Package 'IBclust'

August 27, 2025

Title Information Bottleneck Methods for Clustering Mixed-Type Data Version 1.2.1 Description Implements multiple variants of the Information Bottleneck (TB') method for clustering datasets containing continuous, categorical (nominal/ordinal) and mixed-type variables. The package provides deterministic, agglomerative, generalized, and standard TB' clustering algorithms that preserve relevant information while forming interpretable clusters. The Deterministic Information Bottleneck is described in Costa et al. (2024) <doi:10.48550 arxiv.2407.03389="">. The standard 'IB' method originates from Tishby et al. (2000) <doi:10.48550 0004057="" arxiv.physics="">, the agglomerative variant from Slonium and Tishby (1999) https://papers.nips.cc/paper/1651-agglomerative-information-bottleneck, and the generalized 'IB' from Strouse and Schwab (2017) <doi:10.1162 neco_a_00961="">. License GPL (>= 3) Encoding UTF-8 Depends R (>= 3.5.0) Imports Repp, stats, utils, np, rje, Rdpack, ReppEigen Suggests mclust Linking To Repp, ReppArmadillo, ReppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],</doi:10.1162></doi:10.48550></doi:10.48550>	Type Package
Description Implements multiple variants of the Information Bottleneck ('IB') method for clustering datasets containing continuous, categorical (nominal/ordinal) and mixed-type variables. The package provides deterministic, agglomerative, generalized, and standard 'IB' clustering algorithms that preserve relevant information while forming interpretable clusters. The Deterministic Information Bottleneck is described in Costa et al. (2024) cdoi:10.48550/arXiv.2407.03389 . The standard 'IB' method originates from Tishby et al. (2000) <doi:10.48550 0004057="" arxiv.physics="">, the agglomerative variant from Slonim and Tishby (1999) chittps://papers.nips.cc/paper/1651-agglomerative-information-bottleneck, and the generalized 'IB' from Strouse and Schwab (2017) <doi:10.1162 neco_a_00961="">. License GPL (>= 3) Encoding UTF-8 Depends R (>= 3.5.0) Imports Rcpp, stats, utils, np, rje, Rdpack, RcppEigen Suggests mclust LinkingTo Rcpp, RcppArmadillo, RcppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],</doi:10.1162></doi:10.48550>	Title Information Bottleneck Methods for Clustering Mixed-Type Data
for clustering datasets containing continuous, categorical (nominal/ordinal) and mixed-type variables. The package provides deterministic, agglomerative, generalized, and standard 'IB' clustering algorithms that preserve relevant information while forming interpretable clusters. The Deterministic Information Bottleneck is described in Costa et al. (2024) <doi: 10.48550="" arxiv.2407.03389="">. The standard 'IB' method originates from Tishby et al. (2000) <doi: 0004057="" 10.48550="" arxiv.physics="">, the agglomerative variant from Slonim and Tishby (1999) https://papers.nips.cc/paper/1651-agglomerative-information-bottleneck, and the generalized 'IB' from Strouse and Schwab (2017) <doi:10.1162 neco_a_00961="">. License GPL (>= 3) Encoding UTF-8 Depends R (>= 3.5.0) Imports Rcpp, stats, utils, np, rje, Rdpack, RcppEigen Suggests mclust LinkingTo Rcpp, RcppArmadillo, RcppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],</doi:10.1162></doi:></doi:>	Version 1.2.1
Encoding UTF-8 Depends R (>= 3.5.0) Imports Rcpp, stats, utils, np, rje, Rdpack, RcppEigen Suggests mclust LinkingTo Rcpp, RcppArmadillo, RcppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],	for clustering datasets containing continuous, categorical (nominal/ordinal) and mixed-type variables. The package provides deterministic, agglomerative, generalized, and standard 'IB' clustering algorithms that preserve relevant information while forming interpretable clusters. The Deterministic Information Bottleneck is described in Costa et al. (2024) <doi:10.48550 arxiv.2407.03389="">. The standard 'IB' method originates from Tishby et al. (2000) <doi:10.48550 0004057="" arxiv.physics="">, the agglomerative variant from Slonim and Tishby (1999) <https: 1651-agglomerative-information-bottleneck="" paper="" papers.nips.cc="">,</https:></doi:10.48550></doi:10.48550>
Depends R (>= 3.5.0) Imports Rcpp, stats, utils, np, rje, Rdpack, RcppEigen Suggests mclust LinkingTo Rcpp, RcppArmadillo, RcppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],	
Imports Rcpp, stats, utils, np, rje, Rdpack, RcppEigen Suggests mclust LinkingTo Rcpp, RcppArmadillo, RcppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],	-
Suggests mclust LinkingTo Rcpp, RcppArmadillo, RcppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],	
LinkingTo Rcpp, RcppArmadillo, RcppEigen RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],	Imports Rcpp, stats, utils, np, rje, Rdpack, RcppEigen
RoxygenNote 7.3.2 RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],	Suggests mclust
RdMacros Rdpack NeedsCompilation yes Author Efthymios Costa [aut],	LinkingTo Rcpp, RcppArmadillo, RcppEigen
NeedsCompilation yes Author Efthymios Costa [aut],	RoxygenNote 7.3.2
Author Efthymios Costa [aut],	RdMacros Rdpack
Ioanna Papatsouma [aut], Angelos Markos [aut, cre] Maintainer Angelos Markos <amarkos@gmail.com> Archs x64 Contents AIBmix DIBmix GIBmix IBmix 1</amarkos@gmail.com>	NeedsCompilation yes
Archs x64 Contents AIBmix DIBmix GIBmix IBmix 1	Ioanna Papatsouma [aut],
Contents AIBmix DIBmix GIBmix GIBmix 1	Maintainer Angelos Markos <amarkos@gmail.com></amarkos@gmail.com>
AIBmix DIBmix GIBmix 1 IBmix	Archs x64
AIBmix DIBmix GIBmix 1 IBmix	
DIBmix GIBmix IBmix 1	Contents
l I	DIBmix

AIBmix	Agglomerative Data	Information	Bottleneck	Clustering	for	Mixed-Type	
	Data						

Description

The AIBmix function implements the Agglomerative Information Bottleneck (AIB) algorithm for hierarchical clustering of datasets containing mixed-type variables, including categorical (nominal and ordinal) and continuous variables. This method merges clusters so that information retention is maximised at each step to create meaningful clusters, leveraging bandwidth parameters to handle different categorical data types (nominal and ordinal) effectively (Slonim and Tishby 1999).

Usage

Arguments

s

lambda

scale

contkernel

nomkernel

ordkernel

cat_first

Χ	A data frame containing the data to be clustered. Variables should be of type
	numeric (for continuous variables), factor (for nominal variables) or ordered
	(for ordinal variables).

A numeric value or vector specifying the bandwidth parameter(s) for continuous variables. The values must be greater than 0. The default value is -1, which enables the automatic selection of optimal bandwidth(s). Argument is ignored when no variables are continuous.

A numeric value or vector specifying the bandwidth parameter for categorical variables. The default value is -1, which enables automatic determination of the optimal bandwidth. For nominal variables and nomkernel = 'aitchisonaitken', the maximum allowable value of lambda is (l-1)/l, where l represents the number of categories, whereas for nomkernel = 'liracine' the maximum allowable value is 1. For ordinal variables, the maximum allowable value of lambda is 1, regardless of what ordkernel is being used. Argument is ignored when all variables are continuous.

A logical value indicating whether the continuous variables should be scaled to have unit variance before clustering. Defaults to TRUE. Argument is ignored when all variables are categorical.

Kernel used for continuous variables. Can be one of gaussian (default) or epanechnikov. Argument is ignored when no variables are continuous.

Kernel used for nominal (unordered categorical) variables. Can be one of aitchisonaitken (default) or liracine. Argument is ignored when no variables are nominal.

Kernel used for ordinal (ordered categorical) variables. Can be one of liracine (default) or wangvanryzin. Argument is ignored when no variables are ordinal.

A logical value indicating whether bandwidth selection is prioritised for the categorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when all bandwidths are selected automatically (i.e. s =

-1, lambda = -1).

Details

The AIBmix function produces a hierarchical agglomerative clustering of the data while retaining maximal information about the original variable distributions. The Agglomerative Information Bottleneck algorithm uses an information-theoretic criterion to merge clusters so that information retention is maximised at each step, hence creating meaningful clusters with maximal information about the original distribution. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively.

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

• Gaussian (RBF) kernel (Silverman 1998):

$$K_c\left(\frac{x-x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x-x')^2}{2s^2}\right\}, \quad s > 0.$$

• Epanechnikov kernel (Epanechnikov 1969):

$$K_c(x-x';s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x-x')^2}{5s^2}\right), & \text{if } \frac{(x-x')^2}{s^2} < 5\\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

• Aitchison & Aitken kernel (Aitchison and Aitken 1976):

$$K_u(x=x';\lambda) = \begin{cases} 1-\lambda, & \text{if } x=x'\\ \frac{\lambda}{\ell-1}, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le \frac{\ell-1}{\ell}.$$

• Li & Racine kernel (Ouyang et al. 2006):

$$K_u(x=x';\lambda) = \begin{cases} 1, & \text{if } x=x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le 1.$$

For ordinal (ordered categorical) variables:

• Li & Racine kernel (Li and Racine 2003):

$$K_o(x = x'; \nu) = \begin{cases} 1, & \text{if } x = x' \\ \nu^{|x - x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

• Wang & van Ryzin kernel (Wang and Van Ryzin 1981):

$$K_o(x = x'; \nu) = \begin{cases} 1 - \nu, & \text{if } x = x' \\ \frac{1 - \nu}{2} \nu^{|x - x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

The bandwidth parameters s, λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

A list containing the following elements:

merges	A data frame with 2 columns and n rows, showing which observations are merged at each step.
merge_costs	A numeric vector tracking the cost incurred by each merge $I(Z_m; Y) - I(Z_{m-1}; Y)$.
partitions	A list containing n sub-lists. Each sub-list includes the cluster partition at each step.
I_Z_Y	A numeric vector including the mutual information $I(Z_m;Y)$ as the number of clusters m increases.
I_X_Y	A numeric value of the mutual information $I(X;Y)$ between observation indices and location.
info_ret	A numeric vector of length \boldsymbol{n} including the fraction of the original information retained after each merge.
dendrogram	A dendrogram visualising the cluster hierarchy. The height is determined by the cost of cluster merges.
S	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
lambda	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.

Author(s)

Efthymios Costa, Ioanna Papatsouma, Angelos Markos

References

Slonim N, Tishby N (1999). "Agglomerative Information Bottleneck." *Advances in Neural Information Processing Systems*, **12**.

Aitchison J, Aitken CG (1976). "Multivariate binary discrimination by the kernel method." *Biometrika*, **63**(3), 413–420.

Li Q, Racine J (2003). "Nonparametric estimation of distributions with categorical and continuous data." *Journal of Multivariate Analysis*, **86**(2), 266–292.

Silverman BW (1998). Density Estimation for Statistics and Data Analysis (1st Ed.). Routledge.

Ouyang D, Li Q, Racine J (2006). "Cross-validation and the estimation of probability distributions with categorical data." *Journal of Nonparametric Statistics*, 18(1), 69–100.

Wang M, Van Ryzin J (1981). "A class of smooth estimators for discrete distributions." *Biometrika*, **68**(1), 301–309.

Epanechnikov VA (1969). "Non-parametric estimation of a multivariate probability density." *Theory of Probability & Its Applications*, **14**(1), 153–158.

Costa E, Papatsouma I, Markos A (2025). "A Deterministic Information Bottleneck Method for Clustering Mixed-Type Data." doi:10.48550/arXiv.2407.03389, arXiv:2407.03389, https://arxiv.org/abs/2407.03389.

Examples

```
# Example dataset with categorical, ordinal, and continuous variables
set.seed(123)
data_mix <- data.frame(</pre>
 cat_var = factor(sample(letters[1:3], 100, replace = TRUE)),
                                                                # Nominal categorical variable
  ord_var = factor(sample(c("low", "medium", "high"), 100, replace = TRUE),
                   levels = c("low", "medium", "high"),
                   ordered = TRUE),
                                                                    # Ordinal variable
  cont_var1 = rnorm(100),
                                                                  # Continuous variable 1
                                                                  # Continuous variable 2
  cont_var2 = runif(100)
# Perform Mixed-Type Hierarchical Clustering with Agglomerative IB
result_mix <- AIBmix(X = data_mix, lambda = -1, s = -1, scale = TRUE)
# Print clustering results
plot(result_mix$dendrogram, xlab = "", sub = "") # Plot dendrogram
# Simulated categorical data example
set.seed(123)
data_cat <- data.frame(</pre>
  Var1 = as.factor(sample(letters[1:3], 200, replace = TRUE)), # Nominal variable
  Var2 = as.factor(sample(letters[4:6], 200, replace = TRUE)), # Nominal variable
  Var3 = factor(sample(c("low", "medium", "high"), 200, replace = TRUE),
                levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)
# Run AIBmix with automatic lambda selection
result_cat <- AIBmix(X = data_cat, lambda = -1)</pre>
# Print clustering results
plot(result_cat$dendrogram, xlab = "", sub = "") # Plot dendrogram
# Simulated continuous data example
set.seed(123)
# Continuous data with 200 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(1000), ncol = 5))</pre>
# Run AIBmix with automatic bandwidth selection
result_cont <- AIBmix(X = data_cont, s = -1, scale = TRUE)
# Print clustering results
plot(result_cont$dendrogram, xlab = "", sub = "") # Plot dendrogram
```

DIBmix

Deterministic Information Bottleneck Clustering for Mixed-Type Data

Description

The DIBmix function implements the Deterministic Information Bottleneck (DIB) algorithm for clustering datasets containing continuous, categorical (nominal and ordinal), and mixed-type variables. This method optimizes an information-theoretic objective to preserve relevant information in the cluster assignments while achieving effective data compression (Costa et al. 2025).

Usage

```
DIBmix(X, ncl, randinit = NULL,
    s = -1, lambda = -1, scale = TRUE,
    maxiter = 100, nstart = 100,
    contkernel = "gaussian",
    nomkernel = "aitchisonaitken", ordkernel = "liracine",
    cat_first = FALSE, verbose = FALSE)
```

Arguments

X A data frame containing the input data to be clustered. It should include cate-

gorical variables (factor for nominal and ordered for ordinal) and continuous

variables (numeric).

ncl An integer specifying the number of clusters.

randinit An optional vector specifying the initial cluster assignments. If NULL, cluster

assignments are initialized randomly.

A numeric value or vector specifying the bandwidth parameter(s) for continuous variables. The values must be greater than 0. The default value is -1, which enables the automatic selection of optimal bandwidth(s). Argument is ignored

when no variables are continuous.

lambda A numeric value or vector specifying the bandwidth parameter for categorical

variables. The default value is -1, which enables automatic determination of the optimal bandwidth. For nominal variables and nomkernel = 'aitchisonaitken', the maximum allowable value of lambda is (l-1)/l, where l represents the number of categories, whereas for nomkernel = 'liracine' the maximum allowable value is 1. For ordinal variables, the maximum allowable value of lambda is 1, regardless of what ordkernel is being used. Argument is ignored when all

variables are continuous.

scale A logical value indicating whether the continuous variables should be scaled

to have unit variance before clustering. Defaults to TRUE. Argument is ignored

when all variables are categorical.

maxiter The maximum number of iterations allowed for the clustering algorithm. De-

faults to 100.

nstart The number of random initializations to run. The best clustering solution is

returned. Defaults to 100.

contkernel Kernel used for continuous variables. Can be one of gaussian (default) or

epanechnikov. Argument is ignored when no variables are continuous.

nomkernel Kernel used for nominal (unordered categorical) variables. Can be one of aitchisonaitken

(default) or liracine. Argument is ignored when no variables are nominal.

ordkernel Kernel used for ordinal (ordered categorical) variables. Can be one of liracine

(default) or wangvanryzin. Argument is ignored when no variables are ordinal.

cat_first A logical value indicating whether bandwidth selection is prioritised for the cat-

egorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when data is of mixed-type and all bandwidths are

selected automatically (i.e. s = -1, lambda = -1).

verbose Logical. Defaults to FALSE to suppress progress messages. Change to TRUE to

print.

Details

The DIBmix function clusters data while retaining maximal information about the original variable distributions. The Deterministic Information Bottleneck algorithm optimizes an information-theoretic objective that balances information preservation and compression. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This iterative process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively.

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

• Gaussian (RBF) kernel (Silverman 1998):

$$K_c\left(\frac{x-x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x-x')^2}{2s^2}\right\}, \quad s > 0.$$

• Epanechnikov kernel (Epanechnikov 1969):

$$K_c(x - x'; s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x - x')^2}{5s^2} \right), & \text{if } \frac{(x - x')^2}{s^2} < 5\\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

• Aitchison & Aitken kernel (Aitchison and Aitken 1976):

$$K_u(x=x';\lambda) = \begin{cases} 1-\lambda, & \text{if } x=x'\\ \frac{\lambda}{\ell-1}, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le \frac{\ell-1}{\ell}.$$

• Li & Racine kernel (Ouyang et al. 2006):

$$K_u(x = x'; \lambda) = \begin{cases} 1, & \text{if } x = x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le 1.$$

For ordinal (ordered categorical) variables:

• Li & Racine kernel (Li and Racine 2003):

$$K_o(x = x'; \nu) = \begin{cases} 1, & \text{if } x = x' \\ \nu^{|x - x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

• Wang & van Ryzin kernel (Wang and Van Ryzin 1981):

$$K_o(x=x';\nu) = \begin{cases} 1-\nu, & \text{if } x=x' \\ \frac{1-\nu}{2}\nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

The bandwidth parameters s, λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

A list containing the following elements:

Cluster	An integer vector giving the cluster assignments for each data point.
Entropy	A numeric value representing the entropy of the cluster assignments at convergence.
CondEntropy	A numeric value representing the conditional entropy of cluster assignment, given the observation weights $H(T\mid X)$.
MutualInfo	A numeric value representing the mutual information, $I(Y;T)$, between the original labels (Y) and the cluster assignments (T) .
InfoXT	A numeric value representing the mutual information, $I(X;T)$, between the original observations weights (X) and the cluster assignments (T) .
beta	A numeric vector of the final beta values used in the iterative procedure.
alpha	A numeric value of the strength of conditional entropy used, controlling fuzziness of the solution. This is by default equal to 0 for DIBmix.
S	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
lambda	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.
ents	A numeric vector tracking the entropy values across iterations.
mis	A numeric vector tracking the mutual information values across iterations.

Author(s)

Efthymios Costa, Ioanna Papatsouma, Angelos Markos

References

Costa E, Papatsouma I, Markos A (2025). "A Deterministic Information Bottleneck Method for Clustering Mixed-Type Data." doi:10.48550/arXiv.2407.03389, arXiv:2407.03389, https://arxiv.org/abs/2407.03389.

Aitchison J, Aitken CG (1976). "Multivariate binary discrimination by the kernel method." *Biometrika*, **63**(3), 413–420.

Li Q, Racine J (2003). "Nonparametric estimation of distributions with categorical and continuous data." *Journal of Multivariate Analysis*, 86(2), 266–292.

Silverman BW (1998). Density Estimation for Statistics and Data Analysis (1st Ed.). Routledge.

Ouyang D, Li Q, Racine J (2006). "Cross-validation and the estimation of probability distributions with categorical data." *Journal of Nonparametric Statistics*, 18(1), 69–100.

Wang M, Van Ryzin J (1981). "A class of smooth estimators for discrete distributions." *Biometrika*, **68**(1), 301–309.

Epanechnikov VA (1969). "Non-parametric estimation of a multivariate probability density." *Theory of Probability & Its Applications*, **14**(1), 153–158.

Examples

```
# Example 1: Basic Mixed-Type Clustering
set.seed(123)
# Create a more realistic dataset with mixed variable types
data_mix <- data.frame(</pre>
  # Categorical variables
  education = factor(sample(c("High School", "Bachelor", "Master", "PhD"), 150,
                           replace = TRUE, prob = c(0.4, 0.3, 0.2, 0.1)),
  employment = factor(sample(c("Full-time", "Part-time", "Unemployed"), 150,
                            replace = TRUE, prob = c(0.6, 0.25, 0.15)),
  # Ordinal variable
  satisfaction = factor(sample(c("Low", "Medium", "High"), 150, replace = TRUE),
                       levels = c("Low", "Medium", "High"), ordered = TRUE),
  # Continuous variables
  income = rlnorm(150, meanlog = 10, sdlog = 0.5), # Log-normal income
  age = rnorm(150, mean = 35, sd = 10),
                                                    # Normally distributed age
  experience = rpois(150, lambda = 8)
                                                    # Years of experience
# Perform Mixed-Type Clustering
result_mix <- DIBmix(X = data_mix, ncl = 3, nstart = 50)</pre>
# View results
print(paste("Number of clusters found:", length(unique(result_mix$Cluster))))
print(paste("Mutual Information:", round(result_mix$MutualInfo, 3)))
table(result_mix$Cluster)
# Example 2: Comparing cat_first parameter
# When categorical variables are more informative
result_cat_first <- DIBmix(X = data_mix, ncl = 3,</pre>
                           cat_first = TRUE, # Prioritize categorical variables
                           nstart = 50)
# When continuous variables are more informative (default)
result_cont_first <- DIBmix(X = data_mix, ncl = 3,</pre>
                            cat_first = FALSE,
                            nstart = 50)
# Compare clustering performance
if (requireNamespace("mclust", quietly = TRUE)){  # For adjustedRandIndex
  print(paste("Agreement between approaches:",
              round(mclust::adjustedRandIndex(result_cat_first$Cluster,
                    result_cont_first$Cluster), 3)))
  }
# Simulated categorical data example
data_cat <- data.frame(</pre>
 Var1 = as.factor(sample(letters[1:3], 200, replace = TRUE)),  # Nominal variable
 Var2 = as.factor(sample(letters[4:6], 200, replace = TRUE)), # Nominal variable
 Var3 = factor(sample(c("low", "medium", "high"), 200, replace = TRUE),
                levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)
```

```
# Perform hard clustering on categorical data with Deterministic IB
result_cat <- DIBmix(X = data_cat, ncl = 3, lambda = -1, nstart = 10)
# Print clustering results
print(result_cat$Cluster)
                                # Cluster assignments
print(result_cat$Entropy)
                               # Final entropy
                               # Mutual information
print(result_cat$MutualInfo)
# Simulated continuous data example
set.seed(123)
# Continuous data with 200 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(1000), ncol = 5))</pre>
# Perform hard clustering on continuous data with Deterministic IB
result_cont <- DIBmix(X = data_cont, ncl = 3, s = -1, nstart = 10)
# Print clustering results
print(result_cont$Cluster)
                                # Cluster assignments
print(result_cont$Entropy)
                                # Final entropy
print(result_cont$MutualInfo) # Mutual information
```

GIBmix

Generalised Information Bottleneck Clustering for Mixed-Type Data

Description

The GIBmix function implements the Generalised Information Bottleneck (GIB) algorithm for clustering datasets containing continuous, categorical (nominal and ordinal), and mixed-type variables. This method optimizes an information-theoretic objective to preserve relevant information in the cluster assignments while achieving effective data compression (Strouse and Schwab 2017).

Usage

```
GIBmix(X, ncl, beta, alpha, randinit = NULL,
    s = -1, lambda = -1, scale = TRUE,
    maxiter = 100, nstart = 100,
    contkernel = "gaussian",
    nomkernel = "aitchisonaitken", ordkernel = "liracine",
    cat_first = FALSE, verbose = FALSE)
```

Arguments

X	A data frame containing the input data to be clustered. It should include categorical variables (factor for nominal and ordered for ordinal) and continuous variables (numeric).
ncl	An integer specifying the number of clusters.
beta	Regularisation strength characterizing the tradeoff between compression and relevance. Must be non-negative.
alpha	Strength of conditional entropy term. Must be in the range $[0,1]$. Setting alpha = 0 calls the DIBmix function and ignores the value of beta, while alpha = 1 calls IBmix instead.

randinit	An optional vector specifying the initial cluster assignments. If NULL, cluster assignments are initialized randomly.
S	A numeric value or vector specifying the bandwidth parameter(s) for continuous variables. The values must be greater than 0. The default value is -1 , which enables the automatic selection of optimal bandwidth(s). Argument is ignored when no variables are continuous.
lambda	A numeric value or vector specifying the bandwidth parameter for categorical variables. The default value is -1 , which enables automatic determination of the optimal bandwidth. For nominal variables and nomkernel = 'aitchisonaitken', the maximum allowable value of lambda is $(l-1)/l$, where l represents the number of categories, whereas for nomkernel = 'liracine' the maximum allowable value is 1. For ordinal variables, the maximum allowable value of lambda is 1, regardless of what ordkernel is being used. Argument is ignored when all variables are continuous.
scale	A logical value indicating whether the continuous variables should be scaled to have unit variance before clustering. Defaults to TRUE. Argument is ignored when all variables are categorical.
maxiter	The maximum number of iterations allowed for the clustering algorithm. Defaults to 100 .
nstart	The number of random initializations to run. The best clustering solution is returned. Defaults to 100 .
contkernel	Kernel used for continuous variables. Can be one of gaussian (default) or epanechnikov. Argument is ignored when no variables are continuous.
nomkernel	Kernel used for nominal (unordered categorical) variables. Can be one of aitchisonaitken (default) or liracine. Argument is ignored when no variables are nominal.
ordkernel	Kernel used for ordinal (ordered categorical) variables. Can be one of liracine (default) or wangvanryzin. Argument is ignored when no variables are ordinal.
cat_first	A logical value indicating whether bandwidth selection is prioritised for the categorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when data is of mixed-type and all bandwidths are selected automatically (i.e. $s = -1$, lambda = -1).
verbose	Logical. Defaults to FALSE to suppress progress messages. Change to TRUE to print.

Details

The GIBmix function produces a fuzzy clustering of the data while retaining maximal information about the original variable distributions. The Generalised Information Bottleneck algorithm optimizes an information-theoretic objective that balances information preservation and compression. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This iterative process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively. Set $\alpha=1$ and $\alpha=0$ to recover the Information Bottleneck and its Deterministic variant, respectively. If $\alpha=0$, the algorithm ignores the value of the regularisation parameter $\beta.$

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

• Gaussian (RBF) kernel (Silverman 1998):

$$K_c\left(\frac{x-x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{\left(x-x'\right)^2}{2s^2}\right\}, \quad s > 0.$$

• Epanechnikov kernel (Epanechnikov 1969):

$$K_c(x-x';s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x-x')^2}{5s^2}\right), & \text{if } \frac{(x-x')^2}{s^2} < 5\\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

• Aitchison & Aitken kernel (Aitchison and Aitken 1976):

$$K_u(x=x';\lambda) = \begin{cases} 1-\lambda, & \text{if } x=x'\\ \frac{\lambda}{\ell-1}, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le \frac{\ell-1}{\ell}.$$

• Li & Racine kernel (Ouyang et al. 2006):

$$K_u(x = x'; \lambda) = \begin{cases} 1, & \text{if } x = x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le 1.$$

For ordinal (ordered categorical) variables:

• Li & Racine kernel (Li and Racine 2003):

$$K_o(x=x';\nu) = \begin{cases} 1, & \text{if } x=x' \\ \nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

• Wang & van Ryzin kernel (Wang and Van Ryzin 1981):

$$K_o(x = x'; \nu) = \begin{cases} 1 - \nu, & \text{if } x = x' \\ \frac{1 - \nu}{2} \nu^{|x - x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

The bandwidth parameters s, λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

A list containing the following elements:

Cluster A cluster membership matrix.

Entropy A numeric value representing the entropy of the cluster assignments at the end

of the iterative procedure.

CondEntropy A numeric value representing the conditional entropy of cluster assignment,

given the observation weights $H(T \mid X)$.

MutualInfo A numeric value representing the mutual information, I(Y;T), between the data

distribution and the cluster assignments.

InfoXT A numeric value representing the mutual information, I(X;T), between the

original observations weights (X) and the cluster assignments (T).

beta	A numeric value of the regularisation strength beta used.
alpha	A numeric value of the strength of conditional entropy used.
S	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
lambda	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.
ht	A numeric vector tracking the entropy value of the cluster assignments across iterations.
hy_t	A numeric vector tracking the conditional entropy values between the cluster assignments and observations weights across iterations.
iyt	A numeric vector tracking the mutual information values between original labels and cluster assignments across iterations.
losses	A numeric vector tracking the final loss values across iterations.

Author(s)

Efthymios Costa, Ioanna Papatsouma, Angelos Markos

References

Strouse DJ, Schwab DJ (2017). "The Deterministic Information Bottleneck." *Neural Computation*, **29**(6), 1611–1630.

Aitchison J, Aitken CG (1976). "Multivariate binary discrimination by the kernel method." *Biometrika*, **63**(3), 413–420.

Li Q, Racine J (2003). "Nonparametric estimation of distributions with categorical and continuous data." *Journal of Multivariate Analysis*, **86**(2), 266–292.

Silverman BW (1998). Density Estimation for Statistics and Data Analysis (1st Ed.). Routledge.

Ouyang D, Li Q, Racine J (2006). "Cross-validation and the estimation of probability distributions with categorical data." *Journal of Nonparametric Statistics*, **18**(1), 69–100.

Wang M, Van Ryzin J (1981). "A class of smooth estimators for discrete distributions." *Biometrika*, **68**(1), 301–309.

Epanechnikov VA (1969). "Non-parametric estimation of a multivariate probability density." *Theory of Probability & Its Applications*, **14**(1), 153–158.

Examples

```
# Print clustering results
print(result_mix$Cluster)
                                # Cluster membership matrix
print(result_mix$Entropy)
                               # Entropy of final clustering
print(result_mix$CondEntropy) # Conditional entropy of final clustering
                                # Mutual information between Y and T
print(result_mix$MutualInfo)
# Simulated categorical data example
set.seed(123)
data cat <- data.frame(</pre>
  Var1 = as.factor(sample(letters[1:3], 200, replace = TRUE)), # Nominal variable
  Var2 = as.factor(sample(letters[4:6], 200, replace = TRUE)), # Nominal variable
 Var3 = factor(sample(c("low", "medium", "high"), 200, replace = TRUE),
                levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)
# Perform Fuzzy Clustering on categorical data with Generalised IB
result_cat <- GIBmix(X = data_cat, ncl = 2, beta = 25, alpha = 0.75, lambda = -1, nstart = 10)
# Print clustering results
print(result_cat$Cluster)
                                # Cluster membership matrix
print(result_cat$Entropy)
                                # Entropy of final clustering
print(result_cat$CondEntropy) # Conditional entropy of final clustering
print(result_cat$MutualInfo)
                                # Mutual information between Y and T
# Simulated continuous data example
set.seed(123)
# Continuous data with 200 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(1000), ncol = 5))</pre>
# Perform Fuzzy Clustering on continuous data with Generalised IB
result_cont <- GIBmix(X = data_cont, ncl = 2, beta = 50, alpha = 0.75, s = -1, nstart = 10)
# Print clustering results
print(result_cont$Cluster)
                                 # Cluster membership matrix
print(result_cont$Entropy)
                                 # Entropy of final clustering
print(result_cont$CondEntropy) # Conditional entropy of final clustering
print(result_cont$MutualInfo)
                                 # Mutual information between Y and T
```

IBmix

Information Bottleneck Clustering for Mixed-Type Data

Description

The IBmix function implements the Information Bottleneck (IB) algorithm for clustering datasets containing continuous, categorical (nominal and ordinal), and mixed-type variables. This method optimizes an information-theoretic objective to preserve relevant information in the cluster assignments while achieving effective data compression (Strouse and Schwab 2019).

Usage

```
IBmix(X, ncl, beta, randinit = NULL,
    s = -1, lambda = -1, scale = TRUE,
    maxiter = 100, nstart = 100,
    contkernel = "gaussian",
```

```
nomkernel = "aitchisonaitken", ordkernel = "liracine",
cat_first = FALSE, verbose = FALSE)
```

Arguments

X A data frame containing the input data to be clustered. It should include categorical variables (factor for nominal and Ord. factor for ordinal) and continuous

variables (numeric).

ncl An integer specifying the number of clusters.

beta Regularisation strength characterizing the tradeoff between compression and

relevance. Must be non-negative.

randinit An optional vector specifying the initial cluster assignments. If NULL, cluster

assignments are initialized randomly.

A numeric value or vector specifying the bandwidth parameter(s) for continuous

variables. The values must be greater than 0. The default value is -1, which enables the automatic selection of optimal bandwidth(s). Argument is ignored

when no variables are continuous.

lambda A numeric value or vector specifying the bandwidth parameter for categorical

variables. The default value is -1, which enables automatic determination of the optimal bandwidth. For nominal variables and nomkernel = 'aitchisonaitken', the maximum allowable value of lambda is (l-1)/l, where l represents the number of categories, whereas for nomkernel = 'liracine' the maximum allowable value is 1. For ordinal variables, the maximum allowable value of lambda is 1, regardless of what ordkernel is being used. Argument is ignored when all

variables are continuous.

scale A logical value indicating whether the continuous variables should be scaled

to have unit variance before clustering. Defaults to TRUE. Argument is ignored

when all variables are categorical.

maxiter The maximum number of iterations allowed for the clustering algorithm. De-

faults to 100.

nstart The number of random initializations to run. The best clustering solution is

returned. Defaults to 100.

contkernel Kernel used for continuous variables. Can be one of gaussian (default) or

epanechnikov. Argument is ignored when no variables are continuous.

nomkernel Kernel used for nominal (unordered categorical) variables. Can be one of aitchisonaitken

(default) or liracine. Argument is ignored when no variables are nominal.

ordkernel Kernel used for ordinal (ordered categorical) variables. Can be one of liracine

(default) or wangvanryzin. Argument is ignored when no variables are ordinal.

cat_first A logical value indicating whether bandwidth selection is prioritised for the cat-

egorical variables, instead of the continuous. Defaults to FALSE. Set to TRUE if you suspect that the continuous variables are not informative of the cluster structure. Can only be TRUE when data is of mixed-type and all bandwidths are

selected automatically (i.e. s = -1, lambda = -1).

verbose Logical. Defaults to FALSE to suppress progress messages. Change to TRUE to

print.

Details

The IBmix function produces a fuzzy clustering of the data while retaining maximal information about the original variable distributions. The Information Bottleneck algorithm optimizes an information-theoretic objective that balances information preservation and compression. Bandwidth parameters for categorical (nominal, ordinal) and continuous variables are adaptively determined if not provided. This iterative process identifies stable and interpretable cluster assignments by maximizing mutual information while controlling complexity. The method is well-suited for datasets with mixed-type variables and integrates information from all variable types effectively.

The following kernel functions can be used to estimate densities for the clustering procedure. For continuous variables:

• Gaussian (RBF) kernel (Silverman 1998):

$$K_c\left(\frac{x-x'}{s}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{(x-x')^2}{2s^2}\right\}, \quad s > 0.$$

• Epanechnikov kernel (Epanechnikov 1969):

$$K_c(x - x'; s) = \begin{cases} \frac{3}{4\sqrt{5}} \left(1 - \frac{(x - x')^2}{5s^2} \right), & \text{if } \frac{(x - x')^2}{s^2} < 5\\ 0, & \text{otherwise} \end{cases}, \quad s > 0.$$

For nominal (unordered categorical variables):

• Aitchison & Aitken kernel (Aitchison and Aitken 1976):

$$K_u(x = x'; \lambda) = \begin{cases} 1 - \lambda, & \text{if } x = x' \\ \frac{\lambda}{\ell - 1}, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le \frac{\ell - 1}{\ell}.$$

• Li & Racine kernel (Ouyang et al. 2006):

$$K_u(x = x'; \lambda) = \begin{cases} 1, & \text{if } x = x' \\ \lambda, & \text{otherwise} \end{cases}, \quad 0 \le \lambda \le 1.$$

For ordinal (ordered categorical) variables:

• Li & Racine kernel (Li and Racine 2003):

$$K_o(x = x'; \nu) = \begin{cases} 1, & \text{if } x = x' \\ \nu^{|x - x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

• Wang & van Ryzin kernel (Wang and Van Ryzin 1981):

$$K_o(x=x';\nu) = \begin{cases} 1-\nu, & \text{if } x=x' \\ \frac{1-\nu}{2}\nu^{|x-x'|}, & \text{otherwise} \end{cases}, \quad 0 \le \nu \le 1.$$

The bandwidth parameters s, λ , and ν control the smoothness of the density estimate and are automatically determined by the algorithm if not provided by the user using the approach in Costa et al. (2025). ℓ is the number of levels of the categorical variable. For ordinal variables, the lambda parameter of the function is used to define ν .

Value

A list containing the following elements:

Cluster	A cluster membership matrix.
Entropy	A numeric value representing the entropy of the cluster assignments at the end of the iterative procedure.
CondEntropy	A numeric value representing the conditional entropy of cluster assignment, given the observation weights $H(T\mid X)$.
MutualInfo	A numeric value representing the mutual information, $I(Y;T)$, between the data distribution and the cluster assignments.
InfoXT	A numeric value representing the mutual information, $I(X;T)$, between the original observations weights (X) and the cluster assignments (T) .
beta	A numeric value of the regularisation strength beta used.
alpha	A numeric value of the strength of conditional entropy used, controlling fuzziness of the solution. This is by default equal to 1 for IBmix.
S	A numeric vector of bandwidth parameters used for the continuous variables. A value of -1 is returned if all variables are categorical.
lambda	A numeric vector of bandwidth parameters used for the categorical variables. A value of -1 is returned if all variables are continuous.
ixt	A numeric vector tracking the mutual information values between original observation weights and cluster assignments across iterations.
iyt	A numeric vector tracking the mutual information values between original labels and cluster assignments across iterations.
losses	A numeric vector tracking the final loss values across iterations.

Author(s)

Efthymios Costa, Ioanna Papatsouma, Angelos Markos

References

Strouse DJ, Schwab DJ (2019). "The information bottleneck and geometric clustering." *Neural Computation*, **31**(3), 596–612.

Aitchison J, Aitken CG (1976). "Multivariate binary discrimination by the kernel method." *Biometrika*, **63**(3), 413–420.

Li Q, Racine J (2003). "Nonparametric estimation of distributions with categorical and continuous data." *Journal of Multivariate Analysis*, **86**(2), 266–292.

Silverman BW (1998). Density Estimation for Statistics and Data Analysis (1st Ed.). Routledge.

Ouyang D, Li Q, Racine J (2006). "Cross-validation and the estimation of probability distributions with categorical data." *Journal of Nonparametric Statistics*, **18**(1), 69–100.

Wang M, Van Ryzin J (1981). "A class of smooth estimators for discrete distributions." *Biometrika*, **68**(1), 301–309.

Epanechnikov VA (1969). "Non-parametric estimation of a multivariate probability density." *Theory of Probability & Its Applications*, **14**(1), 153–158.

Examples

```
# Example dataset with categorical, ordinal, and continuous variables
set.seed(123)
data_mix <- data.frame(</pre>
 cat_var = factor(sample(letters[1:3], 100, replace = TRUE)),
                                                               # Nominal categorical variable
  ord_var = factor(sample(c("low", "medium", "high"), 100, replace = TRUE),
                   levels = c("low", "medium", "high"),
                   ordered = TRUE),
                                                                   # Ordinal variable
                                                                 # Continuous variable 1
  cont_var1 = rnorm(100),
                                                                 # Continuous variable 2
 cont_var2 = runif(100)
# Perform Mixed-Type Fuzzy Clustering
result_mix <- IBmix(X = data_mix, ncl = 3, beta = 2, nstart = 10)</pre>
# Print clustering results
print(result_mix$Cluster)
                               # Cluster membership matrix
print(result_mix$InfoXT)
                              # Mutual information between X and T
print(result_mix$MutualInfo)  # Mutual information between Y and T
# Simulated categorical data example
set.seed(123)
data_cat <- data.frame(</pre>
  Var1 = as.factor(sample(letters[1:3], 200, replace = TRUE)), # Nominal variable
  Var2 = as.factor(sample(letters[4:6], 200, replace = TRUE)),  # Nominal variable
 Var3 = factor(sample(c("low", "medium", "high"), 200, replace = TRUE),
                levels = c("low", "medium", "high"), ordered = TRUE) # Ordinal variable
)
# Perform fuzzy clustering on categorical data with standard IB
result_cat <- IBmix(X = data_cat, ncl = 3, beta = 15, lambda = -1, nstart = 10)
# Print clustering results
print(result_cat$Cluster)
                              # Cluster membership matrix
print(result_cat$InfoXT)
                              # Mutual information between X and T
print(result_cat$MutualInfo)  # Mutual information between Y and T
# Simulated continuous data example
set.seed(123)
# Continuous data with 200 observations, 5 features
data_cont <- as.data.frame(matrix(rnorm(1000), ncol = 5))</pre>
# Perform fuzzy clustering on continuous data with standard IB
result_cont <- IBmix(X = data_cont, ncl = 3, beta = 50, s = -1, nstart = 10)
# Print clustering results
print(result_cont$Cluster)
                                # Cluster membership matrix
print(result_cont$InfoXT)
                                # Mutual information between X and T
print(result_cont$MutualInfo)  # Mutual information between Y and T
```

Index

```
* clustering
AIBmix, 2
DIBmix, 5
GIBmix, 10
IBmix, 14

AIBmix, 2

DIBmix, 5
GIBmix, 10

IBmix, 14
```