

INTELIGENTNI SISTEMI MATERIJAL ZA AUDITORNE VJEŽBE

STATIČKE NEURONSKE MREŽE

- nemaju povratne veze (nema povratka u više slojeve)
- kreiranje neuronske mreže se vrši naredbom:

```
net=newff(PR, [S1, S2, ..., SN], {'TF1','TF2',...'TFN'},'BFT');
```

gdje je:

PR – min i max vrijednost funkcije

S – velicina sloja

TF – aktivacijska funkcija sloja

BTF – algoritam učenja, metoda učenja (treniranje)

Naredbe za treniranje neuronske mreže:

npr. neke vrijednosti za parametre

- 1) net.performFcn='sse'; (funkcija performansi sse)
- 2) net.trainParam.goal=30; (ukupna kvadratna pogreška izlaza)
- 3) net.trainParam.show=10; (frekvencija prikaza rezultata u kvadratnom prozoru)
- 4) net.trainParam.epochs=1000; (maksimalni broj epoha, iteracija-vrijeme treniranja neuronske mreže)
- 5) net.trainParam.me=0.95; (momentna konstanta)
- 6) net.trainParam.lr=0.05; (brzina učenja);

Naredba za treniranje mreže:

```
net1=train(net,x,y);
```

gdje je:

net- kreirana mreža

x – ulaz

y – izlaz

Nakon toga treba prikazati istreniranu mrežu metodom simulacije:

```
ytest=sim(net1,x);
```

gdje je:

net1 – istrenirana mreža

x - ulaz

PRIMJER 1: Kreirati funkciju humps, $y = (1/((x-3)^2+0.01) + 1/((x-9)^2+0.04)) - 6$

```
x=0:0.05:2;
y=humps(x);
P=x;
T=y;
plot(P,T,'x');
grid ON

%kreiranje neuronske mreže
net=newff([0 2],[5,1],{'tansig','purelin'},'traingd');

%definiranje parametara mreže
net.trainParam.show=50;
net.trainParam.lr=0.05;
net.trainParam.epochs=1000;
net.trainParam.goal=1e-3; %greška tolerancije

%treniranje neuronske mreže
net1=train(net,P,T);

%pohrana vrijednosti - simulacija
a=sim(net1,P);

%iscrtavanje rezultata i poredenje
plot(P,a,'r',P,T,'g');
legend('neuronska mreza','humps funkcija');
```

PRIMJER 2: Aproksimirati signal sa šumom, ako je zadani signal: $e^{-0.1x^2} \sin(5 \sin(3\pi))$;

```
x=0:0.1:5;
T0=exp(-0.1*x.^2).*sin(5*sin(3*pi)); % signal
T=T0+0.05*randn(size(P)); % signal sa šumom

net=newff(minmax(P),[30 1],{'tansig','purelin'},'traincgf');

%definiranje parametara mreže
net.trainParam.show=100;
net.trainParam.epochs=2000;
net.trainParam.goal=2e-4;

%treniranje neuronske mreže
[net,tr]=train(net,P,T);

figure(1)
plot(P,T0,P,T,':r','linewidth',2);
legend('signal','signal sa šumom');

figure(2)
```

```

plot(P,T,':r',P,a,'b','linewidth',2);
legend('signal sa šumom','neuronska mreža');
figure(3)
plot(P,T0,P,a,':g','linewidth',2);
legend('signal','neuronska mreža');

```

PEIMJER 3: Aproksimirati signal sa šumom, ako je zadani signal: $f(x) = e^{-2\sin^2(x)} \sin(5x)$;

```

x=-4:0.01:4;
T0=exp(-2*sin(x).^2).*sin(5x); % signal
T=T0+0.05*randn(size(P)); % signal sa šumom

net=newff([-4 4],[30 1],{'tansig','purelin'},'traincgf');

%definiranje parametara mreže
net.trainParam.show=100;
net.trainParam.epochs=2000;
net.trainParam.goal=2e-4;

%treniranje neuronske mreže
[net,tr]=train(net,P,T);

```

```

figure(1)
plot(P,T0,P,T,':r','linewidth',2);
legend('signal','signal sa šumom');

```

```

figure(2)
plot(P,T,':r',P,a,'b','linewidth',2);
legend('signal sa šumom','neuronska mreža');
figure(3)
plot(P,T0,P,a,':g','linewidth',2);
legend('signal','neuronska mreža');

```

PRIMJER 4: Za zadanu funkciju $x=5\sin(2\pi i)$, istrenirati neuronsku mrežu ako je $i=0:10$

```

i=0:0.1:10;
x=5*sin(2*pi*i);
plot(i,x);
figure
pause

P=[i];
T=[x];
net=newff([0 10],[20 1],{'tansig','purelin','trainlm'});
izlaz=sim(net,i);
plot(i,izlaz,'*r');
hold ON

plot(i,x);
hold ON

```

pause

```
fprintf('Pocetak treniranja \n');
net.trainParam.epochs=3000;
net.trainParam.show=10;
net.trainParam.time=Inf;
net.PerformFcn='sse';
```

```
tic
net=train(net,P,T);
toc
```

```
figure
izlaz=sim(net,i);
plot(i,izlaz,'g*');
hold ON
```

```
plot(i,x);
```

```
gensim(net,0.1);
```

PRIMJER 5: Predstaviti model 3D funkcije $Z=\cos x \cdot \sin y$ definiranu na opsegu $x=[-2,2]$, $y=[-2,2]$

a)Iscrtati funkciju

b)Kreirati neuronsku mrežu za funkciju pod a) ako je prvi sloj mreže na vrijednosti 25, drugi 17. Koristiti funkcije tansig i purelin. Algoritam treniranja je trainlm. Rezultat prikazati svakih 50 iteracija ako je brzina učenja 0.05, a tolerancija greške 3000.

```
x=-2:0.25:2;
y=-2:0.25:2;
```

```
z=cos(x) .*sin(y);
figure(1)
mesh(x,y,z);
xlabel('x osa');
ylabel('y osa');
zlabel('z osa');
title('Model 3d funkcije');
pause
```

```
P=[x;y];
T=z;
net=newff([-2 2;-2 2],[2 17],{'tansig','purelin'},'trainlm');
net.trainParam.show=50;
net.trainParam.lr=0.05;
net.trainParam.epochs=3000;
net.trainParam.goal=1e-3;
```

```
net1=train(net,P,T);
a=sim(net1,P);
```

```
figure(2)
mesh(x,y,a);
xlabel('x osa');
ylabel('y osa');
```

```

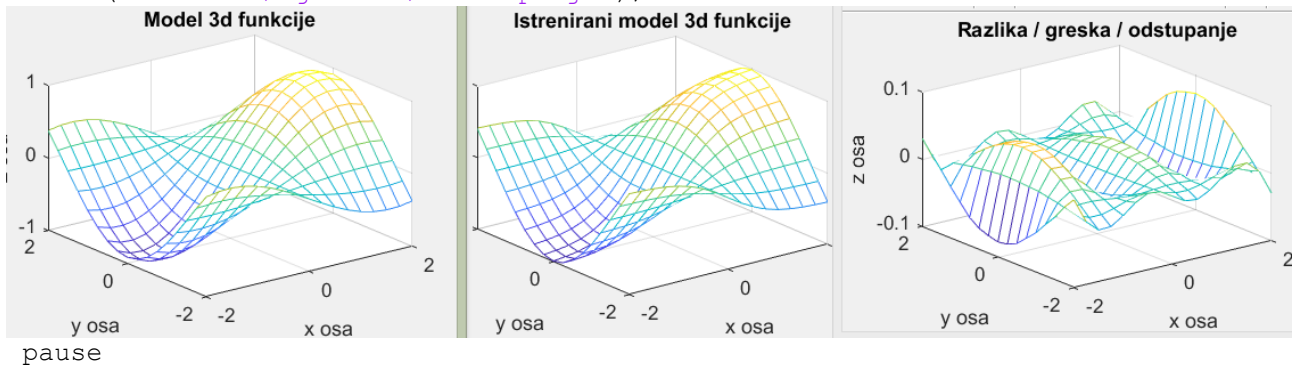
zlabel('z osa');
title('Istrenirani model 3d funkcije');
pause

```

```

figure(3)
mesh(x,y,a-z);
xlabel('x osa');
ylabel('y osa');
zlabel('z osa');
title('Razlika / greska / odstupanje');

```



PRIMJER 6: Kreirati običnu neuronsku mrežu koja će oponašati funkciju

$$10s^2 + 106s + 60 / 4s^3 + 14s^2 + 106s + 60$$

```

P=[y(:,1)];
T=[y(:,2)];

```

```

minulaz=min(P);
maxulau=max(P);
minizlaz=min(T);
maxizlaz=max(T);

```

```

p=2*(P-minulaz)./(maxulaz-minulaz)-1;
t=2*(T-minizlaz)./(maxizlaz-minizlaz)-1;

```

```

net=newff([-1 1], [60 1], {'tansig','purelin'},'trainlm');

```

```

net.trainParam.epochs=1000;
net.trainParam.show=100;
net.trainParam.time=2e-9;
net.performFcn='sse';

```

```

tic
net=train(net,p',t');
toc

```

```

izalz=sim(net,p);
izlaz=(izlaz+1)*(maxizlaz-minizlaz).*2+maxizlaz;

```

```

figure
plot(p',izlaz,'r');

```

```

title('Podaci dobiveni sa treniranom neuronskom mrežom');
xlabel('x osa');
ylabel('y osa');

gensim(net,0.1);

```

PRIMJER 7: Kreirati neuronsku mrežu koja će oponašati inverznu dinamiku sistema:

$$25s^2 + 50s + 50 / 15s^3 + s^2 + 50s + 50$$

```

N=4;
P=y(:,1);
T=y(:,2);

minulaz=min(P);
maxulaz=max(P);
minizlaz=min(T);
maxizlaz=max(T);

net=newff([zeros(2*N,1)-1 zeros(2*N,1)+1], [15 5 1], {'tansig','tansig','purelin'},'trainlm');

net.trainParam.epochs=2000;
net.trainParam.goal=2e-9;
net.trainParam.show=10;
net.trainParam.time=Inf;
net.performFcn='sse';

P=2*(P-minulaz)./(maxulaz-minulaz)-1;
T=2*(T-minizlaz)./(maxizlaz-minizlaz)-1;

vel=length(T);
ulaz=zeros(2*N, vel-N);
izlaz=zeros(1, vel-N);

for k=N:vel-1
    k=flipud(T(k-N+1:k+1));
    p=flipud(P(k-N+1:k-1));
    ulaz(:,k)=[t;p];
    izlaz(k)=p(k);
end

tic
net=train(net,ulaz,izlaz);
toc

izlaz=sim(net,ulaz);
izlaz=(izlaz+1)*(maxulaz-minulaz)./2+minulaz;

gensim(net);

```

PRIMJER 8: Kreirati inverznu neuronsku mrežu za zadanu funkciju: $1/s^2 + s + 2$ ili $1/(s+1)^2 + 1$

```
N=4;
brojepoha=500;

minulaz= -3;
maxulaz= 3;
minizlaz= -2;
maxizlaz= 2;

net=newff([zeros(2*N,1)-1 zeros(2*N,1)+1], [15 5 1], {'tansig','tansig','purelin'},'trainlm');

net.trainParam.epochs=brojepoha;
net.trainParam.goal=0;
net.trainParam.show=10;
net.trainParam.time=Inf;
net.performFcn='sse';

fprintf('Opseg ulaza je: (% g, % g) \n' , minizlaz, maxizlaz);
fprintf('Pocetak treniranja');

P=t(:,1);
T=t(:,2);

P=2*(P-minulaz)./(maxulaz-minulaz)-1;
T=2*(T-minizlaz)./(maxizlaz-minizlaz)-1;

vel=length(T);

ulaz=zeros(2*N, vel-N);
izlaz=zeros(1, vel-N);

for k=N:vel-1
    k=flipud(T(k-N+1:k+1));
    p=flipud(P(k-N+1:k-1)); % okreće niz, zadnji dio stavlja na prvi
    ulaz(:,k)=[t;p];
    izlaz(k)=p(k);
end

fprintf('Pocetak treniranja');

tic
net=train(net,ulaz,izlaz);
toc

izlaz=sim(net,ulaz);
izlaz=(izlaz+1)*(maxulaz-minulaz)./2+minulaz;
```

```
figure
plot(izlaz,'r');
title('Podaci dobiveni sa treniranom mrežom');
```

```
gensim(net, 0.1);
```

PRIMJER 8: Kreirati Elmanovu neuronsku mrežu za zadanu funkciju na intervalu 0-5, brojem iteracija 1500 i greškom 10^{-9} . Algoritam treniranja je traingdx.

$$y = e^{-0.2x^2} \sin(5 \sin 3x)$$

```
p=0:0.01:5;
t=exp(-0.1*p.^2).*sin(5*sin(3*p));
```

```
P=p;
T=t;
```

```
Pseq=con2seq(P); % pretvaranje niza u polje, uzalz
Tseq=con2seq(T);
```

```
net=newelm(minmax(P), [30 10 1], {'tansig','tansig','purelin'},'traingdx');
```

```
net.trainParam.epochs=1500; % 8000
net.trainParam.show=50;
net.trainParam.goal=0.000000001; % 0.00001
```

```
tic
[net,tr]=train(net,Pseq,Tseq);
toc
```

```
a=sim(net,Pseq);
b=cat(2,a{:}); % prikaz polja
```

```
time=1:length(p);
plot(time,t,'b- -',time,b,'r- -');
title('Rezultat treniranje mreže');
xlabel('vrijeme');
ylabel('izlazne vrijednosti');
legend('signal','elmanova mreza');
```

PRIMJER 9: Kreirati Elmanovu neuronsku mrežu za zadanu funkciju, za x na intervalu 0-5, broj iteracija 3000, greška 10^{-4} , algoritam treniranja traingdx. $y = 5 \sin((2 \pi x)/5)$

```
p=0:0.01:5;
t=5*(sin(2*pi*p)/5);
P=p;
T=t;
Pseq=con2seq(P); % pretvaranje niza u polje, uzalz
```



```

Tseq=con2seq(T);

net=newelm(minmax(P), [30 10 1], {'tansig','tansig','purelin'},'traingdx');

net.trainParam.epochs=3000;
net.trainParam.show=50;
net.trainParam.goal=0.0001;

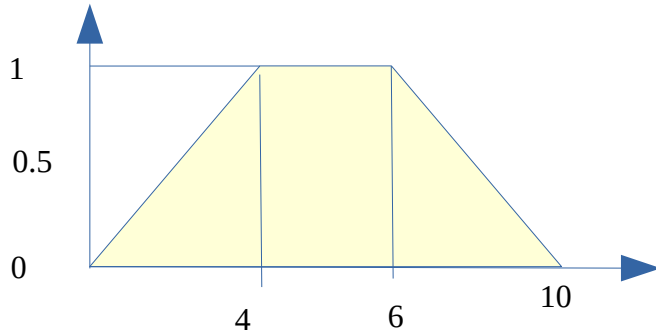
tic
[net,tr]=train(net,Pseq,Tseq);
toc

a=sim(net,Pseq);
b=cat(2,a{:}); % prikaz polja

time=1:length(p);
plot(time,t,'b- -',time,b,'r- -');
title('Rezultat treniranje mreže');
xlabel('vrijeme');
ylabel('izlazne vrijednosti');
legend('signal','elmanova mreza');

```

PRIMJER 10: Kreirati Elmanovu neuronsku mrežu na intervalu 0-10, broj iteracija 3000, greška 10^{-4} i algoritam učenja je traingdx.

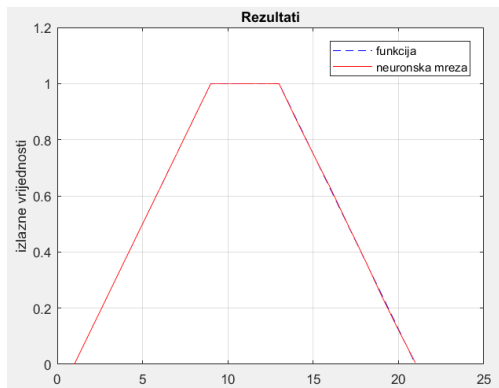


```

p=0:0.5:10;
t=(1/4).*(p.*(p<=4)+4*((p>4) & (p<=6)) + (10-p).*((p>6) & (p<=10)));
P=p;
T=t;
Pseq=con2seq(P);
Tseq=con2seq(T);
net=newelm(minmax(P), [40 1], {'tansig','purelin'}, 'traingdx');
net.trainParam.epochs=2500;
net.trainParam.show=50;
net.trainParam.goal=1e-7;
tic
[net,tr]=train(net,Pseq,Tseq);
toc
a=sim(net,Pseq);
b=cat(2,a{:});
time=1:length(p);
plot(time,t,'b--',time,b,'r')

```

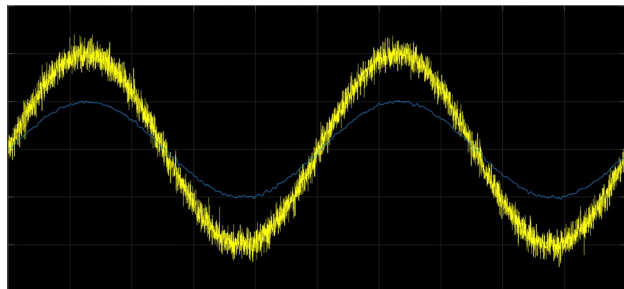
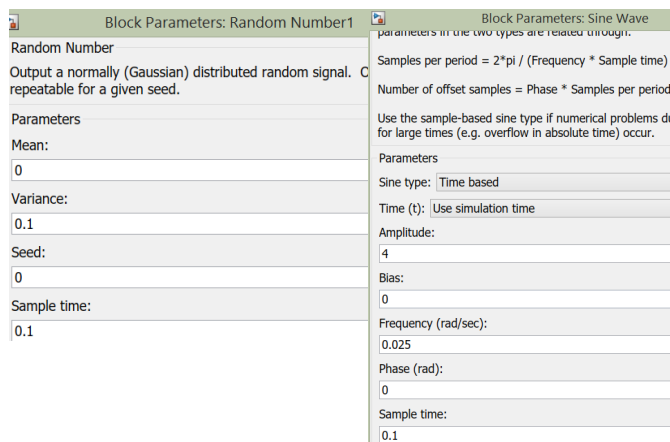
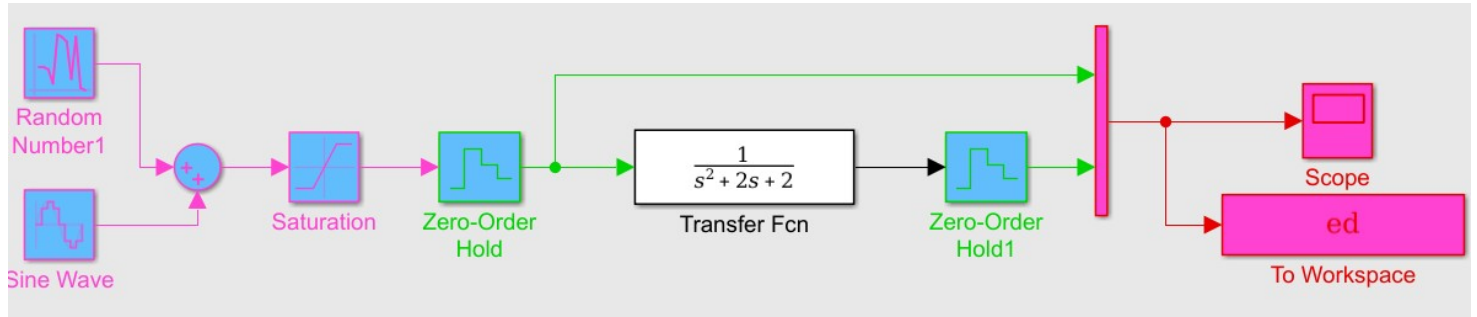
```
grid on
title('Rezultati');
xlabel('vrijeme');
ylabel('izlazne vrijednosti')
legend('funkcija', 'neuronska mreza');
```



INVERZNA DINAMIKA

a) ulazni signal

vrijeme simulacije $t=500$



b) Matlab kod

```
N=4;
% Priprema podataka za treniranje mreze
fprintf('Priprema podataka za treniranje mreze...\n');
P= ed(:, 1);
T = ed(:, 2);
minulaz = min(P);
maxulaz = max(P); %opseg ulaznih vrijednosti
minizlaz = min(T);
maxizlaz = max(T); %opseg moguceg izlaza

net = newff([zeros(2*N,1)-1 zeros(2*N,1)+1], ...
[15 5 1], {'tansig', 'tansig', 'purelin'}, 'trainlm');

net.trainParam.epochs = 2000;
net.trainParam.goal = 2e-9;
net.trainParam.show = 10;
net.trainParam.time = Inf;

fprintf('Opseg ulaza mreze je: [%g, %g].\n', minizlaz, maxizlaz);

% normiranje ulaza i izlaza na opseg [-1, 1]
P= 2 * (P - minulaz) ./ (maxulaz - minulaz) - 1;
T= 2 * (T - minizlaz) ./ (maxizlaz - minizlaz) - 1;
```

```

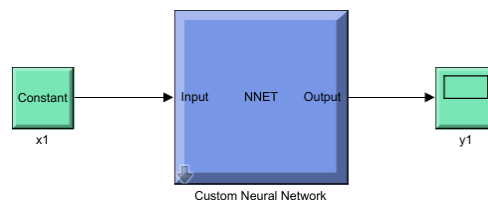
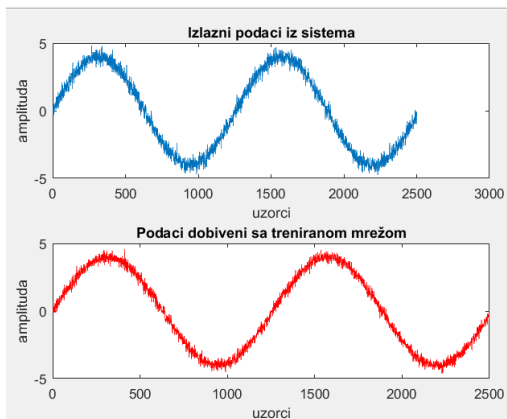
vel = length(T);
ulaz = zeros(2*N, vel-N);
izlaz = zeros(1, vel-N);

for k = N : vel-1
    t = flipud( T(k-N+1:k+1) );
    p = flipud( P(k-N+1:k-1) );
    ulaz(:,k) = [t; p];
    izlaz(k) = P(k);
end;
% Treniranje...
fprintf('Po?etak treniranja\n');
tic
net = train(net, ulaz, izlaz);
toc

izlaz=sim(net,ulaz);
izlaz=(izlaz+1)*(maxulaz-minulaz)./2 +minulaz;

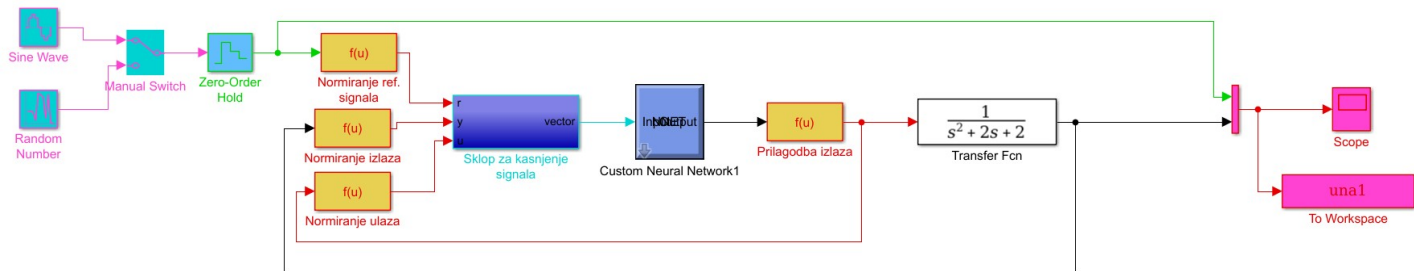
figure
subplot(2,1,1),plot(ed(:,1));
title('Izlazni podaci iz sistema');
xlabel('uzorci')
ylabel('amplituda')
subplot(2,1,2),plot(izlaz,'r')
title('Podaci dobiveni sa treniranjem mrežom');
xlabel('uzorci')
ylabel('amplituda')
gensim(net,0.1)

```



c) završni model

$t=500$



Block Parameters: Sine Wave

Parameters in the two types are related through:

Samples per period = $2\pi / (\text{Frequency} * \text{Sample time})$

Number of offset samples = $\text{Phase} * \text{Samples per period} / (2\pi)$

Use the sample-based sine type if numerical problems due to running for large times (e.g. overflow in absolute time) occur.

Parameters

Sine type: Time based

Time (t): Use simulation time

Amplitude: 2

Bias: 0

Frequency (rad/sec): 0.25

Phase (rad): 0

Sample time: 0.1

☒ Interpret vector parameters as 1-D

Block Parameters: Random Number

Output a normally (Gaussian) distributed random signal. Output repeatable for a given seed.

Parameters

Mean: 0

Variance: 0.05

Seed: 0

Sample time: 20

Block Parameters: Normiranje ref. signala

Fcn

General expression block. Use "u" as the input variable name. Example: $\sin(u(1)) * \exp(2.3 * (-u(2)))$

Parameters

Expression: $2 * (u(1) - \text{minizlaz}) / (\text{maxizlaz} - \text{minizlaz}) - 1$

Sample time: *Not recommended for this block. Set to -1 to inherit from the top-level system.*

0.1

Block Parameters: Normiranje izlaza

Fcn

General expression block. Use "u" as the input variable name. Example: $\sin(u(1)) * \exp(2.3 * (-u(2)))$

Parameters

Expression: $2 * (u(1) - \text{minizlaz}) / (\text{maxizlaz} - \text{minizlaz}) - 1$

Sample time: *Not recommended for this block. Set to -1 to inherit from the top-level system.*

0.1

Block Parameters: Normiranje ulaza

Fcn

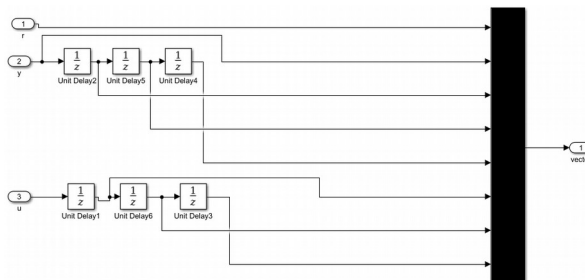
General expression block. Use "u" as the input variable name. Example: $\sin(u(1)) * \exp(2.3 * (-u(2)))$

Parameters

Expression: $2 * (u(1) - \text{minulaz}) / (\text{maxulaz} - \text{minulaz}) - 1$

Sample time: *Not recommended for this block. Set to -1 to inherit from the top-level system.*

0.1



Block Parameters: Prilagodba izlaza

Fcn

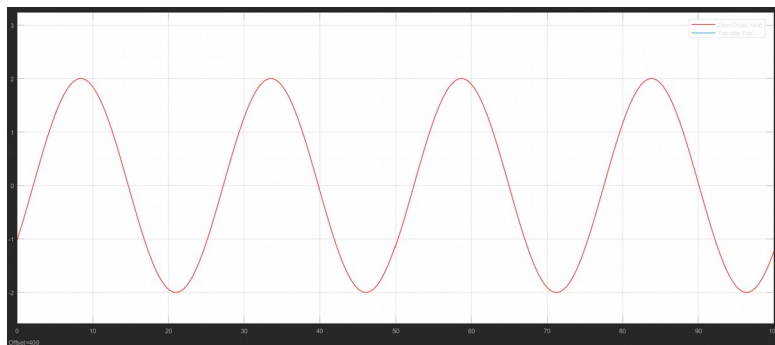
General expression block. Use "u" as the input variable name. Example: $\sin(u(1)) * \exp(2.3 * (-u(2)))$

Parameters

Expression: $(u(1) + 1) * (\text{maxulaz} - \text{minulaz}) / 2 + \text{minulaz}$

Sample time: *Not recommended for this block. Set to -1 to inherit from the top-level system.*

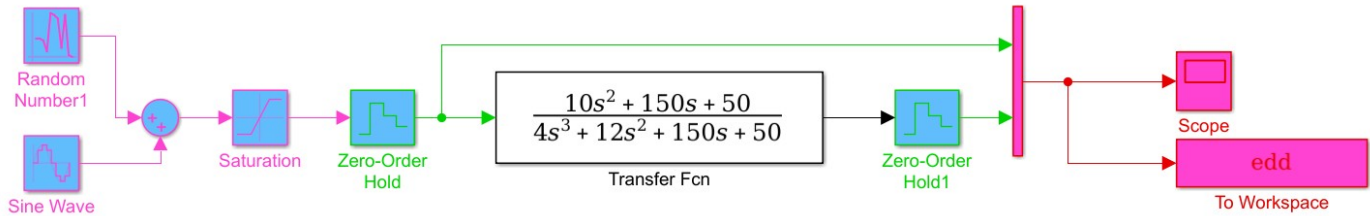
0.1



DINAMIČKA NEURONSKA MREŽA - NARKS

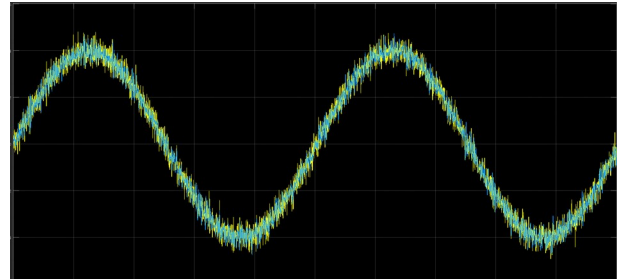
a) ulazni signal

vrijeme simulacije $t=500$



Block Parameters: Random Number1	
Random Number	
Output a normally (Gaussian) distributed random signal, repeatable for a given seed.	
Parameters	
Mean:	0
Variance:	0.1
Seed:	0
Sample time:	0.1

Block Parameters: Sine Wave	
Sine Wave	
Output a sine wave:	
$O(t) = \text{Amp} \cdot \sin(\text{Freq} \cdot t + \text{Phase}) + \text{Bias}$	
Sine type determines the computational technique used. The parameters in the two types are related through:	
Samples per period = $2 \cdot \pi / (\text{Frequency} \cdot \text{Sample time})$	
Number of offset samples = $\text{Phase} \cdot \text{Samples per period} / (2 \cdot \pi)$	
Use the sample-based sine type if numerical problems due to ru for large times (e.g. overflow in absolute time) occur.	
Parameters	
Sine type:	Time based
Time (t):	Use simulation time
Amplitude:	4
Bias:	0
Frequency (rad/sec):	0.025
Phase (rad):	0
Sample time:	0.1



b) Matlab kod

```
P= edd(:, 1);
T = edd(:, 2);
vel = length(P);
minulaz = min(P);
maxulaz = max(P); %opseg ulaznih vrijednosti
minizlaz = min(T);
maxizlaz = max(T); %opseg moguceg izlaza

% normiranje ulaza i izlaza na opseg [-1, 1]
p= 2 * (P - minulaz) ./ (maxulaz - minulaz) - 1;
t = 2 * (T - minizlaz) ./ (maxizlaz - minizlaz) - 1;
N=4;
p=p;
t=t;
for k = N+1 : vel
    t1 = flipud( t(k-N:k-1) );
    p1 = flipud( p(k-N:k-1) );
    ulaz(:,k) = [t1; p1];
    izlaz(k) = t(k)';
end

ulaz
```

```

izlaz

net = newff([-1 1;-1 1;-1 1;-1 1;-1 1;-1 1;-1 1;-1 1],[15 1],{'tansig',
'purelin'}, 'trainlm');

net.trainParam.epochs = 2000;
net.trainParam.goal = 2e-4;
net.trainParam.show = 300;
net.trainParam.time = Inf;
net.performFcn='sse';

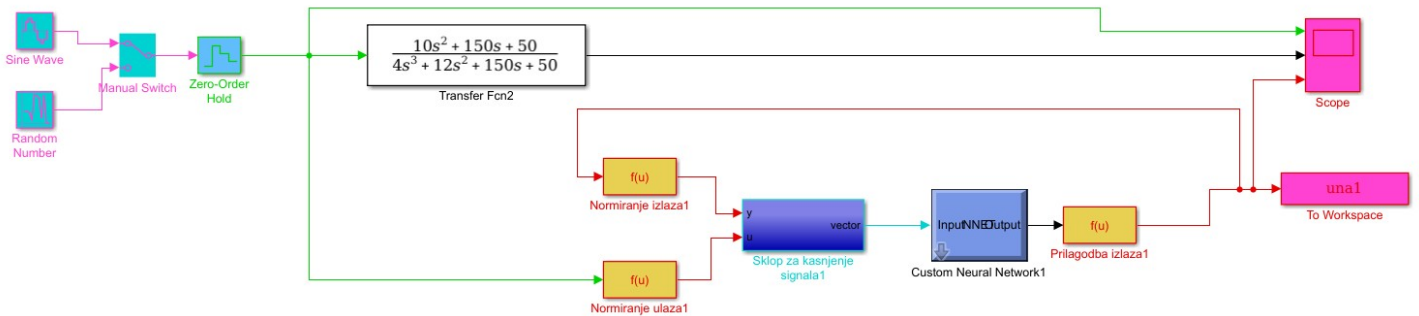
% Treniranje...
fprintf('Po?etak treniranja\n');
tic
net = train(net, ulaz, izlaz);
toc

izlaz=sim(net,ulaz);
izlaz=(izlaz+1)*(maxizlaz-minizlaz)./2 +minizlaz;

figure
subplot(2,1,1),plot(edd(:,1));
title('Izlazni podaci iz sistema');
xlabel('uzorci')
ylabel('amplituda')
subplot(2,1,2),plot(izlaz,'r')
title('Podaci dobiveni sa treniranom mrežom');
xlabel('uzorci')
ylabel('amplituda')
gensim(net,0.1)

```

c) Zadnji model



$$2 \cdot \frac{u(1) - \text{minizlaz}}{\text{maxizlaz} - \text{minizlaz}} - 1$$

$$2 \cdot \frac{u(1) - \text{minulaz}}{\text{maxulaz} - \text{minulaz}} - 1$$

$$(u(1) + 1) \cdot \frac{\text{maxizlaz} - \text{minizlaz}}{2} + \text{minizlaz}$$

