

	Trend	Seasonal		
		N	A	M
Nao Aditiva	N	$\ell_t = \alpha y_t + (1 - \alpha)\ell_{t-1}$ $\hat{y}_{t+h t} = \ell_t$	$\ell_t = \alpha(y_t - s_{t-m}) + (1 - \alpha)\ell_{t-1}$ $s_t = \gamma(y_t - \ell_{t-1}) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t + s_{t-m+h_m^+}$	$\ell_t = \alpha(y_t / s_{t-m}) + (1 - \alpha)\ell_{t-1}$ $s_t = \gamma(y_t / \ell_{t-1}) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t s_{t-m+h_m^+}$
	A	$\ell_t = \alpha y_t + (1 - \alpha)(\ell_{t-1} + b_{t-1})$ $b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)b_{t-1}$ $\hat{y}_{t+h t} = \ell_t + hb_t$	$\ell_t = \alpha(y_t - s_{t-m}) + (1 - \alpha)(\ell_{t-1} + b_{t-1})$ $b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)b_{t-1}$ $s_t = \gamma(y_t - \ell_{t-1} - b_{t-1}) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t + hb_t + s_{t-m+h_m^+}$	$\ell_t = \alpha(y_t / s_{t-m}) + (1 - \alpha)(\ell_{t-1} + b_{t-1})$ $b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)b_{t-1}$ $s_t = \gamma(y_t / (\ell_{t-1} + b_{t-1})) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = (\ell_t + hb_t)s_{t-m+h_m^+}$
	A _d	$\ell_t = \alpha y_t + (1 - \alpha)(\ell_{t-1} + \phi b_{t-1})$ $b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)\phi b_{t-1}$ $\hat{y}_{t+h t} = \ell_t + \phi_h b_t$	$\ell_t = \alpha(y_t - s_{t-m}) + (1 - \alpha)(\ell_{t-1} + \phi b_{t-1})$ $b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)\phi b_{t-1}$ $s_t = \gamma(y_t - \ell_{t-1} - \phi b_{t-1}) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t + \phi_h b_t + s_{t-m+h_m^+}$	$\ell_t = \alpha(y_t / s_{t-m}) + (1 - \alpha)(\ell_{t-1} + \phi b_{t-1})$ $b_t = \beta^*(\ell_t - \ell_{t-1}) + (1 - \beta^*)\phi b_{t-1}$ $s_t = \gamma(y_t / (\ell_{t-1} + \phi b_{t-1})) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = (\ell_t + \phi_h b_t)s_{t-m+h_m^+}$
	M	$\ell_t = \alpha y_t + (1 - \alpha)\ell_{t-1}b_{t-1}$ $b_t = \beta^*(\ell_t / \ell_{t-1}) + (1 - \beta^*)b_{t-1}$ $\hat{y}_{t+h t} = \ell_t b_t^h$	$\ell_t = \alpha(y_t - s_{t-m}) + (1 - \alpha)\ell_{t-1}b_{t-1}$ $b_t = \beta^*(\ell_t / \ell_{t-1}) + (1 - \beta^*)b_{t-1}$ $s_t = \gamma(y_t - \ell_{t-1}b_{t-1}) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t b_t^h + s_{t-m+h_m^+}$	$\ell_t = \alpha(y_t / s_{t-m}) + (1 - \alpha)\ell_{t-1}b_{t-1}$ $b_t = \beta^*(\ell_t / \ell_{t-1}) + (1 - \beta^*)b_{t-1}$ $s_t = \gamma(y_t / (\ell_{t-1}b_{t-1})) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t b_t^h s_{t-m+h_m^+}$
	M _d	$\ell_t = \alpha y_t + (1 - \alpha)\ell_{t-1}b_{t-1}^\phi$ $b_t = \beta^*(\ell_t / \ell_{t-1}) + (1 - \beta^*)b_{t-1}^\phi$ $\hat{y}_{t+h t} = \ell_t b_t^{\phi_h}$	$\ell_t = \alpha(y_t - s_{t-m}) + (1 - \alpha)\ell_{t-1}b_{t-1}^\phi$ $b_t = \beta^*(\ell_t / \ell_{t-1}) + (1 - \beta^*)b_{t-1}^\phi$ $s_t = \gamma(y_t - \ell_{t-1}b_{t-1}^\phi) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t b_t^{\phi_h} + s_{t-m+h_m^+}$	$\ell_t = \alpha(y_t / s_{t-m}) + (1 - \alpha)\ell_{t-1}b_{t-1}^\phi$ $b_t = \beta^*(\ell_t / \ell_{t-1}) + (1 - \beta^*)b_{t-1}^\phi$ $s_t = \gamma(y_t / (\ell_{t-1}b_{t-1}^\phi)) + (1 - \gamma)s_{t-m}$ $\hat{y}_{t+h t} = \ell_t b_t^{\phi_h} s_{t-m+h_m^+}$

In each case, ℓ_t denotes the series level at time t , b_t denotes the slope at time t , s_t denotes the seasonal component of the series at time t , and m denotes the number of seasons in a year; α , β^* , γ and ϕ are constants, $\phi_h = \phi + \phi^2 + \dots + \phi^h$ and $h_m^+ = [(h - 1) \bmod m] + 1$.

Erro aditivo: modelos resultantes

Trend	Seasonal		
	N	A	M
N	$\mu_t = \ell_{t-1}$ $\ell_t = \ell_{t-1} + \alpha \varepsilon_t$	$\mu_t = \ell_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1} + \alpha \varepsilon_t$ $s_t = s_{t-m} + \gamma \varepsilon_t$	$\mu_t = \ell_{t-1} s_{t-m}$ $\ell_t = \ell_{t-1} + \alpha \varepsilon_t / s_{t-m}$ $s_t = s_{t-m} + \gamma \varepsilon_t / \ell_{t-1}$
A	$\mu_t = \ell_{t-1} + b_{t-1}$ $\ell_t = \ell_{t-1} + b_{t-1} + \alpha \varepsilon_t$ $b_t = b_{t-1} + \beta \varepsilon_t$	$\mu_t = \ell_{t-1} + b_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1} + b_{t-1} + \alpha \varepsilon_t$ $b_t = b_{t-1} + \beta \varepsilon_t$ $s_t = s_{t-m} + \gamma \varepsilon_t$	$\mu_t = (\ell_{t-1} + b_{t-1}) s_{t-m}$ $\ell_t = \ell_{t-1} + b_{t-1} + \alpha \varepsilon_t / s_{t-m}$ $b_t = b_{t-1} + \beta \varepsilon_t / s_{t-m}$ $s_t = s_{t-m} + \gamma \varepsilon_t / (\ell_{t-1} + b_{t-1})$
A _d	$\mu_t = \ell_{t-1} + \phi b_{t-1}$ $\ell_t = \ell_{t-1} + \phi b_{t-1} + \alpha \varepsilon_t$ $b_t = \phi b_{t-1} + \beta \varepsilon_t$	$\mu_t = \ell_{t-1} + \phi b_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1} + \phi b_{t-1} + \alpha \varepsilon_t$ $b_t = \phi b_{t-1} + \beta \varepsilon_t$ $s_t = s_{t-m} + \gamma \varepsilon_t$	$\mu_t = (\ell_{t-1} + \phi b_{t-1}) s_{t-m}$ $\ell_t = \ell_{t-1} + \phi b_{t-1} + \alpha \varepsilon_t / s_{t-m}$ $b_t = \phi b_{t-1} + \beta \varepsilon_t / s_{t-m}$ $s_t = s_{t-m} + \gamma \varepsilon_t / (\ell_{t-1} + \phi b_{t-1})$
M	$\mu_t = \ell_{t-1} b_{t-1}$ $\ell_t = \ell_{t-1} b_{t-1} + \alpha \varepsilon_t$ $b_t = b_{t-1} + \beta \varepsilon_t / \ell_{t-1}$	$\mu_t = \ell_{t-1} b_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1} b_{t-1} + \alpha \varepsilon_t$ $b_t = b_{t-1} + \beta \varepsilon_t / \ell_{t-1}$ $s_t = s_{t-m} + \gamma \varepsilon_t$	$\mu_t = \ell_{t-1} b_{t-1} s_{t-m}$ $\ell_t = \ell_{t-1} b_{t-1} + \alpha \varepsilon_t / s_{t-m}$ $b_t = b_{t-1} + \beta \varepsilon_t / (s_{t-m} \ell_{t-1})$ $s_t = s_{t-m} + \gamma \varepsilon_t / (\ell_{t-1} b_{t-1})$
M _d	$\mu_t = \ell_{t-1} b_{t-1}^\phi$ $\ell_t = \ell_{t-1} b_{t-1}^\phi + \alpha \varepsilon_t$ $b_t = b_{t-1}^\phi + \beta \varepsilon_t / \ell_{t-1}$	$\mu_t = \ell_{t-1} b_{t-1}^\phi + s_{t-m}$ $\ell_t = \ell_{t-1} b_{t-1}^\phi + \alpha \varepsilon_t$ $b_t = b_{t-1}^\phi + \beta \varepsilon_t / \ell_{t-1}$ $s_t = s_{t-m} + \gamma \varepsilon_t$	$\mu_t = \ell_{t-1} b_{t-1}^\phi s_{t-m}$ $\ell_t = \ell_{t-1} b_{t-1}^\phi + \alpha \varepsilon_t / s_{t-m}$ $b_t = b_{t-1}^\phi + \beta \varepsilon_t / (s_{t-m} \ell_{t-1})$ $s_t = s_{t-m} + \gamma \varepsilon_t / (\ell_{t-1} b_{t-1}^\phi)$

Erro multiplicativo: modelos resultantes

Trend	Seasonal		
	N	A	M
N	$\mu_t = \ell_{t-1}$ $\ell_t = \ell_{t-1}(1 + \alpha\epsilon_t)$	$\mu_t = \ell_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1} + \alpha(\ell_{t-1} + s_{t-m})\epsilon_t$ $s_t = s_{t-m} + \gamma(\ell_{t-1} + s_{t-m})\epsilon_t$	$\mu_t = \ell_{t-1}s_{t-m}$ $\ell_t = \ell_{t-1}(1 + \alpha\epsilon_t)$ $s_t = s_{t-m}(1 + \gamma\epsilon_t)$
A	$\mu_t = \ell_{t-1} + b_{t-1}$ $\ell_t = (\ell_{t-1} + b_{t-1})(1 + \alpha\epsilon_t)$ $b_t = b_{t-1} + \beta(\ell_{t-1} + b_{t-1})\epsilon_t$	$\mu_t = \ell_{t-1} + b_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1} + b_{t-1} + \alpha(\ell_{t-1} + b_{t-1} + s_{t-m})\epsilon_t$ $b_t = b_{t-1} + \beta(\ell_{t-1} + b_{t-1} + s_{t-m})\epsilon_t$ $s_t = s_{t-m} + \gamma(\ell_{t-1} + b_{t-1} + s_{t-m})\epsilon_t$	$\mu_t = (\ell_{t-1} + b_{t-1})s_{t-m}$ $\ell_t = (\ell_{t-1} + b_{t-1})(1 + \alpha\epsilon_t)$ $b_t = b_{t-1} + \beta(\ell_{t-1} + b_{t-1})\epsilon_t$ $s_t = s_{t-m}(1 + \gamma\epsilon_t)$
A _d	$\mu_t = \ell_{t-1} + \phi b_{t-1}$ $\ell_t = (\ell_{t-1} + \phi b_{t-1})(1 + \alpha\epsilon_t)$ $b_t = \phi b_{t-1} + \beta(\ell_{t-1} + \phi b_{t-1})\epsilon_t$	$\mu_t = \ell_{t-1} + \phi b_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1} + \phi b_{t-1} + \alpha(\ell_{t-1} + \phi b_{t-1} + s_{t-m})\epsilon_t$ $b_t = \phi b_{t-1} + \beta(\ell_{t-1} + \phi b_{t-1} + s_{t-m})\epsilon_t$ $s_t = s_{t-m} + \gamma(\ell_{t-1} + \phi b_{t-1} + s_{t-m})\epsilon_t$	$\mu_t = (\ell_{t-1} + \phi b_{t-1})s_{t-m}$ $\ell_t = (\ell_{t-1} + \phi b_{t-1})(1 + \alpha\epsilon_t)$ $b_t = \phi b_{t-1} + \beta(\ell_{t-1} + \phi b_{t-1})\epsilon_t$ $s_t = s_{t-m}(1 + \gamma\epsilon_t)$
M	$\mu_t = \ell_{t-1}b_{t-1}$ $\ell_t = \ell_{t-1}b_{t-1}(1 + \alpha\epsilon_t)$ $b_t = b_{t-1}(1 + \beta\epsilon_t)$	$\mu_t = \ell_{t-1}b_{t-1} + s_{t-m}$ $\ell_t = \ell_{t-1}b_{t-1} + \alpha(\ell_{t-1}b_{t-1} + s_{t-m})\epsilon_t$ $b_t = b_{t-1} + \beta(\ell_{t-1}b_{t-1} + s_{t-m})\epsilon_t / \ell_{t-1}$ $s_t = s_{t-m} + \gamma(\ell_{t-1}b_{t-1} + s_{t-m})\epsilon_t$	$\mu_t = \ell_{t-1}b_{t-1}s_{t-m}$ $\ell_t = \ell_{t-1}b_{t-1}(1 + \alpha\epsilon_t)$ $b_t = b_{t-1}(1 + \beta\epsilon_t)$ $s_t = s_{t-m}(1 + \gamma\epsilon_t)$
M _d	$\mu_t = \ell_{t-1}b_{t-1}^\phi$ $\ell_t = \ell_{t-1}b_{t-1}^\phi(1 + \alpha\epsilon_t)$ $b_t = b_{t-1}^\phi(1 + \beta\epsilon_t)$	$\mu_t = \ell_{t-1}b_{t-1}^\phi + s_{t-m}$ $\ell_t = \ell_{t-1}b_{t-1}^\phi + \alpha(\ell_{t-1}b_{t-1}^\phi + s_{t-m})\epsilon_t$ $b_t = b_{t-1}^\phi + \beta(\ell_{t-1}b_{t-1}^\phi + s_{t-m})\epsilon_t / \ell_{t-1}$ $s_t = s_{t-m} + \gamma(\ell_{t-1}b_{t-1}^\phi + s_{t-m})\epsilon_t$	$\mu_t = \ell_{t-1}b_{t-1}^\phi s_{t-m}$ $\ell_t = \ell_{t-1}b_{t-1}^\phi(1 + \alpha\epsilon_t)$ $b_t = b_{t-1}^\phi(1 + \beta\epsilon_t)$ $s_t = s_{t-m}(1 + \gamma\epsilon_t)$