

- L.I.S
- Russian Doll Envelopes
- Count of palindromic substrings.
- Palindromic partition

## Longest Increasing Subsequence

arr  $\rightarrow$  [ 10 3 12 7 2 9 11 20 11 13 6 8 ]

$[3, 7, 9, 11, 20] \rightarrow 5$

$[3, 7, 9, 11, 13] \rightarrow 5$

idea. - Consider all increasing subsequences.

[Back-tracking]

T.L  $\rightarrow O(2^N)$

$[lis[i] = \text{length of longest increasing subsequence ending at } idx - i]$

arr  $\rightarrow$   $\left[ \begin{array}{cccccccccccc} 10 & 3 & 12 & 7 & 2 & 9 & 11 & 20 & 11 & 13 & 6 & 8 \end{array} \right]$   
 $\begin{array}{cccccccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 \end{array}$

lis[NT] [ 1 1 2 2 1 3 4 5 4 5 2 3 ]  
 ~10" ~3" ~10,12" ~3A" ~2" ~3A,9" ~3,7,9,11" ~3,7,9,11,20" ~3,7,9,11,13 ~2,6,8  
 ~3,12" ~3,7,9,11

# pseudo-code -

lis[N]; // initialise with 0  
ans = 0

```
for (i = 0; i < N; i++) {  
    max → 0  
    for (j = i-1; j >= 0; j--) {  
        if (arr[j] < arr[i]) {  
            max = Max(max, lis[j])  
        }  
    }  
    lis[i] = max + 1  
    ans = Max(ans, lis[i])  
}
```

$\left[ \begin{array}{l} T.C \rightarrow O(N^2) \\ S.C \rightarrow O(N) \end{array} \right]$

$O(\underline{N \log N})$   
length. [P.S.]

---

main( — ) {

```
    int ans = 1, int dp[N];  
    for (i = 0; i < N; i++) {  
        ans = Max(ans, lis(arr[i], i, dp));  
    }  
    return ans;  
}
```

```

int dis ( int arr[ ], int i, int dp[] ) {
    if ( dp[i] != -1 ) { return dp[i] ; }
    max = 0 ;
    for ( j = i-1 ; j >= 0 ; j-- ) {
        if ( arr[j] < arr[i] ) {
            max = max ( max, dis ( arr, j ) ) ;
        }
    }
    dp[i] = max + 1 ;
}

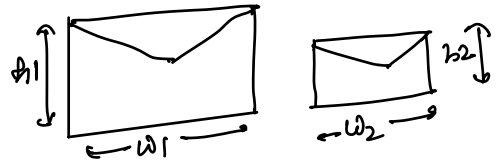
```

# Russian Doll Envelopes

N - different envelopes.

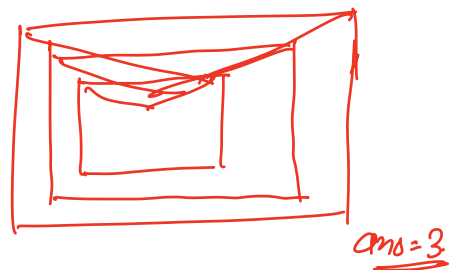
Find max count of envelopes that can be put in a single envelope.

Note → Rotation of envelope is not allowed.



$$\begin{cases} h_1 > h_2 \\ w_1 > w_2 \end{cases}$$

	<u>h</u>	<u>w</u>	
A →	5	6	-
B →	6	4	
C →	6	7	✓
D →	4	3	✓



h →	9	5	10	3	4	2
w →	3	4	8	2	3	7
	1	1	2	3	4	5

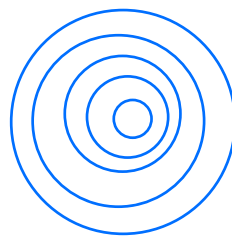
~~Greedy →~~

10	9	3	②
8	3	2	
10	2		②
8	7		

10	5	4	3
8	4	3	2

(ans = 4)

ans 5, 6, 7, 3, 9, 7, 5



Single dimension greedy ✓

h →	10	3	4	9
w →	8	2	3	2
<u>area</u> →	80	6	12	18

Greedy on area ~~X~~

Sort envelopes on the basis of height.

h →	1	2	3	4	4	5	7	10	10	12	15
w →	10	3	7	9	11	20	11	6	12	8	2

- ① Sort the arr according to height
- ② Apply L.I.S on width  $[h_1 \neq h_2]$

$$\begin{bmatrix} T.C \rightarrow O(n^2) \\ S.C \rightarrow O(n) \end{bmatrix}$$

Q1 Given a string. for every substring, check if that is a palindrome or not. (ans  $\rightarrow$  2D array)

$s = a b c b$   
 0 1 2 3

$\xrightarrow{ei}$

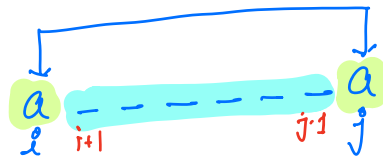
	0	1	2	3
$si \downarrow$ 0	t	f	f	f
1	X	t	f	t
2	X	X	t	f
3	X	X	X	t

ans.

Idea 1.  $\rightarrow$  Consider all substrings &  $\rightarrow \frac{n(n+1)}{2}$   
 iterate & check if that substring  $\rightarrow N$   
 is a palindrome.

$\left[ \begin{array}{l} T.C \rightarrow O(N^3) \\ S.C \rightarrow O(1) \end{array} \right]$

observation



gap = 0

0, 0

1, 1

2, 2

3, 3

gap = 1

0, 1

1, 2

2, 3

gap = 2

0, 2

1, 3

gap = 3

0, 3

boolean dp[N][N]:

```
for(int gap = 0 ; gap < n ; gap++) {  
    i = 0, j = gap  
    while( j < n ) {  
        if (gap == 0) { dp[i][j] = true }  
        else if (gap == 1) {  
            if (s[i] == s[j]) { dp[i][j] = true }  
            else { dp[i][j] = false }  
        }  
        else {  
            if (s[i] == s[j] && dp[i+1][j-1] == true) { dp[i][j] = true }  
            else { dp[i][j] = false }  
        }  
        i++, j++ ;  
    }  
}  
return dp[0][n-1];
```

T.C  $\rightarrow O(N^2)$   
S.C  $\rightarrow O(1)$

→ count of all palindromic substrings.  
T.C  $\rightarrow O(N^2)$  , S.C  $\rightarrow O(N^2)$



Q: Find min no. of cuts to partition the string such that all the partitions are palindrome.

Ex  $\rightarrow$   $xx|y$

$ans = 1$

$a|bcb|b$

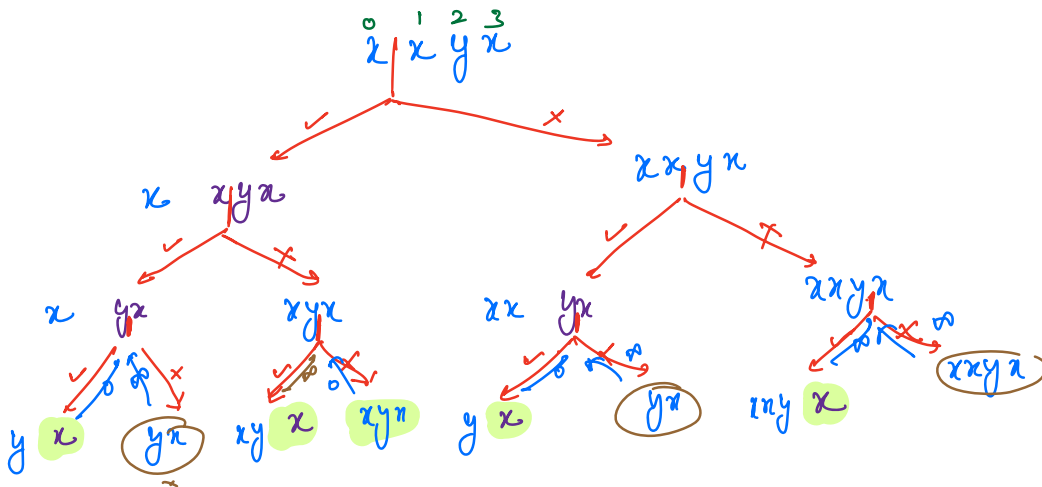
$ans = 2$

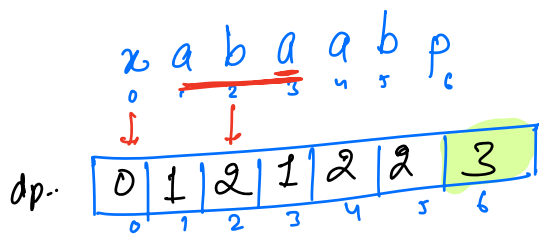
$x|a|b|a|a|b|p$   $ans = 3$

$a|bcb$   $ans = 1$

$a|b|c|d$   
 $\downarrow \downarrow \downarrow$   
 $x \ x \ x$

#ways  $= 2^{n-1} = 2^3 = 8$





$dp(i) \rightarrow$  min cuts required for string  $[0, i]$

$\rightarrow$  make the cut only when you are getting palindrome.

# pseudo-code.

$dp[N], P[7][7] \rightarrow$  // for all substrings if they are palindromes or not.

$dp[0] = 0$  // edge case.

for ( $j = 1; j < N; j++$ ) {

if ( $P[0][j] == true$ ) {  $dp[j] = 0$  }

else {

min  $\rightarrow \infty$

for ( $i = 1; i \leq j; i++$ ) {

if ( $P[i][j] == true$ ) {

min = Min(min,  $dp[i-1]$ )

$dp[j] = min + 1$

}

$dp[N-1];$

$T.C \rightarrow O(N^2)$   
 $S.C \rightarrow O(N^2)$

→ (tree, l.d, hashmap, sorting & searching.)