



**Sunbeam Institute of Information Technology
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Algorithms and Data structures

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Space complexity

- Finding approximate space requirement of the algorithm to execute inside memory

$$\text{Total space} = \text{Input space} + \text{Auxiliary space}$$

\downarrow space required to store data \downarrow extra space required to process input

Linear search :

```
int linearSearch(int arr[], int key)
{
    for (int i = 0; i < arr.length; i++)
        if (key == arr[i])
            return i;
    return -1;
}
```

input variable : arr
processing variable : i, key, size

- Auxiliary space is constant here

$$S(n) = O(1)$$



Algorithm analysis

Iterative
- loops are used

```
int fact(int num) {  
    int f=1;  
    for(int i=1; i<=num; i++)  
        f *= i;  
    return f;  
}
```

Time \propto no. of iterations of the loop

Time $\propto n$

$$T(n) = O(n)$$

$$S(n) = O(1)$$

Recursive
- recursion is used

```
int rfact(int num) {  
    if(num == 1)  
        return 1;  
    return num * rfact(num-1);  
}
```

Time \propto no. of recursive call

Time $\propto n$

$$T(n) = O(n)$$

$$S(n) = O(n)$$





Selection sort

1. Select one position of the array
2. Find smallest element out of remaining elements
3. Swap selected position element and smallest element
4. Repeat above steps until array is sorted

44	11	55	22	66	33
0	1	2	3	4	5

Pass 1

44	11	55	22	66	33
0	1	2	3	4	5

Pass 2

11	44	55	22	66	33
0	1	2	3	4	5

Pass 3

11	22	55	44	66	33
0	1	2	3	4	5

Pass 4

11	22	33	44	66	55
0	1	2	3	4	5

Pass 5

11	22	33	44	66	55
0	1	2	3	4	5

11	44	55	22	66	33
0	1	2	3	4	5

11	22	55	44	66	33
0	1	2	3	4	5

11	22	33	44	66	55
0	1	2	3	4	5

11	22	33	44	66	55
0	1	2	3	4	5

11	22	33	44	55	66
0	1	2	3	4	5

to select the position : $i : 0 \rightarrow N-2$ ($i < N-1$)

to find smallest element : $j : i+1 \rightarrow N-1$ ($j < N$)





Selection sort

44	11	55	22	66	33
0	1	2	3	4	5

i	minIndex	j
0	0	1
1	2	3
2	3	4
3	4	5
4	5	6
5	6	

```

minIndex = i
for(j=i+1; j<N; j++)
    if(qmL[j] < qmL[minIndex])
        minIndex = j;
    
```

mathematical polynomial : $n^2 + n$

Degree : highest power of variable

- while writing time complexities,
consider only degree term, because

it is highest growing term in that
polynomial

11	44	55	22	66	33
0	1	2	3	4	5

i	minIndex	j
1	1	2
2	3	3
3	4	4
4	5	5
5	6	

n	n^2
1	1
10	100
100	10000
1000	1000000

$n \rightarrow$ no. of elements

$n-1 \rightarrow$ no. of passes

Pass	Comps
1	$n-1$ (n)
2	$n-2$
:	:
$n-2$	2
$n-1$	1

$$\text{Total comps} = 1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

$$\text{Time} \propto \frac{1}{2}(n^2 + n)$$

$$T(n) = O(n^2)$$

Best
Avg
Worst

$$S(n) = O(1)$$



Bubble sort

1. Compare all pairs of consecutive elements of the array one by one
2. If left element is greater than right element , then swap both
3. Repeat above steps until array is sorted

Best case :

11 22 33 44 55 66

11 22 33 44 55 66

11 22 33 44 55 66

11 22 33 44 55 66

11 22 33 44 55 66

No. of comps = $n-1$

Time $\propto n-1$

$T(n) = O(n)$ Best

$$\begin{aligned} \text{No. of elements} &= n \\ \text{No. of passes} &= n-1 \end{aligned}$$

pass	comps
1	$n-1$
2	$n-2$
3	\vdots
\vdots	2
5	1

$$\begin{aligned} \text{Total comps} &= 1+2+3+\dots+n \\ &= \frac{n(n+1)}{2} \end{aligned}$$

$$\text{Time} \propto \frac{1}{2}(n^2 + n)$$

$$T(n) = O(n^2)$$

Avg
Worst

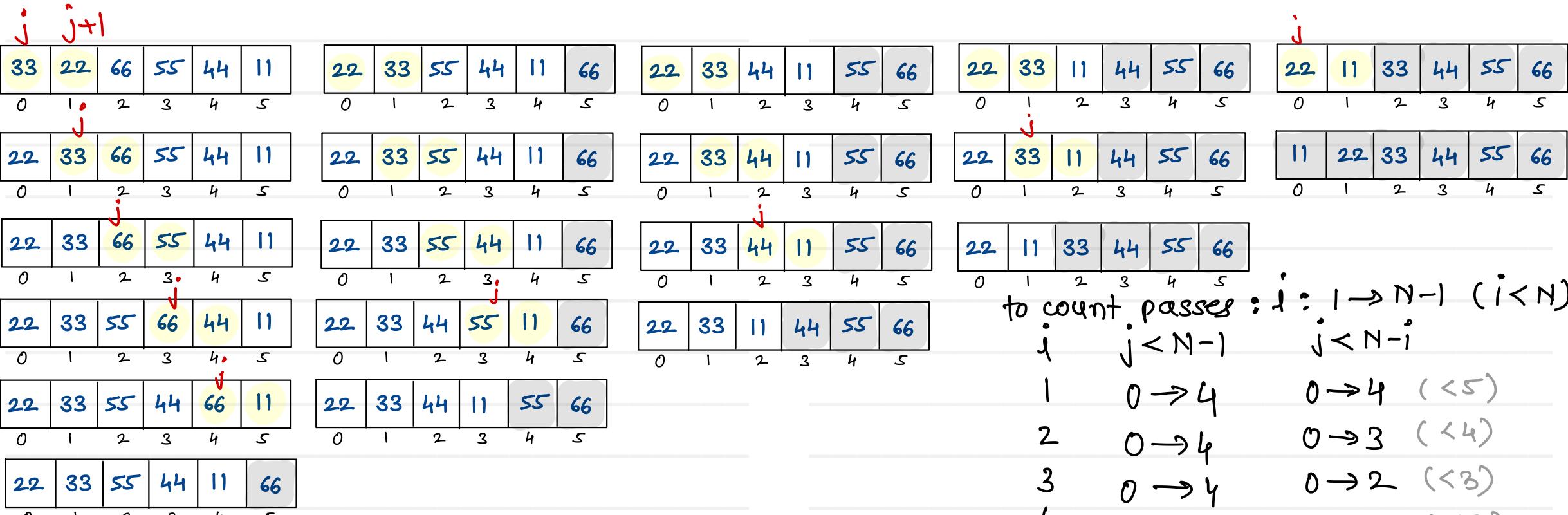
auxiliary space is constant

$$S(n) = O(1)$$



Bubble sort

33	22	66	55	44	11
0	1	2	3	4	5



to count passes : $i = 1 \rightarrow N-1$ ($i < N$)
 $j < N-i$

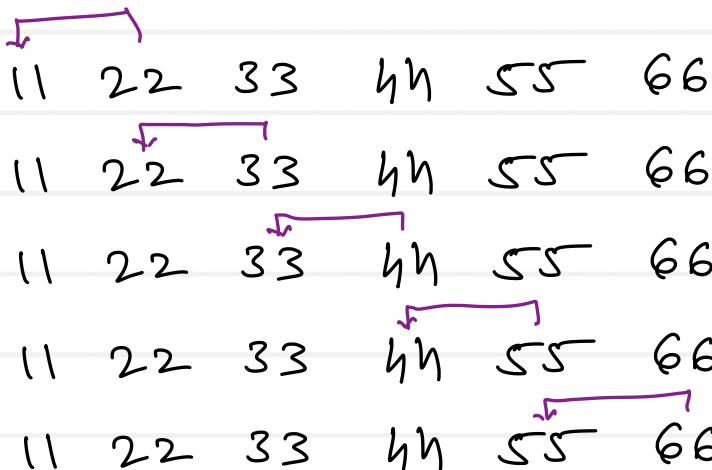
1	$0 \rightarrow 4$	$0 \rightarrow 4$ (< 5)
2	$0 \rightarrow 4$	$0 \rightarrow 3$ (< 4)
3	$0 \rightarrow 4$	$0 \rightarrow 2$ (< 3)
4	$0 \rightarrow 4$	$0 \rightarrow 1$ (< 2)
5	$0 \rightarrow 4$	$0 \rightarrow 0$ (< 1)





Insertion sort

1. Pick one element of the array (start from 2nd index)
2. Compare picked element with all its left neighbours one by one
3. If left neighbour is greater, move it one position ahead
4. Insert picked element at its appropriate position
5. Repeat above steps until array is sorted



No. of comps = $n - 1$
Time $\propto n - 1$

$$T(n) = O(n)$$

	passes	comps
1	1	1
2	2	2
3	3	3
:	:	:
$n-1$	$n-1$	$n-1$
		<u>n</u>

$$\text{Total comps} = 1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

$$\text{Time} \propto \frac{1}{2}(n^2 + n)$$

$$T(n) = O(n^2)$$

worst
Avg





Insertion sort

55	44	22	66	11	33
0	1	2	3	4	5

44
temp

22
temp

66
temp

11
temp

33
temp

55	44	22	66	11	33
0	1	2	3	4	5

44	55	22	66	11	33
0	1	2	3	4	5

22	44	55	66	11	33
0	1	2	3	4	5

22	44	55	66	11	33
0	1	2	3	4	5

11	22	44	55	66	33
0	1	2	3	4	5

j-1

	55	22	66	11	33
0	1	2	3	4	5

44		55	66	11	33
0	1	2	3	4	5

22	44	55	66	11	33
0	1	2	3	4	5

22	44	55		66	33
0	1	2	3	4	5

11	22	44	55	66	
0	1	2	3	4	5

44	55	22	66	11	33
0	1	2	3	4	5

	44	55	66	11	33
0	1	2	3	4	5

22	44	55	66	11	33
0	1	2	3	4	5

22	44		55	66	33
0	1	2	3	4	5

11	22	44		55	66
0	1	2	3	4	5

22	44	55	66	11	33
0	1	2	3	4	5

to pick the element: i: 1 → N-1 ($i < N$)
to compare left neighbors: j: i-1 → 0 ($j \geq 0$)

	22	44	55	66	33
0	1	2	3	4	5

11	22	44	55	66	33
0	1	2	3	4	5

11	22	33	44	55	66
0	1	2	3	4	5





Insertion sort

```
for(i=1; i<N; i++) {  
    temp = arr[i];  
    for(j=i-1; j>=0; j--) {  
        if(arr[j] > temp)  
            arr[j+1] = arr[j];  
        else  
            break;  
    }  
    arr[j+1] = temp;  
}
```

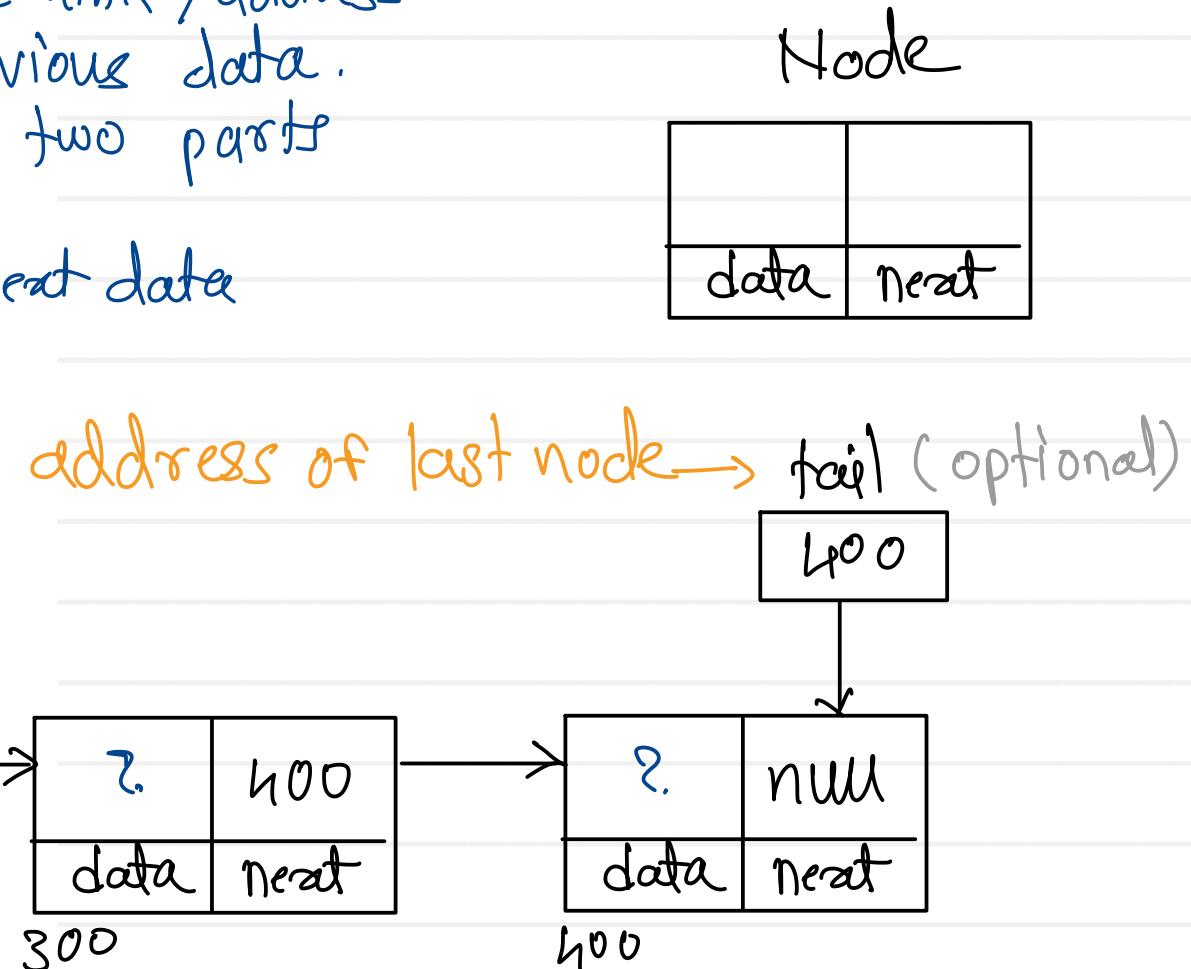
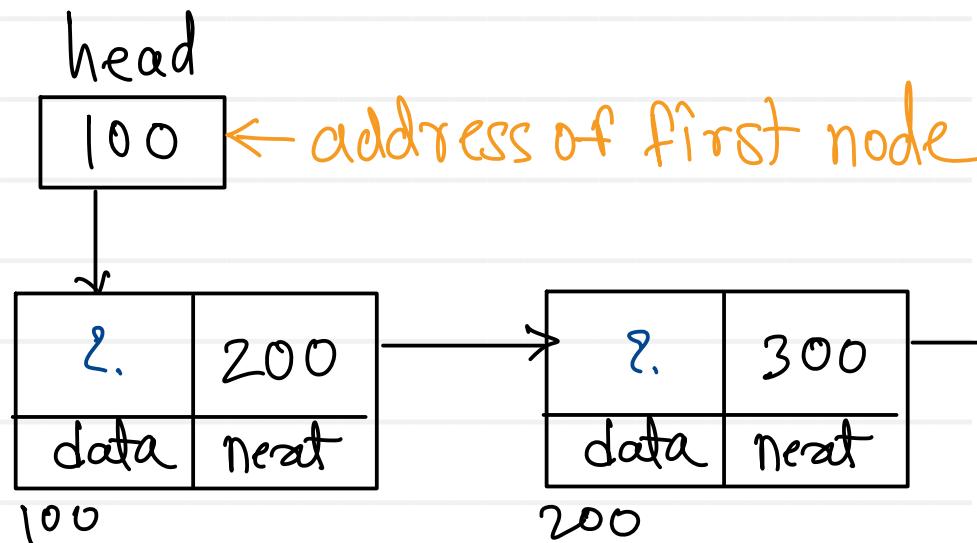
11	22	33	44	55	66
0	1	2	3	4	5

i	i<6	temp	j
1	T	44	0,-1
2	T	22	1,0,-1
3	T	66	2
4	T	11	3,2,1,0,-1
5	T	33	4,3,2,1
6	F		



Linked List

- it is a linear data structure where link / address of next data is kept with its previous data.
- every element of linked list has two parts
 1. data — actual data
 2. link/next — address of next data
- it is referred Node



Operations

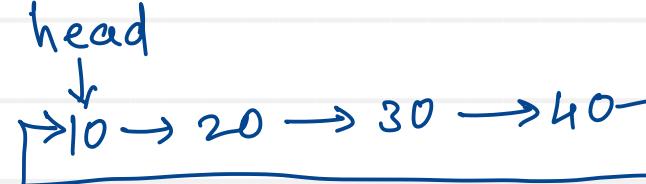
1. Add first
 2. Add last
 3. Add position (insert)
-
1. Delete first
 2. Delete last
 3. Delete position
-
1. Display (traverse) (forward/ backward)
-
1. Search
 2. Sort
 3. Reverse

Types

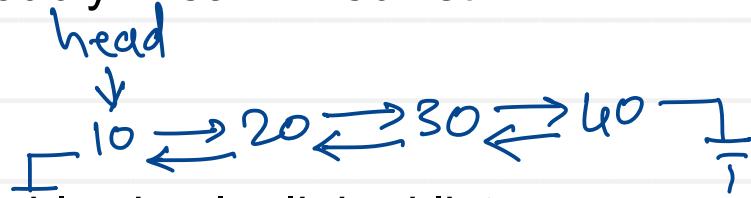
1. Singly linear linked list



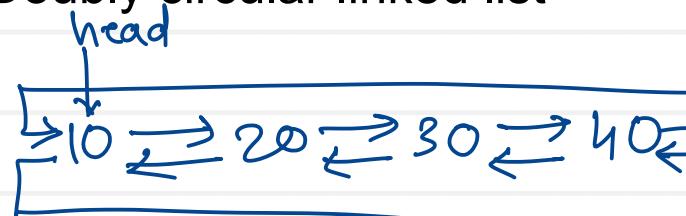
2. Singly circular linked list



3. Doubly linear linked list



4. Doubly circular linked list





Linked List

Node :

data - int, char, short, double, class
next - reference of next Node

class Node { ← self referential class

int data;
Node next;

}

why inner class ?

- to access private fields of Node class
into List class directly

why static ?

- to restrict access of private fields of
List class into Node class directly.

class List {

static class Node {

int data;

Node next;

}
Node head;

Node tail;

int count;

public List() { ... }

public addNode() { ... }

public deleteNode() { ... }

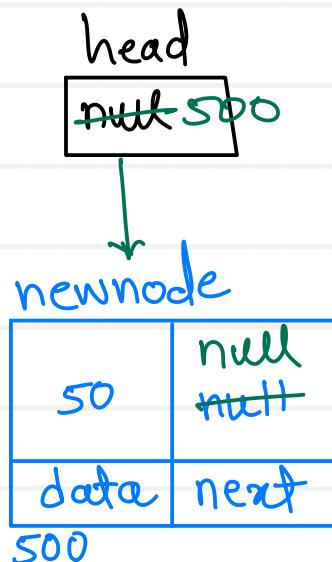
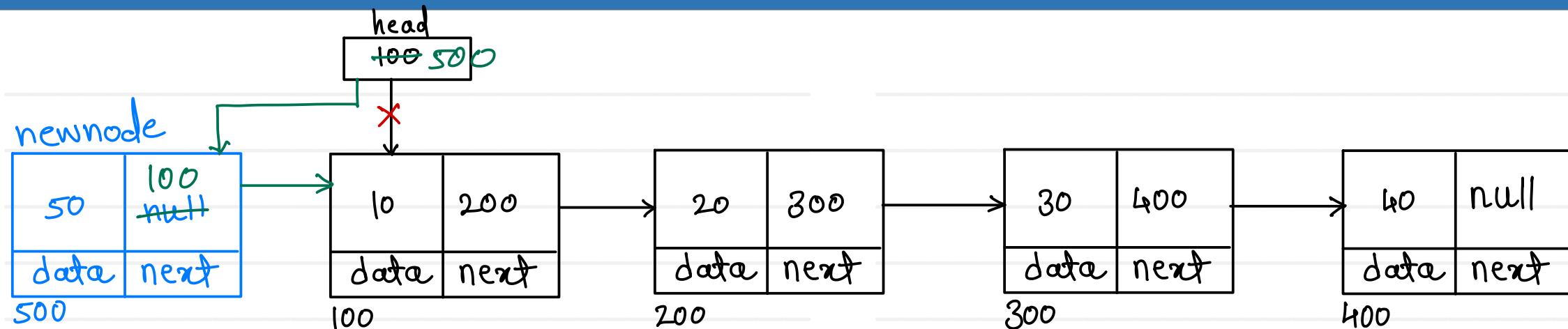
public traverse() { ... }

public deleteAll() { ... }

}



Singly linear Linked List - Add first

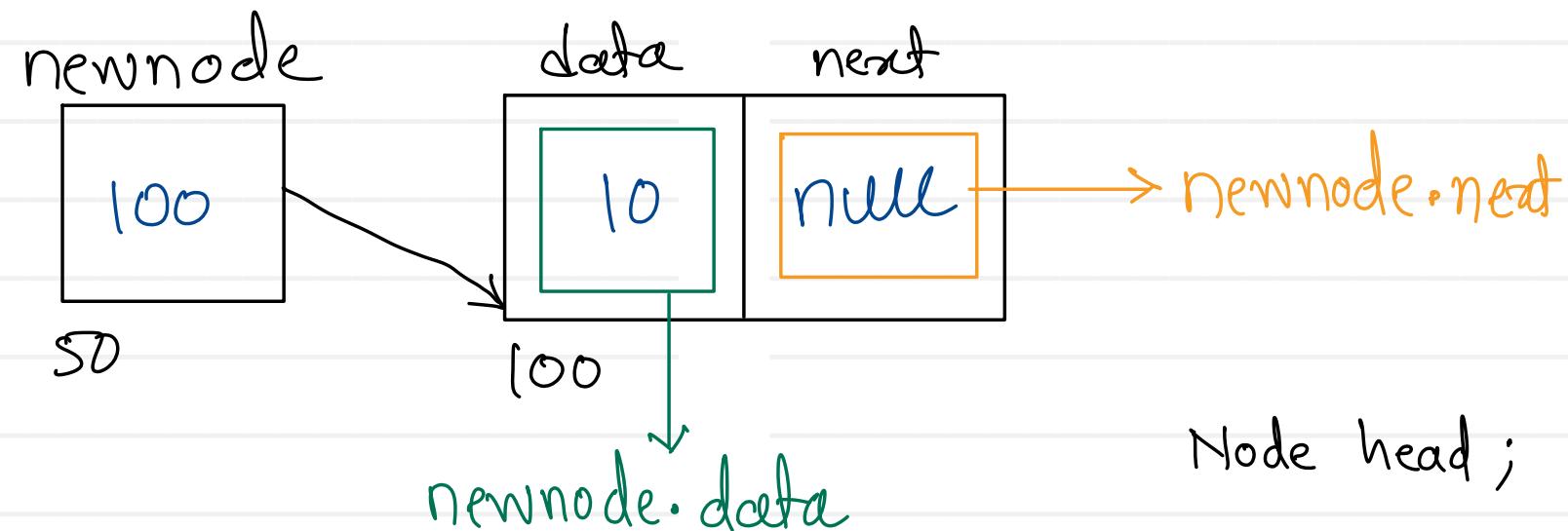


$newnode.next = head$
 $head = newnode$

1. create a newnode
2. add first node into next of newnode
3. Move head on newnode

$$T(n) = O(1)$$

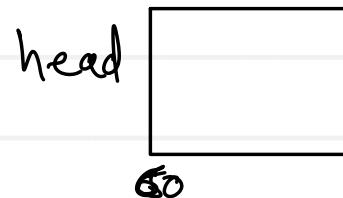
Node newnode = new Node(10);



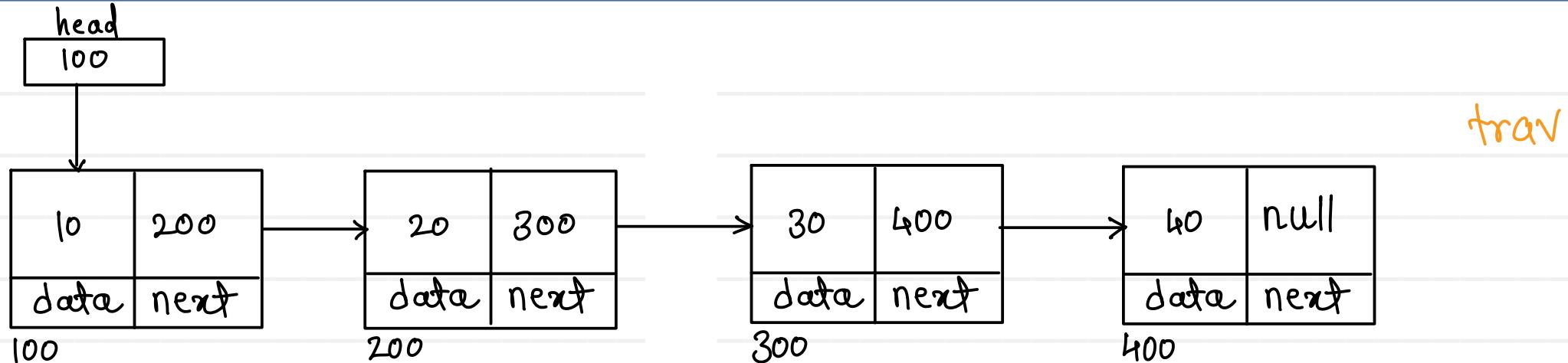
`newnode.data = 2;` ← writing

`2 = newnode.data` ← reading

Node head ;



Singly linear Linked List - Display



```
trav = head;  
while (trav != null) {  
    sysout(trav.data);  
    trav = trav.next;  
}
```

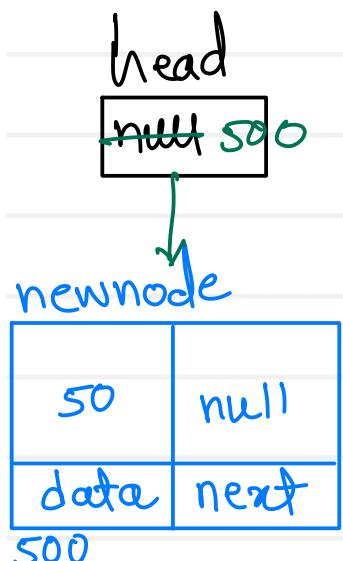
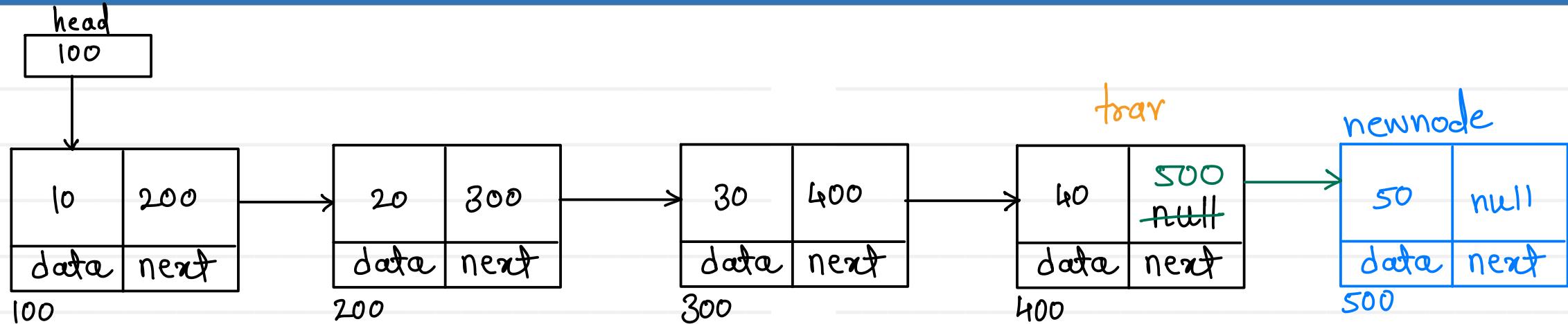
trav trav.data
100 10
200 20
300 30
400 40
null

1. create trav and start at first node
2. print/visit current node (trav.data)
3. go on next node (trav.next)
4. repeat step 2 & 3 till last node

$$T(n) = O(n)$$



Singly linear Linked List - Add last

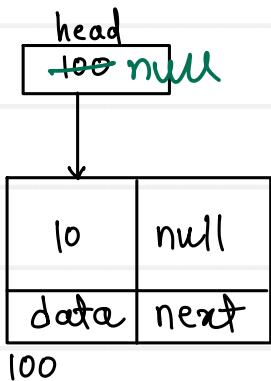
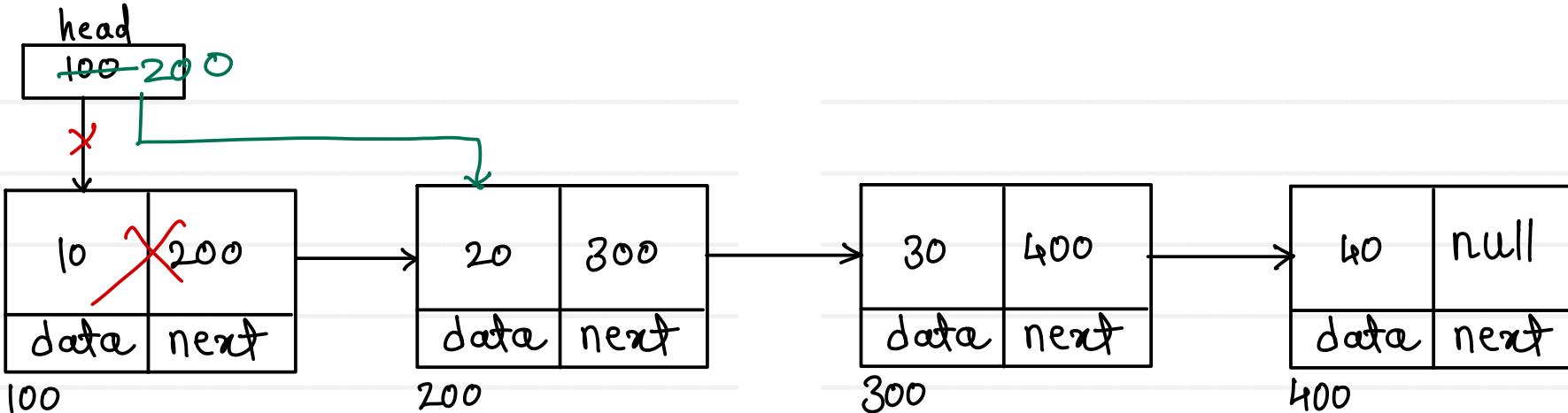


1. create a newnode
2. if list is empty
 add newnode into head
3. if list is not empty
 a. traverse till last node
 b. add newnode into next of last node

```
trav = head;  
while (trav.next != null)  
    trav = trav->next;
```

$$T(n) = O(n)$$

Singly linear Linked List - Delete first

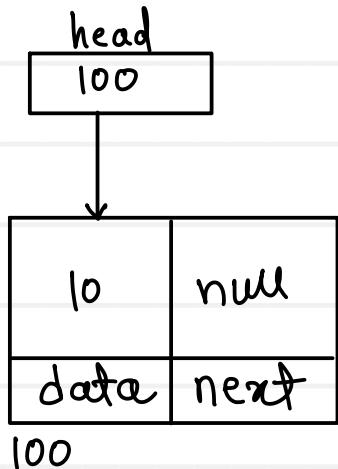
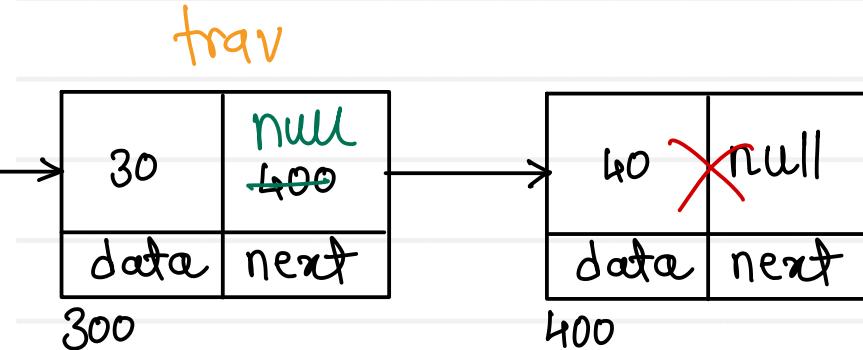
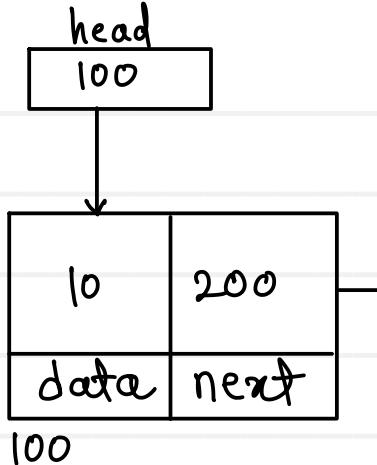


$\text{head} = \text{head.next};$

1. if list is empty
return;
2. if list is not empty
move head on second node

$$T(n) = O(1)$$

Singly linear Linked List - Delete last



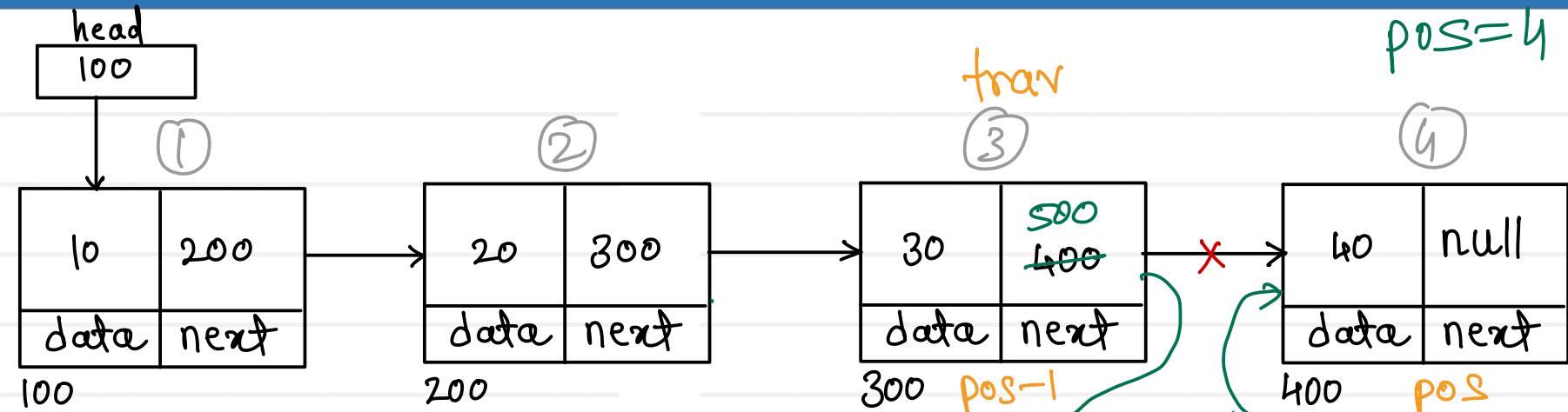
```

Node trav = head;
while(trav.next.next != null)
    trav = trav.next;
  
```

$$T(n) = O(n)$$

1. if list empty
return
2. if list has single node
head = null;
3. if list has multiple node
 - a. traverse till second last node
 - b. make null into next of second last node

Singly linear Linked List - Add position



1. create a newnode

if list is empty

 add newnode into head

if list is not empty

 2. traverse till $pos-1$ node

 3. add pos node into next of newnode

 4. add newnode into next of $pos-1$ node

$$T(n) = O(n)$$

$trav = head;$

$for(i=1; i < pos-1; i++)$

$trav = trav.next;$

$pos = 4$

$trav$	i	$i < 3$
100	1	T
200	2	T
300	3	F



Thank you!!!

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