Process System Engineering #3

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1 Theory

Given reaction rate constant k as a function of temperature. Constant temperature condition therefore k is common in all reactor.

mole balance on reactor 1, with flow rate v, reactor size V, and monomar concentration C_n ,

$$C_0 v - k C_1 V = C_1 v, \tag{1}$$

$$\frac{C_1}{C_0} = \frac{v}{v + kV},\tag{2}$$

mole balance on reactor 2,

$$C_1 v - k C_2 V = C_2 v, (3)$$

$$\frac{C_2}{C_0} = \frac{C_2}{C_1} \frac{C_1}{C_0} = \left(\frac{v}{v + kV}\right)^2,\tag{4}$$

therefore,

$$\frac{C_n}{C_0} = \left(\frac{v}{v + kV}\right)^n,\tag{5}$$

In terms of weight fraction of monomar γ_n ,

$$\frac{\gamma_n}{\gamma_0} = \left(\frac{v}{v + kV}\right)^n,\tag{6}$$

therefore,

$$1 - \zeta = \frac{\gamma_N}{\gamma_0} = \left(\frac{v}{v + kV}\right)^N, \qquad (7)$$

$$\therefore \frac{v}{v + kV} = (1 - \zeta)^{\frac{1}{N}} \qquad (8)$$

$$\therefore \frac{v}{v + kV} = (1 - \zeta)^{\frac{1}{N}} \tag{8}$$

Algorithm $\mathbf{2}$

Power consumption P of each reactor is defined by γ_{in} , γ_{out} , and invariable conditions (e.g. ρ , ΔH , etc.)

therefore the structure of the source program is,

```
class Plant
  initialize(N, gamma_0, T2)
  reactor(gamma_in, gamma_out)
plant = Plant.new(N, gamma_0, T2)
plant.calc()
```

In initialize() function, we setup

- viscosity μ
- flow rate v
- \bullet reactor size V
- $\bullet\,$ diameter of reactor D
- \bullet height of reactor H

based on the method of Home Task #1. Given reactor size V is calculated by,

$$V = \frac{v\tau}{N},\tag{9}$$

In reactor() function, we calculate

- $\bullet\,$ heat transfer rate h
- \bullet dimentionless numbers Pr, Nu, Re
- ullet revolution number n
- \bullet power consumption P

In calc() function,

- 1. calculate γ_n by equation (8)
- 2. call reactor(γ_{n-1} , γ_n) from n=1 to n=N
- 3. output total power consumption P_{tot}

3 Result

```
(1)N = 1, \gamma_0 = 0.05
```

Use listing 1,

```
$ ruby plant.rb
input n[-], gamma_0[wt%], T2[K]
1
0.05
258
Conditions:
(N, gamma_0, T2)=(1, 0.05, 258)
Reactor Size
V = 514.706[m3]
D = 7.959[m]
H = 10.346[m]
Result:
#1
Re = 6893.441
n = 0.316[rps]
P = 32745.985[W]
Total:
Ptot = 32745.985[W]
```

volume	$514.706{\rm m}^3$
$\operatorname{diameter}$	$7.959\mathrm{m}$
height	$10.346\mathrm{m}$
total power consumption	$32{,}745.985\mathrm{W}$

Table 1: Result in $(N, \gamma_0, T_2) = (1, 0.05, 258)$

```
(2)N = 3, \gamma_0 = 0.04
```

Use listing 1,

```
$ ruby reactor.rb
input n[-], gamma_0[wt%], T2[K]
3
0.04
258
Conditions:
(N, gamma_0, T2)=(3, 0.04, 258)
Reactor Size:
V = 214.461[m3]
D = 5.944[m]
H = 7.728[m]
Results:
#1
Re = 3446.108
n = 0.229[rps]
P = 3542.243[W]
#2
Re = 2179.51
n = 0.145[rps]
P = 1018.779[W]
#3
Re = 1378.443
n = 0.092[rps]
P = 293.009[W]
Total:
Ptot = 4854.031[W]
```

volume	$214.461\mathrm{m}^3$		
$\operatorname{diameter}$	$5.944\mathrm{m}$		
height	$7.728\mathrm{m}$		
total power consumption	$4854.031{\rm W}$		

Table 2: Result in $(N, \gamma_0, T_2) = (3, 0.04, 258)$

(3)N = 1to5, $\gamma_0 = 0.02$ to0.10

Use listing 2,

```
$ ruby plant-advanced.rb
2.47   1.25  0.75  0.52  0.38
6.92  3.5  2.11  1.45  1.07
15.9  8.04  4.85  3.33  2.46
32.75  16.55  9.99  6.85  5.07
62.92  31.8  19.21  13.16  9.75
115.28  58.26  35.19  24.11  17.86
203.95  103.08  62.25  42.65  31.61
351.32  177.56  107.23  73.47  54.45
592.59  299.51  180.87  123.93  91.84
```

	N					
γ_0	1	2	3	4	5	
0.02	2.47	1.25	0.75	0.52	0.38	
0.03	6.92	3.5	2.11	1.45	1.07	
0.04	15.9	8.04	4.85	3.33	2.46	
0.05	32.75	16.55	9.99	6.85	5.07	
0.06	62.92	31.8	19.21	13.16	9.75	
0.07	115.28	58.26	35.19	24.11	17.86	
0.08	203.95	103.08	62.25	42.65	31.61	
0.09	351.32	177.56	107.23	73.47	54.45	
0.10	592.59	299.51	180.87	123.93	91.84	

Table 3: Power Consumption P[kW] in each condition

4 Source Program

Listing 1: plant.rb

```
1 include Math
3 \text{ GP} = (63.0*1000/24) \text{ # product flow rate [kg h-1]}
4 ML = 50.0 # polymer length
5 TAU = 5.0 # residence time
6 \text{ RHO} = 850.0 \# \text{ density [kg m-3]}
7 ALPHA = 1.3 # height/diameter of reactor
8\, HP = (72.8*1000) # heat of polymerization [J mol-1]
9 \text{ CV} = 0.6 \text{ \# conversion}
10 \text{ T1} = (273+50) \# [K]
11 TC = 0.128 \# thermal conductivity [W m-1 K-1]
12 CP = (1.68*1000) # specific heat of toluene [J kg-1 K-1]
13 M = 54.0 # molecular weight of butadiene [g mol-1]
14
15 class Plant
     def initialize(n, feed, coolant)
16
       @n = n # number of reactors [-]
17
       @feed = feed # feed [wt%]
18
       @visc = ((ML)**1.7)*(CV**2.5)*exp(21.0*feed)*1e-3 # viscosity [
19
20
       @rate = GP/(RHO*CV*feed) # feed speed [m3 h-1]
21
       @volume = @rate*TAU/n # [m3]
22
       @diameter = (@volume/(ALPHA*2*PI))**(1/3.0)*2 # [m]
       @height = @diameter*ALPHA # [m]
23
       @coolant = coolant # T2 [K]
24
25
     end
26
     def calc()
27
28
       tpc = 0 # total power consumption [W]
       prop = (1-CV)**(1.0/@n) # proportional constant [-]
29
30
       # show conditions
31
32
       puts "Conditions:"
       puts "(N,_{\square}gamma_0,_{\square}T2)="+
33
         "("+@n.to_s+",_{\sqcup}"+@feed.to_s+",_{\sqcup}"+@coolant.to_s+")"
34
35
       # show reactor size
36
       puts "Reactor_Size:"
37
       puts V_{\perp}=_{\perp}+0volume.round(3).to_s+[m3]"
38
       puts "D_{\sqcup}=_{\sqcup}"+@diameter.round(3).to_s+"[m]"
39
       puts "H_{\sqcup}=_{\sqcup}"+@height.round(3).to_s+"[m]"
40
42
       # show result of each reactor
43
       puts "Results:"
44
       for n in 1..@n
         puts "#"+n.to_s
45
         tpc += reactor(@feed*(prop**(n-1)),@feed*(prop**n))
46
47
       end
48
       # show total power consumption
49
```

```
puts "Total:"
50
        puts "Ptot_{\sqcup}=_{\sqcup}"+tpc.round(3).to_{s}+"[W]"
51
52
53
      def reactor(gamma_in, gamma_out)
54
55
        # heat transfer rate
        \label{eq:hamma_in-gamma_out)*1000/3600)/M/(@diameter*)} h = HP*(@rate*RHO*(gamma_in-gamma_out)*1000/3600)/M/(@diameter*)
56
             PI*@height)/(T1-@coolant)
57
        # dimensionless numbers
58
        pr = @visc*CP/TC
59
        nu = h*@diameter/TC
60
        re = (2*nu/pr**(1/3.0))**1.5
61
        puts "Re_{\square} = "+re.round(3).to_s
62
63
        # revolution number
64
65
        revnum = re*@visc/RHO/(@diameter/2)**2
66
        puts "n_=_"+revnum.round(3).to_s+"[rps]"
67
        # power consumption
68
        np = 14.6*re**(-0.28)
69
        p = np*RH0*(revnum**3)*(@diameter/2)**5
70
        puts "P_{\sqcup}=_{\sqcup}"+p.round(3).to_s+"[W]"
71
72
73
        return p
      end
74
75 end
76
77 puts "input_{\square}n[-],_{\square}gamma_{\square}0[wt_{\square}],_{\square}T2[K]"
78 n = gets.to_i
79 feed = gets.to_f
80 coolant = gets.to_i
81
82 plant = Plant.new(n, feed, coolant)
83 plant.calc()
```

Listing 2: plant-advanced.rb

```
1 include Math
3 \text{ GP} = (63.0*1000/24) \text{ # product flow rate [kg h-1]}
4 ML = 50.0 # polymer length
5 TAU = 5.0 # residence time
6 RHO = 850.0 # density [kg m-3]
7 ALPHA = 1.3 # height/diameter of reactor
8 HP = (72.8*1000) # heat of polymerization [J mol-1]
9 \text{ CV} = 0.6 \text{ \# conversion}
10 \text{ T1} = (273+50) \# [K]
11 TC = 0.128 \# thermal conductivity [W m-1 K-1]
12 CP = (1.68*1000) # specific heat of toluene [J kg-1 K-1]
13 M = 54.0 # molecular weight of butadiene [g mol-1]
14
15 class Plant
     def initialize(n, feed, coolant)
16
       @n = n # number of reactors [-]
17
       @feed = feed # feed [wt%]
18
       @visc = ((ML)**1.7)*(CV**2.5)*exp(21.0*feed)*1e-3 # viscosity [
19
           Pa s]
20
       @rate = GP/(RHO*CV*feed) # flow rate [m3 h-1]
21
       @volume = @rate*TAU/n # [m3]
22
       @diameter = (@volume/(ALPHA*2*PI))**(1/3.0)*2 # [m]
23
       @height = @diameter*ALPHA # [m]
24
       @coolant = coolant # T2 [K]
25
     end
26
     def calc()
27
       tpc = 0 # total power consumption [W]
28
       prop = (1-CV)**(1.0/@n) # proportional constant [-]
29
31
       for n in 1..@n
        tpc += reactor(@feed*(prop**(n-1)),@feed*(prop**n))
32
33
34
       return ((tpc)/1000).round(2)
35
     end
36
37
     def reactor(gamma_in, gamma_out)
38
39
       # heat transfer rate
       h = HP*(@rate*RHO*(gamma_in-gamma_out)*1000/3600)/M/(@diameter*
40
           PI*@height)/(T1-@coolant)
41
42
       # dimensionless numbers
43
       pr = @visc*CP/TC
       nu = h*@diameter/TC
44
      re = (2*nu/pr**(1/3.0))**1.5
45
46
       # revolution number
47
       revnum = re*@visc/RHO/(@diameter/2)**2
48
       # power consumption
       np = 14.6*re**(-0.28)
```

```
p = np*RHO*(revnum**3)*(@diameter/2)**5
52
53
54
    return p
   end
55
56 end
57
58 coolant = 258
59 for feed in 2..10
60 f = feed*0.01
61
   for n in 1..5
    plant = Plant.new(n, f, coolant)
62
    print plant.calc().to_s + "\t"
63
   end
64
65 print "\n"
66 end
```