

## Today's Quote →



## Today's Content

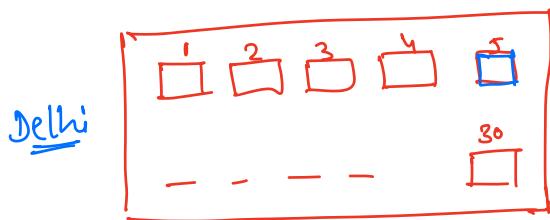
- Hash Map Intro
- frequency of each query.
- first non-repeating element
- Distinct elements
- Subarray with sum = 0



[ Dussehra : 4<sup>th</sup> - 5<sup>th</sup> October ]  
[ Diwali : 22<sup>nd</sup> - 26<sup>th</sup> October ]

## HashMap Intro

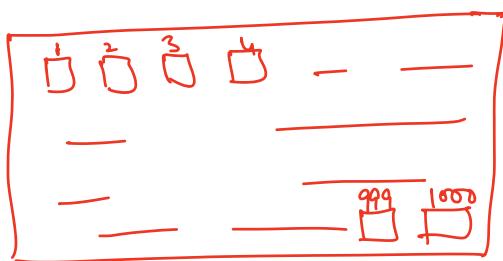
① Aravindhan + Meenakshi



Register

Room No.	Available
1	✗
2	✗
3	✗
4	✗
5	✓
⋮	
30	✓

② Aravindhan + Meenakshi



$[1000^1] \Rightarrow [1 - 1000]$

→ boolean arr  $[1001]$

index → 0 to 1000

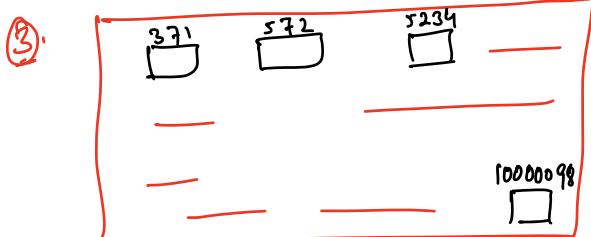
Check for room=3

arr[3] : false.

Check for room=572

arr[572] = true.

Aravindhan + Meenakshi



1000 no's in range  $[1, 10^9]$

→ boolean arr  $[10^9 + 1]$

Disadvantage → Huge Space wastage.

Advantage → TC :  $O(1)$  [arr[i]]

[If you need to check room availability].

$\langle \text{Key}, \text{Value} \rangle$

$\langle 79, \text{ava.} \rangle$

$\langle 95, \text{ava.} \rangle$

$\langle 572, \text{ava.} \rangle$

Check for room = 85

If Key is not there, room 85 is  
not available.

check for room = 572

[572 is available.]

T.C  $\rightarrow O(1)$  for Key-search in hashmap.

S.C  $\rightarrow O(N)$

[Note : - Keys must be unique.  
→ Value can be anything.]

Q1) Store population of every country :

Key : country name → String

Value : population → int / long

HashMap <String, Long> hm.

Q2) Number of states in each country :

Key : country name → String

Value : # no. of states → int

HashMap <String, int> hm

Q3) For every country we want to store all state names.

Key : country name → String

Value : All states names → List <String>

↳ dynamic arrays.

HashMap <String, List<String>> hm

Q4) For every country, store population of each state.

Key : country name → String

Value : population of every state ] ⇒ HashMap <key, value>

state name      ↴      population.

HashMap <String, HashMap <String, Long>> hm.

<u>Key</u>	<u>Value</u>
India	state population
	Delhi → 200
	Andhra → 800
	Gujarat → 600
	Telangana → 550
	Maharashtra → 1000
USA	Texas → 60
	N.Y → 80
	California → 100
	Virginia → 90

### observation

- ① → value can be anything.
- ② → Key can be of primitive data-types only.
  - ↙
  - int|long|float|double|**String**|charach.

### HashSet

- we only store keys.
- keys have to be unique.

## HashMap functionality

$\langle \text{Key}, \text{value} \rangle$

size → {Number of keys in a }  
hashmap

insert (Key, value)

search (Key)

delete (Key)

update (Key, value)

↳ India → ~~143~~ 170

China → 165

U.S.A → 80

again insert (India → 170)

When we insert the same key, it will over-ride the previous value.

A single operation  
will take  
 $O(r)$

## HashSet functionality

$\langle \text{Key} \rangle$

size → {No. of keys in the }  
hashset

insert (Key)

search (Key)

delete (Key)

update (Key) \*

[ HashSet-  
→ India \*  
→ Bharat ]

[ Implementation of HashMap ]  
↓  
Adv. module. ]

Conclusion → A single operation in hashmap / hashset  $\Rightarrow O(1)$

↳ If we insert  $N \langle \text{key}, \text{value} \rangle$  pairs.

T.C  $\rightarrow O(N)$

S.C  $\rightarrow O(N)$

# Hashing library name in Java & python

pseudo-code	Java	Python
HashMap	HashMap	Dictionary.
HashSet	HashSet.	Set.

## Q1) Find frequency of Numbers

Given N array elements & Q queries . for each query ,

find frequency of each element in array-

constraints :  $1 \leq N \leq 10^5$  ,  $1 \leq Q \leq 10^5$  ,  $1 \leq arr[i] \leq 10^9$

$arr[11] : \{ 2_0 \ 6_1 \ 3_2 \ 8_3 \ 2_4 \ 8_5 \ 2_6 \ 3_7 \ 8_8 \ 10_9 \ 6_{10} \}$

$Q=4$       freq.

2 : 3

8 : 3

3 : 2

5 : 0

idea:

For every query , iterate & get count .

$\{ T.C \rightarrow O(N \cdot Q) , S.C \rightarrow O(1) \}$

ideal : store data in hashmap .

Key  $\rightarrow$  array element  $\rightarrow$  (integer)

Value  $\rightarrow$  frequency  $\rightarrow$  (integer)

HashMap < integer, Integer > hm .

$arr[11] : \{ 2_0^{\checkmark} \ 6_1^{\checkmark} \ 3_2^{\checkmark} \ 8_3^{\checkmark} \ 2_4^{\checkmark} \ 8_5^{\checkmark} \ 2_6^{\checkmark} \ 3_7^{\checkmark} \ 8_8^{\checkmark} \ 10_9^{\checkmark} \ 6_{10}^{\checkmark} \}$

Key.	Value.
2	$\rightarrow 3$
6	$\rightarrow 2$
3	$\rightarrow 2$
8	$\rightarrow 3$
10	$\rightarrow 1$

## # pseudo-code:

```
void point freq { int[ ] arr , int[ ] queries; }  
N = arr.length // n → no. of elements  
Q = queries.length // q → no. of queries.  
HashMap <int, int> hm;  
for( i = 0 ; i < N ; i++ ) {  
    if ( hm.search( arr[i] ) == true ) {  
        // arr[i] is already present  
        hm [ arr[i] ] += 1 // increment the  
        freq by 1  
    } else {  
        hm.insert ( arr[i] , 1 );  
    }  
}
```

```
for( i = 0 ; i < Q ; i++ ) {  
    if ( hm.search( Q[i] ) == true ) {  
        // print the value of Q[i] key  
        print ( hm [ Q[i] ] );  
    } else {  
        print ( 0 );  
    }  
}
```

T.C  $\rightarrow O(N+Q)$   
S.C  $\rightarrow O(N)$

Q1) Find the first non-repeating element.  $\Rightarrow$  { first element that is not repeating }

arr[6] : { 1 2 3 1 2 5 } ans = 3

arr[8] : { 4 3 3 2 5 6 4 5 } ans = 2.

arr[7] : { 2 6 8 4 7 2 9 } ans = 6.

Ideas: X① Insert all the elements in hashmap.

iterate in hashmap and find the first element with freq = 1

arr → { 1 2 3 2 4 1 }

key	value
4	1
1	2
2	2
3	1

Note: → order of insertion of key is not maintained.

✓② Insert all the elements in hashmap.

iterate in array and find the first element with freq = 1

arr → { 1 2 3 2 4 1 }

key	value
4	1
1	2
2	2
3	1

T.C → O(N)  
S.C → O(N)

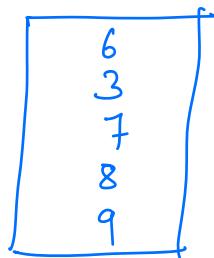
[first non-repeating element]

Q) Given  $\text{arr}[N]$  elements, find no. of distinct elements.

$\text{arr}[5] = \{3, 5, 6, 5, 4\}$ , ans=4, [consider every unique element.]

$\text{arr}[5] = \{1, 1, 1, 2, 2\}$ , ans=2

$\text{arr}[7] = \{6, 3, 7, 3, 8, 6, 9\}$ , ans=5.



ans = hs.size()

Note → In hashset, if you re-insert a key, nothing will happen. [only 1 occurrence will be stored].

### Pseudo-Code

HashSet < int > hs;

{  
for (i=0 ; i < N ; i++) {  
hs.insert(arr[i])  
}

return hs.size()

T.C  $\rightarrow O(n)$   
S.C  $\rightarrow O(n)$

Q1 Given arr[N] elements . Check if all elements are distinct or not ?

arr[S] : { 6 8 3 2 7 } : true

arr[F] : { 3 1 6 1 4 9 6 } : false.

idea: → insert all elements in hashset -

```
if (hs.size() == N){  
    // all elements are distinct  
    return true  
}  
else { // elements are repeating  
    return false.  
}
```

3

T.C  $\rightarrow O(N)$   
S.C  $\rightarrow O(N)$

Q1) Given arr[N] elements . Check if there exists a subarray with sum = 0 . [ true | false ].

arr[10]: { 2 2 1 -3 4 3 1 -2 -3 2 }  
 0 1 2 3 4 5 6 7 8 9

idea1

① For every subarray , calculate sum & check if sum == 0

T.C  $\Rightarrow O(N^2)$   
 S.C  $\Rightarrow O(1)$

3 nested loops      prefix sum      carry forward.  
 $O(N^3)$        $O(N^2)$        $O(N^2)$

idea2.

arr[10]: { 2 2 1 -3 4 3 1 -2 -3 2 }  
 0 1 2 3 4 5 6 7 8 9

pSum: [ 2 4 5 2 6 9 10 8 5 7 ]

observation: In pSum[], no's are repeating.

$$pSum[2] = 5 = \text{sum}[0-2]$$

$$pSum[8] = 5 = \text{sum}[0-8] = \text{sum}[0-2] + \text{sum}[3-8]$$

$$5 = 5 + \cancel{\text{sum}[3-8]}$$

$$pSum[0] = 2 = \text{sum}[0-0]$$

$$pSum[3] = 2 = \text{sum}[0-3] = \text{sum}[0-0] + \text{sum}[1-3]$$

$$2 = 2 + \cancel{\text{sum}[1-3]}$$

Doubt:

$$\text{arr}[4]: \{ 2, -5, 3, 6 \}$$

$$\text{pSum}: \begin{bmatrix} 2 & -3 & 0 & 6 \\ 0 & 2 & 3 \end{bmatrix}$$

$\Rightarrow$  In pSum[] no repeating elements but we do have a sub-array with sum = 0.

$$\text{pSum}[2] = 0$$

$$\text{sum}[0-2] = 0$$

Note → In your pSum[], if a single zero is present, then we have a sub-array with sum = 0

Final observation

- ① if elements are repeating in pSum[]
  - ② if 0 is present in pSum[]
- ⇒ subarray with sum = 0

$$\text{arr} \rightarrow \boxed{1 \ 2 \ 0 \ 4}$$

$$\text{pSum} \rightarrow \boxed{1 \ 3 \ 3 \ 4}$$

$$\text{arr} \rightarrow \boxed{0 \ 1 \ 2 \ 3}$$

$$\text{pSum} \rightarrow \boxed{0 \ 1 \ 3 \ 0}$$

# pseudo-code:

```
boolean checkSubarraySum( arr, N) {  
    psum[N] : // to-do  
    Hashset<int> hs;  
    for( i=0 ; i < N ; i++) {  
        if ( psum[i] == 0) { return true }  
        hs.insert( psum[i]);  
    }  
    if ( hs.size() < N) { // elements repeating  
        in psum[]  
        return true  
    }  
    else {  
        return false  
    }  
}
```

T.C  $\rightarrow O(N)$   
S.C  $\rightarrow O(N)$

Doubts:

Min. value of  $A^T X + B^T X$ .

1^1 = 0
0^0 = 0
0^1 = 1
1^0 = 1

$$\begin{array}{l} A \rightarrow \begin{array}{ccccccccc} 7 & 0 & 5 & 3 & 2 & 1 & 0 \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 0 & 1 & 0 & | & 1 & 0 & | & 0 \end{array} \\ \wedge \quad \begin{array}{ccccccccc} 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ \vdots & & & & & & \\ 0 & 1 & 0 & 0 & 0 & 1 & 0 \end{array} \\ \hline 0 & 1 & 0 & 0 & 0 & 1 & 0 \end{array}$$

+

$$\Rightarrow 2^6 + 2^1$$

$$\begin{array}{l} B \rightarrow \begin{array}{ccccccccc} 7 & 0 & 5 & 4 & 3 & 2 & 1 & 0 \\ \downarrow & \downarrow \\ 0 & 0 & 1 & 1 & 0 & 0 & 1 & 0 \end{array} \\ \wedge \quad \begin{array}{ccccccccc} 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 \\ \vdots & & & & & & & \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \end{array} \\ \hline 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \end{array}$$

$$2^5 + 2^0$$

[idea  $\rightarrow$  unset the bit in both the numbers.]

$$ans = 2^6 + 2^1 + 2^5 + 2^0$$

$$\begin{array}{r}
 A \rightarrow \begin{array}{ccccccccc}
 & 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\
 \underline{0} & | & 0 & | & 1 & 0 & | & 0 & \\
 \swarrow & & \downarrow & & \downarrow & & \downarrow & \\
 \underline{0} & 1 & 1 & 1 & 1 & 0 & 1 & 1 \\
 \hline
 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1
 \end{array} \\
 + \\
 B \rightarrow \begin{array}{ccccccccc}
 & 7 & 6 & 5 & 4 & 3 & 2 & 1 & 0 \\
 \underline{0} & 0 & | & 1 & 1 & 1 & 0 & 0 & 1 \\
 \swarrow & & \downarrow & & \downarrow & & \downarrow & \\
 \underline{0} & 1 & 1 & 1 & 1 & 0 & 1 & 1 \\
 \hline
 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0
 \end{array}
 \end{array}$$

$\Rightarrow 2^5 + 2^1 + 2^6 + 2^0$   
 $\Rightarrow (2^6 + 2^5 + 2^1 + 2^0)$

final observation: → if  $i$ th-bit in both the no's.  
 {  
 → 1, then in X it should be 1.  
 → 0, then in X it should be 0  
 }  
 → if  $i$ th-bit is different in both the no's.  
 It can be 0 or 1 in X.  
 for simplicity, consider it 0.

To achieve this, take AND of A, B.

$$\underline{[X = A \& B]}$$

$$\rightarrow \underbrace{A^{\wedge}(A \& B) + B^{\wedge}(A \& B)}_{\boxed{T.C \rightarrow O(1) \\ S.C \rightarrow O(1)}}$$

A = 6

B = 12.

$A \rightarrow \begin{array}{r} 3 \\ 2 \\ 1 \\ 0 \\ \hline 0 \ 1 \ 1 \ 0 \\ \hline 0 \ 0 \ 1 \ 0 \end{array}$

$B \rightarrow \begin{array}{r} 3 \\ 2 \\ 1 \\ 0 \\ \hline 1 \ 1 \ 0 \ 0 \\ \hline 0 \ 1 \ 0 \ 0 \end{array}$

$x = 4$

$\begin{array}{r} 0 \ 0 \ 1 \ 0 \\ + \\ 1 \ 0 \ 0 \ 0 \\ \hline 1 \ 0 \ 0 \ 0 \end{array}$

$2^1 + 2^3 = \boxed{10} \Rightarrow \text{minimum possible value.}$