

# Price Discrimination in Production Networks

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# Motivation

## What is the price formation process of firms in production network structures?

In inefficient economies, firms are usually modeled as choosing a single price with one distortionary markup, often considered a wedge, that can cumulate downstream production networks and generate production factors missallocation.

But if firms can discriminate prices, firm-specific or product-specific markups are not necessarily distortionary.

A possible starting point for analyzing firm-specific price discrimination distortionary effects is to (try to) understand why firms can discriminate prices.

# This paper (1)

Assuming that firms are multiproduct objects that discriminate prices within production networks:

## Questions:

- 1 Why do firms can endogenously discriminate prices in production networks?
- 2 What are the aggregate implications of price discrimination in supply chains on (i) Production efficiency and (ii) Welfare?

# This paper (2)

## What this paper **PLANS** to do:

- (a) Present evidence of price discrimination in Chile.
- (b) Develop a theoretical framework to endogenize product pricing decisions by firms facing heterogeneous demand elasticities downstream.
- (c) Estimate firm-level elasticities of substitution and buyer-product level demand elasticities.
- (d) Aggregate price discrimination effects on:
  - ① Heterogeneous Producers and Consumers Welfare.
  - ② TFP in supply chains with firm-product pairs markups.
- (e) Run counterfactuals: What are the aggregate gains/losses of eliminating/reducing price discrimination heterogeneity?

# Related Literature

## Price discrimination and missallocation

Bornstein and Peter (AER R&R 2023), Burstein, Cravino & Rojas (WP, 2024)

## Endogenous multi-product market power

Edmond, Midrigan & Xu (JPE, 2023)

## Aggregating in presence of distortions

Liu (QJE 2019), Baqaee & Farhi (QJE 2020), Davila & Schaab (WP, 2022)

## Firm level elasticities of substitution

Fujiy, Ghose, Khanna (STEG WP, 2023)

## 1 Price discrimination evidence from Chile

## 2 Theoretical framework

- Simplified model
- Quantitative exploration simplified model

## 3 Application

# Data: Chilean IRS Electronic Invoices

Transaction-based data for the universe of formal Chilean firms from 2018.



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Centro de Distribución:  
Villa del Mar:  
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Camino Internacional 2440 Local 72, Villa del Mar  
Circunvalación 1055, Local 250/257, Talca - Teléfono: (56-2) 24117748  
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**FECHA EMISIÓN : 01/08/2022**

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TIPO DESPACHO :

FORMA DE PAGO : Contado

COD. VENDEDOR :

Orden de Venta: 793325

Número de OC:

CÓDIGO	DETALLE	CANTIDAD	PRECIO UNITARIO	PRECIO ÍTEM
13452	Lavaplatos FDU Small Acqua bajo cubierta	1	92.428,57	92.429
14761	Encimera FDU Design 4T GLTX 65 BUT 2.0	1	142.848,74	142.849
14265	Campana Kubli Neu Slider	1	100.831,93	100.832
19110	Horno FDU Design	1	201.672,27	201.672
13377	Lavavajillas FS FDU Element 14C	1	243.689,07	243.689
14917	Grifería FDU CONICA FLEX	1	84.025,21	84.025
10232	Transporte - Providencia	1	15.529,41	15.529

## Price variance decomposition

$\ln p_{ijg}$  is log price charged by firm  $i$  to  $j$  for product  $g$  and  $G$  is the mean of  $\ln p_{ijg}$  across all  $ijg_s$  triples.  $\psi_{ig}$  is a seller-product fixed effect,  $\theta_j$  is a buyer fixed effect,  $\gamma_q$  is a quantity fixed effect, and  $\omega_{ijg}$  is the residual and accounts for the match-specific characteristics.

$$\ln p_{ijg} = \ln G + \ln \psi_{ig} + \ln \theta_j + \ln \gamma_q + \ln \omega_{ijg}$$

There are 4.5 Million seller-product fixed effects, but the focus is on buyers ( $\theta_j$ ) and quantities ( $\gamma_q$ ) variance decomposition:  $\text{var}(\theta_j + \gamma_q)$ .

$\frac{\text{var}(\theta_j)}{\text{var}(\theta_j + \gamma_q)}$	$\frac{\text{var}(\gamma_q)}{\text{var}(\theta_j + \gamma_q)}$	$\frac{2\text{cov}(\theta_j, \gamma_q)}{\text{var}(\theta_j + \gamma_q)}$	N obs	R2	Adj R2
0.64	0.50	-0.14	91,815,975	0.94	0.93

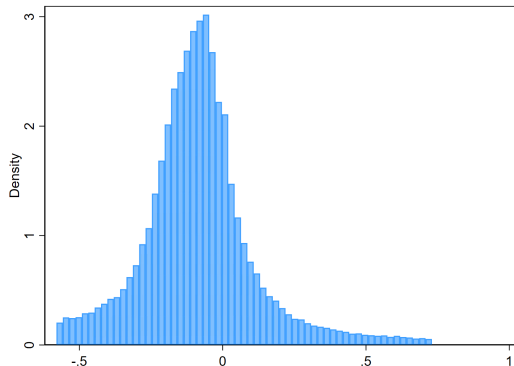
- Results suggest evidence of second and third-degree price discrimination.

second-degree data

third-degree data



## Buyers fixed effect ( $\theta_j$ ) distribution

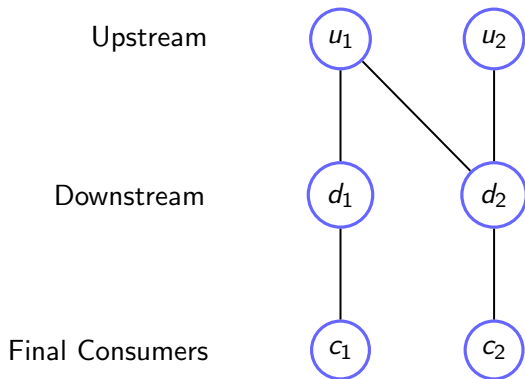


- Buyers fixed effect (which could capture bargaining power, market power, centrality) varies.
- Which might suggest upstream competition forces driving the price formation process.

**Upstream competition will motivate my modeling strategy.**

- 1 Price discrimination evidence from Chile
- 2 Theoretical framework
  - Simplified model
  - Quantitative exploration simplified model
- 3 Application

# Simplified Model



- Firm  $u_1$  sells quantity  $m_{1,d1}$  and  $m_{1,d2}$  at prices  $w_{1,d1}$  and  $w_{1,d2}$  to  $d_1$  and  $d_2$  respectively. While Firm  $u_2$  sells quantity  $m_2$  at prices  $w_2$  to  $d_2$ .
- Firms  $d_1$  and  $d_2$  produce  $q_1$  and  $q_2$  that sells to  $c_1$  and  $c_2$  respectively.

## Final consumers

Each final consumer consumes only one good and has the following symmetric demand:

$$q_c = p_c^{-\eta} \quad \text{with } c \in \{1, 2\}$$

## Downstream firms: $d_1$

Firm  $d_1$  production function is  $q_{d1} = m_{1,d1}$  and it faces marginal cost that equals the price that it pays to upstream firm 1  $w_{1,d1} = mc_{d1}$ .

Assuming the firm competes Bertrand, it will charge a constant markup over marginal cost to  $c_1$  as a function of its elasticity and produce according to the consumer's demand:

$$p_1 = \frac{\eta}{\eta - 1} w_{1,d1}$$
$$q_1 = \left( \frac{\eta}{\eta - 1} w_{1,d1} \right)^{-\eta}$$

## Downstream firms: $d_2$ (1)

Firm  $d_2$  buys production inputs from both upstream firms,  $m_{1,d2}$ ,  $m_{2,d2}$  at prices  $w_{1,d2}$ ,  $w_{2,d2}$ , following a CES production function with elasticity of substitution  $\sigma$ :

$$q_2(m_{1,d2}, m_{2,d2}) = A \left( \alpha_1 m_{1,d2}^{\frac{\sigma-1}{\sigma}} + \alpha_2 m_{2,d2}^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}}$$

The profit maximization problem will yield prices and quantities:

$$q_2 = \left( \frac{\eta}{\eta - 1} \frac{1}{A} \underbrace{\left( \alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma} \right)^{\frac{1}{1-\sigma}}}_{mc_{d2}} \right)^{-\eta}$$
$$p_2 = \frac{\eta}{\eta - 1} mc_{d2}$$

Downstream firm  $d_2$  will charge a constant markup to consumer  $c_2$  as a function of its demand elasticity.

## Downstream firms: $d_2$ (2)

$d_2$  conditional (on output and input prices) demands for each input are:

$$m_{1,d2}^*(w_{1,d2}, w_{2,d2}, q_2) = \frac{q_2}{A} \left( \frac{\alpha_1}{w_{1,d2}} \right)^\sigma \left( \alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma} \right)^{\frac{\sigma}{1-\sigma}}$$

$$m_{2,d2}^*(w_{1,d2}, w_{2,d2}, q_2) = \frac{q_2}{A} \left( \frac{\alpha_2}{w_{2,d2}} \right)^\sigma \left( \alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma} \right)^{\frac{\sigma}{1-\sigma}}$$

## Upstream firms: $u_1$ (1)

If  $u_1$  **can** discriminate prices, it maximizes profits by choosing prices for downstream firms by observing its factor demands:

$$\max_{\{w_{1,d1}, w_{1,d2}\}} \pi_{u1} = m_{1,d1}(w_{1,d1} - mc_u) + m_{1,d2}(w_{1,d2} - mc_u)$$

While if  $u_1$  **cannot** price discriminate, it will choose only one price for both downstream firms:

$$\max_{\{w_1\}} \pi_{u1} = (m_{1,d1} + m_{1,d2})(w_1 - mc_u)$$

Both upstream firms face a constant marginal cost  $mc_u$ .



## Upstream firms: $u_1$ (2)

Downstream firm 1 only uses input from upstream 1 in production, hence when  $u_1$  can price discriminate, applying the Bertrand pricing rule ( $p = \frac{e}{e-1}mc$ ):

$$m_{1,d1} = q_{d1}$$

$$m_{1,d1} = \left( \frac{\eta}{\eta - 1} w_{1,d1} \right)^{-\eta}$$

$$\log(m_{1,d1}) = -\eta \log \left( \frac{\eta}{\eta - 1} \right) - \eta \log(w_{1,d1})$$

$$-e_{m_{1,d1}, w_{1,d1}} = -\frac{\partial \log m_{1,d1}}{\partial \log w_{1,d1}} = \eta$$

Hence:

$$q_{u1,d1} = m_{1,d1} = q_{d1}$$

$$w_{1,d1} = \frac{\eta}{\eta - 1} mc_u$$

## Upstream firms: $u_1$ (3)

$u_1$  decisions with respect to  $d_2$  are different, because  $d_2$  uses two production inputs under a CES technology. The conditional factor demand of  $d_2$  for  $u_1$  is  $m_{1,d2}$ , hence solving for  $w_{1,d2}$

$$m_{1,d2} = \left(\frac{1}{A}\right)^{1-\eta} \left(\frac{\eta}{\eta-1}\right)^{-\eta} \left(\alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma}\right)^{\frac{\sigma-\eta}{1-\sigma}} \left(\frac{\alpha_1}{w_{1,d2}}\right)^\sigma$$

$$-\frac{\partial \log m_{1,d2}}{\partial \log w_{1,d2}} = (\eta - \sigma) \underbrace{\frac{\alpha_1^\sigma w_{1,d2}^{1-\sigma}}{\alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma}}}_{s_1} + \sigma$$

$$-e_{m_{1,d2}, w_{1,d2}} = \eta s_1 + \sigma(1 - s_1)$$

where  $s_1$  is the share of  $u_1$  good on  $d_2$  total costs. (Nested CES with inner and outer elasticity similar to Atkeson & Burstein, AER 2008)

## Upstream firms: $u_1$ (4)

Applying the same logic when  $u_1$  **cannot** discriminate:

$$-e_{m_1, w_1} = \eta (sh_{m1} + sh_{m2}s_1) + \sigma sh_{m2}(1 - s_1)$$

Where  $sh_{m1} = \frac{m_{1,d1}}{m_1}$  is the share of  $u_1$  production that  $d1$  purchases.

In sum:

$$e_{m_1, w_1} = \begin{cases} \eta s_1 + \sigma(1 - s_1) & \text{Price discrimination} \\ \eta (sh_{m1} + sh_{m2}s_1) + \sigma sh_{m2}(1 - s_1) & \text{NO price discrimination} \end{cases}$$

## Upstream firms $u_2$

Upstream 2 sells only to downstream 2, then:

$$m_{2,d2} = \left(\frac{1}{A}\right)^{1-\eta} \left(\frac{\eta}{\eta-1}\right)^{-\eta} \left(\alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma}\right)^{\frac{\sigma-\eta}{1-\sigma}} \left(\frac{\alpha_1}{w_{2,d2}}\right)^\sigma$$

$$-e_{2,d2} = \eta s_2 + \sigma(1 - s_2)$$

$$w_{2,d2} = \frac{\eta s_2 + \sigma(1 - s_2)}{\eta s_2 + \sigma(1 - s_2) - 1} mc_u$$

## Discussion: The $\eta - \sigma$ relation will govern markups

Upstream firm's demand elasticity is determined by how easy it is to substitute production inputs by downstream firms ( $\sigma$ ) and the demand elasticity downstream firms face ( $\eta$ ).

$$e_{i,di} = \eta s_i + \sigma(1 - s_i)$$

Large  $\eta$  and  $\sigma$  will prevent upstream firms from charging high markups. Hence, upstream firms can charge high markups:

- If the upstream firm good represents a small share of the total cost (small  $s_i$ ), then upstream can charge a high markup (small  $e_{i,di}$ ) as long as the downstream firm cannot substitute upstream firm good relatively easy (small  $\sigma$ ).
- If the upstream firm good represents a large share of the total cost (large  $s_i$ ), the upstream firm can charge a high markup as long as the demand elasticity downstream is low (small  $\eta$ )

## Quantitative exploration: Welfare

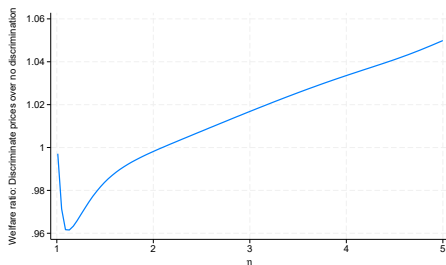
Welfare is defined as the sum of consumer surplus and firm profits.

$$W = CS_{c1} + CS_{c2} + \pi_{d1} + \pi_{d2} + \pi_{u1} + \pi_{u2}$$

$$W = \int_0^{q_1^*} q^{-\frac{1}{\eta}} dq - p_1^* q_1^* + \int_0^{q_2^*} q^{-\frac{1}{\eta}} dq - p_2^* q_2^* \\ + \pi_{d1} + \pi_{d2} + \pi_{u1} + \pi_{u2}$$

## Quantitative exploration: Variant $\eta$ Welfare

Assume  $mc_u = 0.5$ ,  $\alpha_1 = 0.6$ ,  $\alpha_2 = 0.4$ ,  $\sigma = 2$

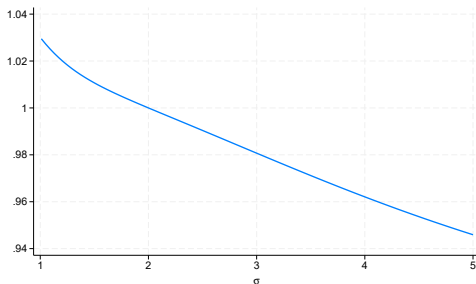


(a) Welfare ratio: Price disc./ no disc.

- With  $\sigma > \eta$ , final good has a relatively inelastic demand:  $u_1$  charges a high markup to  $d_1$  (not to  $d_2$ ) distorting  $d_1$  input and output and hence  $c_1$  consumer surplus.
- With  $\eta > \sigma$ , price discrimination is welfare enhancing as  $u_1$  can extract part of downstream firms' profits by tailoring specific prices.

# Quantitative exploration: Variant $\sigma$ Welfare

Assume  $\eta = 2$



(b) Welfare ratio: Price disc./ no disc.

Price discrimination is welfare enhancing only with  $\eta > \sigma$ .

Factor Prices

Welfare components



## Quantitative exploration: Aggregate TFP with shock to $\mu$

Using Baqaee & Farhi, QJE 2020, growth accounting in the presence of distortions formula:

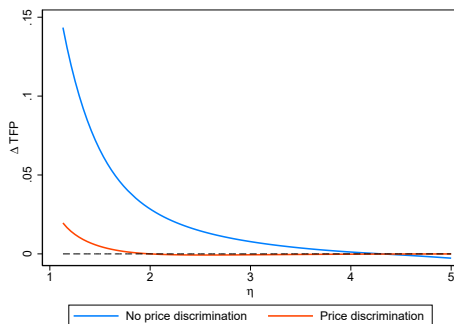
$$d \log TFP = \underbrace{\sum_i \tilde{\lambda}_i d \log A_i}_{\text{Technology}} - \underbrace{\sum_i \tilde{\lambda}_i d \log \mu_i + \sum_f \tilde{\Lambda}_{(f)} d \log \Lambda_f}_{\text{Allocative efficiency}}$$

Where  $\tilde{\lambda}_i$  and  $\tilde{\Lambda}_{(f)}$  are cost-based Domar weights for firms and factors respectively.

Assume a shock to markups given a 25% reduction of upstream marginal cost,  $d \log A_i = d \log \Lambda_f = 0$ , then:

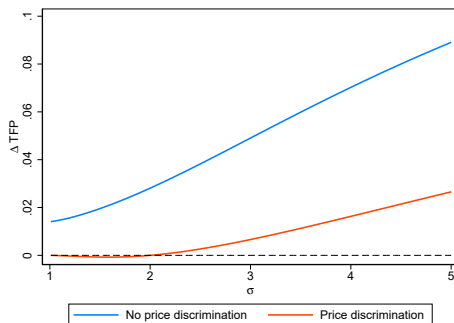
$$d \log TFP = - \sum_i \tilde{\lambda}_i d \log \mu_i$$

## Quantitative exploration: Aggregate TFP $\eta$ variant



- A reduction of marginal cost where firms cannot price discriminate (or face a unique demand downstream) will increase TFP if  $\eta$  is not too large.
- While if firms can discriminate prices (or face heterogeneous demands downstream), TFP will increase when  $\sigma > \eta$ .
- With  $\eta > \sigma$ , TFP changes tend to disappear as high demand elasticity erases markups.

## Quantitative exploration: Aggregate TFP $\sigma$ variant



(c) TFP change

- With no price discrimination, TFP changes increase with a higher elasticity of substitution, and most of the mc reduction will be passed downstream.
- While with price discrimination, TFP increases only when  $\sigma > \eta$ .

- 1 Price discrimination evidence from Chile
- 2 Theoretical framework
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## First data test

- (a) Take one month of transactions to get monthly weighted average prices and quantities for every seller-buyer-product.
- (b) Keep only buyers that purchase at most two intermediate inputs.
- (c) Keep only sellers that sell only one product.

# Identification Strategy (1)

$$w_{1,d2} = \frac{\eta s_1 + \sigma(1 - s_1)}{\eta s_1 + \sigma(1 - s_1) - 1} mc_u \quad (1)$$

$$w_{2,d2} = \frac{\eta s_2 + \sigma(1 - s_2)}{\eta s_2 + \sigma(1 - s_2) - 1} mc_u \quad (2)$$

Observed:  $s_1, s_2, w_{1,d2}, w_{2,d2}$

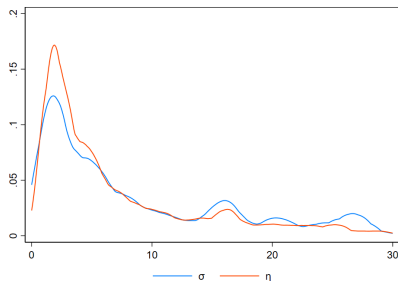
If the firm exhibits CRS, then average variable cost (which is observed) equals marginal costs. Therefore,  $\eta$  and  $\sigma$  are identified.

Define the learner index to be:  $L = \frac{w - mc}{w}$

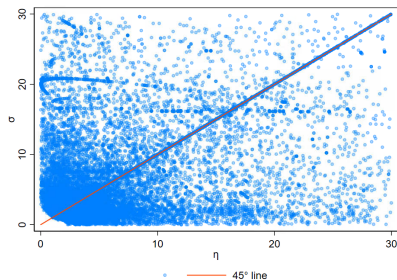
$$\sigma = \frac{s_1 L_1 - s_2 L_2}{(s_1 - s_2) L_1 L_2}$$
$$\eta = \frac{1 + L_1 \sigma (s_1 - 1)}{s_1 L_1}$$

# Preliminary Results: elasticities

Distribution



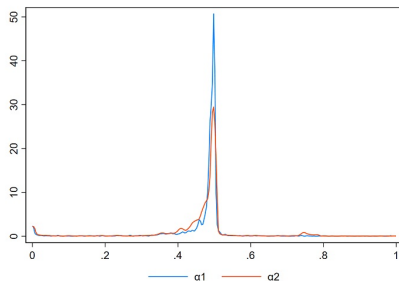
Scatter plot



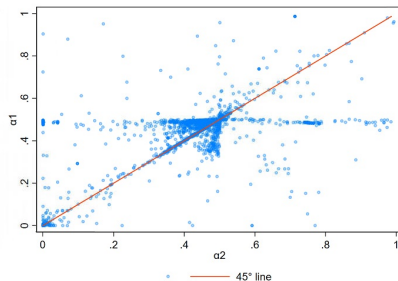
Estimations above and below 95% percentiles are trimmed.

# Preliminary Results: Alphas

Distribution



Scatter plot



$$s_1 = \frac{\alpha_1^\sigma w_{1,d2}^{1-\sigma}}{\alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma}}$$
$$s_2 = \frac{\alpha_2^\sigma w_{2,d2}^{1-\sigma}}{\alpha_1^\sigma w_{1,d2}^{1-\sigma} + \alpha_2^\sigma w_{2,d2}^{1-\sigma}}$$



## Next steps: Research plan

- (a) Extend model to  $n$  inputs and  $g$  products.
- (b) Evaluate more flexible production functions like CRESH, or at least include product nests inside the CES production function.
- (c) Deal with the over-identification problem. Build GMM estimators for  $\sigma_i$  and  $\eta_{jg}$  to profit panel data.
- (d) Run counterfactuals: What are the aggregate gains/losses of eliminating/reducing price discrimination heterogeneity?

## Price discrimination evidence: Second degree

► Go back

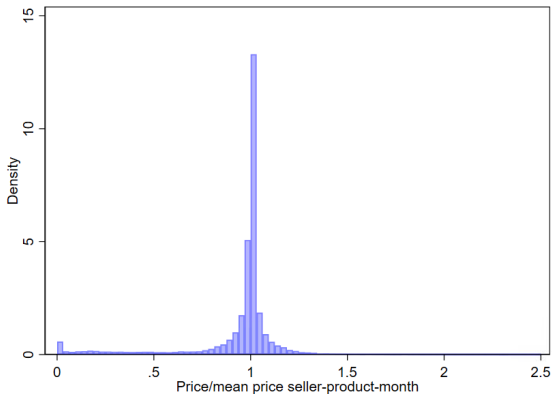
$$\log p_{ijt} = \beta_0 + \beta_1 \log q_{ijt}$$

	(1)	(2)	(3)	(4)
Log q	-0.1048	-0.0579	-0.1621	-0.1037
(SE)	0.00008	0.00006	0.00009	0.00007
Seller FE	Yes	Yes	Yes	Yes
Product FE	Yes	Yes	Yes	Yes
Buyer FE	No	No	Yes	Yes
Q > 1	No	Yes	No	Yes
R2	0.9112	0.9489	0.9246	0.9655
N obs	72,178,033	44,656,779	71,809,764	44,496,689

# Price discrimination evidence: Third degree

► Go back

Price variation by seller-product-month



## Bertrand pricing rule

$$\max_{\{p\}} \pi = q(p) \cdot p - q(p) \cdot mc$$

$$\frac{\partial q(p)}{\partial p} \cdot p + q(p) - \frac{\partial q(p)}{\partial p} \cdot mc = 0$$

$$\frac{\partial q(p)}{\partial p} (p - mc) + q(p) = 0$$

Multiplying by  $\frac{p}{q(p)}$

$$\underbrace{\frac{\partial q(p)}{\partial p} \frac{p}{q(p)}}_{-\eta} (p - mc) + q(p) \frac{p}{q(p)} = 0$$

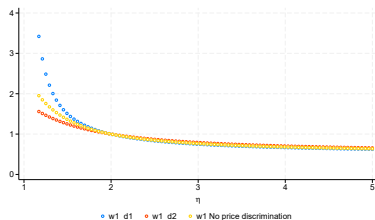
$$-\eta(p - mc) + p = 0$$

$$p(1 - \eta) = -\eta \cdot mc$$

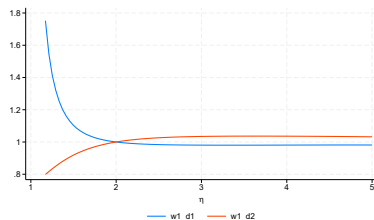
$$p = \frac{-\eta}{1 - \eta} \cdot mc$$

$$p = \frac{\eta}{\eta - 1} \cdot mc$$

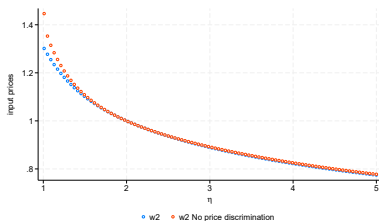
# Variant $\eta$ prices

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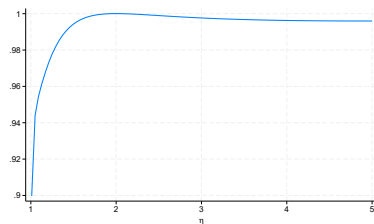
(d)  $w1$  level



(e)  $w1$  ratio: Price disc./ no disc.



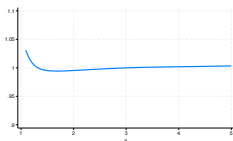
(f)  $w2$  level



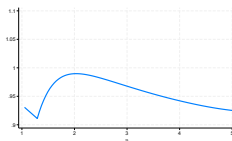
(g)  $w2$  ratio: Price disc./ no disc.

# Variant $\eta$ welfare components ratio: Price disc./ no disc.

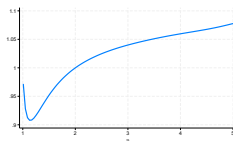
► Go back



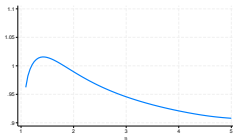
(h)  $\pi$  Upstream 1



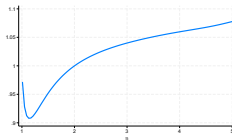
(i)  $\pi$  Upstream 2



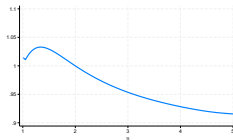
(j)  $\pi$  Downstream 1



(k)  $\pi$  Downstream 2

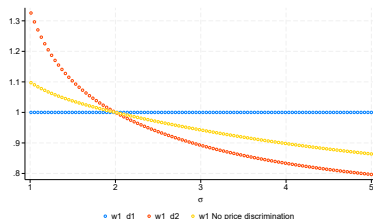


(l) Consumer 1 surplus

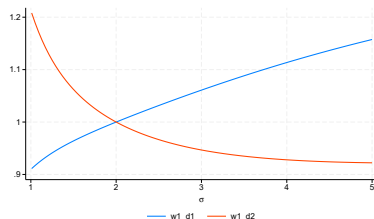


(m) Consumer 2 surplus

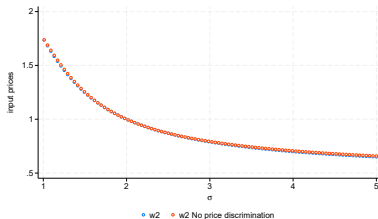
# Variant $\sigma$ prices [Go back](#)



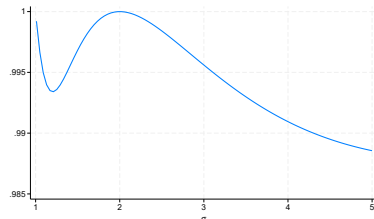
(n)  $w1$  level



(o)  $w1$  ratio: Price disc./ no disc.



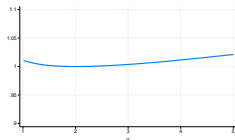
(p)  $w2$  level



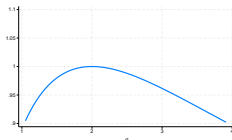
(q)  $w2$  ratio: Price disc./ no disc.

# Variant $\sigma$ welfare components ratio: Price disc./ no disc.

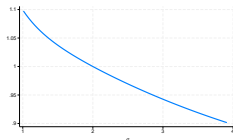
► Go back



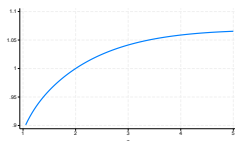
(r)  $\pi$  Upstream 1



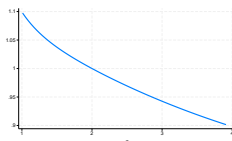
(s)  $\pi$  Upstream 2



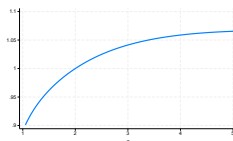
(t)  $\pi$  Downstream 1



(u)  $\pi$  Downstream 2



(v) Consumer 1 surplus



(w) Consumer 2 surplus