

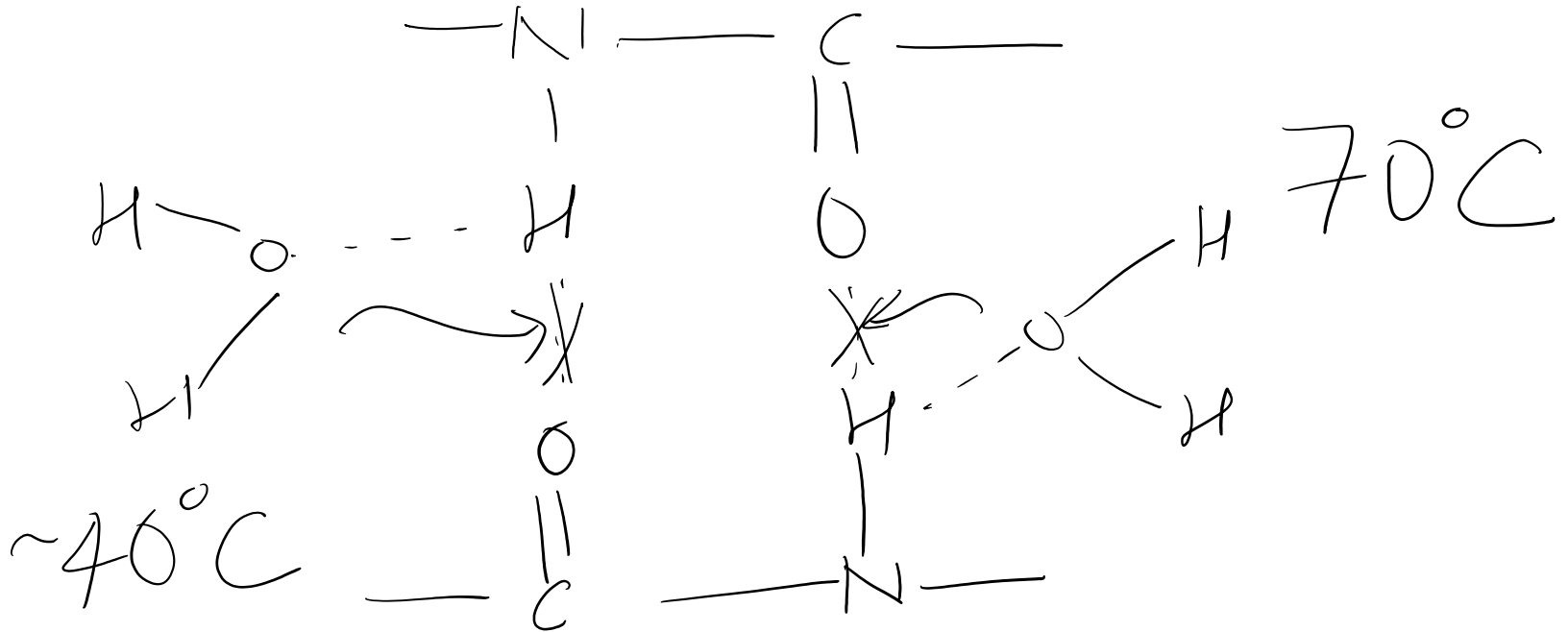
# TXL211

## Lecture 7



# Factors affecting Tg

## Plasticizer



PLASTICIZED

PVC

RT

80°C



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$T_Z X$



# VOLUME

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## The concept of Free Volume

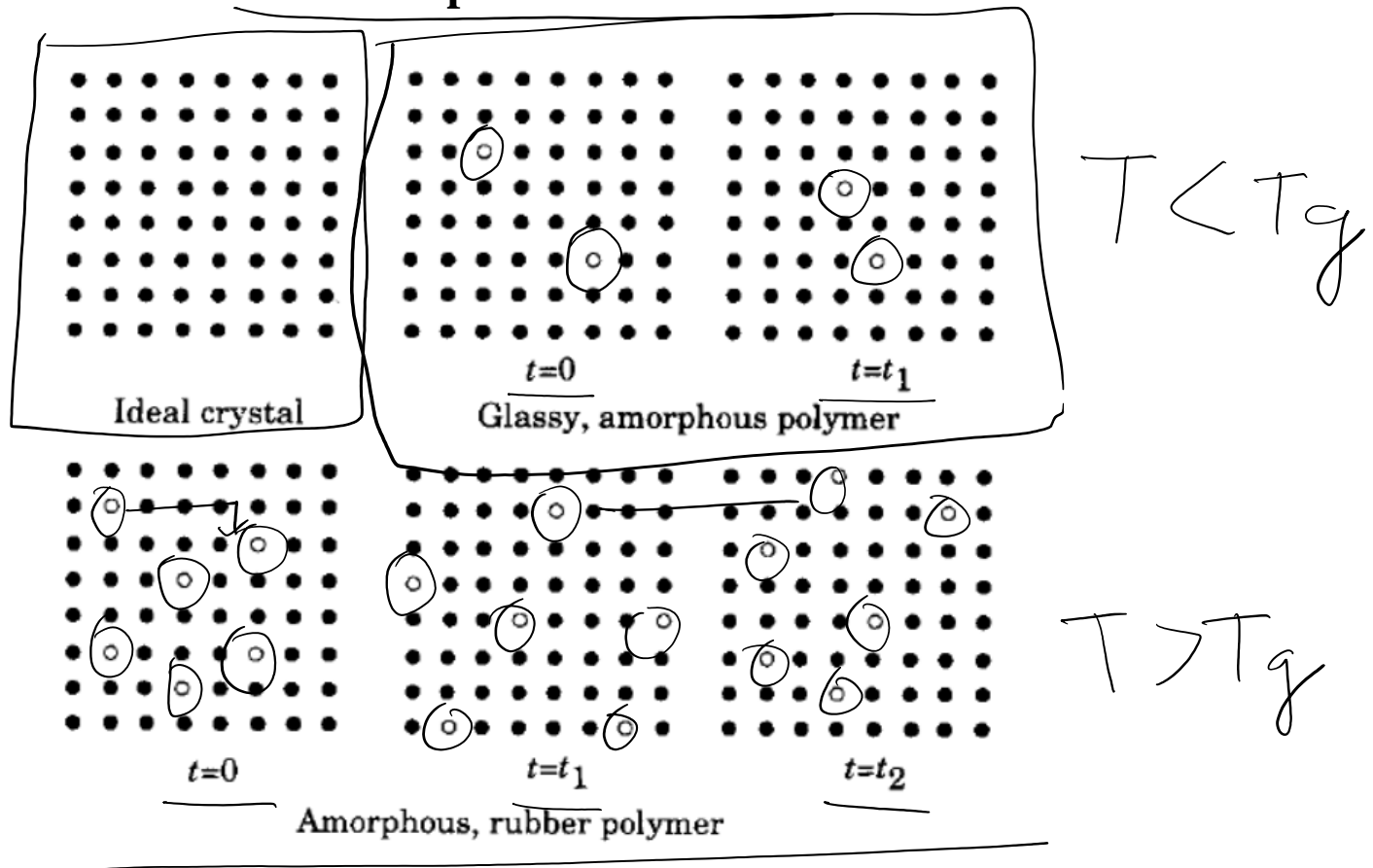
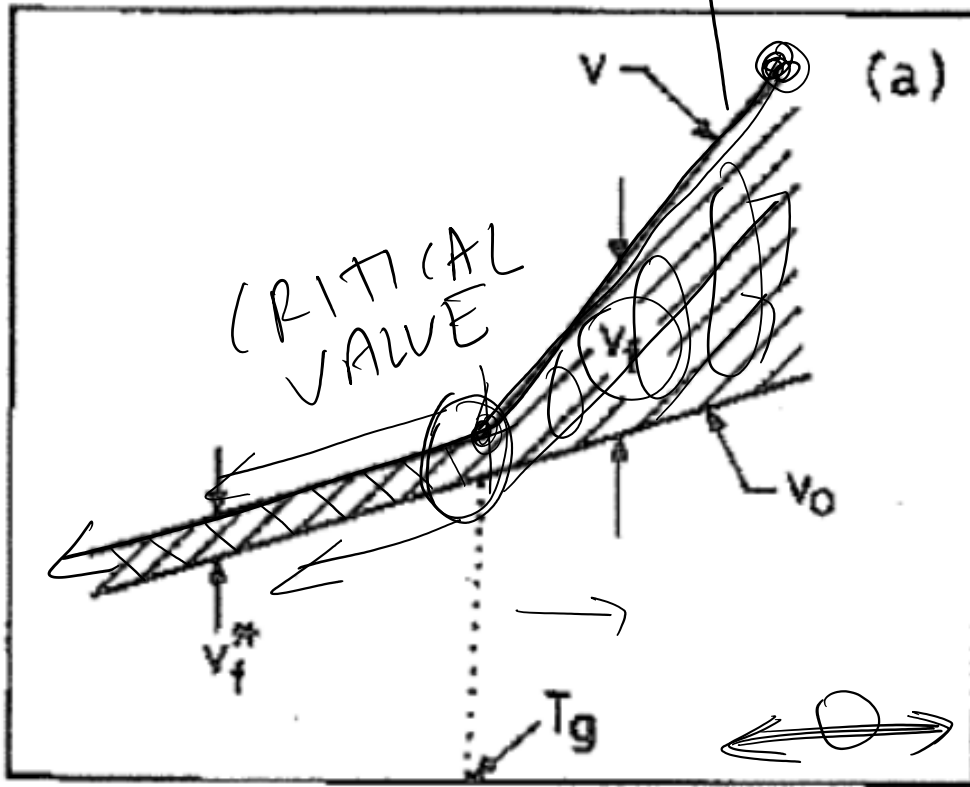


Illustration of the free volume concept. Occupied volume is marked by filled circles and free volume (hole) by open circles. Snapshots are taken at different times ( $t$ ).

**Molecular motion cannot take place without the presence of holes. These holes, collectively, are called free volume.**



Specific volume ( $v$ )



Temperature ( $T$ )

$$V = V_0 + \textcircled{V_f} \text{ FREE VOLUME THEORY}$$

FRACTIONAL FREE VOLUME

$$f = \frac{V_f}{V}$$

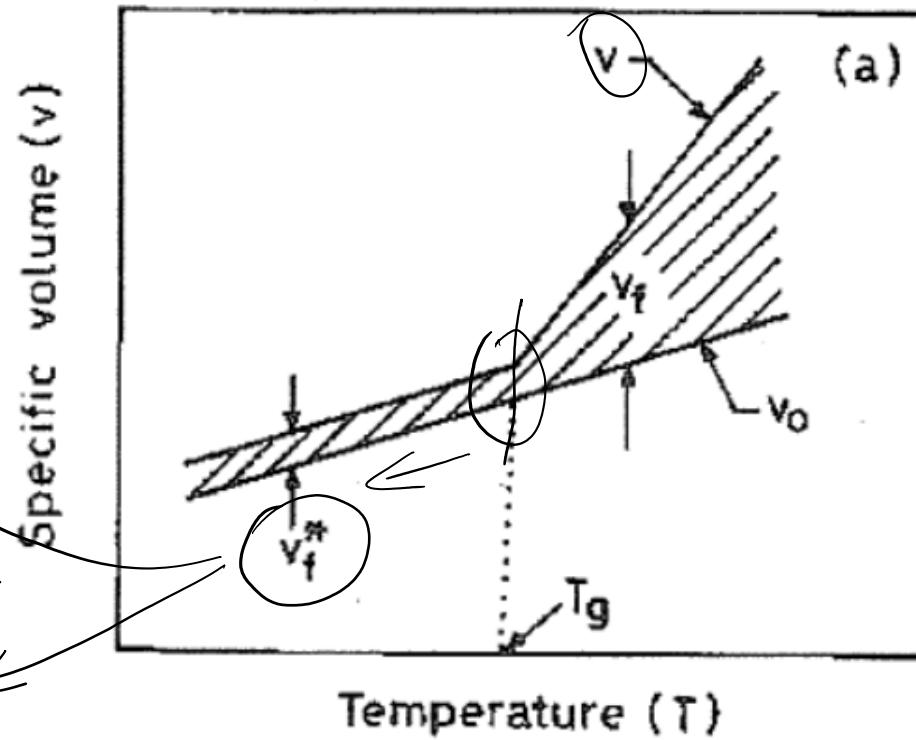


$$v = \textcircled{v_0} + \textcircled{v_f}$$



$$f_g = \frac{v_x}{v}$$

constant



$$T > T_2$$

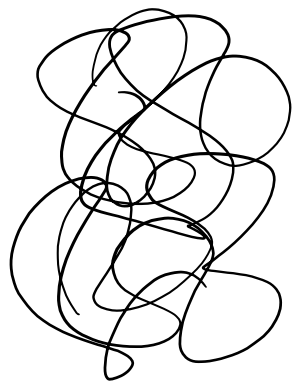
$$\Rightarrow \underline{v_f} = \left[ v_f^* + (T - T_g)(\partial v / \partial T) \right] \frac{1}{v}$$

Dividing through by  $v$  gives

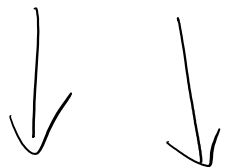
$$\underline{\underline{f_T = f_g + (T - T_g)\alpha_f}}$$



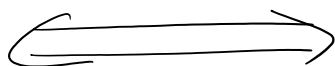
# Effect of molecular weight on Tg



$$f = f^0 + \frac{C_2}{M}$$

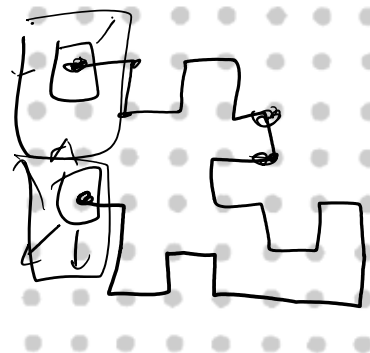


$$f \approx (C_3 + C_4 T) + \frac{C_2}{M}$$

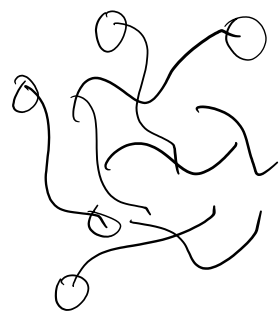
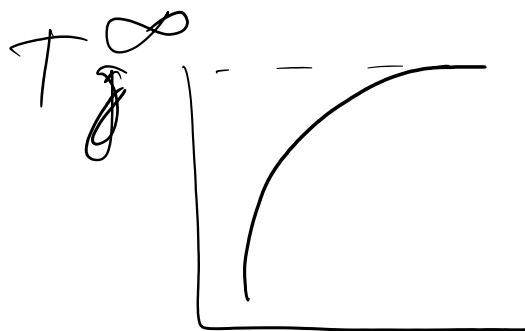


$$f_g \approx C_3 + C_4 T_g + \frac{C_2}{M}$$

$$T_g \approx \frac{f_g - C_3}{C_4} - \frac{C_2}{C_4 M} = C_5 - \frac{C_6}{M}$$



$$f_e \propto \frac{1}{M} = \frac{C_2}{M}$$



$V_g^*$

$f_g$

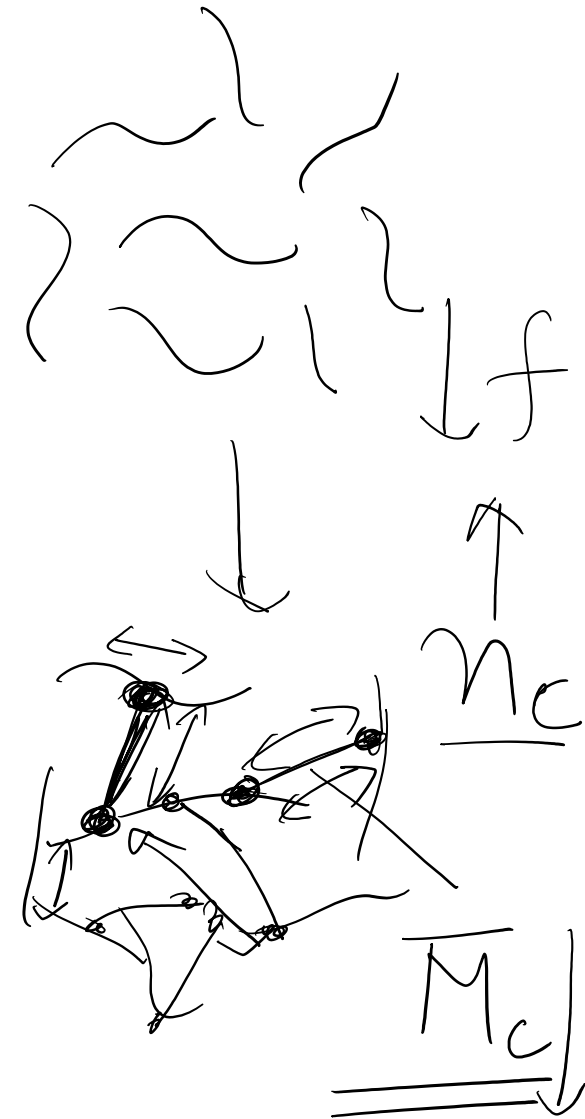
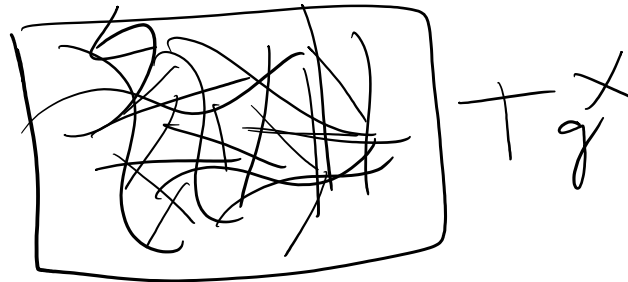


## Effect of crosslinking on Tg

$$\underline{f \approx f^0 - n_c C_7 = f^0 - \frac{C_8}{\bar{M}_c}}$$

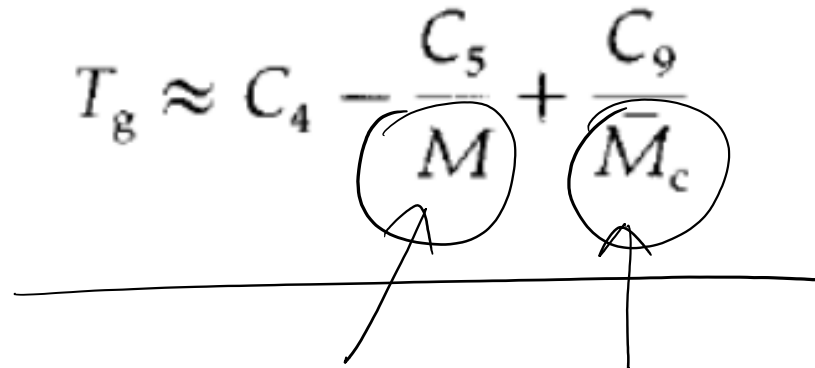


$$\underline{T_g \approx C_9 + \frac{C_{10}}{\bar{M}_c}}$$





**In a polymer which, prior to curing, has a molar mass of  $M$ , following glass transition equation is obtained:**

$$T_g \approx C_4 - \frac{C_5}{M} + \frac{C_9}{M_c}$$




## Isothermal Volume Recovery / Physical Aging

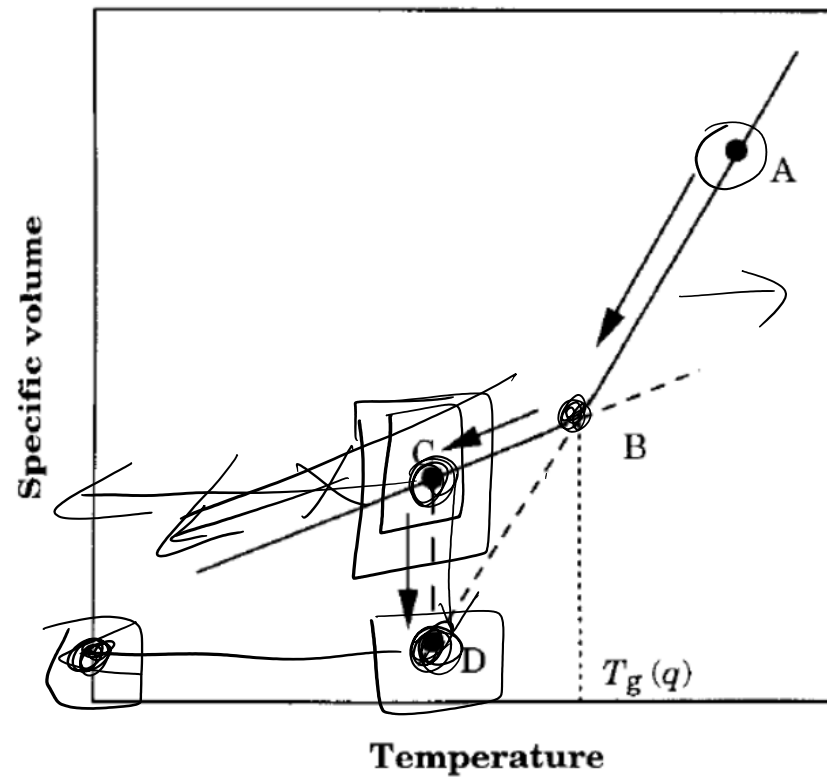
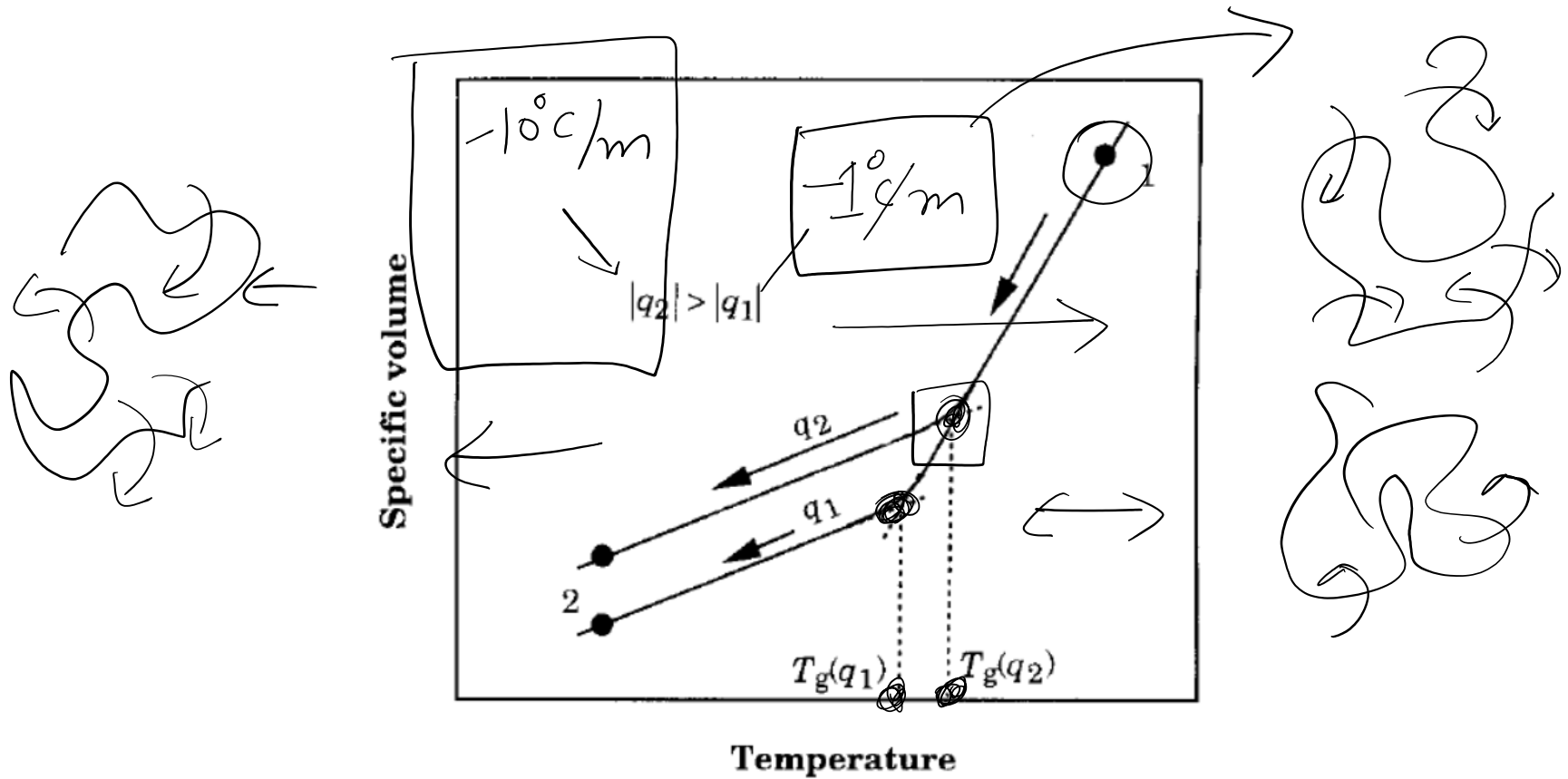


Illustration of the non-equilibrium nature of a glassy polymer.



## Dependence of $T_g$ on rate of cooling



Schematic curves showing the cooling rate dependence of the specific volume of a glass-forming wholly amorphous polymer.

