

Jan 2022

Q1. From the list of given terms find out the best possible options for each of the given subquestions:

- 1) Rank
- 2) Limit
- 3) Determinant
- 4) Closure with respect to addition and scalar multiplication
- 5) Existence of zero element
- 6) Existence of additive inverse
- 7) Communitative of addition
- 8) Associativity of addition
- 9) Elements
- 10) Local maxima
- 11) Local minima
- 12) Saddle points
- 13) Gradient
- 14) Directional Derivative
- 15) Partial Derivative
- 16) Set of orthonormal vectors
- 17) Standard ordered basis
- 18) Affine spaces

The conditions that need to be checked to identify a subspace W of a vector space V

:_____.

(Enter 2 best possible options. Enter only the serial numbers of those options in increasing order

without adding any comma or space in between them.) [Suppose your answer is 7, 14 and 17, then

you should enter 71417]

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Q2. From the list of given terms find out the best possible options.

- 1) Rank 2
- 2) Non-zero nullity
- 3) Non -zero determinant
- 4) Closure with respect to addition and scalar multiplication
- 5) Existence of additive inverse
- 6) Existence of additive inverse
- 7) Commutative of addition
- 8) Associativity of addition
- 9) Elements
- 10) Global maxima
- 11) Global minima
- 12) A critical points
- 13) Gradient exists
- 14) Directional derivative exist in any direction
- 15) Partial derivatives exist
- 16) Orthonormal columns
- 17) Standard ordered basis
- 18) Affine subspaces
- 19) Limit exists

Some of the conditions that need to be checked to identify a vector space V are

(Enter 5 best possible options. Enter only the serial numbers of those options in increasing order

without adding any comma or space in between them.) [Suppose your answer is 7, 14, 11, 15 and

17, then you should enter 714111517]

May 2023

Q3. Let V be the vector space of all $n \times n$ matrices with usual addition and scalar multiplication. Which of the following set(s) form an subspace of V ?

Options:

A. $W_1 = \{A \in M_n(\mathbb{R}) : A \text{ is invertible}\}$

B. $W_2 = \{A \in M_n(\mathbb{R}) : \det(A) = 1\}$

C. $W_3 = \{A \in M_n(\mathbb{R}) : A \text{ is upper triangular}\}$

D. $W_4 = \{A \in M_n(\mathbb{R}) : A \text{ is symmetrix i.e. } A^T = A\}$