

# Future Virtual Particle Force Model

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## **Abstract**

We present a novel method to simulate virtual pedestrians based on the social force model. In our model, each pedestrian has a point in front of him called Future Virtual Particle (FVP) which represents where the pedestrian is headed to and at what speed.

keywords:

pedestrian, collision avoidance, future virtual particle, force model

# 1 Introduction

## 1.1 Motivation and previous work

Navigation of biological, synthetic or virtual agents is a relevant problem in several fields such as pedestrian dynamics, moving robots and animation of characters for videogames and motion pictures.

Modelling and simulating the displacement of agents through arbitrarily complex environments may be stated in an hierarchical structure of mechanisms depending mainly on the distance from the agent. This level has been named, from closer to further, as operational (walking, lowest level physical-computational model for displacement), tactical (wayfinding, route choice) and strategic (general activity planning) [Hoogonen and Bovy 2004]. These levels are not independent, factors affecting one level may impact in the following and vice versa, for example, the route choice may vary due to congestion of agents producing from previous route choice and walking behavior. Also, obstacles can impact on the operational level or tactical level depending on the particular geometry of the environment. The particular mechanism we want to address is the avoidance of obstacles being fixed or moving (another agent) which involves operational and tactical aspects of the navigation.

A general approach is to take an existing operational model and equip it with a higher level model which allows better and smoother collision avoidance behavior. Existing low level models can be taken from pedestrian dynamics field and in general these models can be classified into rule based and force based, discrete and continuous space description, etc. [Schadschneider 2009].

A famous example of continuous and force based model is the Social Force Model [Helbing 1995, 2000]. In this model the dynamic for virtual pedestrians is derived from the Newton equation's considering the total force exerted over each agent is the result of three forces: Contact, Social and Driving Force. While the driving force points towards the final objective of each pedestrian, the social force is repulsive and acts as a kind of collision avoidance force. However this social force term introduces several artefacts in some configurations [see for example Lakoba et al. 2005, Parisi et al 2009].

Cellular automata models make use of a spatial grid, which can be occupied or empty, along with a set of rules determining the evolution and conflict resolution of virtual pedestrians moving over the cells of the grid. An emblematic cellular automata model is the one proposed by Kirchner and Schadschneider [2002].

It has been also proposed hybrid models such as the Contractile Particle Model [Baglietto and Parisi, 2011] in which a continuous description of the space is combined with a set of simple rules governing the dynamics of the system.

The basic operational model as the ones described above can be improved if higher level mechanisms were added to manage more complex issues as efficient avoidance. Some recent examples can be found in the literature.

Karamouzas et al. (2009) proposed a method for collision avoidance modifying the social force model, basically, replacing the social force term by a new "evasive" force which tends to avoid future collisions. The magnitude and direction of this force is calculated considering the predictions of these possible collisions.

Kretz et al. 2011 have arisen the point that the key ingredient in social force model is the driving force instead of interaction force, so in this work the authors propose a method for dynamically adjust the desired velocity following the gradient of a field given by a time map, in other words, the desired velocity is chosen as the quickest path to the objective taking into account the geometry and other agents (collision, congestions, jams, etc.). Also mounted on the SFM, Moussaïd et al. [2011] have presented a model using a "cognitive heuristics" to determine the norm and direction of the desired velocity for each agent dynamically during the evolution of the system.

In the same line, we also proposed that the navigation capacity of virtual agents should be concentrated in the on-line decision of the desired velocity. Similar to this approach, we postulate a new method derived from the methods used in robotics/artificial intelligence... The method deals with two aspects of the navigation mechanism. The first one is geometrical problem of finding intermediate goals when the final goal is not visible from the current position of the virtual agent. The second aspect is the local avoidance of other agents, which is performed via a reactive mechanism inspired in (robot navigation / artificial intelligence) approaches [Ref.??? ??? ].

The method proposed could be mounted on different basic displacement models like de SFM or the CPM, in the present work we have chosen the first one.

## 1.2 Social Force Model

[Helbing 1995, 2000] presents a Model in which each pedestrian feels a “desire force” towards his objective and a “repulsion force” towards other pedestrians. On a lower level, a collision force is present.

Collision force (Granular):

$$F_{G_i} = \sum_{j=1, j \neq i}^{N_P} [-\epsilon_{ij} k_n e_{ij}^n + v_{ij}^t \epsilon_{ij} k_t e_{ij}^t] g(\epsilon_{ij})$$

Where:  $\epsilon_{ij} = r_{ij} - (R_i + R_j)$

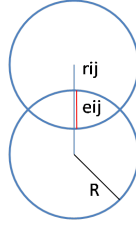


Figure 1: Fuerza de contact granular

Social Force:

$$F_{S_i} = \sum_{j=1, j \neq i}^{N_P} A \exp\left(-\frac{\epsilon_{ij}}{B}\right) e_{ij}^n$$

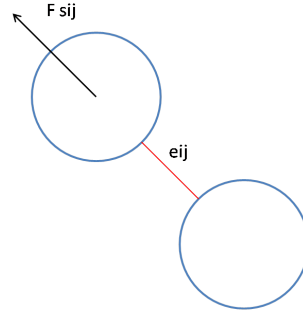


Figure 2: Social Force

Desire Force:

$$F_{D_i} = m_i \frac{v_{di} e_i - v_i}{\tau}$$

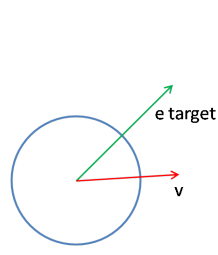


Figure 3: Driving force

Afterwards  $F_i = F_{G_i} + F_{S_i} + F_{D_i}$  is calculated

Fixed parameter values:  $A = 2000 [N]$ ,  $B = 0.08 [m]$ ,  $k_n = 1.2 \cdot 10^5 [\frac{N}{m}]$ ,  $k_t = 2.4 \cdot 10^5 [\frac{kg}{m/s}]$  y  $\tau = 0.5 [s]$ .

While this model doesn't present a very real behaviour for pedestrians, it worked as a starting point for numerous projects.

### 1.3 Future Virtual Particle Model

Given that the SFM adds a fictional force on pedestrians, navigation stops imitating reality when there's a big quantity of pedestrians. Pedestrians also show a collision avoidance method that resembles magnetism, with movements that are clearly governed by the squared distance to the other pedestrian. Also, SFM didn't have the same values as well known metrics for real-case scenarios such as the flow of pedestrians going out a door and the fundamental diagram.

Because of this, we present a new model.

## 2 The Model

### 2.1 Hipotesis

The main effects that govern the motion of a pedestrian are the same as Helbin's:

1. The pedestrian wants to reach his goal in the shortest possible path.
2. The pedestrian's movement is influenced by other pedestrians. Depending on the distance between the two of them and the predicted trayectory, the pedestrian will feel the need to change his route to be able to avoid the other pedestrians. It is because of this effect that pedestrians will need to recalculate their route as new pedestrians get closer to them.
3. Movement speed will be influenced by needs.

### 2.2 Definition

A pedestrian is defined as follows:

- Circular shape  
Represents the space that this pedestrian occupies. Circle's radio is generated randomly to represent different types of pedestrians. The range of values is distributed uniformly in  $[0.25, 0.29][cm]$ .
- Long term objective  
Represented by a static area. When it is touched by a pedestrian, it is considered as accomplished. Multiple objectives can by defined in a list, in this case, each of them must be reached in order.

- Short term objective

Called FVP, it represents a point at a relative distance from the pedestrian's center. It's a dynamic objective.

It is defined as a1 [kg] mass. Not collisionable.

- Desired speed

Represents the speed the pedestrian would walk if he was alone. Varies randomly between [1.2, 1.4] [m/s].

- Reaction distance

Maximum distance between a pedestrian and his FVP, it represents the distance at which a real pedestrian would react from an obstacle.

Fig 1: Pedestrian and his FVP.

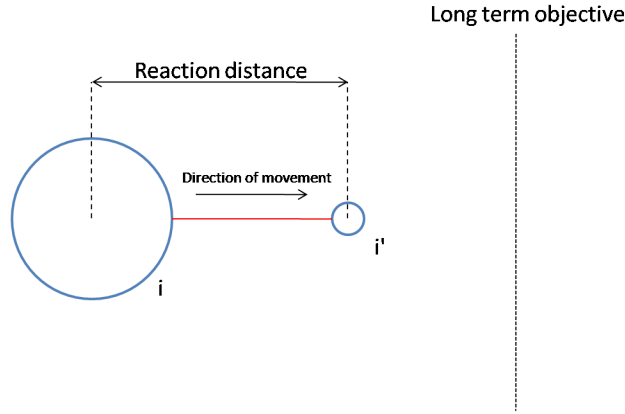


Figure 4: Pedestrian top view

In the document, we will call pedestrians with a letter and FVP of pedestrian  $x$  will be called  $x'$ .

## 2.3 Algorithm

Each pedestrian has to reach the long term objective at some point, to ensure this, the FVP always feels the need to be aligned with the shortest path to the long term objective. On the other hand, there are sometimes obstacles in the way, which will make this impossible, in this cases, the route will have to change depending on the situation.

The pedestrian movement is calculated in four steps:

1. Calculate forces for each FVP.
2. Update positions for each FVP.
3. Calculate forces for each pedestrian.
4. Update positions for each pedestrian.

Each step is defined as follows:

1. FVP force calculation.

In each iteration, the FVP from pedestrian  $i$  feels a force generated by the other pedestrians and FVPs. First of all, we filter the pedestrians  $j$  who are not in the range of sight of pedestrian  $i$  as follows:

$$k = i + \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \vec{ii'}$$

The following must be valid:

$$(k_x - i_x) * (j_y - i_y) - (k_y - i_y) * (j_x - i_x) > 0$$

Once filtered, the force is calculated for every other FVP. The repulsion force between  $i'$  and  $j'$  is defined as follows:

$$F_{ext}(i) = \sum_j F_{i',j'} = \sum_j \alpha e^{-dist(i',j')/\beta}$$

where  $\alpha$  and  $\beta$  are predefined constants. Afterwards, we calculate the repulsion force between  $i'$  and  $j$  using the same formula but different  $\alpha$  and  $\beta$ . Afterwards, we calculate the force between pedestrian  $i$  and his FVP  $i'$ , this is a force that pushes  $i'$  to be in its desired relative distance from the pedestrian. This force is represented with a spring of length “reaction distance” and constant  $K$ . When we sum all these, we get the final  $F_{ext}$ .

Fig 2: FVP force calculation.

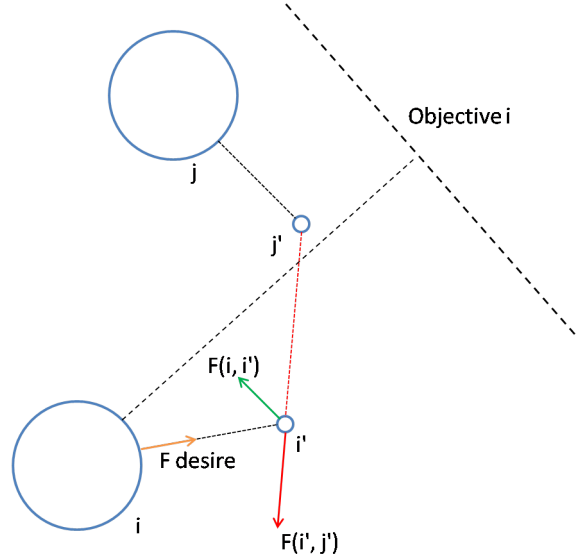


Figure 5: Fuerzas que actúan sobre el Future  $i'$

(a) FVP position update.

In this stage, the position of the FVP is updated with Euler's formula and the forces calculated in the previous step.

To avoid high simetry situations, a low noise  $P = 10\%$  is added to  $F$ . There are two ways to apply this noise:

- Radial noise:
  - A value  $p$  is taken randomly from a uniform distribution  $[-P, P]$  and calculate:  
 $FL_{i'} = F_{i'} * p$
  - Angular noise:
    - \* A value  $sgn = \{-1, 1\}$  is taken randomly from a uniform distribution and a value  $p$  from  $[-P, P]$ . Then  $FA_{i'} = rotation(F_{i'}, \pi * sgn) * p$  is calculated.

At last, we find  $F'_{i'} = F_{i'} + FL_{i'} + FA_{i'}$  and apply euler's movement equations.

- (a) Pedestrian forces calculation.

The pedestrian always wants to move in the direction his FVP is pointing and its magnitude is defined as  $F_d$  or desire force:

$$F_{desire_i} = m_i \frac{\frac{dist(i', i)}{dist_{react}} e_i - v_i}{\tau}$$

Where  $\tau = 0.5$

- (a) Pedestrian position update.

The new position of the pedestrian will be calculated using Euler's formula and the desire force calculated in the previous step.

## 3 Calibration

### 3.1 Metrics

The results were compared to the SFM using the values proposed by Dirk Helbing [2]. The test scenarios were crossing and hallway for they present the main two types of symmetry (90 degrees and 180 degrees).

The metrics used were:

1. Number of collisions

When a pedestrian's body is touching another one, a counter is incremented, it won't be incremented again unless it separates and touch again. This counter represents the amount of collisions.

2. Total duration of collisions:

When a pedestrian's body is touching another one, a counter is incremented by the time step of the simulation. This counter will represent the total time pedestrians were colliding.

3. Average walking speed:

//TODO

4. Average travel time:

When a pedestrian appears in the map, this time is recorded, once he reaches his goal, the travel time is calculated with this value. The average of all this times represents the average travel time.

5. Average travel distance:

Each step, the distance a pedestrian has traveled from the source is saved. When this pedestrian reaches his goal, that distance is considered as finished and it is saved elsewhere. Afterwards, an average of all finished distances is calculated.

6. Average turn angle:

Each step, the angle of the previous velocity of a pedestrian and the current one is saved and added to a total. When this pedestrian reaches his goal, this total is considered as finished and it is saved elsewhere. Afterwards, an average of all finished turn angles is calculated.

### 3.2 Values

To calibrate the model, runs varying parameters were made. A wide spectrum of values was covered, testing every combination of every possible one. After seeing clear preferences towards certain values, the values were refined within that scope. After numerous iterations of this process, the values that best suit these metrics are  $\alpha = 800$  y  $\beta = [0.65, 0.85]$  uniformly distributed.

//TODO todos los demás parámetros

## 4 Results

Values	1	2	3	4	5	6
$\alpha = 800, \beta = [0.65, 0.85]$	(1.800, 0.748)	(34.600, 8.333)	(1.024, 0.016)	(1.910, 0.022)	(2.392, 0.005)	(111.062, 19.122)
$\alpha = 2000, \beta = 0.08$	(5.333, 2.625)	(12.333, 8.340)	(1.052, 0.003)	(1.876, 0.003)	(2.391, 0.002)	(106.185, 13.778)

Table 1: Metrics comparing SFM vs FVPM. Average of 10 runs.

// Poner Graficos indicando distancias y esquemas del future y la particula.

## 5 Conclusions

// agregar al final futuras opciones que se abren con este trabajo



## 6 References

- [1] ... Karamouzas ...
- [2] ... Helbing ...