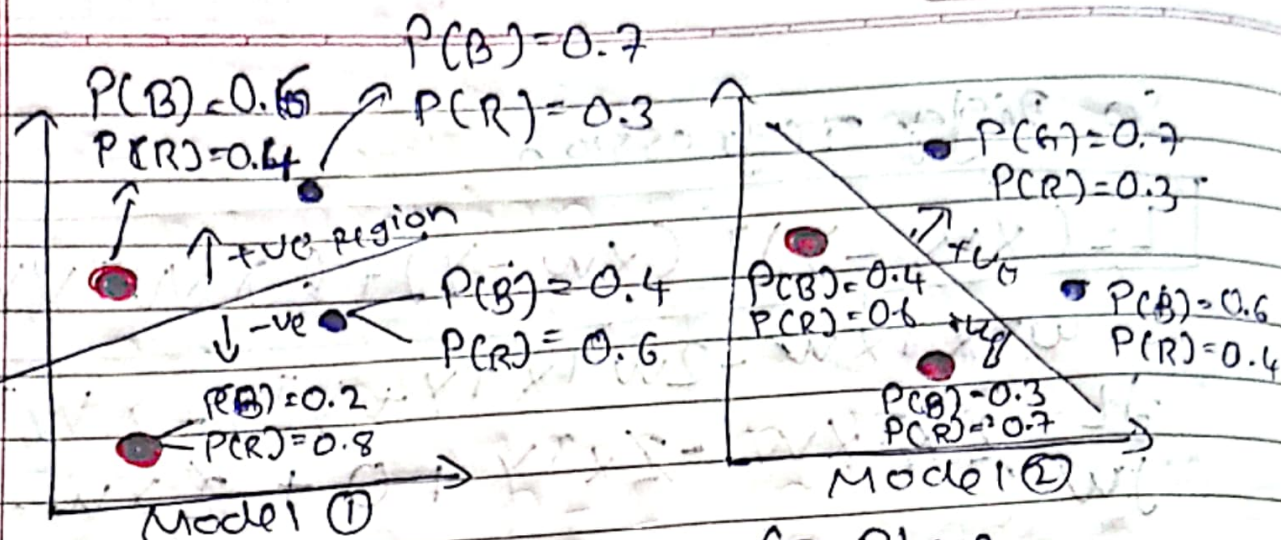


Maximum

Likelihood

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$P(B)$  = Probability of Blue  
 $P(R)$  = Probability of Red

~~Maximum Likelihood~~

\* If you want to find which model is better than the other using Maximum Likelihood (calculate product) all the  $P(B)$  of the model and prediction then compare that with the other model.

whichever model has higher value that model is the better model.

\* Calculating Maximum Likelihood of Model 1

Note: In maximum likelihood we only consider that value of point which is Actual its colour/character meaning IF the point is Blue we only consider  $P(B)$  not the  $P(R)$



① Calculating Maximum L of Model ①

As we can see there are 2 Red and 2 Blue points.

$$= 0.7 \times 0.4 \times 0.4 \times 0.8$$

$$ML1 = 0.0896$$

② Calculating M-L of Model ②

2 Blue, 2 Red

$$= 0.7 \times 0.6 \times 0.6 \times 0.7$$

$$ML2 = 0.1764$$

$$ML2 > ML1$$

meaning model 2 is better than

Model 1

But the problem with this method is if there is a large Dataset with large no. of Rows and Columns the product (multiple) get too small so, some how we have to convert this product (x) to + Sum (+).

So As we know

$$\log(ab) = \log(a) + \log(b)$$

$$\log(max) = \log(0.7) + \log(0.4) + \log(0.4) + \log(0.8)$$



But we still have problem with this equation

$$\log(\max) = \log(0.7) + \log(\dots) + \log(\dots) + \log(\dots)$$

Because the Maximum Likelihood Range is 0-1 and for every value from 0-1 there log is **NEGATIVE**

So we have to change positive to -ve this called as Cross Entropy.

The summation of ~~the~~ Negative logs of Maximum Likelihood is called as Cross Entropy.

$$\log(\max) = -\log(0.7) - \log(0.4) - \log(0.4) - \log(0.8)$$

In Maximum Likelihood we choose a Better Model by comparing ~~Maximum~~ product of each model. We have larger product than the other that model is Better.

But,

In ~~the~~ Cross Entropy we ~~can~~ minimize the value because

$$\log 0.1 \text{ value} > \log 0.9 \text{ value}$$

$$-0.1 > -0.9$$



In Maximom L we Maximize the Value

and in

Cross Entropy we minimize the Value.

Now,

we will choose that model whose cross Entropy is less than the other model's cross Entropy

Formula is  $-y_i \log(\hat{y}_i) - (1-y_i) \log(1-\hat{y}_i)$

$$\textcircled{1} = -y_i \log(\hat{y}_i) - (1-y_i) \log(1-\hat{y}_i)$$

Putting point in the formula.

$$P(B) = 0.7$$

$$P(R) = 0.3$$

Blue point

correctly classified as Blue (1) ( $y_i = 1$ )

Target Value

Predicted Value

$$= -y_1 \log(\hat{y}_1) - (1-y_1) \log(1-\hat{y}_1)$$

$$= -1 \log(\hat{y}_1) - (1-1) \log(1-\hat{y}_1)$$

$$= -1 \log(\hat{y}_1)$$

$$= -\log(0.7)$$



We are seeing that what the probability of getting Blue that why in we are putting Blue value

② Now for the 2<sup>nd</sup> point putting in the formula.

$P(B) = 0.6$   $y_2 = 0$   
 $P(R) = 0.4$  ← Target Value

So,

$$= -y_2 \log(\hat{y}_2) - (1 - y_2) \log(1 - \hat{y}_2)$$

$$= -0 \log(\hat{y}_2) - (1 - y_2) \log(1 - \hat{y}_2)$$

$$= - (1 - y_2) \log(1 - \hat{y}_2)$$

$$= - (1 - 0) \log(1 - 0.6)$$

$$= -1 \log(1 - 0.6)$$

$$= -\log(1 - 0.6)$$

$$= \boxed{-\log(0.4)}$$

③ 3<sup>rd</sup> point

$P(B) = 0.4$   $y_3 = 1$   
 $P(R) = 0.6$

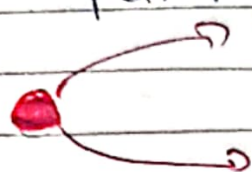
$$= -y_3 \log(\hat{y}_3) - (1 - y_3) \log(1 - \hat{y}_3)$$

$$= -y_3 \log(\hat{y}_3)$$

$$= -1 \log(\hat{y}_3) = \boxed{-\log(0.4)}$$

$$= -\log(0.4)$$

(4) 4th point


 $P(B) = 0.2$   
 $P(R) = 0.8$

$$y_4 = 0$$

$$= -y_4 \log(\hat{y}_4) - (1 - y_4) \log(1 - \hat{y}_4)$$

$$= -0 \log(\hat{y}_4) - (1 - 0) \log(1 - \hat{y}_4)$$

$$= 0 - (1 - 0) \log(1 - \hat{y}_4)$$

$$= -\log(\hat{y}_4)$$

$$= -1 \log(1 - \hat{y}_4)$$

$$= -\log(1 - 0.2)$$

$$= -\log(0.8)$$

$$= -\log(0.7) - \log(0.4) - \log(0.4) - \log(0.8)$$

Our Loss function is

$$L = -y_i \log(\hat{y}_i) - (1 - y_i) \log(1 - \hat{y}_i)$$

$$L = -\sum_{i=1}^n y_i \log(\hat{y}_i) - (1 - y_i) \log(1 - \hat{y}_i)$$

For Average Loss/Error

$$L = -\frac{1}{n} \sum_{i=1}^n y_i \log(\hat{y}_i) + (1 - y_i) \log(1 - \hat{y}_i)$$

These loss func also known as Log-Loss and Binary Cross Entropy Error