

Today's content:

→ Next Smaller Element

↙ on l.h.s      ↘ on r.h.s

→ Next Greater Element (NGE)

↙ on l.h.s      ↘ on r.h.s

→ Index of nearest smaller.

→ Largest Rectangle in Histogram.

→ Sum of (max-min) for all subarrays

→ Solve Reverse Polish Notation / Postfix Notation Expression.

2L + Stacks.

## Nearest Smaller Element

Given an array of size  $N$ . For every index  $i$ , find the nearest element which is smaller than  $i$ th element on left side.

Eg.  $\rightarrow$  arr:  $\begin{bmatrix} 4 & 5 & 2 & 10 & 3 & 2 \end{bmatrix}$   
 $\begin{matrix} \text{0} & \text{1} & \text{2} & \text{3} & \text{4} & \text{5} \\ \text{X} & 4 & \text{X} & 2 & 2 & \text{X} \\ \text{-1} & & \text{-1} & & & \text{-1} \end{matrix}$

arr:  $\begin{bmatrix} 4 & 6 & 10 & 11 & 7 & 8 & 3 & 5 \end{bmatrix}$   
 $\begin{matrix} \text{0} & \text{1} & \text{2} & \text{3} & \text{4} & \text{5} & \text{6} & \text{7} \\ \text{X} & 4 & 6 & 10 & 6 & 7 & \text{X} & 3 \\ \text{-1} & & & & & & \text{-1} & \end{matrix}$

Idea: For every element, iterate on its l.h.s. elements & find nearest smaller element on l.h.s.

ans[]  $\rightarrow$  -1

```
for( i = 0; i < N; i++) {  
    for( j = i-1; j >= 0; j--) {  
        if (arr[j] < arr[i]) {  
            ans[i] = arr[j];  
            break;  
        }  
    }  
}  
return ans;
```

$\left[ \begin{matrix} \text{T.C} \rightarrow O(N^2) \\ \text{S.C} \rightarrow O(1) \end{matrix} \right]$

Ex-      5    2    8    10    6    1    7    15

          ↓    ↓    ↓    ↓    ↓    ↓    ↓

          X    X    2    8    2    X    1

~~5~~ ~~2~~ ~~8~~ ~~10~~ ~~6~~ 1

↓  
Stack.

Ex:    [ 4    5    2    10    8    2 ]

        -1   4   -1    2    2   -1

2
<del>8</del>
<del>10</del>
<del>2</del>
<del>5</del>
<del>4</del>

Ex:    [ 4    6    10    11    7    6    3    5 ]

ans → [ -1   4    6    10    6    4    -1   3 ]

11
10
6
4

- pop all greater & equal.
- update ans.
- push curr element in st.

# pseudo-code -

Stack < Integer > st, ans[N]

```
for (i = 0; i < N; i++) {  
    while (!st.isEmpty() && st.peek() >= arr[i]) {  
        st.pop();  
    }  
    if (st.isEmpty()) { ans[i] = -1; }  
    else { ans[i] = st.peek(); }  
    st.push(arr[i]);  
}  
return ans;
```

T.C  $\rightarrow O(N)$   
S.C  $\rightarrow O(N)$

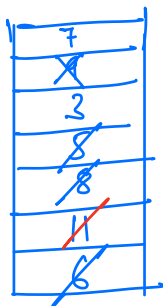
Q2: Nearest Smaller Element on r.h.s.



① iterate from N-1 to 0

② Reverse the array & apply same method.

arr: [ 7 9 3 5 8 11 6 ]  
[ 3 3 -1 -1 6 6 -1 ]



- & equal.
- pop all greater ↑ elements.
- update ans.
- push curr element in st.

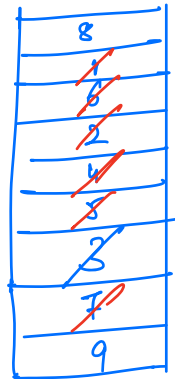
Q2)

Nearest Greater Element on the Left.

arr [9 7 3 5 4 2 6 1 8]

ans [-1 9 7 7 5 4 7 6 9]

→ pop all smaller & equal elements.  
→ update ans.  
→ push curr element in st.



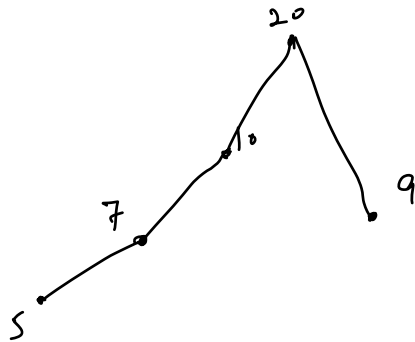
Stack <Integer> st, ans[N]

```
for (i = 0; i < N; i++) {
    while (!st.isEmpty() && st.peek() ≤ arr[i]) {
        st.pop();
    }
    if (st.isEmpty()) { ans[i] = -1; }
    else { ans[i] = st.peek(); }
    st.push(arr[i]);
}
return ans;
```

Q4) Nearest Greater Element on the Right.

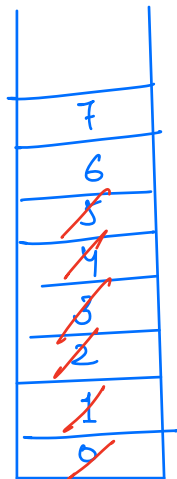
↳ traverse from N-1 to 0

→ index of next smaller element on left / right.



eg-1, arr:  $\begin{bmatrix} 4 & 6 & 10 & 11 & 7 & 6 & 3 & 5 \end{bmatrix}$   
 $\begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \end{matrix}$

(indices of nearest smaller element on l.h.s) arr:  $\begin{bmatrix} -1 & 0 & 1 & 2 & 1 & 0 & -1 & 6 \end{bmatrix}$



- pop all greater & equal.
- update ans.
- push curr index in st.

# pseudo-code:

Stack < Integer > st , ans[n];

for (i=0; i < n; i++) {

while[ !st.isEmpty() && arr[st.peek()] ≥ arr[i] ] {

{  
    st.pop();

if (st.isEmpty() ) { ans[i] = -1 }

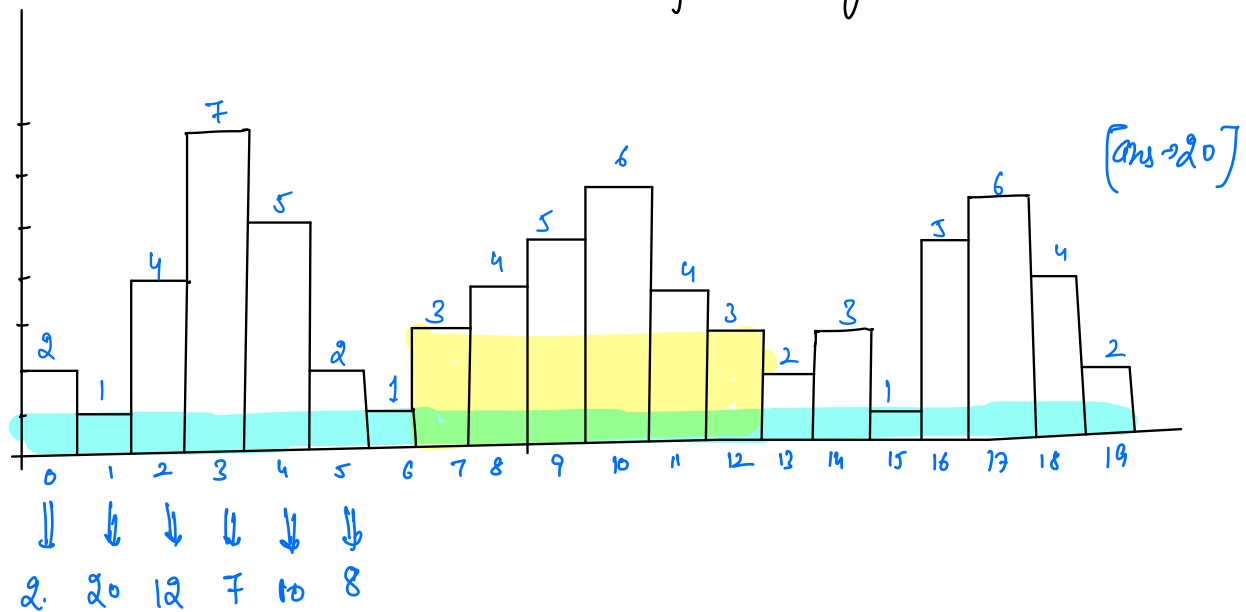
else { ans[i] = st.peek(); }

st.push (i);

}

[ T.L → O(N)  
  S.L → O(N) ]

Q1 Find the largest area of rectangle in histogram  
 ↳ formed by continuous bars.



Max width possible with ht of current bar =  $r - l - 1$ .

↳ Nearest smaller on r.h.s      ↳ Nearest smaller on l.h.s

idea-1 for every bar,  
 traverse & find index of nearest smaller element on l.h.s and  
 traverse & find index of nearest smaller element on r.h.s

$$\max_{i=0}^{n-1} [arr[i] * (r - l - 1)]$$

TC  $\rightarrow O(N^2)$

↳  $O(N)$  ?



Step 1. Create `nsL[N]` (default  $\rightarrow -1$ )  
Step 2. Create `nsR[N]` (default  $\rightarrow N$ )

`ans = 0`

```
for (i = 0; i < N; i++) {  
    ans = Max( ans , arr[i] * (nsR[i] - nsL[i] - 1));  
}  
return ans;
```

$\left[ \begin{array}{l} T.C \rightarrow O(N) \\ S.C \rightarrow O(N) \end{array} \right]$

Q1 Find sum of (max-min) for all subarrays.

	2	5	3
	0	1	2
	max	min	max-min
0-0	2	2	0
0-1	5	2	3
0-2	5	2	3
1-1	5	5	0
1-2	5	3	2
2-2	3	3	0
			<u>8</u>

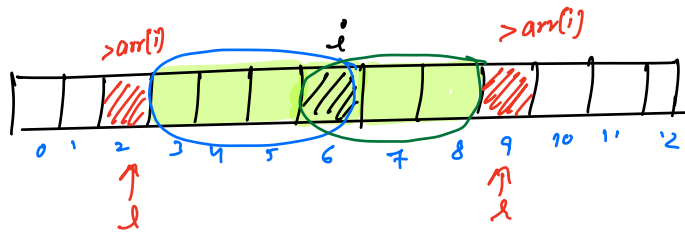
idea-1 Consider all subarrays. T.C  $\sim O(N^2)$

idea-2 Contribution?

$$\sum \max_s - \min_s$$

$$\underbrace{\sum \max_s - \sum \min_s}_{\downarrow}$$

$i^{\text{th}}$  element  $\rightarrow$  in how many subarrays  $i^{\text{th}}$  element will be max.



subarray  
 $\downarrow$   
st, end

3-6	6-6
3-7	6-7
3-8	6-8
4-6	
4-7	
4-8	

5-6  
5-7  
5-8

default value  $\frac{2}{-1}$

$$\max_S = 0$$
$$\max_i += (arr[i] * (i - ngl[i]) * (ngr[i] - i))$$

```
for ( i = 0; i < N; i++) {
    min_i += arr[i]
}
```

$$\min_k = (arr[i] * (i - nsl[i]) * (nsr[i] - i));$$
$$\left[ \begin{array}{l} \text{T.C} \rightarrow O(N) \\ \text{S.C} \rightarrow O(1) \end{array} \right]$$

# Reverse Polish Notation / Postfix Notation

infix: { 8 \* 5 + 4

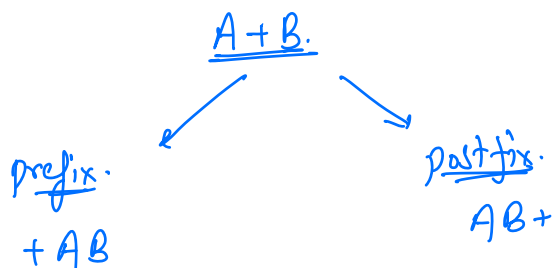
op1 operator op2

prefix: { + \* 8 5 4

operator op1 op2

postfix: { 8 5 \* 4 +

op1 op2 operator



→ 10 + 3 \* 4 - 7

[ 10 3 + 4 \* 7 - X ]

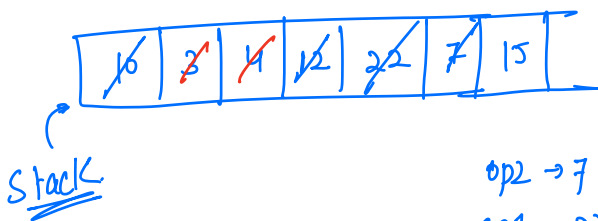
13 4 \* 7 -

52 7 -

45.

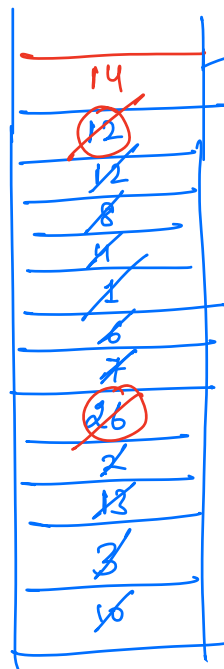
10 3 4 \* + 7 -

↑ ↑ ↑



RPN / postfix →

[ 10 3 + 2 \* 7 6 - 4 8 + \* - ]  
          ↑    ↑    ↑    ↑    ↑    ↑



ans = 14.

op2 → ~~12~~ 12

op1 → ~~1~~ 26

