

Stack.
(data structure) — (LIFO) → Last In First Out.

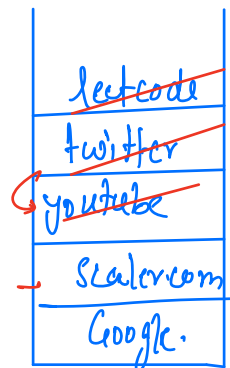
① Recursion } Call Stack.

② Undo / Redo

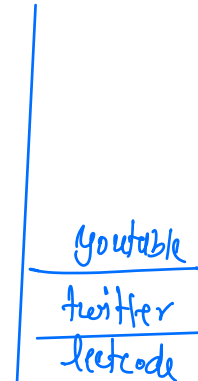
A → B → ~~C~~ → ~~D~~

③ Browser History. →

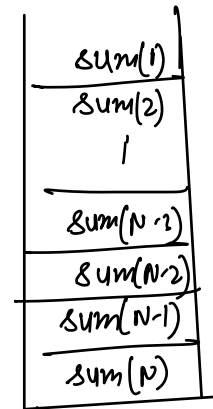
Backward & forward Tab



Backward.



Forward.



Operations by stack.

- O(1)
- push(x) → insert x in stack
 - pop() → removes the topmost element
 - top() / peek() → access the topmost element
 - size(), isEmpty() → If stack is empty → true
↓
return size of stack
otherwise → false.

push(17)

push(15)

push(2)

push(2)

pop()

push(12)

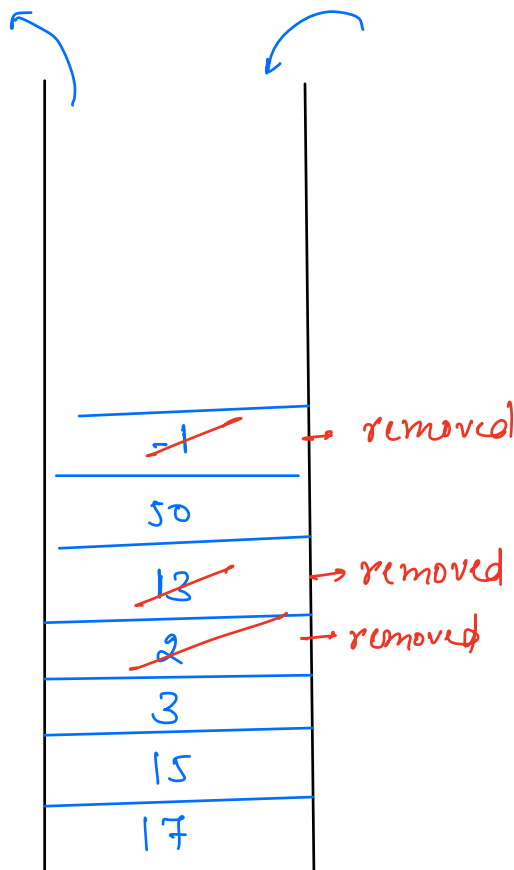
pop()

push(50)

push(-1)

pop()

top() → 50



Implementation of Stack.

→ Arrays

$top \rightarrow -1$ → last position where top-most element exists.

push (17)

push (15)

push (3)

push (2)

pop()

push (13)

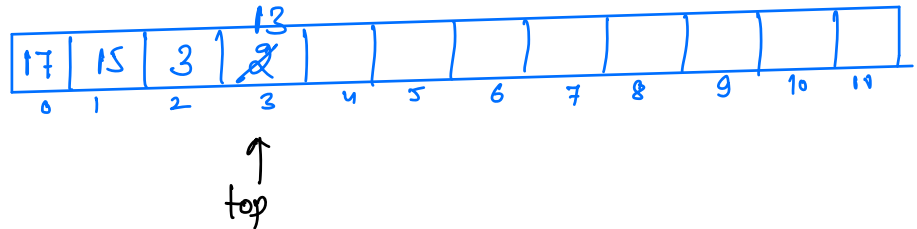
pop()

push (50)

push (-1)

pop()

top()



```
void push (int n) {  
    if (top == N-1) { // stack overflow }  
        top++ ;  
        arr[top] = n;  
}
```

```
void pop () {  
    if (top == -1) { // stack is empty }  
        top--  
}
```

```
int top () {  
    if (top == -1) { // stack is empty }  
        return arr[top];  
}
```

```
int size () {  
    return top+1  
}
```

max \rightarrow 10^4 operations.

\uparrow
initial size of stack.

push(10)

pop()

push(20)

pop()

push(30)

pop()

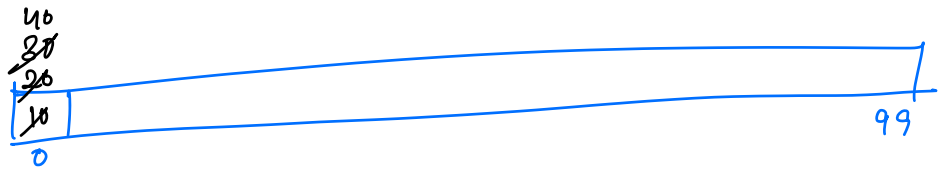
push(40)

pop()

/

|

100 operations.



\rightarrow huge memory wastage.

* Linked-list — insertion/deletion

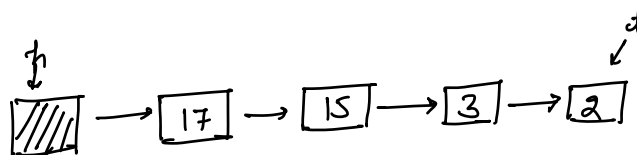
head/tail

- ① insertion → At tail → $O(1)$
removal → At tail → $O(N)$

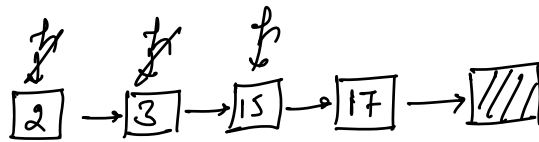
Solution :
DLL can be used.

↓
(but more space will be used)

push(17)
push(15)
push(3)
push(2)
pop()
push(13)
pop()
push(50)
push(-1)
pop()
top()

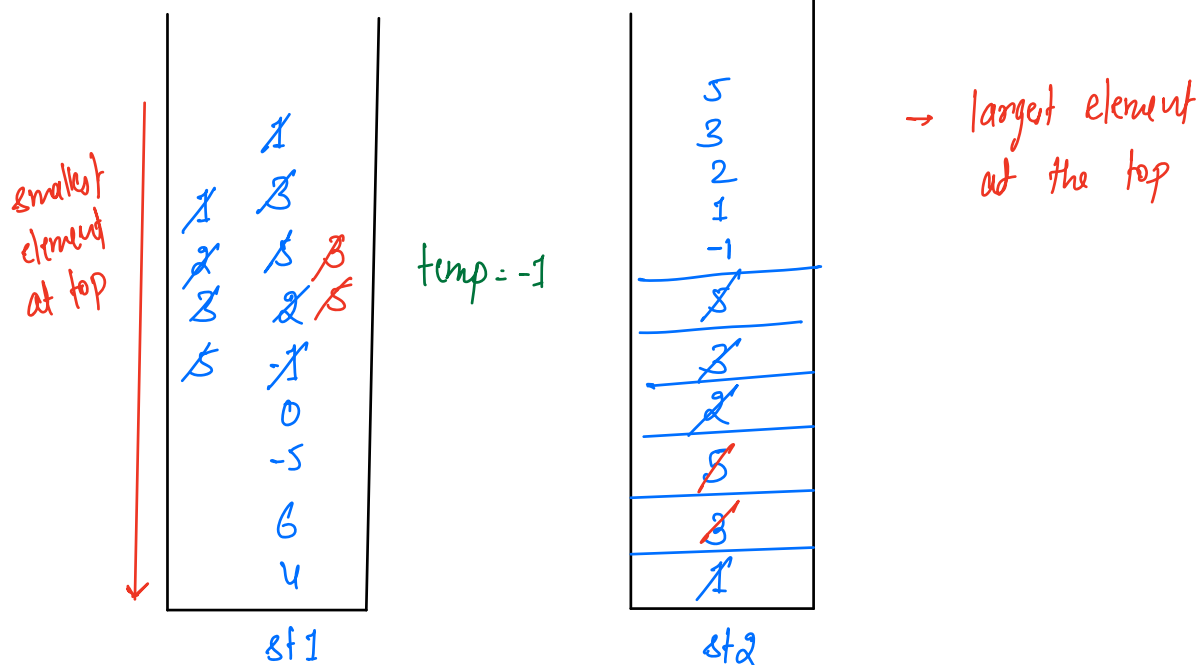


- ② insertion → At head → $O(1)$
removal → At head → $O(1)$



Q1) Sort a given stack in ascending order. [Smallest element should be present at top]

→ [Use another 1 stack.]



⇒ For one element, $2N$ operations will be performed in worst case.

T.C → $N \cdot 2N \rightarrow \underline{O(N^2)}$, S.C → $O(N)$

#pseudo-code.

st1, st2. {aux. stack}

```
while ( !st1.isEmpty() ) {  
    int temp = st1.top()  
    st1.pop()  
    while ( !st2.isEmpty && st2.top() > temp ) {  
        x = st2.top()  
        st2.pop()  
        st1.push(x)  
    }  
    st2.push(temp);  
}
```

→ Shift back all the elements from st2 to st1

```
while ( !st2.isEmpty() ) {  
    x = st2.top()  
    st2.pop();  
    st1.push(x)  
}
```

Q. Check if the given sequence of parenthesis is valid or not.

$()$, $\{\}$, $[]$

$() [] \rightarrow \underline{\text{Yes.}}$

$() [\{ \}] \rightarrow \underline{\text{Yes.}}$

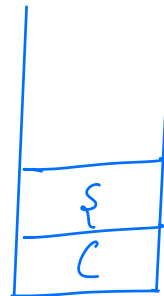
$(\{ \}) \rightarrow \underline{\text{No}}$

$([\}]) \rightarrow \underline{\text{No}}$

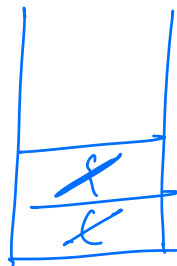
$(\{ [\} \} ()] \} ())$

$(\{ [\} \} ()] \} ())$

$(\{) \} \rightarrow \underline{\text{false.}}$



$(\{ \})] \rightarrow \underline{\text{false.}}$



$[() \rightarrow \underline{\text{false.}}$



pseudo-code.

```
Stack < character > st;  
for ( i = 0; i < N; i++ ) {  
    ch = str[i];  
    if ( ch == '(' || ch == '{' || ch == '[' ) {  
        st.push(ch);  
    }  
    else {  
        if ( st.size() == 0 ) { // more closing brackets  
            return false;  
        }  
        else if ( st.top() is not the counterpart  
                  of current closing parenthesis )  
            return false // mis-match  
        else {  
            st.pop();  
        }  
    }  
}  
  
if ( st.isEmpty() ) { return true }  
else { return false }
```

$$\left[\begin{array}{l} T.C \rightarrow O(N) \\ S.C \rightarrow O(N) \end{array} \right]$$

[Stack < character > st = new Stack < > ();]

*→ Double Character Trouble

Given a string s . Remove equal pair of adjacent characters.
Return the string without adjacent duplicates.

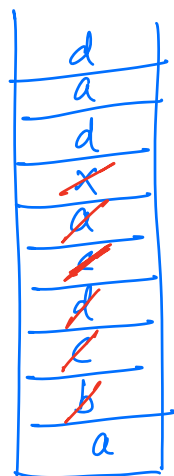
① $a\cancel{b}\cancel{b}d \rightarrow ad$

② $a\cancel{b}\cancel{c}\cancel{c}bde \rightarrow a\cancel{b}\cancel{b}de \rightarrow ade.$

③ $a\cancel{b}\cancel{b}bd \rightarrow abd$

④ $\underset{\uparrow}{a}\cancel{b}\cancel{b}\cancel{c}\cancel{c}\cancel{b}\cancel{b}\cancel{c}\underset{\uparrow}{d}cx \rightarrow cx$

⑤ $\check{a}\check{b}\check{c}\check{d}\check{c}\check{c}\check{d}\check{c}\check{a}\check{a}\check{b}\check{x}\check{x}\check{d}\check{a}\check{d}$



→ dada

↓ reverse

adad → ans.

traverse the string.



curr ch == st.top()

yes

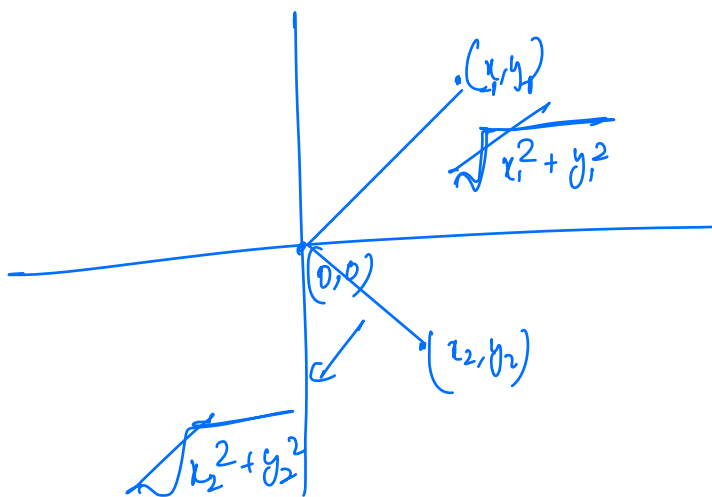
pop()

no

push curr ch

$T.C \rightarrow O(N)$
 $S.C \rightarrow O(N)$

* Reverse the string to get the final ans.



(x_1, y_1) and (x_2, y_2)

$$\sqrt{(y_2 - y_1)^2 + (x_2 - x_1)^2}$$

	P_0	P_1	P_2	P_3
a →	1	2	4	3
b →	2	3	1	3
	0	1	2	3

Arrays.sort(arr , comparator)