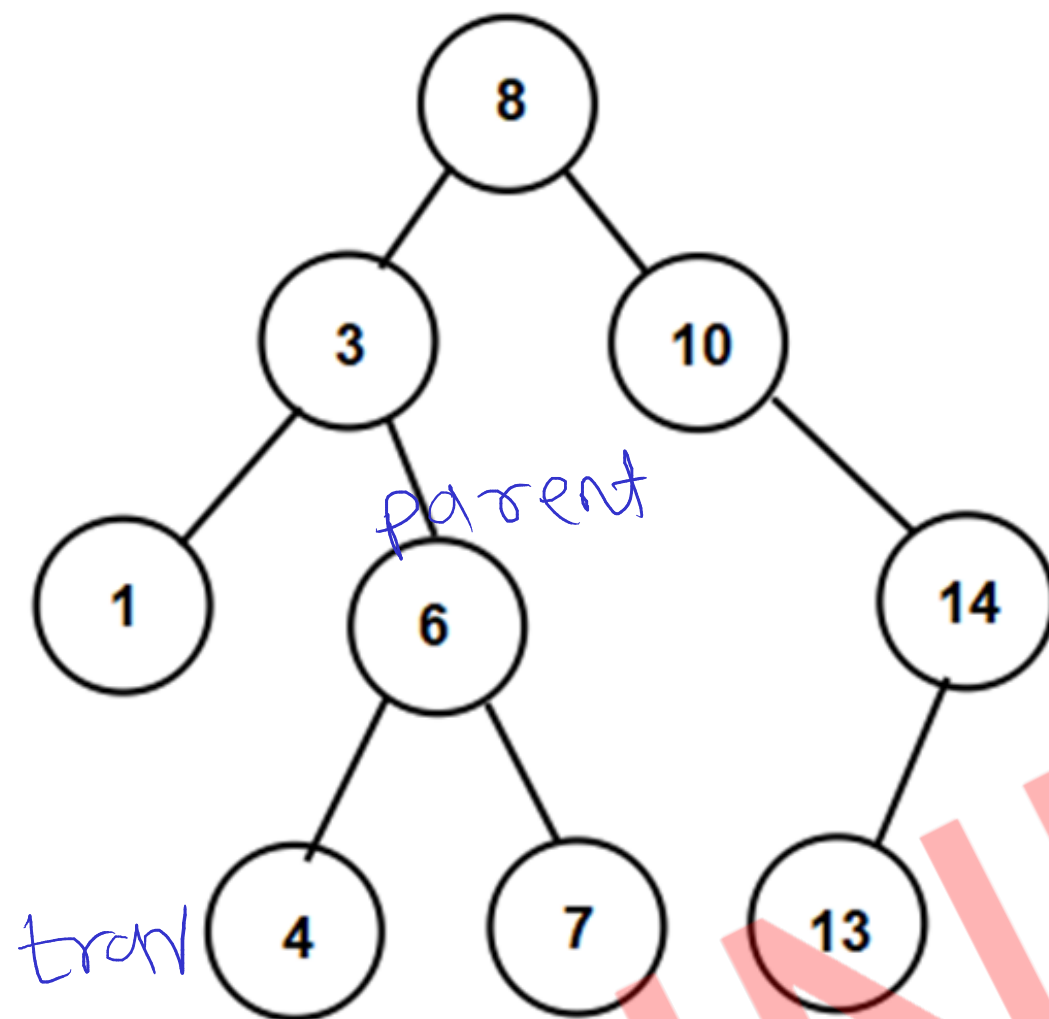
//5. repeat step 2 to 4 till leaf nodes

Key = 4 — key found

Key = 15 — Key not found

Key = 13 — key found

## BST - Binary Search with Parent



key = 4

trav	parent
8	null
3	8
6	3
4	6

key = 15

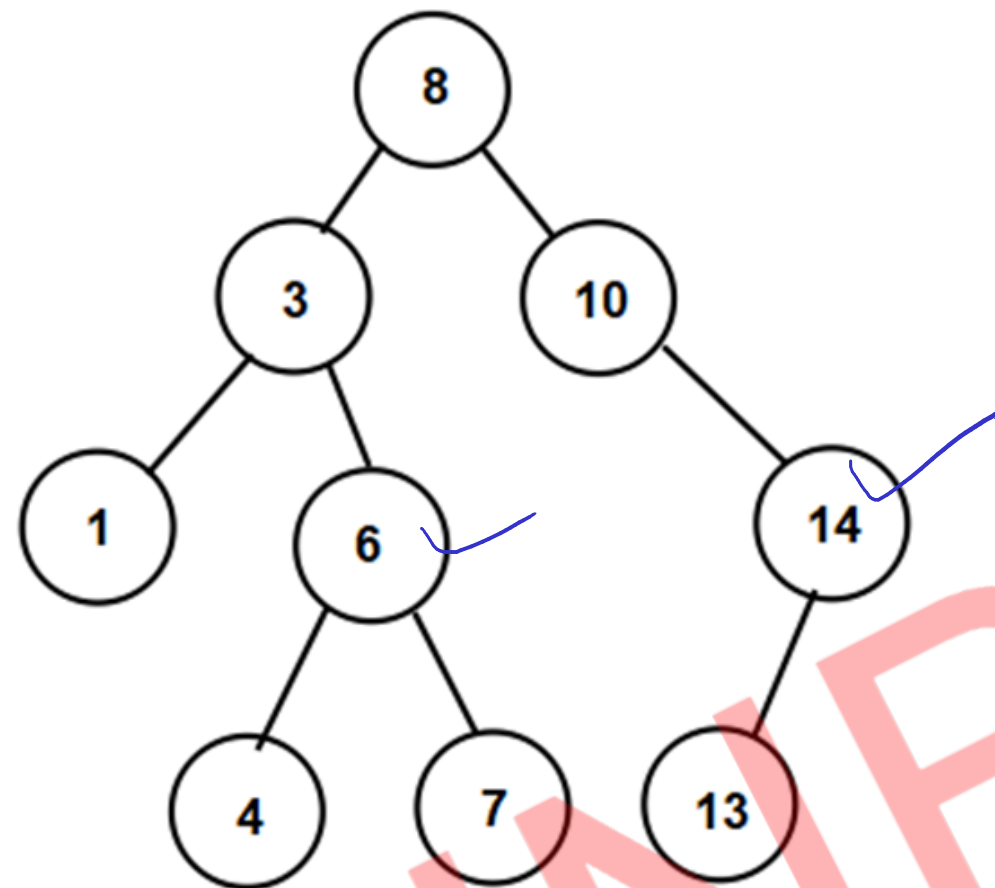
trav	parent
8	null
10	8
14	10
null	14

key = 8

trav	parent
8	null



## BST - Delete Node



Parents left      Parents right      root

Node

Non leaf

leaf

single child

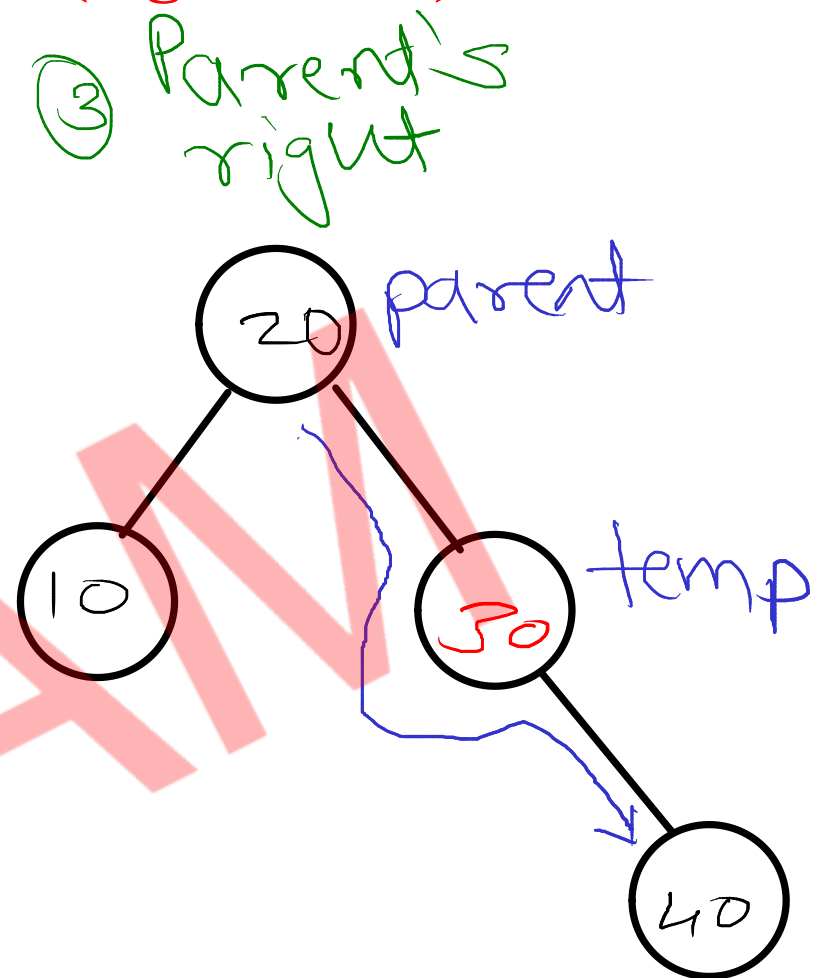
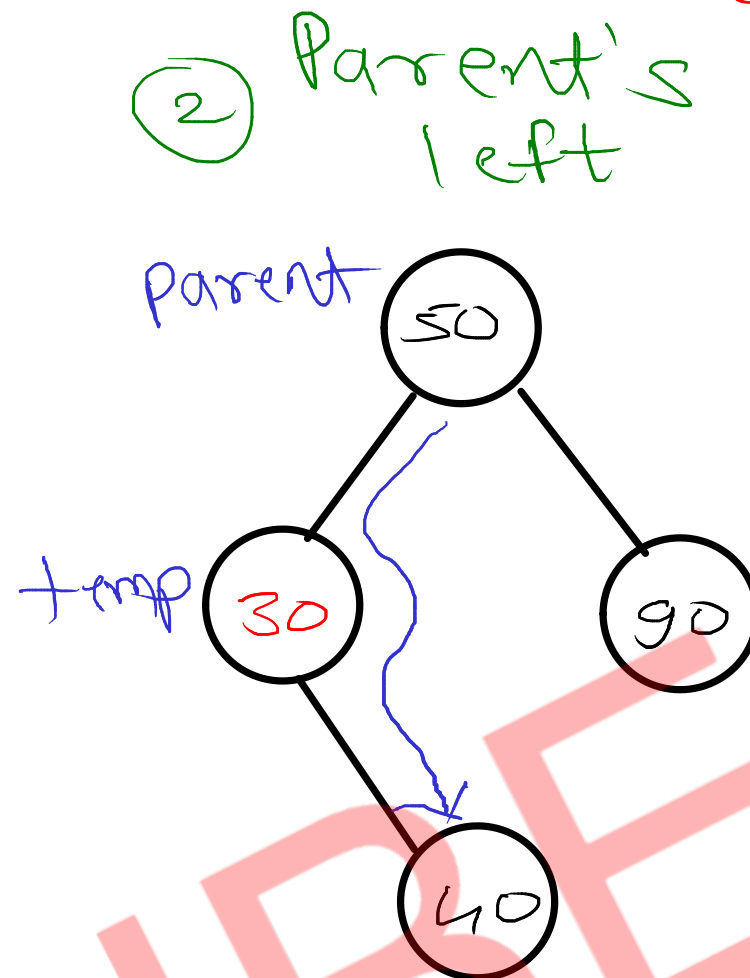
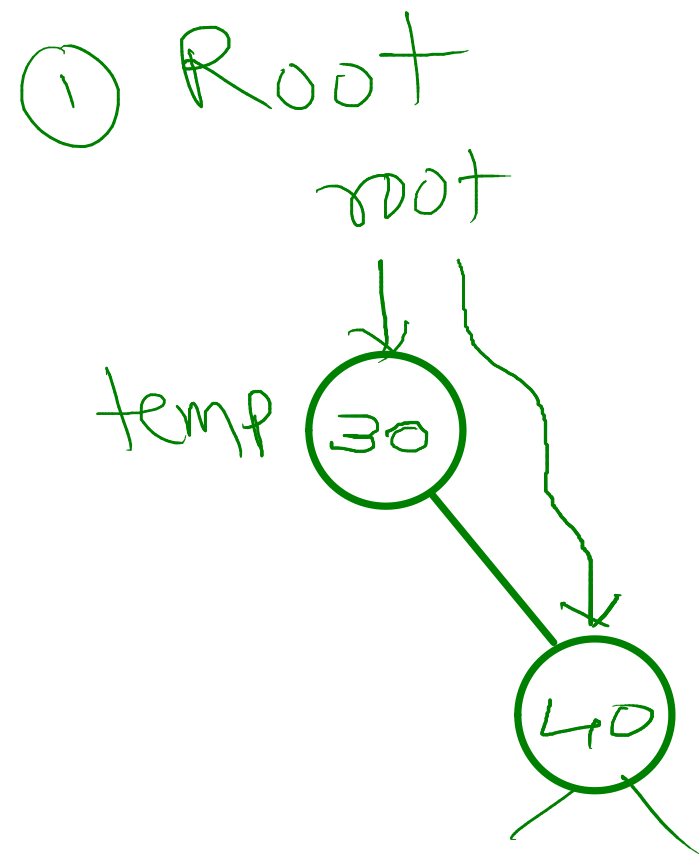
two child

left child

right child



## BST - Delete node which has single child (right child)



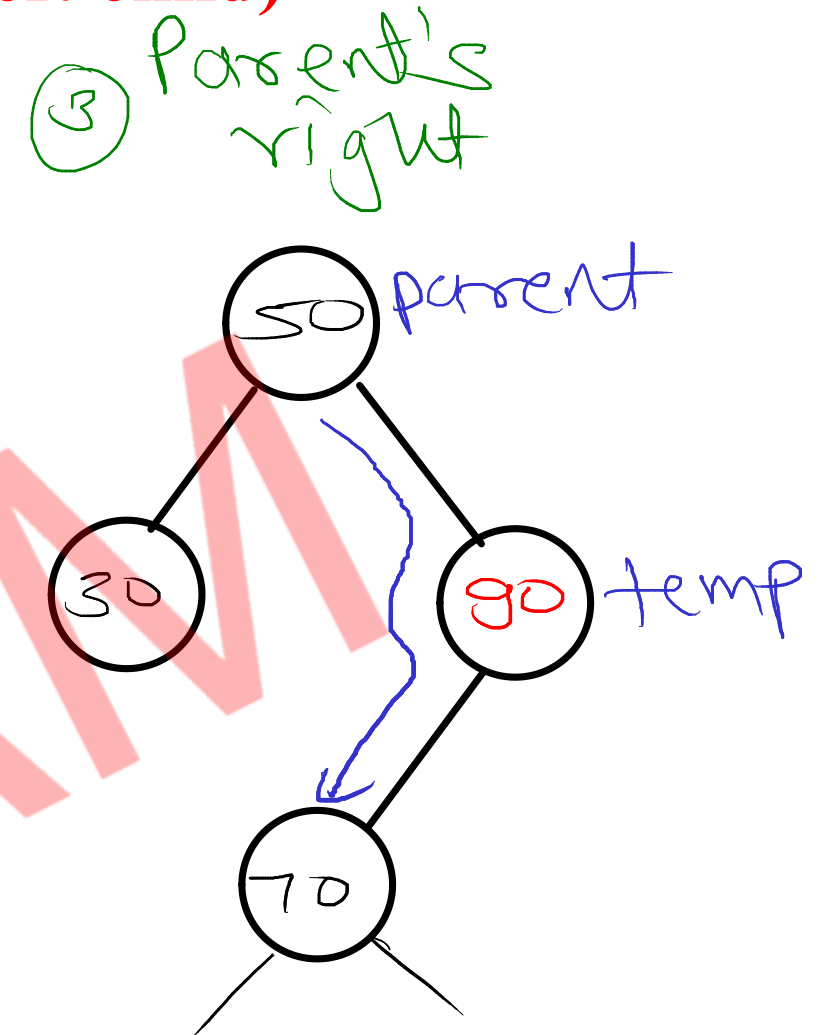
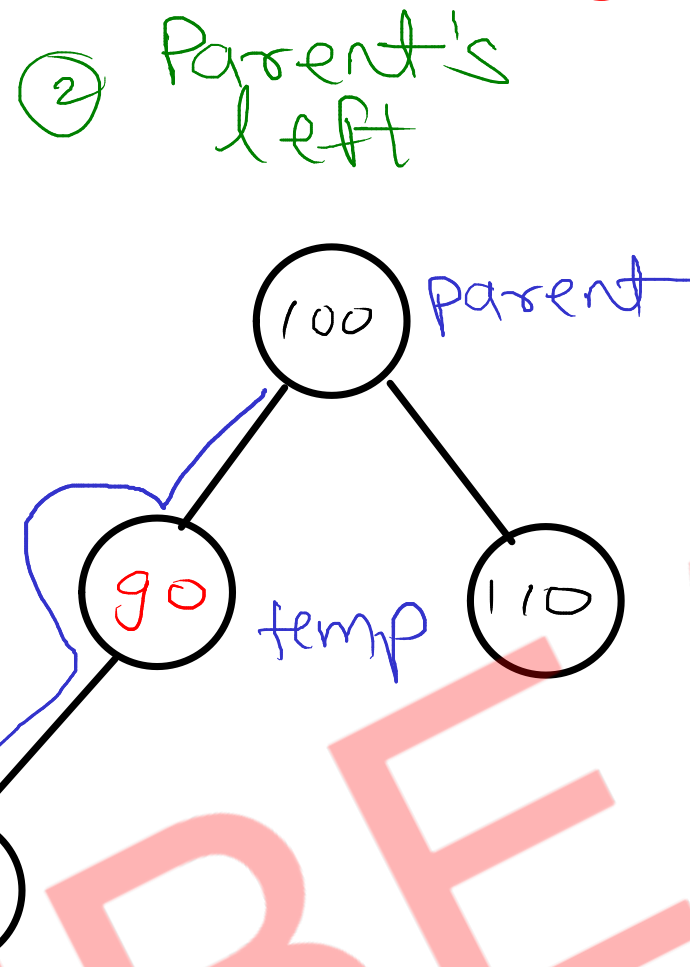
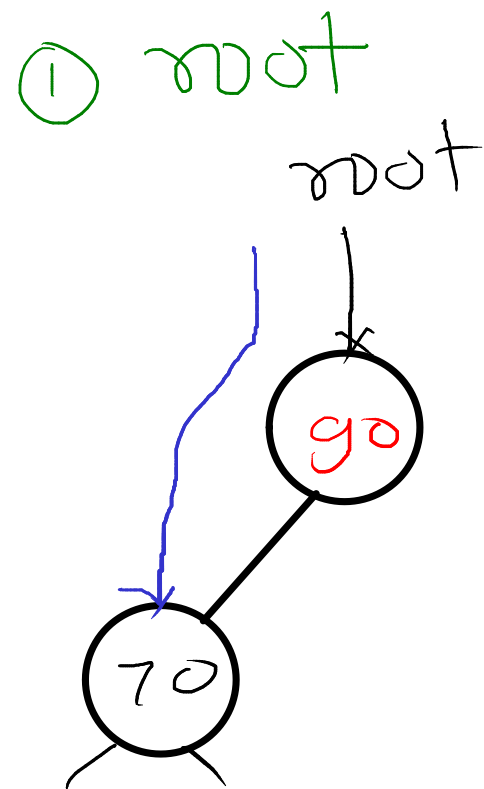
```
if(temp.left == null){  
  if(temp == root)  
    ① root = temp.right;  
  else if(temp == parent.left)  
    ② parent.left = temp.right;  
  else if(temp == parent.right)  
    ③ parent.right = temp.right;  
}
```

→ single child (left missing)  
→ not node

→ parent's left child

→ parent's right child

## BST - Delete node which has single child (left child)



```
if(temp.right == null){  
  if(temp == root)  
    ① root = temp.left;  
  else if(temp == parent.left)  
    ② parent.left = temp.left;  
  else if(temp == parent.right)  
    ③ parent.right = temp.left;  
}
```

→ single child (right missing)  
→ root node

→ parent's left child

→ parent's right child

parent

## BST - Delete node which has two childs

```
if(temp.left != null && temp.right != null){
```

```
//1. find predecessor of temp.data
```

```
Node pred = temp.left;
```

```
parent = temp;
```

```
while(pred.right != null){
```

```
    parent = pred;
```

```
    pred = pred.right
```

```
}
```

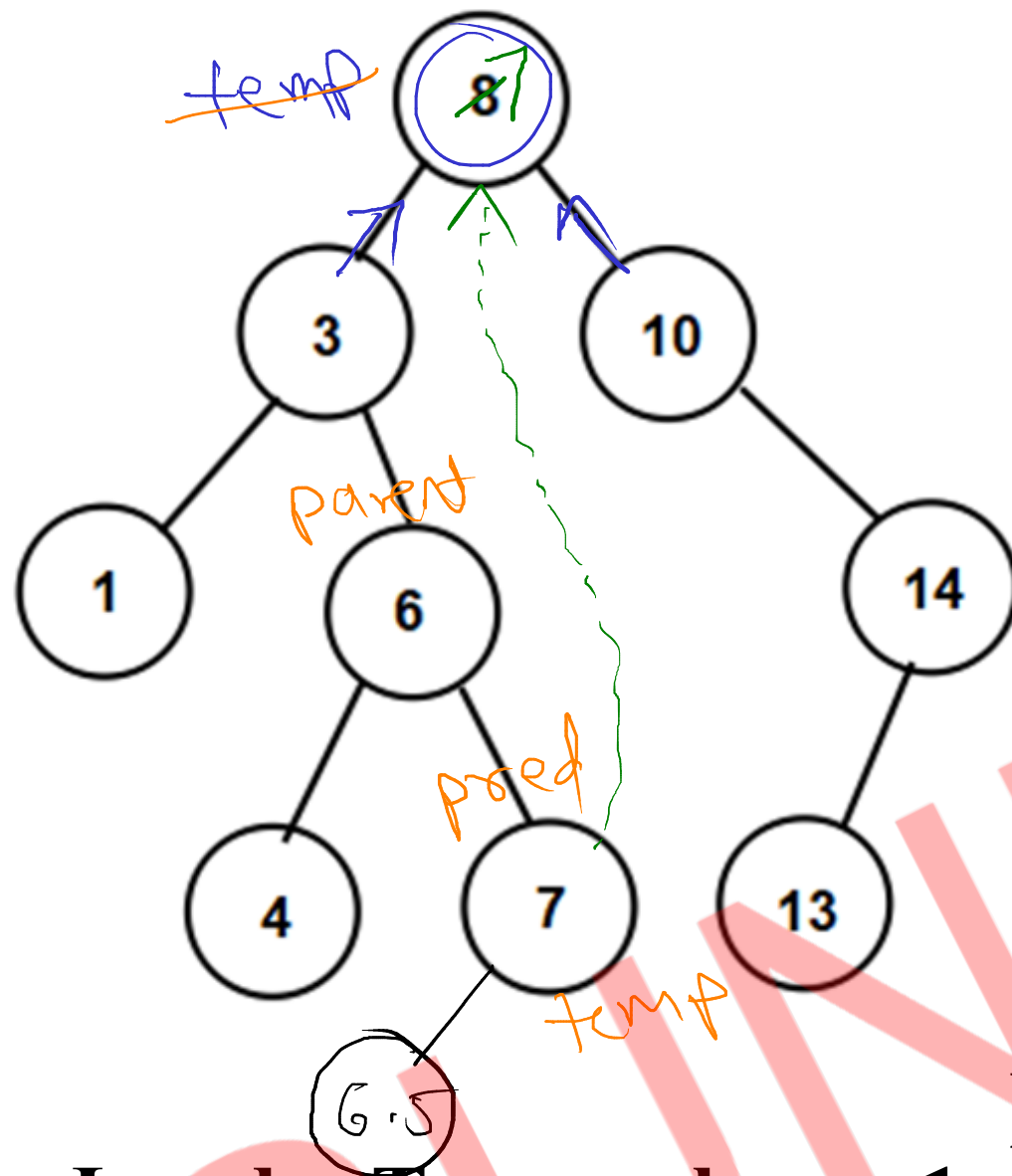
```
//2. replace temp's data by predecessor's data
```

```
temp.data = pred.data;
```

```
//3. delete predecessor
```

```
temp = pred;
```

```
}
```



Inorder Traversal :

1 3 4 6 7 8 10 13 14

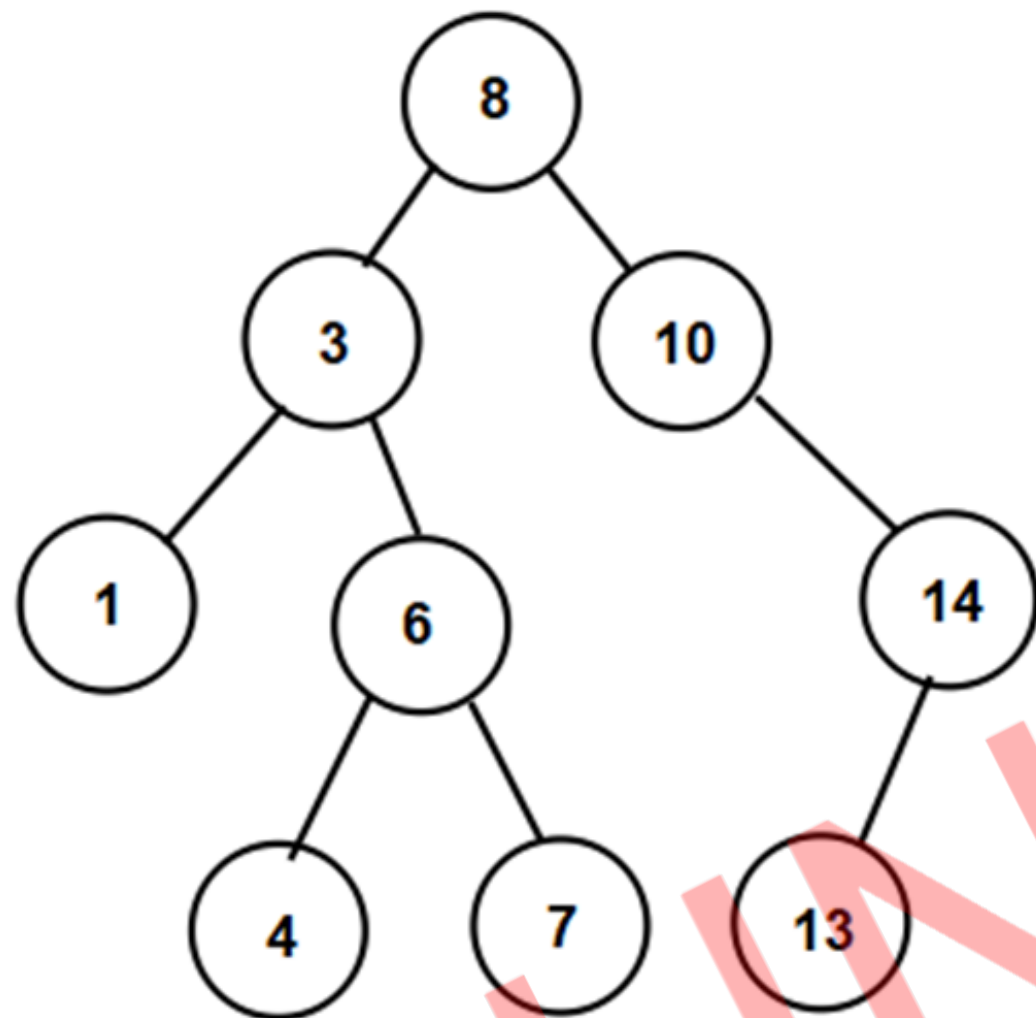
inorder  
predecessor

inorder  
successor

left  
extreme right

right  
extreme left

## BST - DFS (Depth First Search)



stack

<del>13</del>
<del>14</del>
<del>4</del>
<del>7</del>
<del>1</del>
<del>6</del>
<del>3</del>
<del>10</del>
<del>8</del>

//1. push root on stack

//2. pop one node from stack

//3. visit(print) node

//4. if right exist, push it on stack

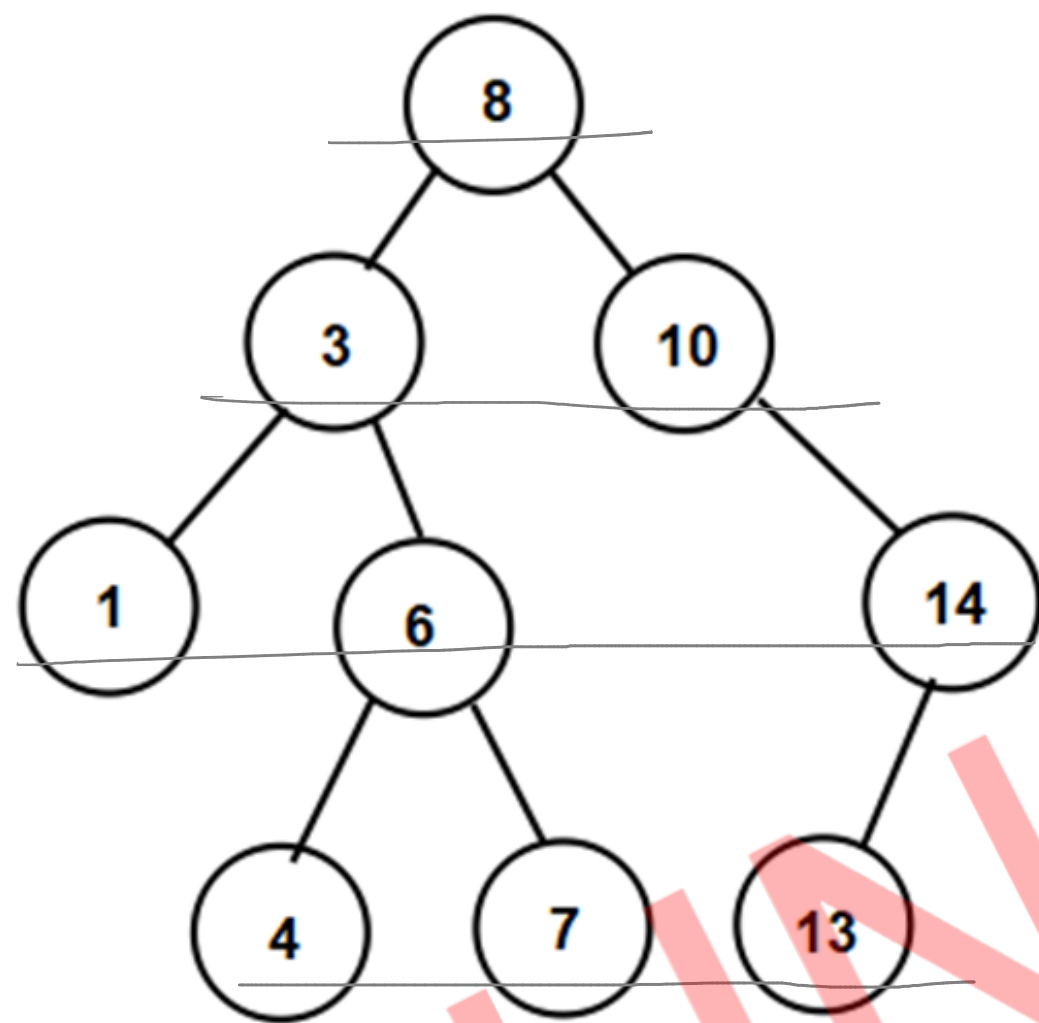
//5. if left exist, push it on stack

//6. while stack is not empty

//repeat ste 2 to 5

Traversal : 8, 3, 1, 6, 4, 7, 10, 14, 13

## BST - BFS (Bredth First Search)



Queue

<del>13</del>
<del>7</del>
<del>4</del>
<del>14</del>
<del>6</del>
<del>1</del>
<del>10</del>
<del>3</del>
<del>8</del>

//1. push root on queue

//2. pop one **node** from queue

//3. visit(**print**) **node**

//4. if left exist, push it on queue

//5. if right exist, push it on queue

//6. while queue is not empty

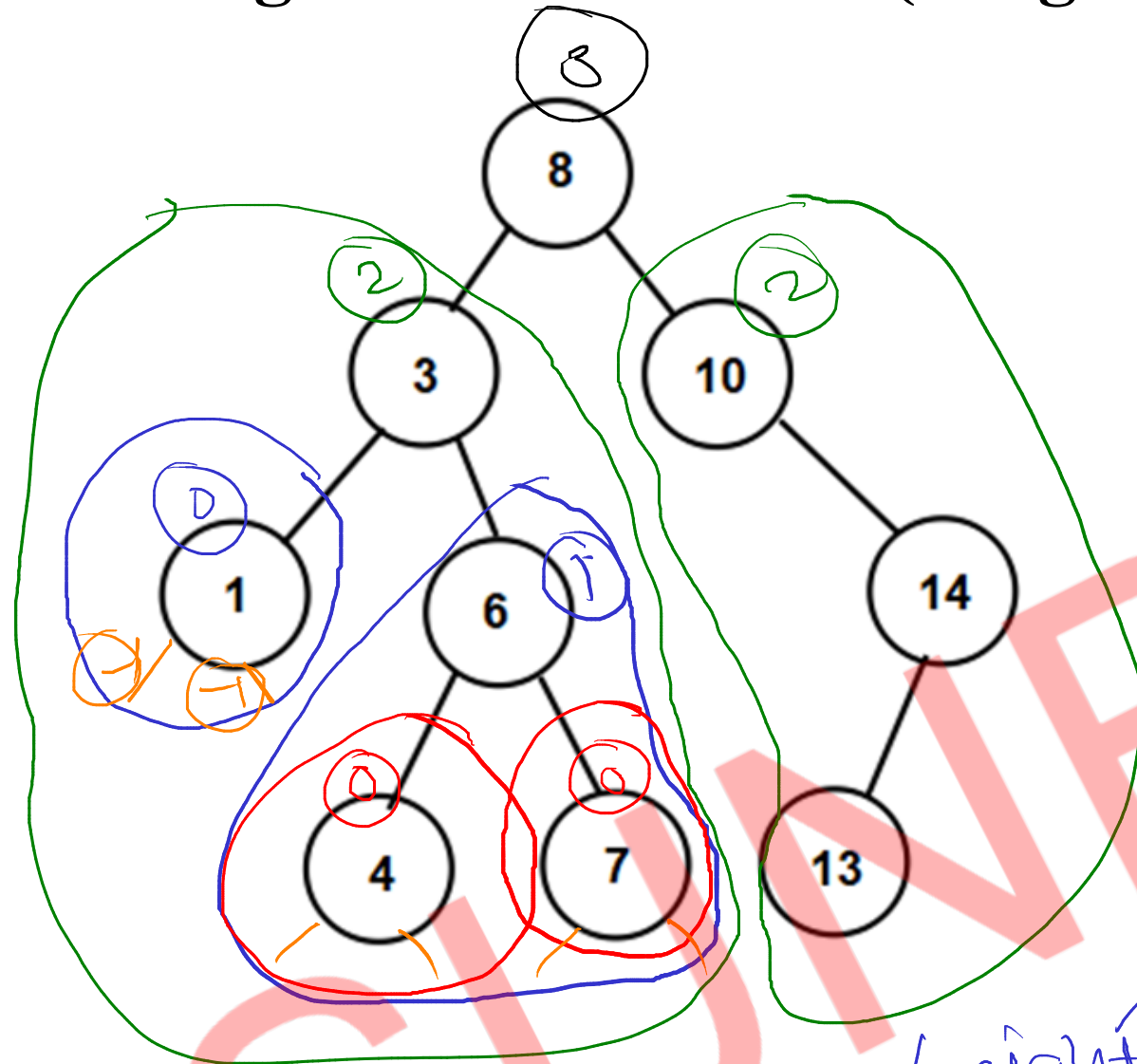
//repeat ste 2 to 5

Traversal : 8, 3, 10, 1, 6, 14, 4, 7, 13



## BST - Height

**Height of tree = MAX(Height(left sub tree), Height(right sub tree)) + 1**



**//0. if left or right sub tree is absent**

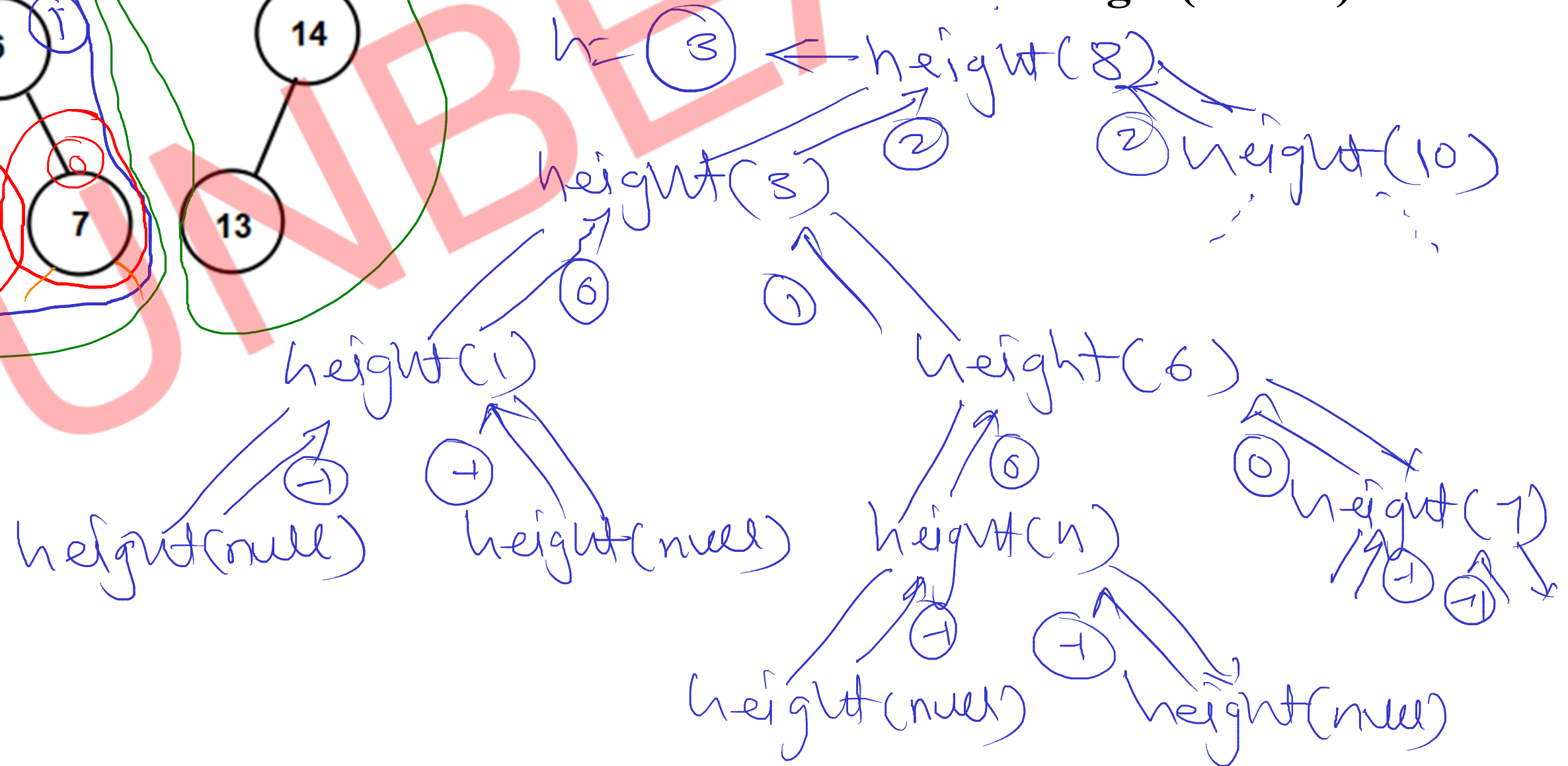
**//then return -1**

**//1. find height of left subtree**

**//2. find height of right subtree**

**//3. find max height**

**//4. add one into max height(return)**



## BST - Time complexity of operations

No. of nodes =  $n$   
height =  $h$

$$n = 2^{h+1} - 1$$

$h$	$n$
0	1
1	3
2	7
3	15

ADD

$$T(h) = O(h)$$

$$T(n) = O(\log n)$$

Search

$$T(h) = O(h)$$

$$T(n) = O(\log n)$$

DELETE

$$T(h) = O(h)$$

$$T(n) = O(\log n)$$

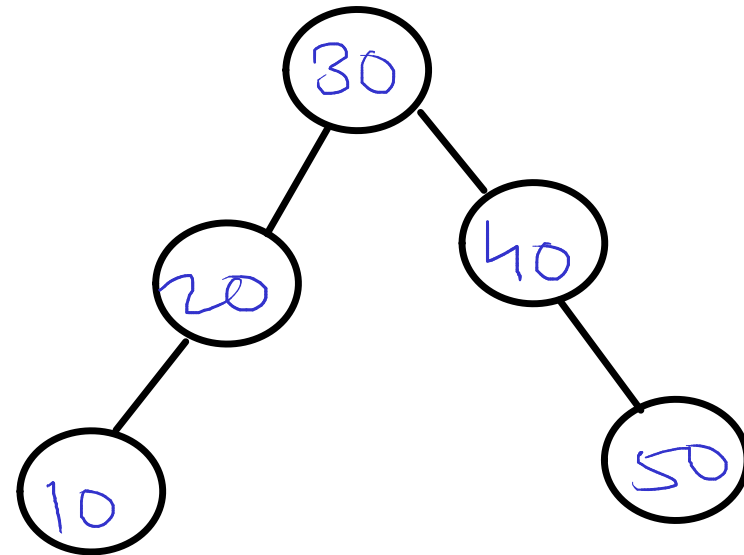
Traversed

$$T(n) = O(n)$$



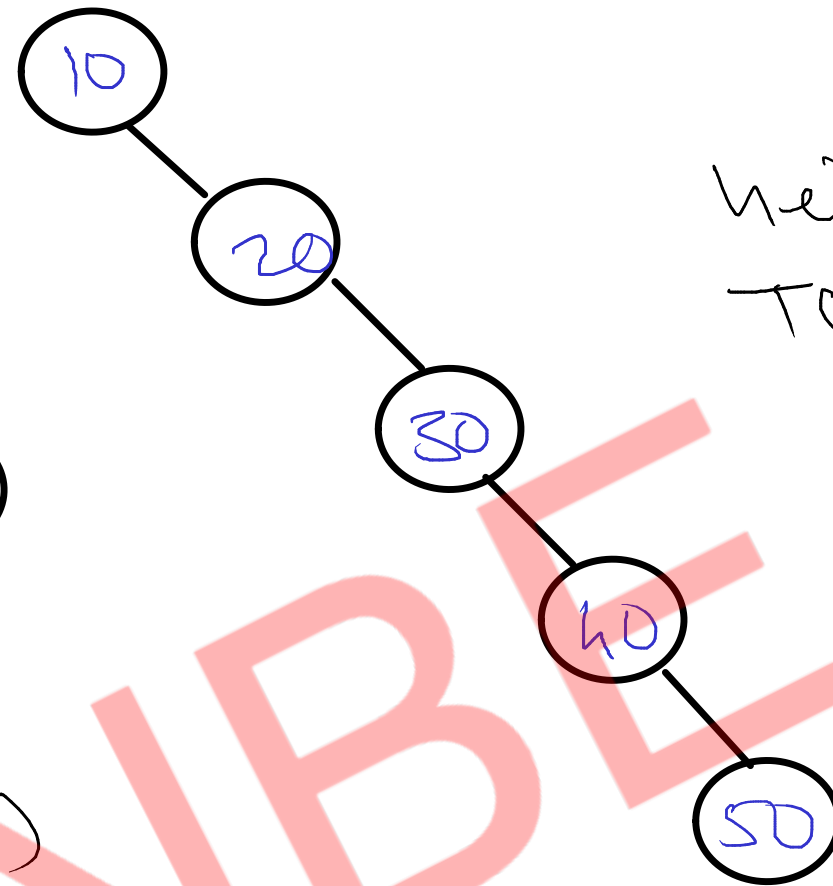
## Skewed BST

Keys : 30, 40, 20, 50, 10



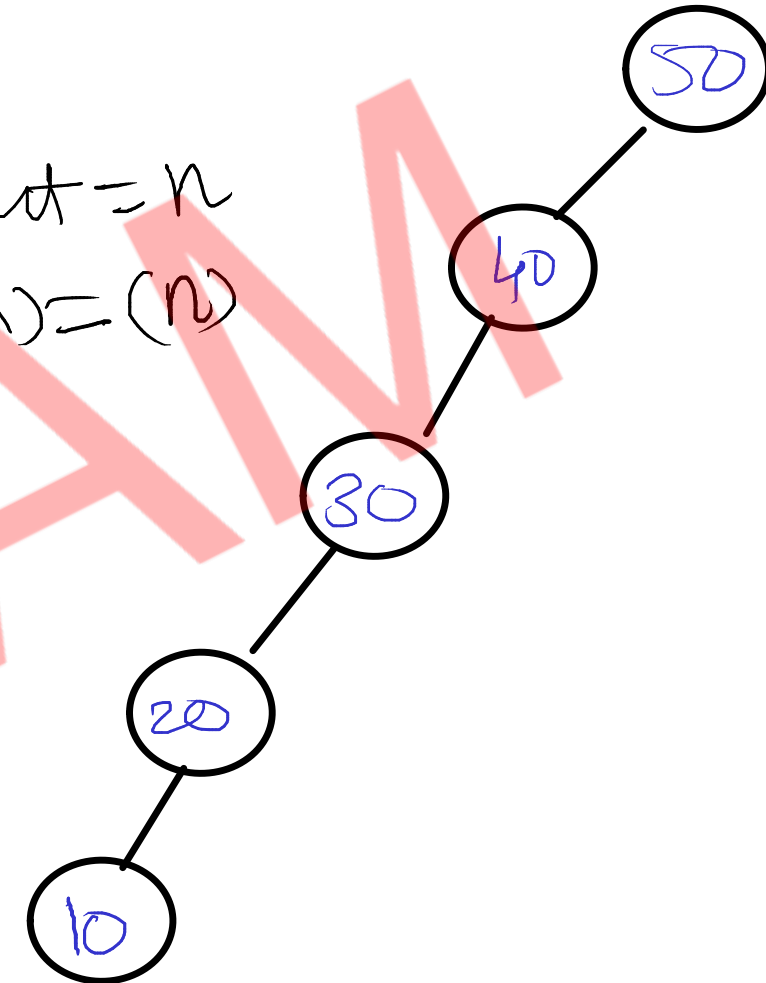
height =  $\log n$   
 $T(n) = O(\log n)$

Keys : 10, 20, 30, 40, 50



height =  $n$   
 $T(n) = (n)$

Key : 50, 40, 30, 20, 10



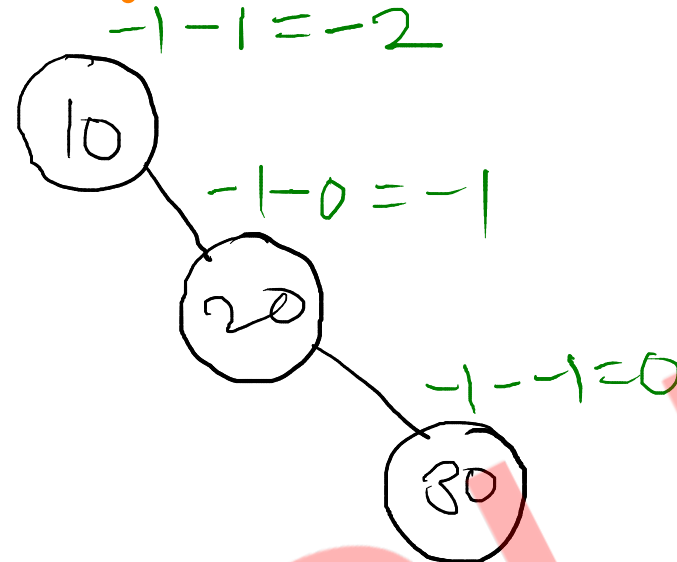
- tree is growing in only one direction either left or right
- if tree is growing in only left direction : left skewed BST
- if tree is growing in only right direction : right skewed BST

## Balanced BST

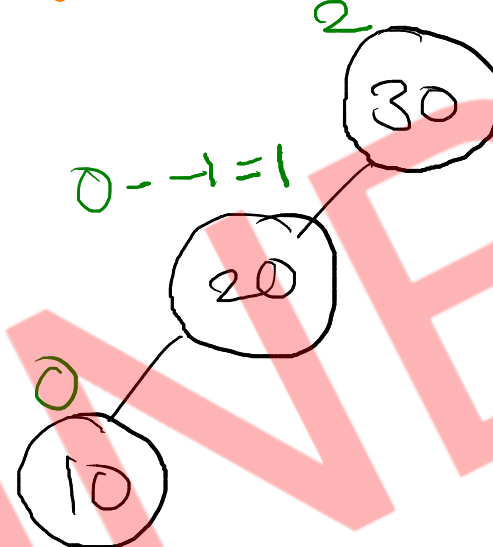
$$\text{Balance Factor} = \text{height}(\text{left sub tree}) - \text{height}(\text{right sub tree})$$

- tree is balanced if balance factor of all the nodes is either -1, 0 or +1
- balance factor = {-1, 0, +1}

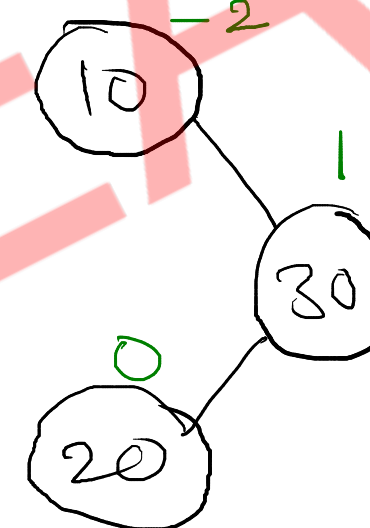
Keys : 10, 20, 30



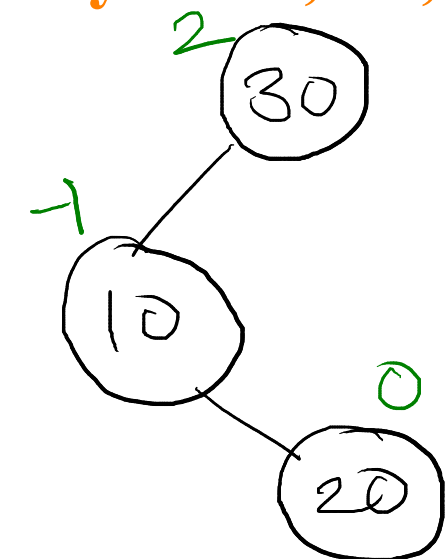
Keys : 30, 20, 10



Keys : 10, 30, 20

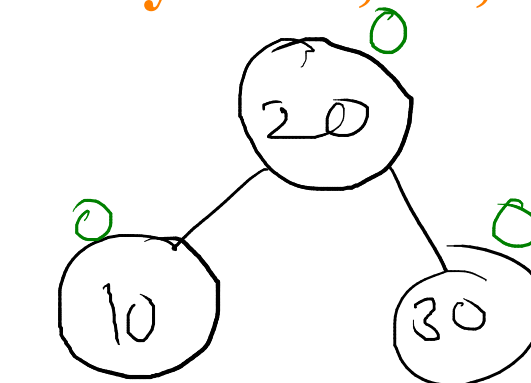


Keys : 30, 10, 20



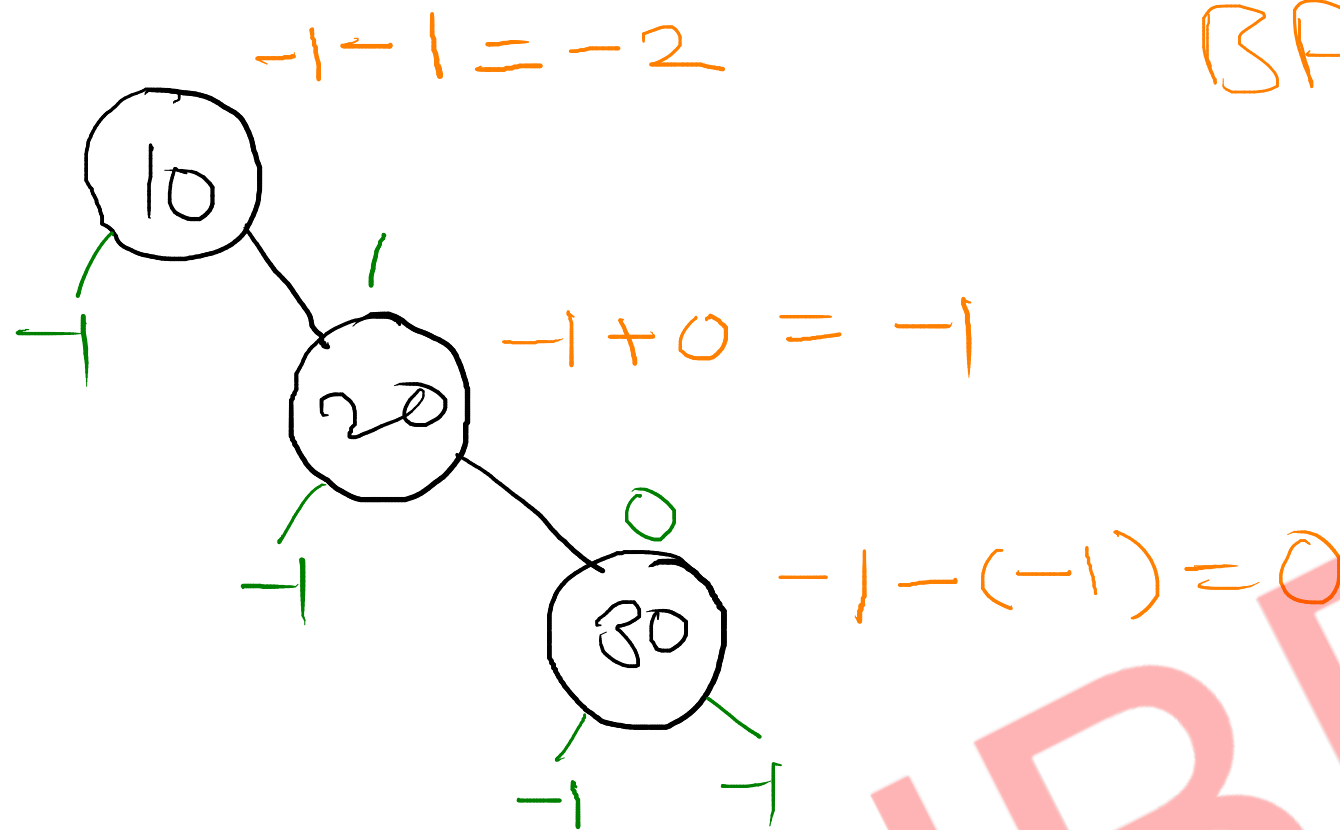
Keys : 20, 10, 30

Keys : 20, 30, 10



Balanced BST

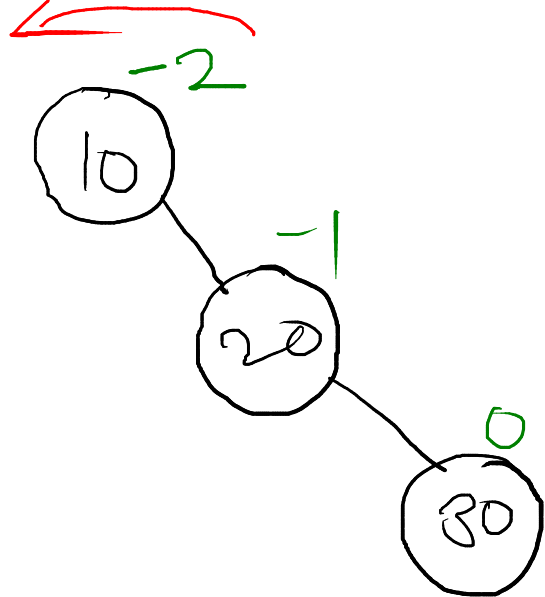
$$BF = HL - HR$$



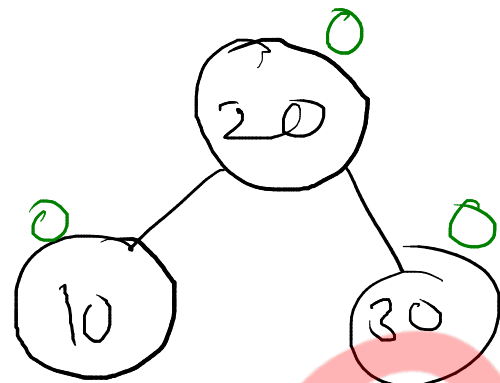
## Rotations

### RR Imbalance

Keys : 10, 20, 30



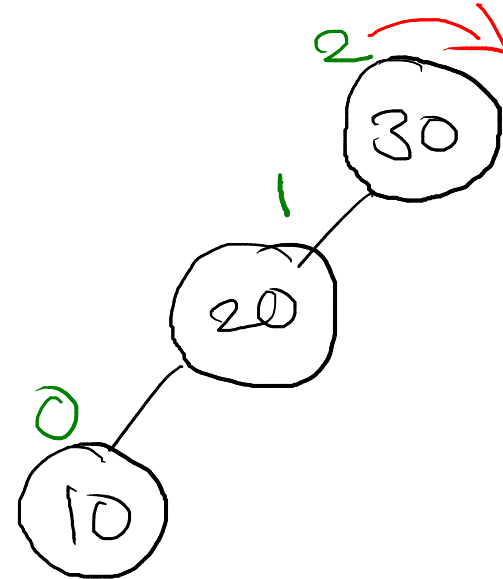
Left Rotation



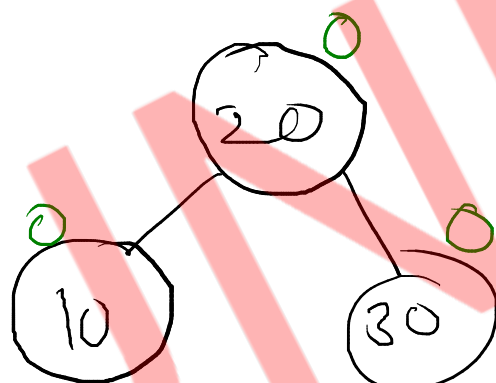
Single Rotation

### LL Imbalance

Keys : 30, 20, 10

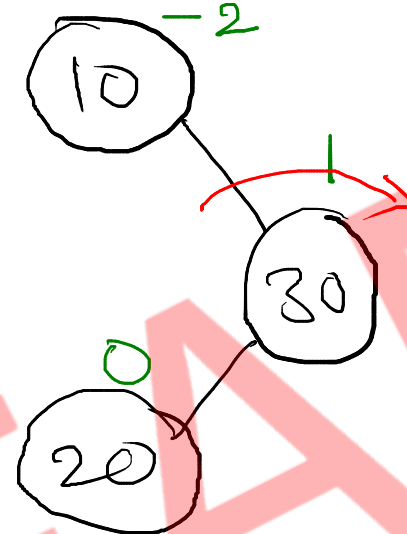


Right Rotation

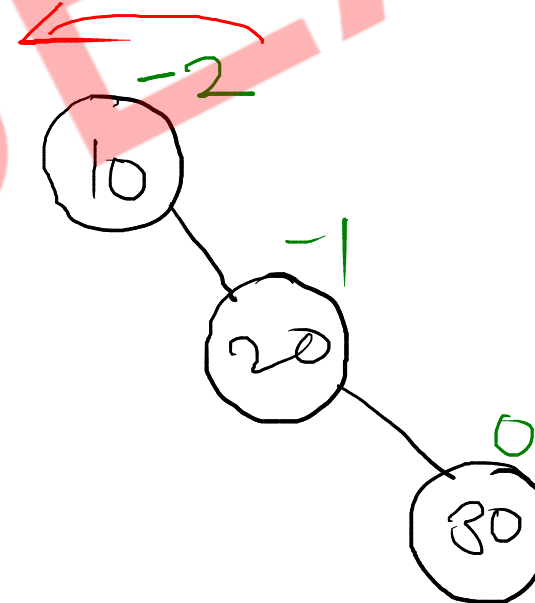


### RL Imbalance

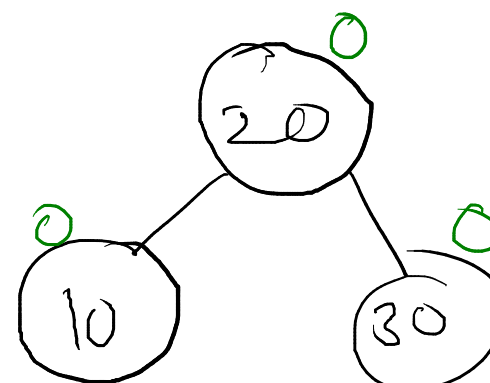
Keys : 10, 30, 20



Right Rotation

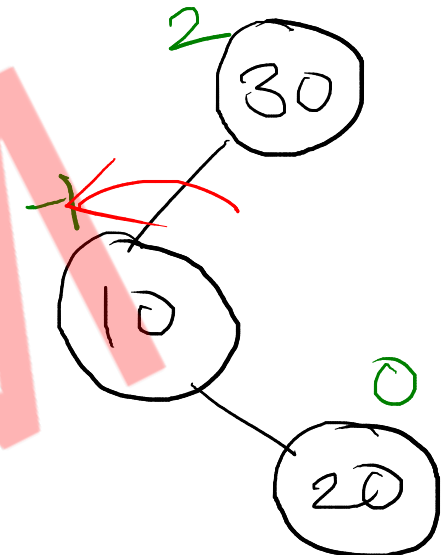


Left Rotation

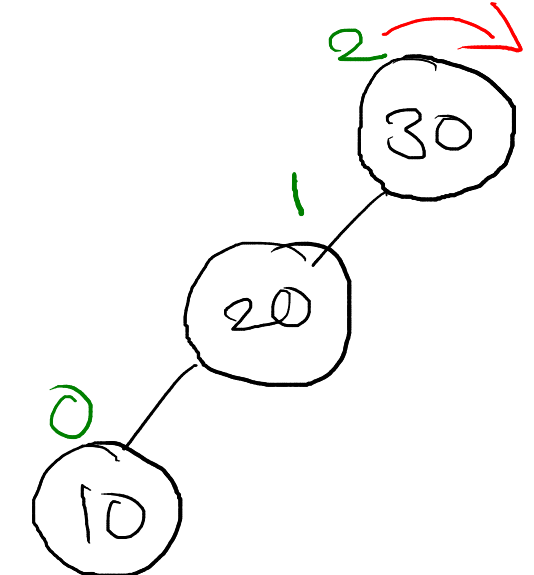


### LR Imbalance

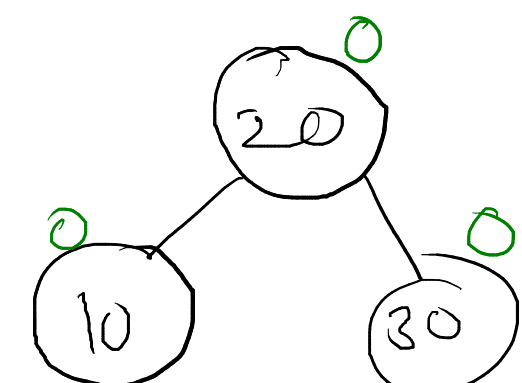
Keys : 30, 10, 20



Left Rotation



Right Rotation



Double rotations