Aggregate Outcomes of Nonlinear Prices in Supply Chains*

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October 22, 2025

^{*}The views expressed are those of the authors and do not necessarily represent the views of the Central Bank of Chile or its board members.

Introduction

Motivation and Research Question

- Understanding the aggregate costs of market power is central in research and policy debates
- But market power aggregate analysis often omit price discrimination

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"Price discrimination is one of the most prevalent forms of marketing practices"

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- o Policy revival: first Robinson-Patman lawsuits in 20+ years; FTC v. Southern Glazer's (2024):
 - "Southern engages in discriminatory pricing ... offering quantity discounts and rebates to large buyers that are inaccessible to smaller rivals and not justified by cost."

 —FTC Press Release, Dec. 2024
 - "When local businesses get squeezed ... Americans face fewer choices, higher prices, and communities suffer."
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Research Question

Introduction

What are the aggregate outcomes of price discrimination in supply chains?

Introduction

Market Power and Aggregate Efficiency

- Market power aggregate costs measurement relies on observed prices interpretation
- Standard interpretation is uniform pricing: a single quantity-invariant price to all buyers (average prices = marginal prices)
- o In supply chains in Chile, we find indicative evidence of widespread **nonlinear prices** (average prices ≠ marginal prices)
- Nonlinear pricing interpretation: average prices are not fully allocative, marginal prices are
- o Relevant in supply chains: marginal (allocative) distortions in prices can accumulate

This Paper: Main Mechanism

o Under standard assumptions, the optimal nonlinear price is equivalent to a two-part tariff:

$$\frac{pq}{\text{Total Payment}} = \underbrace{F}_{\text{Flat fee}} + \underbrace{p_{\text{marg}}}_{\text{Marginal price}} C$$

Flat Fee Distorts Entry

Introduction

- The flat fee does not affect input choices; it reallocates rents from buyer to seller
- Affects firm profits distribution and distorts entry decisions (ambiguous sign in supply chains)

Marginal Price Improves Allocation Relative to Uniform Prices

- The marginal price determines quantity allocations (it is allocative)
- o In our setting, it's unambiguously lower relative to the allocative price under uniform pricing

This Paper: What we do

Theory

- o Optimal nonlinear price characterization in partial equilibrium and testable prediction
- Multi-sector supply chain model where firms charge and pay nonlinear prices

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Indicative Evidence and Measurement (Population-level B2B transactions for Chile)

- o Pricing Diagnosis: Nonlinear prices by buyer industry (combination of $2^{nd} + 3^{rd}$ degree PD)
- o Calibration: Estimate all model parameters under uniform and nonlinear pricing lenses

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Quantification (NLP=nonlinear pricing)

- Lens: NLP lens yields lower distance to efficiency rel. to uniform price lens, 75% v. 57%
- o Policy (NLP lens): A price discrimination ban reduces welfare from 75% to 49% rel. to efficiency

Selected Related Literature

Distorted Economies, Misallocation and Firm Entry

Quesnay (1758), Harberger (1956), Mankiw & Whinston (1986), Hopenhayn (1992), Hsieh & Klenow (2009), Jones (2011), Baqaee & Farhi (2019, 2020), Edmond, Midrigan & Xu (2023), Bornstein & Peter (2025), Burstein, Cravino, & Rojas (2025)

Price Discrimination and Screening

Dupuit (1849), Mirrlees (1971), Spence (1977), Mussa & Rosen (1978), Maskin & Riley (1984),
 Borenstein (1985), Tirole (1988), Varian (1989), Wilson (1993), Laffont & Tirole (1993),
 Armstrong (1996), Stole (2007)

Our contribution:

Introduction

- Using standard IO tools and particular functional forms:
- ullet We embed ${f 2}^{nd}+{f 3}^{rd}$ degree price discrimination into a GE model in supply chains

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Primitives and Behavior (Standard)

- One seller with constant marginal cost c faces a continuum of buyers indexed by z
- Seller has full bargaining power and makes a take-it-or-leave-it offer
- Seller knows the distribution of buyer types, but type information is private
- o Chooses a nonlinear transfer T(z) and quantity q(z) for each type z

$$\max_{\{T(z),q(z)\}} \Pi_{\text{seller}} = \int_{\underline{z}}^{\infty} \left[T(z) - c \, q(z) \right] f(z) \, dz$$

Subject to

- o (IR) Buyers receive non-negative surplus: $\Pi(z, q(z)) = zq(z) T(z) \ge 0$, $\forall z$
- o (IC) Buyers choose their tailored contract: $zq(z) T(z) \ge zq(\tilde{z}) T(\tilde{z}), \quad \forall z, \tilde{z}$

Mirrlees Reduction and Virtual Surplus (Standard)

o Using the virtual surplus ϕ , the problem can be written as a pointwise optimization problem

$$\max_{\{q(z)\}} \Pi_{\text{seller}} = \int_{\underline{z}}^{\infty} \left[\phi(\mathbf{z}, \mathbf{q}(\mathbf{z})) - cq(z) \right] f(z) \, dz,$$
with
$$\phi(\mathbf{z}, \mathbf{q}) = \underbrace{R(z, q)}_{1} - \underbrace{\frac{1}{h(z)} \frac{\partial R(z, q)}{\partial z}}_{2}$$

- o Inverse hazard rate, $h(z)^{-1} = (1 F(z))/f(z)$ is the weight on the remaining higher types
- o The virtual surplus represents the seller's effective revenue from serving type z:
 - Buyer z total revenue from the transaction (seller wants to extract it)
 - 2 Rents the seller must leave to higher types to prevent them from mimicking type z

Functional Forms and Optimal Nonlinear Price (New)

- So far, standard screening problem, now we impose two additional new assumptions:
 - f 1 Buyer types are Pareto distributed with tail parameter κ
 - 2 Buyers have isoelastic contingent demands ($\sigma > 1$)
- Buyer type shifts demand without altering curvature

Lemma 1: Optimal Nonlinear Price

Under (i) constant marginal cost, (ii) Pareto distributed types, and (iii) isoelastic contingent demands, the optimal nonlinear price schedule is equivalent to a two-part tariff when $\kappa > \sigma - 1$:

$$T(z) = F + p^{\mathrm{NLP}} \, q(z), \qquad p^{\mathrm{NLP}} = rac{
ho}{
ho - 1} \, c, \qquad
ho \equiv rac{\kappa \, \sigma}{\sigma - 1} > \sigma, \qquad extit{F is set so that} \colon \, \Pi(\underline{z}) = 0.$$

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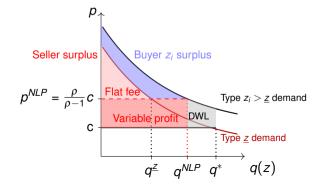
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$$T(z) = F + p^{\text{NLP}} q(z), \qquad p^{\text{NLP}} = \frac{\rho}{\rho - 1} c, \qquad \rho \equiv \frac{\kappa \sigma}{\sigma - 1} > \sigma, \qquad \textit{F is set so that} : \ \Pi(\underline{z}) = 0.$$

- Contract structure holds in supply chains with arbitrary links where firms charge and pay NLP
- o Can extend to Nash bargaining setup, where F depends on barg. weights, but $p^{\rm NLP}$ does not

Optimal Nonlinear Price: Allocations

- Virtual surplus for lower type is strictly positive: All types are served
- o Quantities are pinned down by marginal price p^{NLP}
- Flat fee only redistributes surplus; is not allocative



Optimal Nonlinear Price: Testable Prediction

- o If pricing in the data is equivalent to a two-part tariff: $T(z) = F + p^{\text{NLP}} q(z)$
- o Average unit price is: $\frac{T(z)}{q(z)} = \frac{F}{q(z)} + \rho^{\text{NLP}}$
- \circ Decreasing and convex in q
- o Has a horizontal asymptote at $p^{
 m NLP}$

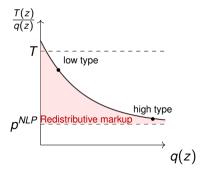


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Data Sources Invoice example

Invoice transactions for the universe of Chilean formal firms for 2024

- 1.4 billion transactions
- More than 10 million different products. We assume products are seller-specific
- Data on prices and quantities for every product transacted

Merged with firms' accounting balance sheet data

- Sales, materials, investment, 6-digit industry
- Employer-employee: Wages, headcount of employees
- Capital stock and investment



Indicative Evidence of Nonlinear Prices (assume equilibrium $\{p, q\}$)

Seller j, product g, buyer i, time t, day d, quantity q, buyer group B (11 sectors \times 3 sizes \times 16 regions)

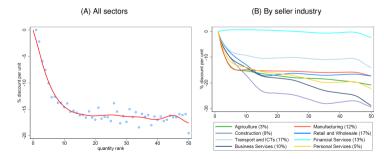
$$\ln p_{jgit} = eta_0 + eta_1 \ln q_{jgit} + \Psi_S + arepsilon_{jgit}$$

- o Unconditional average discount is 2.9% $(\ln 2 * 0.042)$ per unit when doubling quantity purchased
- Conditioning on buyers (and groups of buyers), the average discount increases
- Even within buyer groups, the average discount is 90% of the unconditional average

	(1)	(2)	(3)	(4)
In q _{jgit}	-0.042	-0.084	-0.065	-0.037
	(0.0001)	(0.0001)	(0.0001)	(0.0001)
$S_{Base} = j \times g \times d$	✓			
S = Base + i		✓		
S = Base + B			✓	
$S = Base \times B$				✓
N	430M	430M	430M	430M
R ²	0.9646	0.9678	0.9659	0.9790

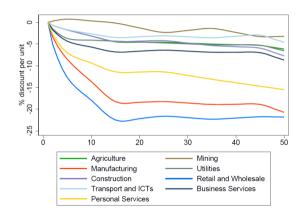
Nonlinear Prices by Quantity Bins and Seller Industry Bins construction

$$\ln
ho_{jgit} = eta_0 + \sum_{b=2}^{50} eta_b \mathbb{1}_{\{B_{jgit}=b\}} + \Psi_{jgd} + arepsilon_{jgit}$$



- Unit prices fall steeply at small q and flatten as q grows (consistent with Lemma 1)
- Large between seller sector heterogeneity in both steepness and curvature

Retail & Wholesale Seller Sector: Pricing to Different Buyer Sectors



- Within a seller sector, nonlinear price schedules differ by buyer sector
- Buyer industry shifts price schedule without altering (too much) curvature

Taking Stock

- o Within seller×product×day, unit prices decline with quantity and flatten at higher ranks
- o Curvature, levels, and steepness are different across seller industries
- Within a seller industry, curvature shifts with buyer sector
- Inconsistent with uniform pricing
- o Pricing consistent with a combination of $2^{nd} + 3^{rd}$ degree price discrimination:
 - 2nd degree screening drives curvature
 - 3rd degree shifts levels and steepness across buyer industries

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Environment

- o Two observable firm types, $\ell \in \{u, r\}$, defined by their position relative to final demand \bullet Evidence
- o Upstream firms u sell both to other u and to retailers firms r, and buy from other u
- o r purchase inputs from u and sell exclusively to the representative final consumer
- o Within each type $\ell \in \{u,r\}$ observable sectors are indexed by $s \in S$
- o Firms as buyers are denote by i and by j as sellers, buyer sectors as s and seller sectors as s'
- o Each (ℓ,s) has a continuum of firms with unobserved productivity z_i distributed Pareto, tail κ_s^ℓ
- o A firm i is thus characterized by the triple (ℓ, s, z_i) , denoting type, sector, and productivity

Market Structure: Second and Third Degree Price Discrimination

- Retail firms sell to the representative consumer at uniform per-unit prices
- Upstream firms set nonlinear prices to other upstream firms and retailers
- o Firms can price discriminate across types and sectors (ℓ, s) but no z_i within a (ℓ, s) $(2^{nd} + 3^{rd})$
- o Firms are atomistic in input markets as buyers and take the wage as given

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Main Challenge: Endogenously sufficient conditions to make $2^{nd} + 3^{rd}$ tractable in supply chains:

- Constant marginal costs
- Isoelastic demands

Preferences

- o The representative consumer owns all firms and inelastically supplies one unit of labor (L=1)
- Final demand is Cobb—Douglas across retail sectors with within—sector CES over reatil varieties:

$$Y = \prod_{s \in S} Y_s^{\theta_s}, \qquad \sum_{s \in S} \theta_s = 1, \qquad Y_s = \left(\int_{j \in R_s} y_j^{\frac{\varphi_s - 1}{\varphi_s}} \, dv_s(j) \right)^{\frac{\varphi_s}{\varphi_s - 1}}$$

- o $\theta_s \in (0,1)$ are Cobb–Douglas output elasticities
- o $\varphi_s > 1$ is the within-sector elasticity, and $dv_s(j)$ denotes number active retail varieties R_s in s
- o The total number of active varieties in (r,s) is $N_s^r := v_s(R_s)$, an endogenous equilibrium object

Technology

o Firm $i \in (\ell, s)$ output (Q_i) use CD in labor (I_i) and a CD aggregator of sectoral materials (M_i)

$$Q_i = z_i I_i^{\alpha_s^\ell} M_i^{1-\alpha_s^\ell}, \qquad 0 < \alpha_s^\ell < 1,$$

$$M_i = \prod_{s' \in S} M_{is'}^{\theta_{ss'}^\ell}, \qquad \sum_{s' \in S} \theta_{ss'}^\ell = 1, \qquad M_{is'} = \left(\int_{j \in U_{s'}} m_{ij}^{\frac{\sigma_{s'} - 1}{\sigma_{s'}}} dv_{s'}(j) \right)^{\frac{\sigma_s}{\sigma_{s'} - 1}}$$

- o $lpha_{\mathbf{s}}^\ell$ is the labor output elasticity, $M_{i\mathbf{s}'}$ is firm i material bundle from upstream sector \mathbf{s}'
- o $heta_{ss'}^{\ell} \geq$ 0 are sector–s firm type ℓ input elasticities
- o m_{ij} is firm i's input of upstream variety j in sector s'
- o $\sigma_{s'}>$ 1 is the CES across varieties inside upstream sector s'
- o $N_{s'}:=v_{s'}(U_{s'})$ is the endogenous measure over the active upstream firms in sector s'

Firm Entry

- o In each (ℓ, s) there is an unbounded pool of identical potential entrants
- o Entryants pay a sunk cost $c_s^{E\ell} > 0$ in units of labor, and then observe their productivity z
- o Active firms exit exogenously at the end of the period with probability $\delta_s^\ell \in [0,1)$
- o Free entry requires that the expected discounted value of profits $(\pi_i^{\ell s}(z))$ equals entry cost $(c_s^{E\,\ell})$

$$\frac{1}{1-\delta_s^{\ell}}\mathbb{E}_{z}\Big[\pi_i^{\ell s}(z)\Big] = c_s^{E\ell} w, \quad \forall (\ell,s)$$

Model Recap

- 1 In every period potential entrants in each (ℓ, s) pay $c_s^{E\ell}$ and then draw productivity z
- 2 Each upstream seller j observes only the buyer's pair (ℓ, s) (not z_i) and offers a pair–specific nonlinear contract menu $\{m_i^{\ell,s}, T_i^{\ell,s}\}$
- Retail sellers j post uniform prices to final consumers
- 4 Buyers $i = (\ell, s, z_i)$ observe menus and w and choose l_i and $\{m_{ij}\}_j$ to max. profits
- **6** Production and trade occur, transfers $\{T_{ij}\}_j$ are realized, and final demand $\{y_j\}$ is met
- $_{f 6}$ Firms exit with probability δ_s^ℓ
- Contracts are enforceable, resale/arbitrage is ruled out
- We consider a steady state: all aggregates are time-invariant

Guess and Verify

Guess 1: Optimal contracts are isomorphic to a two-part tariff specific to (ℓ,s)

$$T_{ij} = p_{js}^{\ell} m_{ij} + F_{js'}^{\ell} = \mu_{ss'}^{\ell} c_j m_{ij} + F_{js'}^{\ell}$$

- o Transfer T_{ij} depends on allocation m_{ij} , markup $\mu_{ss'}^\ell$, and flat fee $F_{js'}^\ell$
- o The marginal (allocative) price is $p_{js}^\ell = \mu_{ss'}^\ell c_j$
- Flat fees are inframarginal and do not affect marginal input choices;

Guess 2: Revenue functions are homogeneous in quantity

$$\mathit{R}_{i,s}^{\ell} \, = \, \mathit{A}_{s}^{\ell} \left(\mathit{Q}_{i,s}^{\ell}
ight)^{\psi_{s}^{\ell}}$$

- o For parameters A_s^ℓ and ψ_s^ℓ that are constants at buyer type and sector (ℓ,s)
- Imply isoelastic contingent demands for intermediate inputs

Costs and Price Indices Under Guess 1

o Marginal prices are quantity–invariant within a buyer type–sector (i, s) and seller sector s'

CES Sectoral Price Index

$$P_{ss'}^\ell = \left(\int_{j\in U_{s'}} \left(p_{js'}^\ell
ight)^{1-\sigma_{s'}} d
u_{ss'}(j)
ight)^{rac{1}{1-\sigma_{s'}}}$$

Cobb-Douglas Materials Cost Index

$$P_i^M = \prod_{s' \in S} \left(P_{ss'}^\ell \right)^{\theta_{ss'}^\ell}, \qquad \sum_{s' \in S} \theta_{ss'}^\ell = 1, \ \ \theta_{ss'}^\ell \geq 0$$

Firm-Level Marginal Cost

$$c_i = rac{\Theta_s^\ell}{z_i} \ w^{lpha_s^\ell} \ \left(P_i^M
ight)^{1-lpha_s^\ell}, \qquad \Theta_s^\ell \ \equiv \ \left(lpha_s^\ell
ight)^{-lpha_s^\ell} \left(1-lpha_s^\ell
ight)^{-(1-lpha_s^\ell)} \prod_{s' \in S} \left(heta_{ss'}^\ell
ight)^{-(1-lpha_s^\ell) heta_{ss'}^\ell}$$

Type Re-parametrization and Distribution for Screening

- o For a seller $j \in s'$, each buyer $i \in s$ matters only through the valuation index: $au_{is'}^\ell \equiv P_{ss'}^\ell M_{is'}^{1/\sigma_{s'}}$
- o For a seller $j,\ au_{is'}^\ell$ is a sufficient statistic for buyer's heterogeneity
- o $P_{ss'}^{\ell}$ price level faced by *i* for inputs from s', and $M_{is'}$ is the buyer's demand shifter (scale)
- o Under Pareto distributed buyer productivity, $au_{is'}^\ell$ is Pareto with tail parameter:

$$ho_{ss'}^\ell = \sigma_{s'} \, \xi_s^\ell \, > \, 1$$

o Type-specific heterogeneity maps to ξ_s^ℓ :

$$\xi_s^r = rac{\kappa_s^r}{\varphi - 1}$$
 (retail), $\xi_s^u = rac{\kappa_s^u}{\sigma_s - 1}$ (upstream)

Upstream Seller Profit Maximization Problem

o A seller $j \in s'$ chooses a menu of total transfer and a allocation $\{T_{ij}^\ell, m_{ij}^\ell\}$ for each (ℓ, s)

$$\max_{\{T,m\}} \ \sum_{\ell \in \{u,r\}} \sum_{s \in S} N_s^\ell \, \mathbb{E}_{\tau_{is'}} \big[\, T(\tau) - c_j m_{ij}(\tau) \big], \quad \text{s.t. for each } (\ell,b) \text{: IC, IR}$$

- o The problem is additively separable across (ℓ,s) and can be solved partition-by-partition.
- Following Lemma 1, the virtual—surplus reduction yields the pointwise optimization problem:

$$\max_{\{m(\tau)\}} N_s^{\ell} \mathbb{E}_{\tau_{is'}} \left[\left(\tau - \frac{\tau}{\rho_{ss'}^{\ell}} \right) \frac{\sigma_{s'}}{\sigma_{s'} - 1} m(\tau)^{\frac{\sigma_{s'} - 1}{\sigma_{s'}}} - c_j m(\tau) \right].$$

o which is strictly concave in m since $(\sigma_{s'}-1)/\sigma_{s'}\in(0,1)$

Optimal Nonlinear Price

Proposition 1: Optimal Nonlinear Price in Supply Chains

There is an equilibrium where the optimal contract offered by an upstream seller $i \in U_{S'}$ to any buyer $i = (\ell, s, z_i)$ is a two-part tariff:

$$T_{ij} = p_{js}^{\ell} m_{ij} + F_{js}^{\ell},$$

with a marginal price p that is constant across types and equals:

$$\rho_{js}^{\ell} = \mu_{ss'}^{\ell} \, c_j, \qquad \mu_{ss'}^{\ell} = \frac{\rho_{ss'}^{\ell}}{\rho_{ss'}^{\ell} - 1}, \qquad \rho_{ss'}^{\ell} = \xi_s^{\ell} \, \sigma_{s'}, \qquad \xi_s^{r} \equiv \frac{\kappa_s^{r}}{\varphi - 1}, \ \ \text{for retailers} \quad \xi_s^{u} \equiv \frac{\kappa_s^{r}}{\sigma_s - 1}, \ \ \text{for upstream}$$

and a flat fee F chosen so that the lowest type's participation constraint binds,

$$\Pi(\underline{z}_{s}^{\ell}) = 0 \iff F_{js}^{\ell} = \frac{1}{\sigma_{s'}} R_{ss'}^{\ell}(\underline{z}_{i}^{\ell}, m^{*}(\underline{z}_{i}^{\ell})).$$

For all partitions on firm types $\ell \in \{u, r\}$ and buyer sectors s, each with its sector-specific two-part tariffs.





Two Upstream Pricing Counterfactuals For Welfare Comparisons

Planer Efficient Pricing (as in Baqaee and Farhi, 2021)

- Firms must charge markups to incentivize the optimal entry level
- But markup distorts input choices by acting as a uniform tax on production
- An output subsidy can restore undistorted marginal-cost, conditional on entry
- The subsidy is paid via a lump sum tax to the representative consumer

Uniform prices (e.g, as in Edmond, Midrigan & Xu, 2023)

- Constant markup over marginal cost from monopolistic competition
- o CES markups $\mu^{LP}=rac{\sigma}{\sigma-1},$ strictly higher than $\mu^{NLP}=rac{\rho}{\rho-1}$
- o Because unambiguously $\sigma <
 ho$

Welfare Decomposition: Intensive vs. Extensive Margins Profit Functions

o If wage is the numeraire, welfare is the inverse final price index: $W \equiv \frac{1}{P_V}$ derivation

$$\Delta \log W = \underbrace{-\sum_{s \in S} \tilde{\lambda}_{s}^{c} \Delta \log \mu_{s}^{rc} - \sum_{s \in S} \tilde{\lambda}_{s}^{ru} \Delta \log \mu_{s}^{ur} - \sum_{s \in S} \tilde{\lambda}_{s}^{uu} \Delta \log \mu_{s}^{uu}}_{\text{Intensive Margin } (r \rightarrow c), \ (u \rightarrow r), \ (u \rightarrow u)} + \underbrace{\sum_{s \in S} \frac{\tilde{\lambda}_{s}^{ru}}{\varphi_{s} - 1} \Delta \log N_{s}^{r} + \sum_{s \in S} \frac{\tilde{\lambda}_{s}^{uu}}{\sigma_{s} - 1} \Delta \log N_{s}^{u}}_{\text{Extensive Margin: } variety(masses)}$$

- o $\,\hat{\lambda}\,$ are final consumption direct and indirect costs exposures (direct imes network exposure)
- o Markups drive the intensive margin (extent of double marginalization)
- Flat fees drive the extensive margin (firm masses, N, love of variety)

Welfare Ratios Across Price Regimes: Nonlinear vs. Uniform

$$\frac{W^{\text{NLP}}}{W^{\text{Uni}}} = \underbrace{\prod_{s \in S} \left(\frac{\mu_s^{ur, \text{NLP}}}{\mu_s^{ur, \text{Uni}}}\right)^{-\tilde{\lambda}_s^{ru}} \prod_{s \in S} \left(\frac{\mu_s^{uu, \text{NLP}}}{\mu_s^{uu, \text{Uni}}}\right)^{-\tilde{\lambda}_s^{uu}}}_{s \in S} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{r, \text{NLP}}}{N_s^{r, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}} \prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Intensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{r, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}} \prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}} \prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}} \prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}} \prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{Uni}}}{N_s^{u, \text{Uni}}}\right)^{\frac{\lambda_s^{uu}}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{Uni}}}{N_s^{u, \text{Uni}}}\right)^{\frac{uu}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{Uni}}}{N_s^{u, \text{Uni}}}\right)^{\frac{uu}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{Uni}}}{N_s^{u, \text{Uni}}}\right)^{\frac{uu}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{Uni}}}{N_s^{u, \text{Uni}}}\right)^{\frac{uu}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{Uni}}}{N_s^{u, \text{Uni}}}\right)^{\frac{uu}{q_s - 1}}}_{\text{Extensive Margin}} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{u, \text{Uni}}}{N$$

- o Intensive margin (unambiguous gain): $\mu^{\rm NLP} < \mu_u^{\rm Uni}, \mbox{ attenuating double marginalization}$
- Extensive margin (ambiguous):
 Flat fees shift profits with ambiguous sign, firm entry could go either way
- Welfare comparison? Need to quantify the model fully

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- 1. Nonlinear Price Characterization
- 2. Descriptive Evidence
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Three Quantitative Exercises

- Calibration using population-level B2B transactions and firm balance sheets accounts for Chile
- Two calibrations depending on observed prices interpretation (Nonlinear and Uniform)

o 1. Model fit

How much of observed nonlinear prices the model can explain

o 2. Policy

Welfare outcomes of banning any form of price discrimination

o 3. Measurement

Welfare cost under two interpretations of the same data: nonlinear vs. uniform pricing

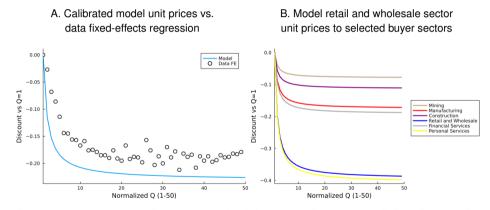
Parameter Estimation

Parameter	Strategy	Granularity
Labor output elasticity $(lpha_s^\ell)$	Measured from data	626 sectors \times firm type
Final demand elasticity (θ_r)	Measured from data	626 sectors
Input-Output elasticity $(heta_{ss'}^\ell)$	Measured from data	626 sectors \times firm type
Final demand bundle elasticity (φ_s)	Pin down by CES results and data	11 sectors
Material bundle elasticity ($\sigma_{s'}$)	Covid shock for Chile estimation	11 sectors
Exit rate($oldsymbol{\delta}^\ell$)	Measured from data	626 sectors \times firm type
Entry cost (c_e^ℓ)	Pin down by free entry and data	626 sectors \times firm type
Productivity Pareto tail (κ^ℓ)	MLE estimation	11 sectors \times firm type

- o $\sigma_{s'}$, κ^{ℓ} jointly pin the marginal price: Lower $\sigma_{s'}$, κ^{ℓ} (fatter tail, more dispersion) implies higher marginal marked-up prices
- o Buyer surplus can be extracted by flat fees (F), will be mainly determined by κ^{ℓ} : Large κ^{ℓ} implies low marginal price and thus a higher F



Model Fit (untargeted): Nonlinear Prices Interpretation



o For the average upstream firm price schedule to retailers, normalizing the continuous input quantity to be in the bounds of 1 to 50

Policy: Ban on Price Discrimination Welfare Outcome

$$\frac{\mathbf{W}^{\text{Reg}}}{\mathbf{W}^{\text{Eff}}} = \underbrace{\prod_{s \in S} \left(\frac{\mu_s^{ur, \text{Reg}}}{\mu_s^{ur, \text{Eff}}}\right)^{-\tilde{\lambda}_s^{ru}} \prod_{s \in S} \left(\frac{\mu_s^{uu, \text{Reg}}}{\mu_s^{uu, \text{Eff}}}\right)^{-\tilde{\lambda}_s^{uu}}}_{s \in S} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{r, \text{Reg}}}{N_s^{r, \text{Eff}}}\right)^{\frac{\theta_s}{\varphi_s - 1}} \prod_{s \in S} \left(\frac{N_s^{u, \text{Reg}}}{N_s^{u, \text{Eff}}}\right)^{\frac{\tilde{\lambda}_s^{uu}}{\varphi_s - 1}}}_{s \in S}\right)}$$

Price Regime	W^R/W^{Eff}	W^{Reg}/W^{Lin}
Nonlinear (NLP) Uniform Pricing (Uni)	0.745 0.486	1.534

- o Banning price discrimination reduces welfare from $\approx 75\%$ of efficient welfare to $\approx 50\%$
- o Allowing for price discrimination closes about half of the efficiency gap:

$$\frac{W^{\text{NLP}} - W^{\text{Uni}}}{W^{\text{Eff}} - W^{\text{Uni}}} = \frac{0.745 - 0.486}{1 - 0.486} \approx 0.50.$$

Policy: Aggregate Welfare Decomposition (v. efficient)

$$\frac{\mathbf{W}^{\mathrm{Reg}}}{\mathbf{W}^{\mathrm{Eff}}} = \underbrace{\prod_{s \in S} \left(\frac{\mu_s^{ur,\mathrm{Reg}}}{\mu_s^{ur,\mathrm{Eff}}}\right)^{-\tilde{\lambda}_s^{nu}}}_{s \in S} \underbrace{\prod_{s \in S} \left(\frac{\mu_s^{uu,\mathrm{Reg}}}{\mu_s^{uu,\mathrm{Eff}}}\right)^{-\tilde{\lambda}_s^{uu}}}_{s \in S} \times \underbrace{\prod_{s \in S} \left(\frac{N_s^{r,\mathrm{Reg}}}{N_s^{r,\mathrm{Eff}}}\right)^{\frac{\theta_s}{\phi_s - 1}}}_{s \in S} \underbrace{\left(\frac{N_s^{u,\mathrm{Reg}}}{N_s^{u,\mathrm{Eff}}}\right)^{\frac{\tilde{\lambda}_s^{uu}}{\phi_s - 1}}}_{s \in S} \underbrace{\left(\frac{N_s^{u,\mathrm{Eff}}}{N_s^{u,\mathrm{Eff}}}\right)^{\frac{\tilde{\lambda}_s^{uu}}{\phi_s - 1}}}_{s \in S} \underbrace{\left(\frac{N_s^{u,\mathrm{Eff}}}{N_s^{u,\mathrm{Eff}}}\right)^{\frac{\tilde{\lambda}_s^{uu}$$

Intensive Margin Extensive Margin

Regime	Intensive	Extensive	Share _{int}	Share _{ext}	Nu	N ^r
Nonlinear (NLP)	0.67	1.12	0.79	0.21	1.18	1.17
Uniform (Uni)	0.46	1.06	0.93	0.07	1.03	1.44

- o Result
 - Relative to efficiency, markups create higher expected profits, and thus more entry: More firms at a smaller scale
- Intensive Margin Dominates (as a share of total log deviation relative to Eff.)
 NLP: 79%, Uni: 93%. banning price discrimination raises double marginalization along the supply chain
- Extensive Margin: Entry Responses
 Extensive is pro-competitive (factors > 1) but modest

Introduction

Policy: Opening Welfare Ratios by Sector

$$\frac{W^{\text{NLP}}}{W^{\text{Uni}}} = \prod_{s \in S} \left(\frac{\mu_s^{ur, \text{NLP}}}{\mu_s^{ur, \text{Uni}}} \right)^{-\tilde{\lambda}_s^{ru}} \prod_{s \in S} \left(\frac{\mu_s^{uu, \text{NLP}}}{\mu_s^{uu, \text{Uni}}} \right)^{-\tilde{\lambda}_s^{uu}} \times \prod_{s \in S} \left(\frac{N_s^{r, \text{NLP}}}{N_s^{r, \text{Uni}}} \right)^{\frac{\theta_s}{\phi_s - 1}} \prod_{s \in S} \left(\frac{N_s^{u, \text{NLP}}}{N_s^{u, \text{Uni}}} \right)^{\frac{\tilde{\lambda}_s^{uu}}{\sigma_s - 1}}$$

Intensive Margin

Extensive Margin

Sector	Intensive	(allocative)	Extensiv	Extensive (variety)		
	Retailers	Upstream	Retailers	Upstream	Net NLP/Uni	
Agriculture	1.010	1.010	0.997	1.005	1.022	
Mining	1.003	1.003	0.999	1.014	1.019	
Manufacturing	1.024	1.029	0.991	1.002	1.047	
Utilities	1.016	1.006	0.996	1.033	1.051	
Construction	1.061	1.022	0.980	1.119	1.189	
Retail and Wholesale	1.037	1.070	0.992	1.005	1.106	
Transport and ICTs	1.007	1.023	0.981	1.000	1.011	
Financial Services	1.012	1.008	0.943	0.998	0.960	
Real Estate Services	1.009	1.004	0.996	1.023	1.033	
Business Services	1.005	1.006	0.989	0.999	0.999	
Personal Services	1.001	1.001	0.998	1.000	1.000	
Product over sectors	1.197	1.198	0.870	1.207	1.507	

Measurement: Nonlinear vs. Uniform Pricing Interpretation

Price Lens	${\it W}^{\it L}/{\it W}^{\it Eff}$	Intensive	Extensive
Nonlinear Uniform	0.748 0.565	0.68 (81%) 0.55 (97%)	1.10 (19%) 1.02 (3%)
	0.000	0.00 (07 70)	1.02 (070

- 2 model quantifications, data-interpretation dependent
- Welfare is 0.75 of efficiency under the nonlinear d 0.57 under the uniform price interpretation
- Nonlinear prices interpretation closes the welfare cost gap by about 18%
- Market power aggregate costs are lower if model allows for price discrimination

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Conclusion

Conclusion

- o We find indicative evidence of combined $2^{nd} + 3^{rd}$ degree PD in supply chains
- NLP improves allocations relative to Uniform, but shifts rents via flat fees: distorts entry
- Banning PD drops welfare from 75% vs. 50% rel. to efficiency
- Average prices can mislead. Policy should monitor marginal prices and rent extractions
- o Don't necessarily ban quantity discounts; target markup accumulation along the supply chain
- The method is plug-and-play with standard microdata on transactions:
 - Ex-ante evaluations of Robinson–Patman–style enforcement
 - Ex-post sector-specific contracting rules evaluations

Is it profitable to exclude any buyer type? PREUTO

In nonlinear pricing with private information, the seller always faces a choice:

- 1 Exclude low types to better extract surplus from high types
- Serve all types, but give up some rent from high types
- However, Pareto distribution has heavy mass for low types
- Even though low types buy little q, because of their large density the seller maximizes profits by serving them

No, Positive Virtual Surplus for all types Peturn

Virtual surplus: profit from serving a buyer type, net of the informational rents that must be left to higher types to preserve IC

o Virtual surplus for type z (with $\alpha = \frac{\sigma}{\sigma - 1}$):

$$VS(z) = \underbrace{\left(\frac{z^{\sigma-1}}{\alpha}\right)q(z)^{1-1/\sigma}}_{\text{Gains from serving type } z} - \underbrace{\left(\frac{1-F(z)}{f(z)} \cdot \frac{d}{dz} \left(\frac{z^{\sigma-1}}{\alpha}\right)\right)q(z)^{1-1/\sigma}}_{\text{Informational rents left to ensure IC}}$$

o For the lowest type $z_0 = 1$, the virtual surplus simplifies:

$$VS(1) = \left[\frac{1}{\alpha}\left(1 - \frac{\sigma - 1}{\kappa}\right)\right]q(1)^{1 - 1/\sigma}$$

- o This is strictly positive whenever $\kappa > \sigma 1$ (necessary condition for finite output)
- o If its profitable to serve the lowest type, the seller will not exclude any buyer

Is price deviation profitable for any $z > z_a$? •Return

- o Heuristic argument (Wilson 1993) to derive the optimal price p(q)
- o Define marginal buyer z(q,p) by inverting demand for the q^{th} unit (equation 1)

$$z(q,p)=q^{\frac{1}{\sigma-1}}p^{\frac{\sigma}{\sigma-1}}$$

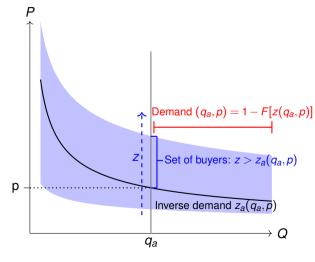
o Demand for qth unit:

$$D(q,p) = 1 - F(z(q,p))$$

Seller chooses a price for unit "q" to solve:

$$\max_{p} \left[1 - F\left(z_{a}(q_{a}, p)\right)\right](p - c)$$

No profitable deviation in price Peturn

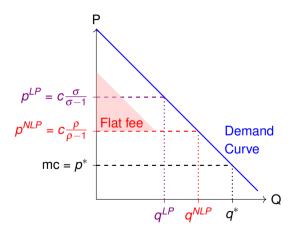


$$\max_{\{P\}} [1 - F(z_a(q_a, p))](P - c)$$

FOC:
$$\frac{P}{c} = \frac{\frac{\kappa\sigma}{\sigma-1}}{\frac{\kappa\sigma}{\sigma-1} - 1} = \frac{\rho}{\rho - 1}$$

- The optimal price is equal to the allocative price of the two-part tariff
- Seller has no incentive to charge different prices for different quantities

Two-Part Tariff: NLP vs LP CES markup $(ho>\sigma)$



 Allocations in NLP are less distorted relative to LP

$$q^* > q^{NLP} > q^{LP}$$

 Because of the flat fee, rents are subject to different distortions in NLP vs. LP

General Equilibrium NLP • Return

A decentralized nonlinear pricing equilibrium is a collection of firm level productivity z_i , linear prices $\{p_u, p_r\}$, flat fees $\{F_u, F_r\}$, wage w, and quantities $\{y_i, q_i, I_i, m_{iu}, N_U, N_R\}$ such that:

- Each producer minimizes its costs and charges a linear price that equals marginal cost times the markup
- Each producer pays a transfer, such that the lowest types have zero surplus from transacting with upstream sellers
- o Entrants earn zero expected profit
- The representative consumer maximizes its consumption
- Markets clear for all goods and factors

Invoice Example • Return



KITCHEN CENTER SPA

Av Elifado 1485 Sacoleta Santiano

An Nurve Costoners 3900, Vitanura

In No. 514, With del Mar. do: Kennedy 9001 Local 1017, Las Condes. do: El Salto 3460, Recolate, Settlero.

IMPORTACIÓN Y DISTRIBUCIÓN DE ELECTRODOMÉSTICOS

FIDE SIMPLE COOK Cuisinart QUBLL (Riversi) agrameg SLPER/COOK - Relete. LOFFRA

Sucursales: Secursales: Cana Contamera: Hall Parque Arauco: Hall Plaza Los Dominicos: Hall Plaza La Serrea: Outlet Dark Wife: Temaco: Hali Fauton Temaco:

Servicio Técnico:

Alto Las Condes:

Concepción:

An Norve Customers 9900, Viscours
An Norve Customers 9900, Viscours
An Korreel's 1443 Local 572, Las Condes - Teléfons (96-2) 24117777 - Pacc (96-2) 24117718
Fadre Invertado Sur EFS, Local ACOSC/2076, Las Condes - Teléfons (+66-2) 24117798
San Igracio 993 Local 12, Quillours - Teléfons (+66-2) 24117793
An Hoan/Mark 106 SA 106, La Exercia - Teléfons (6-5) 24117793 Av. Liberted 1348, Local PD-01/02, VAs del War - Teléfono: (\$6-2) 24117767/68 An. Libertad 1348, Local PD G120, VAN del Naz - Yabilino. (14-2) 24317797/MR Carrion Herractoria? 2400 (cod 72, VRS del Har Circumvilación 1010s, Local 220/227, Yibra - Yabilino. (14-2) 24317748 Pariard 2004, Local Z, Taliferas (16-2) 241, 1716 (17 Antin. Alemania G613, Nervas - Yabilino. (456 2) 241,37744 (1 Antinio) CHILL (16-17), Nervas - Taliferas (16-17), Ner Rudencia Ortego 91790, Local L168-179, Terrisco - Telefona: (+ Lautara #290, Quilliura - Telefona: 6004117709 / 737 / 604 Carrino lo Boza #5887, Putahuel, Sartingo E Ma. 316, Villa del Mo.

R.U.T. 96,999,930-7

BOLETA ELECTRÓNICA

Nº 0015959119 S.I.I. - SANTIAGO NORTE

FECHA EMISIÓN: 01/08/2022

SEÑORES Antonio Martner

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Dirección Origen: Camino lo Roza 8887 Comuna : Pudahuel Cludad: Santiago Dirección Destino: Los Misjoneros 1923

Comuna : Providencia

Ciudad - Santiago

FECHA EMISIÓN FECHA VENCIMIENTO: 03/08/2022 TIPO DESPACHO

FORMA DE PAGO - Contado COD. VENDEDOR

Orden de Venta:

Número de OC:

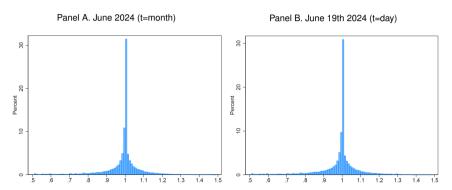
	CÓDIGO	DETALLE	CANTIDAD	PRECIO UNITARIO	PRECIO ÎTEM	1
		Lavaplatos FDV Small Acqua bajo cubierta	1	92.428,57	92.429	
	14761	Encimera FDV Design 4T GLTX 65 BUT 2.0	1	142.848,74	142.849	ı
	14265	Campana Kubli Neu Slider	1	100.831,93	100.832	ı
	19110	Horno FDV Design	1	201.672,27	201.672	ı
ı	13377	Lavavajillas FS FDV Element 14C	1	243.689,07	243.689	ı
ì	14917	Griferia FDV CONICA FLEX	1	84.025,21	84.025	ı
i	10232	Transporte - Providencia	1	15.529,41	15.529	ı

Data cleaning Return

Goal: Keep all plausible transactions

- Prices are net of discounts and recharges
- Drop if a transaction has missing or zero price or quantity
- Drop if product description is missing
- Drop transactions where seller-product-day maxmin price ratio is above the 99th percentile
- Under this cleaning we keep around 95% of transactions

Price Dispersion Return



- o $\theta_{jgt} = \frac{\rho_{jgit}}{\bar{\rho}_{igt}}$; seller j, product g, buyer i, time t (excluding products with one transaction)
- o $Var(log \theta_{iad}) = 0.65$
- o indicative evidence inconsistent with uniform pricing in 70% of transactions Residual Drivers

Price Variance Determinants for 2024: Strategy Reum

Step 1

- Make goods comparable and eliminate possible demand and supply shocks
- o Store residuals from:

In
$$p_{jgit} = eta_0 + \Psi_{jgd} + oldsymbol{arepsilon}_{jgit}$$

 p_{jgit} is the price for seller j, product g, buyer i in time t, Ψ is a fixed effect including day d

Step 2

- Project residuals on different observables (quantity transacted and buyers' observables)
- Compare R²

Price Determinants for 2024: Results Return

Seller j, product g, buyer i, time t, day d, quantity g, buyer group B (11 sectors \times 3 sizes \times 16 regions)

$$arepsilon_{jgit} = eta_0 + \Psi_{jgdS} + arepsilon_{jgit}$$

	(1)	(2)	(2)
R^2	0.34	0.28	0.53
S = Quantity	\checkmark		
$S = Buyer \; Group$		\checkmark	
$S\!=\!Quantity imesBuyer$ group			\checkmark
N	147M	147M	147M

Consistent whit hybrid second + thrid dregree price discrimination schemes







Price Determinants for 2024: Monthly Fixed Effects Reum

Seller j, product g, buyer i, time t, month m, quantity q, buyer group B (11 sectors×3 sizes×16 regions)

$$\ln p_{jgit} = eta_0 + \Psi_{jgdS} + arepsilon_{jgit}$$

	(1)	(2)	(3)	(4)
R^2	0.34	0.51	0.41	0.62
$\mathcal{S}\!=\!Quantity$	\checkmark			
$\mathit{S} = Buyer$		\checkmark		
$S\!=\!$ Buyer Group			\checkmark	
$S\!=\!Quantity imes Buyergroup$				\checkmark
N	363M	363M	363M	363M

Price Determinants for 2024: Manufacturing Return

Seller j, product g, buyer i, time t, month m, quantity q, buyer group B (11 sectors×3 sizes×16 regions)

In
$$ho_{jgit} = eta_0 + \Psi_{jgmS} + arepsilon_{jgit}$$

	(1)	(2)	(3)	(4)
R^2	0.45	0.54	0.46	0.81
$\mathcal{S}\!=\!Quantity$	\checkmark			
$S\!=\!Buyer$		\checkmark		
$S = Buyer \; Group$			\checkmark	
$S\!=\!Quantity imes Buyergroup$				\checkmark
N	136M	136M	136M	136M

Price Determinants for 2024: Retail and Wholesale Return

Seller j, product g, buyer i, time t, month m, quantity q, buyer group B (11 sectors×3 sizes×16 regions)

$$\ln
ho_{jgit} = eta_0 + \Psi_{jgmS} + arepsilon_{jgit}$$

	(1)	(2)	(3)	(4)
R^2	0.38	0.65	0.49	0.68
$\mathcal{S}\!=\!Quantity$	\checkmark			
$\mathit{S} = Buyer$		\checkmark		
$S\!=\!$ Buyer Group			\checkmark	
$\mathit{S} = Quantity imes Buyer$ group				\checkmark
N	180M	180M	180M	180M

Buyer Market Power? Return

- Exploit cross-sectional variation in the number of suppliers each buyer transacts with
- A larger number of providers may indicate stronger outside options; better pricing terms

$$\ln p_{jgim} = eta_0 + eta_1 \ln q_{jgim} + eta_2 \left(\log q_{jgim} imes \log \mathsf{NumProviders}_i
ight) + \Psi_{jgm} + arepsilon_{jgit},$$

- o $\beta_2 > 0$ would suggest that quantity discounts become flatter as buyer power increases
- o We find that $\beta_1 = -0.0462$ (0.0001) and $\beta_2 = -0.0098$ (0.0001)
- Buyer power does not appear to be the primary mechanism generating quantity discounts

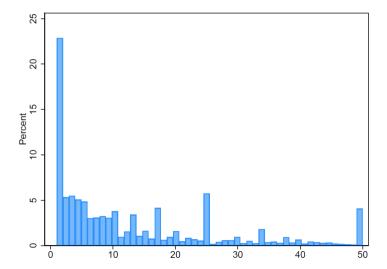
Nonlinear Prices by Sector PReturn

Sector	Mean Q discount	N transactions
All sectors	-0.042	430M
Agriculture	-0.042	2M
Mining	-0.016	1 M
Manufacturing	-0.036	118M
Utilities	0.000	6M
Construction	-0.129	1 M
Retail and Wholesale	-0.048	270M
Transport & ICTs	-0.032	12M
Financial Services	-0.002	49M
Real Estate Services	-0.052	1 M
Business Services	-0.089	5M
Personal Services	-0.053	1M

Quantity Quantiles Bins Return

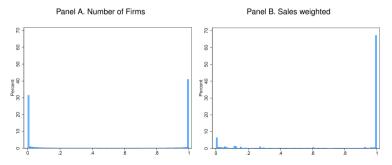
- \circ Products have different scales, we compare prices across each product's q rank distribution
- o For each product g, $F_g(\cdot)$: empirical CDF of transacted quantities q_{jgit}
- o Define the within-product rank: $r_{jgit} \equiv F_g(q_{jgit})$.
- o Partition [0,1] into 50 equal-probability intervals $I_b \equiv \left((b-1)/50,\ b/50\right]$ for $b=1,\ldots,50$
- o Assign each transaction to a bin $B_{jgit} = b$ whenever $r_{jgit} \in I_b$
- With discrete quantities and mass points, we assign observations to the smallest b

Quantity Quantiles Bins Histogram Return



Sales partition • Return

$$X_i = \begin{cases} 0 & \text{if all sales go to final consumers} \\ 1 & \text{if all sales go to other firms} \end{cases}$$



More than 70% of firms sell only to final consumers or to other firms (By sector)

Sales partition: Sales shares (excluding exports)

Sector (sales)	All to final consumer	All to other firms
Firm population	0.08	0.67
Agriculture (2%)	0.04	0.60
Mining (1%)	0.27	0.08
Manufacturing (15%)	0.05	0.68
Utilities (3%)	0.20	0.51
Construction (8%)	0.02	0.89
Retail and Wholesale (32%)	0.09	0.68
Transport & ICTs (10%)	0.16	0.68
Financial Services (18%)	0.18	0.67
Real Estate Services (1%)	0.24	0.37
Business Services (7%)	0.08	0.81
Personal Services (2%)	0.68	0.10

Guesses Verification Return

Guess 1 (two-part tariffs with quantity-invariant marginal price within each (ℓ, b, u))

o follows immediately from the two-part tariff and constant markup in Proposition 1

Guess 2 (homogenous link revenue)

- o Is verified by aggregating optimal link choices across partitions
- o The seller's total revenue is isoelastic in own quantity with exponent $(\sigma_u 1)/\sigma_u$
- Admits a closed-form scale A_{su} that explicitly includes a flat-fee component driven by the seller's CES share in buyers' materials bundles

General Equilibrium Under Nonlinear Prices Petur

A general equilibrium under nonlinear pricing is a collection

$$\left\{ (\textit{m}_{\textit{ubi}}^{\ell}(\cdot), \textit{T}_{\textit{ubi}}^{\ell}(\cdot), \textit{B}_{\ell \textit{bi}})_{(\ell, \textit{b}), i}, \, (\textit{p}_{\textit{bi}}^{\ell, *})_{(\ell, \textit{b}), i}, \, (\textit{P}_{\textit{ub}}^{\ell})_{\textit{u}, \textit{b}, \ell}, \, (\textit{N}_{\textit{s}}^{\ell})_{\textit{s}, \ell}, \, (\textit{Q}_{\textit{j}}, \textit{I}_{\textit{j}})_{\textit{j}} \right\}$$

such that: (i) mechanisms $(m_{ubi}^{\ell}(\cdot), T_{ubi}^{\ell}(\cdot))$ implement the two–part–tariff optimum with $p_{bi}^{\ell,*}$ and $F_{ubi}^{\ell,*}$ in Proposition 1; (ii) buyers' choices satisfy the best–response condition above; (iii) price and cost indices satisfy; (iv) materials and labor markets clear with L=1; and (v) free entry holds in each (ℓ,s) . A detailed proof of existence and uniqueness is provided in the paper.

Upstream Firm Profits Under Nonlinear Prices: • Return

$$\mathbb{E}\left[\Pi_{j}^{u}\right] = \underbrace{\sum_{\ell} \sum_{s} \int_{i \in B_{\ell s}} \left(p_{j s}^{\ell} - c_{j}\right) m_{i j} \, dv_{\ell s}^{i}}_{\text{allocative margin}} + \underbrace{\sum_{\ell} \sum_{s} \int_{i \in B_{\ell s}} F_{j s i}^{\ell} \, dv_{\ell s}^{i}}_{\text{flat-fee payments}} - \underbrace{\sum_{s'} \int_{j' \in D_{j}} F_{j', s'}^{u} \, dv_{s'}^{j}}_{\text{flat-fee payments}}$$

- B denotes seller firm j client set, D denote seller firm j suppliers set (exogenous sets)
- o NLP Marginal Prices. Charge and pay smaller marginal prices (p_{is}^{ℓ}, c_{i}) relative to Lin. P.
- o Rents. Through flat fees seller j, extracts rents, but it's also rent extracted
- o **GE** incidence. Cheaper c_j lift downstream demand; double marginizalization attenuation
- o **Entry.** Depends on m_{ij} expansion and net rent extraction (firm entry is misallocated)

Retailer Firm Profits Under Nonlinear Prices Petur

$$\mathbb{E}\left[\Pi_i^r\right] = \underbrace{\left(\frac{1}{\varphi_s}\right)R_i}_{\text{allocative margin}} - \underbrace{\sum_{s'}\int_{j\in D_j}F_{ijs'}^r\,dv_{s'}^j}_{\text{Flat fees payments to upstream}}$$

- Constant markup Allocative margin has a constant markup and a fixed share of revenue
- o NLP Marginal Prices. NLP lowers input costs, retail prices fall with constant markup and revenue expands; the allocative term scales proportionally with R_i
- o Rents. Extracted via fee payments to upstream
- Entry. Depends on change in profits: revenue expansion versus rent extraction

Welfare Decomposition: Intensive vs. Extensive Margins • Reum

Welfare is the inverse final price index:

$$W \equiv \frac{1}{P_Y}, \qquad \log P_Y = \sum_{s \in \mathscr{S}} \theta_s \log P_s.$$

With wage normalization and free entry, the representative household's income equals the wage, so $W = 1/P_Y$

- θ_s : final-expenditure share on retail sector s.
- P_s: sectoral retail price index.

Sectoral Price Indices (Retail Interface)

Within each retail sector s:

$$P_{s} = \mu_{s}^{r} \Theta_{s}^{r} w^{\alpha_{s}^{r}} \left(\prod_{s' \in \mathscr{S}} \left(P_{s's}^{r} \right)^{(1-\alpha_{s}^{r})} \theta_{ss'}^{r} \right) \left(N_{s}^{r} \right)^{-\frac{1}{\varphi_{s}-1}} \mathscr{V}_{s}, \qquad P_{s's}^{r} = \mu_{s's}^{r} C_{s'}. \tag{1}$$

- μ_s^r : retail-to-consumer markup (allocative wedge).
- $\mu_{s's}^r$: buyer-specific markup charged by upstream s' to retail s.
- $C_{s'}$: upstream sector-s' marginal cost index.
- N_s^r : mass of active retail varieties; \mathcal{V}_s : CES selection term.

Upstream Marginal Cost Recursion

For each upstream seller sector s':

$$C_{s'} = \Theta_{s'}^{u} \, \mathbf{w}^{\alpha_{s'}^{u}} \left(\prod_{v \in \mathscr{S}} \left(P_{vs'}^{u} \right)^{(1 - \alpha_{s'}^{u})} \theta_{s'v}^{u} \right) \left(N_{s'}^{u} \right)^{-\frac{1}{\sigma_{s'} - 1}} \, \mathscr{V}_{s'}^{u}, \qquad P_{vs'}^{u} = \mu_{vs'}^{u} \, C_{v}. \tag{2}$$

Taking logs and substituting $P_{vs'}^{u} = \mu_{vs'}^{u} C_{v}$:

$$\log C_{s'} = \sum_{v \in \mathscr{S}} (1 - \alpha_{s'}^u) \, \theta_{s'v}^u \left(\log \mu_{vs'}^u + \log C_v \right) + \alpha_{s'}^u \log w + \log \Theta_{s'}^u - \frac{1}{\sigma_{s'} - 1} \log N_{s'}^u + \log \mathscr{V}_{s'}^u. \tag{3}$$

Upstream System and Response Across Regimes

Stacking (3) with $A^{uu}_{s'v} := (1 - \alpha^u_{s'}) \, \theta^u_{s'v}$ gives

$$\log C^{u} = A^{uu} \log C^{u} + \log \mu^{uu} + \alpha^{u} \log w + \log \Theta^{u} - \frac{\log N^{u}}{\sigma - 1} + \log \mathcal{V}^{u}, \tag{4}$$

where division by $(\sigma - 1)$ is elementwise and $\log \mu^{uu}$ stacks upstream \rightarrow upstream wedges. In changes across regimes (technology and w drop out):

$$\Delta \log C^{u} = (I - A^{uu})^{-1} \left(\Delta \log \mu^{uu} - \frac{\Delta \log N^{u}}{\sigma - 1} + \Delta \log \mathcal{V}^{u} \right). \tag{5}$$

Final Demand Exposures

Define upstream—upstream and retail—upstream cost-share matrices:

$$A_{s'v}^{uu} := \left(1 - \alpha_{s'}^u\right) \theta_{s'v}^u, \qquad B_{ss'}^{ru} := \left(1 - \alpha_{s}^r\right) \theta_{ss'}^r.$$

Final-demand exposures that load upstream objects into $\log P_Y$:

$$\tilde{\lambda}_{ru} := \theta^{\top} B^{ru} \in \mathbb{R}^{1 \times |\mathscr{S}|}, \qquad \tilde{\lambda}_{u} := \tilde{\lambda}_{ru} (I - A^{uu})^{-1} \in \mathbb{R}^{1 \times |\mathscr{S}|}. \tag{6}$$

- $\tilde{\lambda}_{ru}$: exposure at the retail interface (no upstream propagation).
- $\tilde{\lambda}_u$: full upstream propagation via the Leontief inverse.

Exact Welfare Decomposition

Starting from (1)–(6) and the upstream recursion, the change in welfare satisfies

$$\Delta \log W = -\sum_{s} \theta_{s} \Delta \log \mu_{s}^{r} - \tilde{\lambda}_{ru} \Delta \log \mu^{r} - \tilde{\lambda}_{u} \Delta \log \mu^{uu}$$

Intensive (allocative) markups: retail→consumer, retail↔upstream, upstream⇔upstream

$$+ \underbrace{\sum_{s} \frac{\theta_{s}}{\varphi_{s} - 1} \Delta \log N_{s}^{r} + \tilde{\lambda}_{u} \left(\frac{\Delta \log N^{u}}{\sigma - 1} \right)}_{s}$$

Extensive (variety/masses)

$$-\sum_{s}\theta_{s}\Delta\log\mathscr{V}_{s}-\tilde{\lambda}_{u}\Delta\log\mathscr{V}^{u}.$$

Selection (composition)

Labor Output Elasticity α_s Return

- What. Cobb-Douglas weight on *non-materials* (labor + user cost of capital).
- o Identify. Cost-share mapping under cost minimization:

$$\alpha_i = 1 - \frac{\sum_j p_{ji} m_{ji}}{w_i L_i + r_i K_i + \sum_j p_{ji} m_{ji}}.$$

Flat fees: $TC_i = F_i + VC_i$; for large buyers F_i/TC_i is small \Rightarrow variable share \approx total share.

- o **Sample.** Keep firms above 75th pctl. revenue; winsorize α_i at 1–99; aggregate to (s, ℓ) at 6-digit; average 2005–2022.
- o Why. Governs response to wage vs. input-price shocks: higher α_s amplifies wage relevance, dampens price conduct action from materials prices.

Labor Shares by Sector (Results)

Labor Shares by Sector (mean)

Sector	Retailers	Upstream	Sector mean
Agriculture	0.43	0.41	0.42
Mining	0.25	0.32	0.29
Manufacturing	0.39	0.42	0.41
Utilities	0.37	0.38	0.38
Construction	0.48	0.42	0.45
Retail and Wholesale	0.37	0.31	0.34
Transport and ICTs	0.55	0.47	0.51
Financial Services	0.58	0.62	0.60
Real Estate Services	0.66	0.53	0.59
Business Services	0.72	0.65	0.69
Personal Services	0.71	0.57	0.64
Type mean	0.50	0.46	0.48

Final-Demand Output Elasticity θ_s

- What. Cobb—Douglas weights across retail sectors in final demand.
- Identify. With linear pricing to consumers, retail revenues identify expenditure shares:

$$heta_s pprox rac{ ext{retail revenue in } s}{\sum_{s'} ext{retail revenue in } s'}.$$

- Sample. Large retailers (>75th pctl.), compute annual sector shares, average 2005–2022; check revenue-weighted robustness.
- Why. Anchors final-demand system and welfare accounting in counterfactuals.

Final-Demand Shares θ_s (Results)

Cobb-Douglas Output Elasticities by Retail Sector

Sector	$ heta_{s}$
Agriculture	0.0446
Mining	0.0085
Manufacturing	0.1318
Utilities	0.0505
Construction	0.1521
Retail and Wholesale	0.2768
Transport and ICTs	0.0979
Financial Services	0.1132
Real Estate Services	0.0152
Business Services	0.0911
Personal Services	0.0183

Materials Input–Output Shares $oldsymbol{ heta}_{iss'}^{\ell}$

What. Buyer-facing expenditure shares over upstream seller sectors s':

$$\theta_{iss'}^{\ell} = \frac{\sum_{j \in \mathscr{U}_{s'}} \rho_{ij} m_{ij}}{\sum_{s'} \sum_{j \in \mathscr{U}_{s''}} \rho_{ij} m_{ij}}, \quad \sum_{s'} \theta_{iss'}^{\ell} = 1.$$

- o **Identify.** From transaction-level variable payments (VC); TC = F + VC, large buyers $\Rightarrow F/TC$ small.
- o **Sample.** Compute firm-level θ for $\ell \in \{r, u\}$; keep >75th pctl. revenue; aggregate to 6-digit, then to 1-digit by year; average 2005–2022.
- Why. Micro foundation for the IO network; pins exposures and intensive-margin substitution scope.

Materials IO Shares: Retailers as Buyers (Results)

Input-output Elasticities by Retailers as Buyers

Buyer \ Seller	Agr.	Min.	Man.	Uti.	Cons.	R. & W.	T. & ICTs	F. Serv.	RE. Serv.	B. Serv.	P. Serv.
Agriculture	0.25	0.00	0.21	0.02	0.03	0.32	0.05	0.07	0.00	0.04	0.00
Mining	0.00	0.04	0.19	0.06	0.15	0.30	0.07	0.02	0.00	0.17	0.00
Manufacturing	0.13	0.02	0.35	0.02	0.03	0.25	0.11	0.03	0.00	0.06	0.00
Utilities	0.07	0.01	0.18	0.03	0.03	0.26	0.17	0.05	0.00	0.20	0.00
Construction	0.10	0.00	0.10	0.02	0.22	0.24	0.15	0.03	0.00	0.14	0.00
Retail and Wholesale	0.16	0.01	0.24	0.01	0.02	0.34	0.08	0.05	0.00	0.09	0.00
Transport and ICTs	0.07	0.01	0.14	0.02	0.03	0.24	0.19	0.04	0.00	0.26	0.00
Financial Services	0.08	0.00	0.12	0.01	0.01	0.22	0.06	0.15	0.01	0.33	0.00
Real Estate Services	0.03	0.00	0.12	0.01	0.02	0.30	0.04	0.06	0.05	0.37	0.00
Business Services	0.07	0.00	0.13	0.01	0.01	0.22	0.09	0.06	0.00	0.41	0.00
Personal Services	0.07	0.00	0.17	0.02	0.02	0.25	0.07	0.08	0.00	0.33	0.01

Materials IO Shares: Upstream as Buyers (Results)

Input-output Elasticities by Upstream Firms as Buyers

Buyer \ Seller	Agr.	Min.	Man.	Uti.	Cons.	R. & W.	T. & ICTs	F. Serv.	RE. Serv.	B. Serv.	P. Serv.
Agriculture	0.26	0.00	0.12	0.02	0.04	0.29	0.10	0.06	0.00	0.10	0.00
Mining	0.01	0.07	0.39	0.05	0.06	0.13	0.11	0.03	0.00	0.15	0.00
Manufacturing	0.08	0.02	0.49	0.03	0.02	0.15	0.09	0.02	0.00	0.10	0.00
Utilities	0.06	0.02	0.18	0.07	0.03	0.18	0.15	0.04	0.00	0.27	0.00
Construction	0.07	0.00	0.14	0.03	0.30	0.18	0.12	0.03	0.00	0.13	0.00
Retail and Wholesale	0.12	0.01	0.27	0.01	0.02	0.38	0.07	0.03	0.00	0.10	0.00
Transport and ICTs	0.06	0.02	0.14	0.02	0.04	0.21	0.22	0.03	0.00	0.26	0.00
Financial Services	0.05	0.00	0.12	0.02	0.01	0.20	0.07	0.12	0.01	0.41	0.00
Real Estate Services	0.03	0.00	0.11	0.01	0.02	0.27	0.04	0.04	0.06	0.41	0.00
Business Services	0.07	0.00	0.13	0.01	0.01	0.23	0.09	0.05	0.00	0.40	0.00
Personal Services	0.06	0.00	0.15	0.03	0.02	0.21	0.07	0.11	0.00	0.33	0.01

Upstream Materials Elasticity σ_{II}

- o What. Substitutability across varieties within an upstream seller sector u'.
- Identify. IV from March 2020 municipal lockdown of main supplier u*:

$$\Delta_{12}\log\frac{\textit{m}_{\textit{isut}}}{\textit{m}_{\textit{isu}^*t}} = -\sigma_{\textit{u'}}\,\Delta_{12}\widehat{\log\frac{\textit{p}_{\textit{isut}}}{\textit{p}_{\textit{isu}^*t}}} + \gamma_{\textit{s}} + \varepsilon.$$

- o **Design.** 2SLS by seller sector; instrument $Z_{isu} = \mathbf{1}\{u^* \text{ locked}\}$; 12m diffs; large buyers; exclude buyer/clients/other inputs under lockdown; cluster at buyer level.
- o Why. Higher σ \Rightarrow faster rewiring, stronger intensive reallocation, lower pass-through; feeds κ mapping. (Conservatively set $\sigma \geq$ 1.45 where $\hat{\sigma} <$ 1.)

Estimated Elasticities $\sigma_{ii'}$ (Results)

Estimated Elasticities of Substitution by Seller Sector

Sector	$\sigma_{u'}$	SE	1 st Stage F stat.	Obs.
Agriculture	2.59	(1.35)	10.24	4,387
Manufacturing	3.41	(0.84)	16.37	186,912
Construction	1.45	(0.42)	7.36	6,062
Retail and Wholesale	3.80	(0.39)	94.08	680,985
Transport and ICTs	5.07	(2.22)	25.19	24,054
Financial Services	3.09	(1.56)	9.35	3,631
Business Services	5.21	(2.02)	17.55	4,514
Personal Services	6.69	(3.37)	13.29	7,579
All sectors	3.04	(1.12)	149.87	918,124

Three sectors (Mining, Utilities, Real Estate Services) yield $\hat{\sigma}_{u'} < 1$; we set $\sigma_{u'} = 1.45$ (minimum estimate above one) for model quantification.

Final-Consumer Variety Elasticity ϕ_{s_r}

- o What. CES elasticity across retail *varieties* within sector s_r ; markup $\mu = \varphi/(\varphi 1)$.
- o Identify. Sectoral accounting identity under linear pricing:

$$\varphi_{s_r,t} = \frac{\sum_j R_{j,t}}{w_{s_r,t} \sum_j F_{j,t} + \sum_j \Pi_{j,t}}, \quad \Pi_j^{\text{var}} = \frac{1}{\varphi_{s_r}} R_j.$$

- o **Sample.** Large retailers; $F_{i,t}$ small, pool to sector-year; average 2005–2022.
- o Why. Higher $\varphi \Rightarrow$ keener competition, smaller wedges; also maps retailer labor tails v into productivity tails $\kappa = (\varphi 1)v$.

Final-Consumer Elasticities ϕ_{s_r} (Results)

Retailer Parameter φ_{s_r} by Sector

Sector	$oldsymbol{arphi}_{\mathcal{S}_r}$
Agriculture	4.54
Mining	2.68
Manufacturing	4.22
Utilities	3.94
Construction	2.59
Retail and Wholesale	8.17
Transport and ICTs	2.05
Financial Services	1.40
Real Estate Services	1.82
Business Services	2.73
Personal Services	2.56
Type mean	3.34

Notes: φ_{s_r} computed from pooled sectoral sums of revenue, fixed costs (labor units), and profits.

Exit Hazard $\boldsymbol{\delta}_{s_{\ell}}$

- What. One-year hazard that an active firm exits.
- o **Measure**. For cell (s, ℓ, t) :

$$\delta_{s_{\ell},t} = 1 - \frac{\mathsf{survivors}_{s_{\ell},t}}{\mathsf{active}_{s_{\ell},t}}, \qquad \delta_{s_{\ell}} = \frac{1}{|\mathscr{T}|} \sum_{t \in \mathscr{T}} \delta_{s_{\ell},t}.$$

- o Sample. Compute at 6-digit \times type; track 2005–2022; average across years.
- o Why. Disciplines expected lifespan and shock persistence; higher δ increases payoff needed for entry, tilts adjustments toward the extensive margin.

Exit Rates δ by Sector (Results)

Exit Rates (δ) by Sector (Means)

Sector	Retailers	Upstream	Sector mean
Agriculture	0.090	0.086	0.088
Mining	0.084	0.093	0.088
Manufacturing	0.093	0.071	0.082
Utilities	0.070	0.064	0.067
Construction	0.140	0.110	0.125
Retail and Wholesale	0.103	0.076	0.089
Transport and ICTs	0.088	0.093	0.091
Financial Services	0.101	0.062	0.081
Real Estate Services	0.115	0.099	0.107
Business Services	0.099	0.077	0.088
Personal Services	0.093	0.090	0.092
Type mean	0.098	0.084	0.091

Entry Cost $c_{e,s_{\ell}}$ (in labor units)

- o What. Sunk labor resources required to create an operating firm.
- o **Identify.** Free entry with survival hazard δ :

$$ext{PV}_{s_\ell} = rac{ar{\mathsf{\Pi}}_{s_\ell}}{1 - eta(1 - \delta_{s_\ell})}, \quad \pmb{w}_{s_\ell} \pmb{c}_{e,s_\ell} = \pmb{p}_{s_\ell}^{ ext{succ}} \cdot ext{PV}_{s_\ell} \Rightarrow \pmb{c}_{e,s_\ell} = rac{\pmb{p}_{s_\ell}^{ ext{succ}}}{\pmb{w}_{s_\ell}} \cdot rac{ar{\mathsf{\Pi}}_{s_\ell}}{1 - eta(1 - \delta_{s_\ell})}.$$

- o **Sample.** Use observed profits Π , wages w, positive-profit share p^{succ} , and δ at 6-digit \times type; report currency and wage-bill equivalents.
- Why. Shapes steady-state firm mass/scale; interacts with NLP's rent reallocation along the chain.

Entry Costs ce by Sector (Results)

Entry Costs and Equivalent Yearly Wage-Bills by Sector

	Reta	ailers	Upstream			
Sector	Entry cost ce	Wage-bill eq.	Entry cost ce	Wage-bill eq.		
Agriculture	81.03	3.68	84.12	4.78		
Mining	29212.81	43.99	177.12	7.20		
Manufacturing	101.87	4.25	120.80	4.53		
Utilities	700.66	14.15	306.11	5.50		
Construction	109.72	7.78	109.05	4.18		
Retail and Wholesale	63.92	6.06	83.61	5.13		
Transport and ICTs	299.85	10.28	98.03	6.40		
Financial Services	263.84	8.64	248.44	9.05		
Real Estate Services	82.11	11.68	100.69	8.70		
Business Services	82.91	5.76	125.21	3.11		
Personal Services	127.87	4.56	94.76	4.57		
Type mean	2829.69	10.98	140.72	5.74		

Notes: Entry costs c_e are in the currency units used for calibration; "Wage-bill eq." reports multiples of the annual wage bill.

Productivity Tail Exponent K

- What. Thickness of the upper tail of firm productivity.
- o Identify. Estimate labor tail by MLE above threshold:

$$\widehat{\mathbf{v}} = \frac{n}{\sum_{i:L_i > L_{\min}} \ln(L_i/L_{\min})}, \quad \mathrm{SE}(\widehat{\mathbf{v}}) \approx \widehat{\mathbf{v}}/\sqrt{n}.$$

Map to productivity using $I(z) \propto z^{\sigma-1}$ (or $\varphi-1$ for retail):

$$\kappa^{u} = (\sigma - 1)v^{u}, \qquad \kappa^{r} = (\varphi - 1)v^{r}.$$

- o Sample. Compute ν by 1-digit \times type; combine with sectoral σ / φ ; report implied κ .
- o Why. Thicker tails (small κ) magnify selection/reallocation gains and shape how NLP shifts surplus across the distribution.

Labor and Implied Productivity Tails $\boldsymbol{v}, \boldsymbol{\kappa}$ (Results)

Labor and Implied Productivity Pareto Tails by Sector

		Retailers			
Sector	$\overline{v_r}$	$\kappa_r = (\varphi_s - 1)\nu_r$	v_u	$\kappa_u = (\sigma_{u'} - 1)\nu_u$	$\sigma_{u'}$
Agriculture	2.49	8.82	2.63	4.18	2.59
Mining	1.43	2.40	2.20	0.99	1.45
Manufacturing	2.66	8.58	2.15	5.18	3.41
Utilities	2.17	6.38	1.94	0.87	1.45
Construction	3.23	5.13	2.19	0.99	1.45
Retail and Wholesale	3.45	24.74	2.40	6.72	3.80
Transport and ICTs	2.20	2.32	3.04	12.37	5.07
Financial Services	2.55	1.02	2.26	4.72	3.09
Real Estate Services	4.36	3.59	3.03	1.36	1.45
Business Services	2.45	4.25	1.93	8.13	5.21
Personal Services	2.03	3.17	2.58	14.69	6.69

Notes: $\kappa = (\sigma_{u'} - 1)\nu$ uses seller-sector elasticities $\sigma_{u'}$ from the IV estimates. For Mining, Utilities, and Real Estate Services, we set $\sigma_{u'} = 1.45$ (minimum estimate above one).

Sectoral Allocative Markups Final-Demand Weighted Petur

Sector	Lin	NLP: $u \rightarrow r$	NLP: $u \rightarrow u$	Share(r $ ightarrow$ u)	Share(full up)
Agriculture	1.63	1.18	1.17	0.053	0.050
Mining	3.27	1.94	1.46	0.005	0.009
Manufacturing	1.41	1.12	1.16	0.186	0.175
Utilities	3.27	1.47	1.56	0.036	0.024
Construction	3.27	1.27	1.46	0.121	0.084
Retail & Wholesale	1.36	1.08	1.12	0.319	0.364
Transport & ICTs	1.25	1.10	1.07	0.096	0.136
Financial Services	1.48	1.15	1.17	0.087	0.071
Real Estate Services	3.27	1.19	1.30	0.018	0.013
Business Services	1.24	1.08	1.11	0.067	0.065
Personal Services	1.18	1.08	1.06	0.012	0.009
Weighted aggregate	1.61	1.14	1.17		