

# Amicable numbers

## Problem 21 (<http://projecteuler.net/problem=21>)

Let  $d(n)$  be defined as the sum of proper divisors of  $n$  (numbers less than  $n$  which divide evenly into  $n$ ). If  $d(a) = b$  and  $d(b) = a$ , where  $a \neq b$ , then  $a$  and  $b$  are an amicable pair and each of  $a$  and  $b$  are called amicable numbers.

For example, the proper divisors of 220 are 1, 2, 4, 5, 10, 11, 20, 22, 44, 55 and 110; therefore  $d(220) = 284$ . The proper divisors of 284 are 1, 2, 4, 71 and 142; so  $d(284) = 220$ .

Evaluate the sum of all the amicable numbers under 10000.

## Solution

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In [1]: ▶ def dn(n):  
        x, h, s = 1, n//2, 0  
        while x<=h:  
            if n % x == 0:  
                s += x  
            x += 1  
        return s  
  
        print(sum(x for x in range(10000) if x == dn(dn(x)) and x  
31626
```