

Norve Bayes Classifier Intuition

Chennai (CSK)

	toss	venue	outlook	Result
1	won	Mumbai	Overcast	won
2	lost	Chennai	Sunny	won
3	won	Kolkata	Sunny	won
4	won	Chennai	Sunny	won
5	lost	Mumbai	Sunny	lost
6	won	Chennai	Overcast	lost
7	won	Kolkata	Overcast	lost
8	won	Mumbai	Sunny	won

Q We have to find (given) this $\{ \text{lost, Mumbai, Sunny} \}$ will coll win or lose.

$P(W / \text{lost n Mumbai n Sunny})$ and $P(L / \text{lost n Mumbai n Sunny})$

* Using Bayes Theorem,

$$P(A/B) = \frac{P(B/A) \times P(A)}{P(B)}$$

$$\textcircled{1} = P(W / \text{lost, Mumbai, Sunny}) = \frac{P(\text{lost, Mumbai, Sunny} / W) \times P(W)}{P(\text{lost, Mumbai, Sunny})}$$

$$\textcircled{2} = P(L / \text{lost, Mumbai, Sunny}) = \frac{P(\text{lost, Mumbai, Sunny} / L) \times P(L)}{P(\text{lost, Mumbai, Sunny})}$$

* we will ~~not~~ calculate Denominator because Denominator is same for both equation and it will not provide any information.

So, $P(w | \text{lost, mumbai, sunny}) =$

$$P(\text{lost, mumbai, sunny}) P(w)$$

$$= P(\text{lost} | w) \times P(\text{mumbai} | w) \times P(\text{sunny} | w) \times P(w)$$

↑
we are adding Naive Bayes Assumption in above equation.

Naive Bayes add this Assumption because we are asking very specific question

Here, $P(\text{lost, mumbai, sunny})$ and generally this type of specific question are not present in data set and if we do not add this Assumption the output of the specific question will be 0 and Naive Bayes will not perform well.

Now $P(w | \text{lost, mumbai, sunny}) =$

$$= P(\text{lost} | w) \times P(\text{mumbai} | w) \times P(\text{sunny} | w) \times P(w)$$

In our dataset

$$= \frac{1}{5} \times \frac{2}{5} \times \frac{4}{5} \times \frac{5}{8} = \boxed{0.04}$$

$$\begin{aligned}
 P(L/\text{lost, mumbai, sunny}) &= \\
 &= P(\text{lost, mumbai, sunny} / L) \times P(L) \\
 &= P(\text{lost} / L) \times P(\text{mum} / L) \times P(\text{sun} / L) \times P(L) \\
 &= \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{3}{8}
 \end{aligned}$$

~~0.01~~ = 0.013

So, 0.04 > 0.013

Meaning

If Toss = Lost

Venue = Mumbai

Outlook = Sunny

CSK will win