



Building trustworthy ML

The role of label quality and availability

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Introduction

Aspect 1: Trustworthiness of ML Algorithms

An overloaded term

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Fairness

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Fairness



Whether Machine Learning Algorithms
have disproportionately worse impact
on some groups of people than others

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An overloaded term

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Privacy

The New York Times

A.I. Could Worsen Health Disparities

In a health system riddled with inequity, we risk making dangerous biases automated and invisible.

TOM SIMONITE BUSINESS AUG 21, 2017 9:00 AM

Machines Taught by Photos Learn a Sexist View of Women

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Whether Machine Learning algorithms leak *personal* (training) data

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Whether Machine Learning model can generalise to different data distributions



Aspect 1: Trustworthiness of ML Algorithms

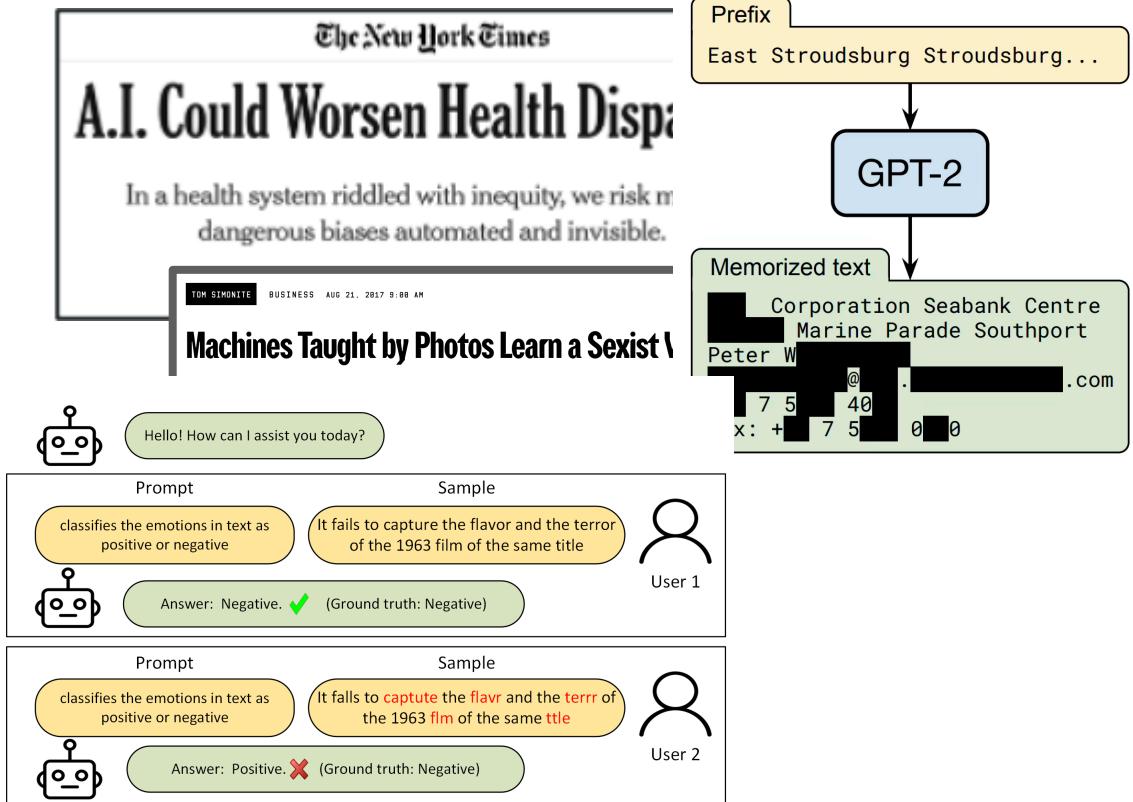
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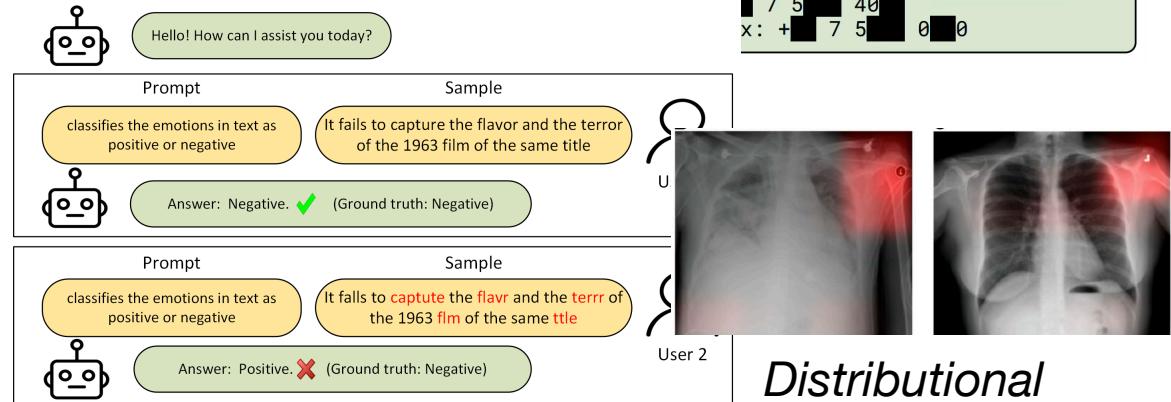
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Adversarial

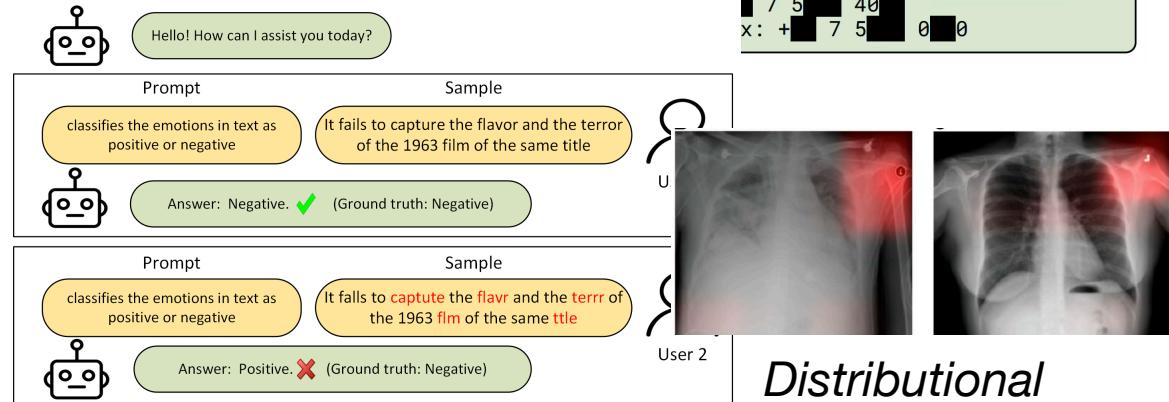
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Distributional

Aspect 2: Label/data quality and availability

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Two problems with data in ML

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Caltech-256 [†]	image	1.54
ImageNet*	image	5.83
QuickDraw [†]	image	10.12
20news	text	1.09
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How **availability and quality of labels** (and data) specifically impact **Fairness, Privacy, and Robustness** of ML Algorithms

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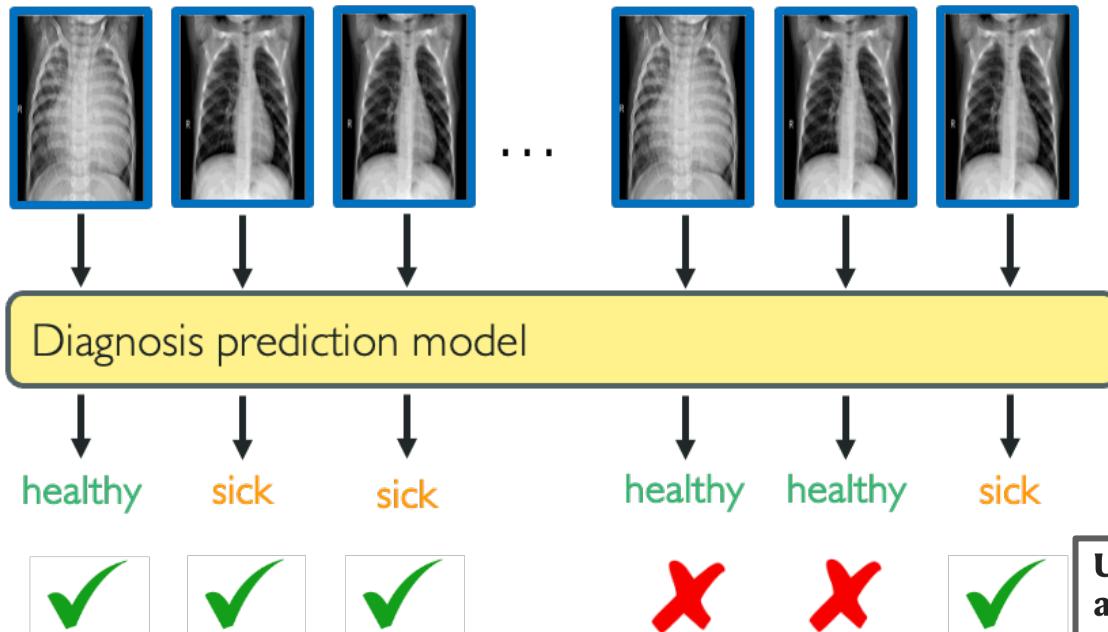
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- Outlook and Future Direction

Fairness in Machine Learning

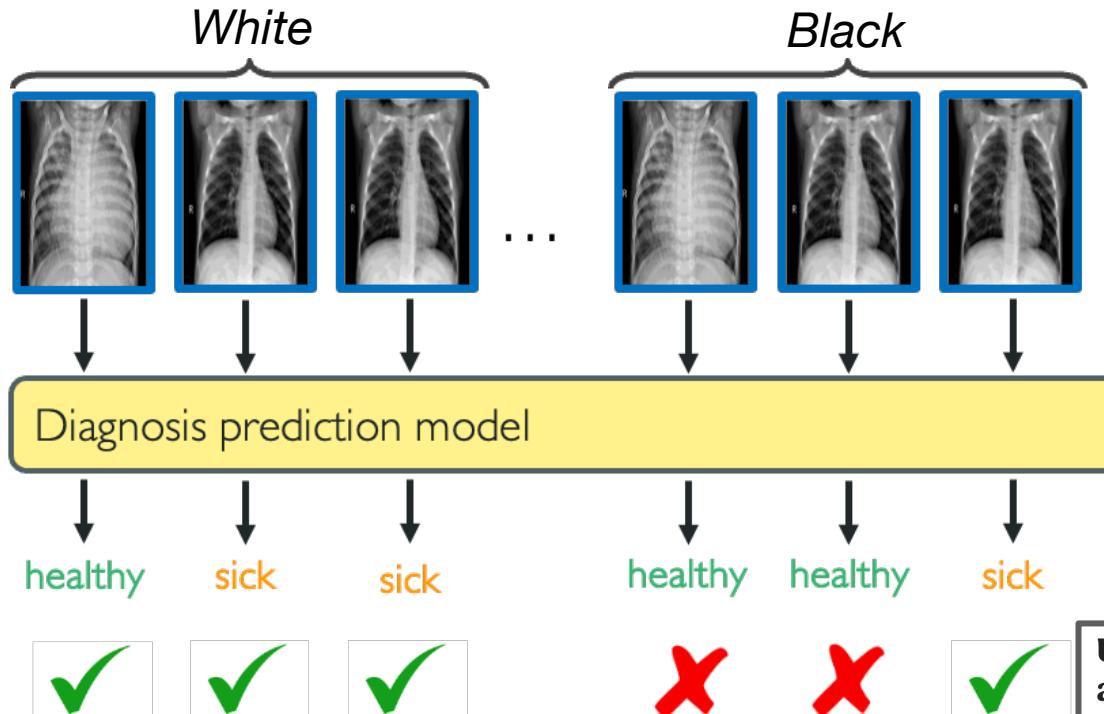
Example of ML model unfairness



Underdiagnosis bias of artificial intelligence algorithms applied to chest radiographs in under-served patient populations

Laleh Seyyed-Kalantari , Haoran Zhang, Matthew B. A. McDermott, Irene Y. Chen & Marzyeh Ghassemi

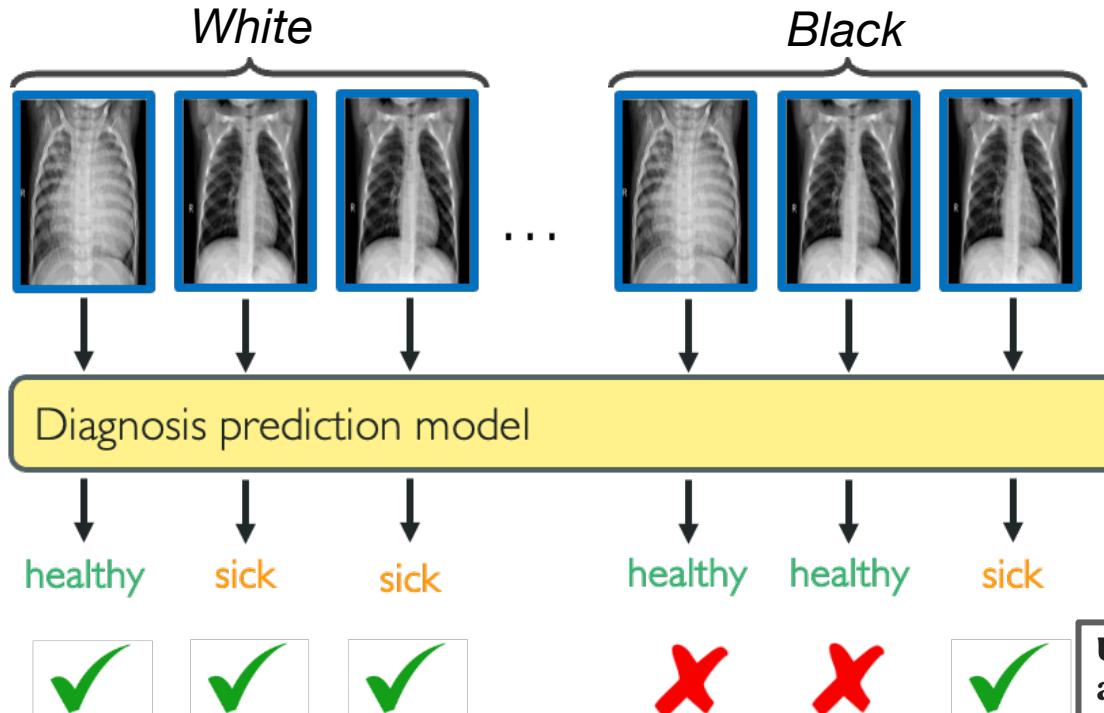
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False positive rate:

$$\text{FPR} = P[\text{predicted healthy} \mid \text{actually sick}]$$

$$\text{FPR}[White] = 0.16$$

$$\text{FPR}[Black] = 0.27$$

$$\text{FPR gap} = 0.11$$

**The model is accurate
but not fair!**

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Prediction problem: $\hat{Y} = \hat{f}(X)$ with categorical or continuous labels

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Fairness Through Awareness

Cynthia Dwork* Moritz Hardt† Toniann Pitassi‡ Omer Reingold§
Richard Zemel¶

'treating similar individuals similarly'

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Group fairness: Three broad categories of fairness notions

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Limitations and Opportunities

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- Equal acceptance rates
e.g. statistical parity

$$\mathbb{P}(\hat{Y}|A = \text{White}) = \mathbb{P}(\hat{Y}|A = \text{Black})$$

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Remark: Different ML problems (e.g. generative ML) employ similar fairness definitions.

Fairness-error trade-off

State-of-the-art prediction models are often unfair

The New York Times

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TOM SIMONITE BUSINESS AUG 21, 2017 9:08 AM

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ON CAMPUS AND AROUND THE WORLD

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These models, which can predict a patient's race, gender, and age, seem to use those traits as shortcuts when making medical diagnoses.

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PRO PUBLICA

Machine Bias

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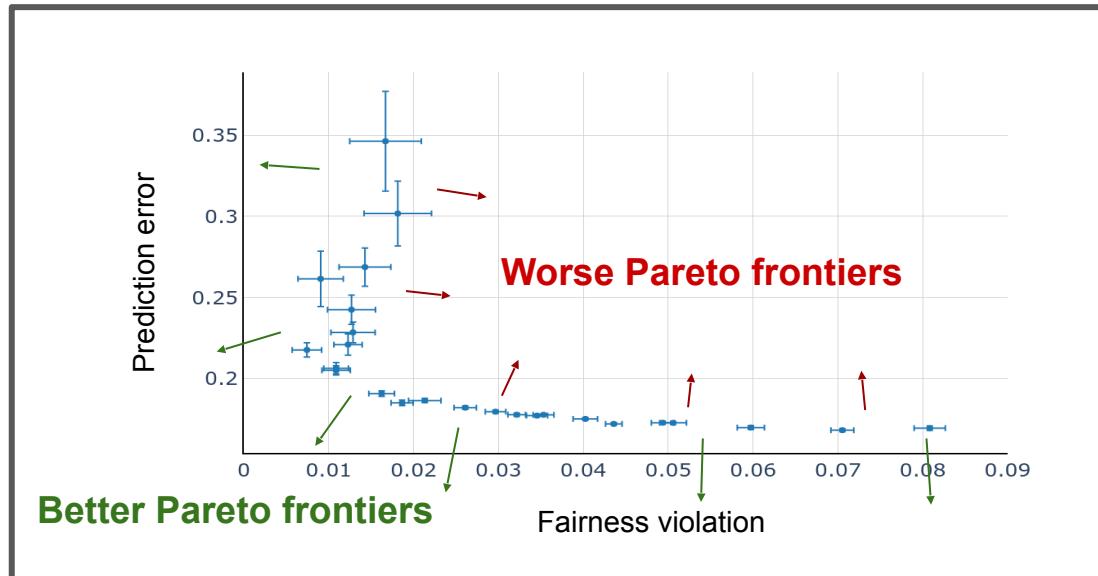
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Trivial prediction models (e.g. random guessing) can achieve perfect fairness
e.g. for binary classification and two groups $P(\hat{Y} = 1|A = 0) = P(\hat{Y} = 1|A = 1) = 0.5$

Fairness-error Pareto frontier



need special mitigation algorithms

Fairness mitigation strategies

$\text{OPT}_{\text{base}} : \arg \min_f \mathcal{L}_{\text{pred}}(f; \mathcal{D}_{\text{pred}}), \quad \mathcal{D}_{\text{pred}} = \{(x_i, y_i)\}_{i=1}^n \sim \mathbb{P}_{XY}$ (potentially unfair model)

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1) Pre-processing mitigations

High-level idea: *Change the training data*

Inspired by principle of “Fairness Through Unawareness”

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Examples:

- feature selection
- fair representation learning
- importance sampling

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Employ ideas from multi-objective learning

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Examples:

- regularized learning
- constrained learning

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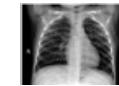
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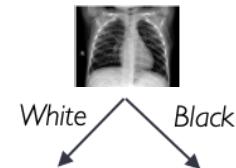
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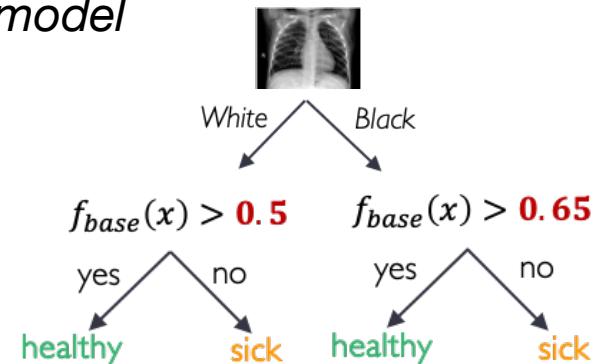
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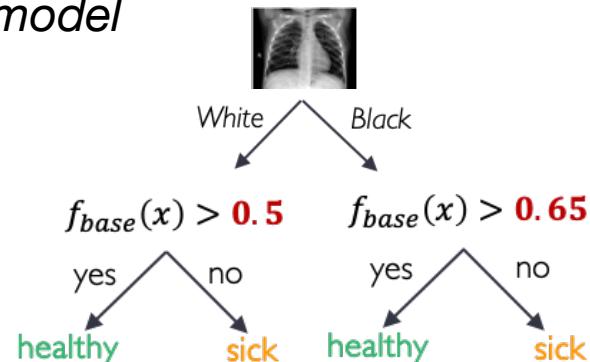
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Examples:

- group-dependent post-hoc transformations
- group-agnostic transformations

e.g. *fair predictions irrespective of person's willingness to provide sensitive attribute*



Challenges faced by fairness mitigations

Pre-, in-, post-processing mitigations need training data with group labels.

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Naive baseline: “predict according to pre-trained model with probability p , and predict 0 with probability $(1-p)$ ”

In-processing mitigation: state-of-the-art MinDiff method



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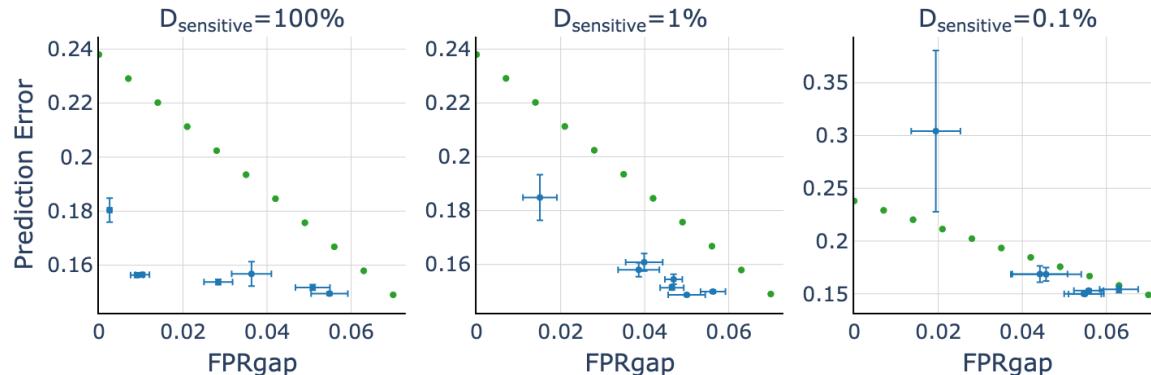
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Y = income; A = gender

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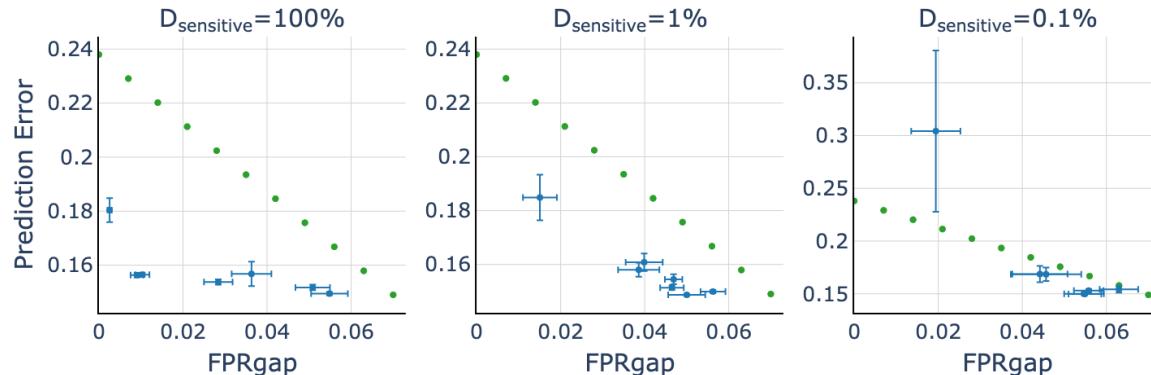
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→ SOTA method as poor as naive baseline

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Y = income; A = gender

Challenges faced by fairness mitigations

Labeled data can be expensive to collect.

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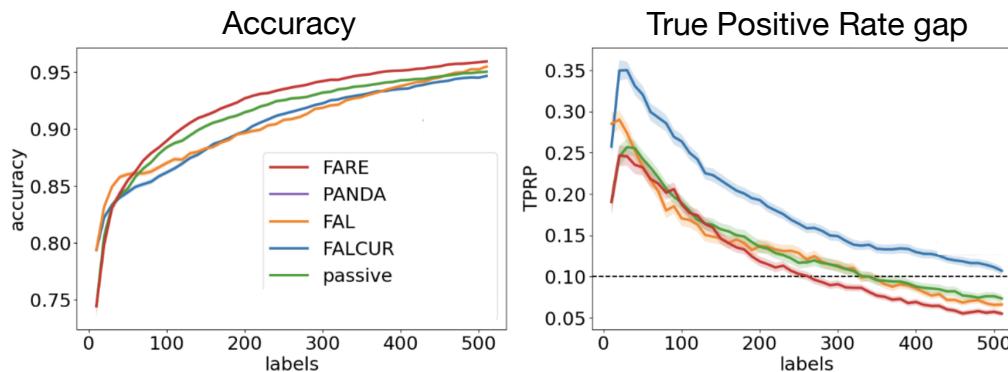
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What happens in the low-label regime?

e.g. fair active learning strategies



Dataset: Communities & Crime

Y = crime rate; A = ethnicity

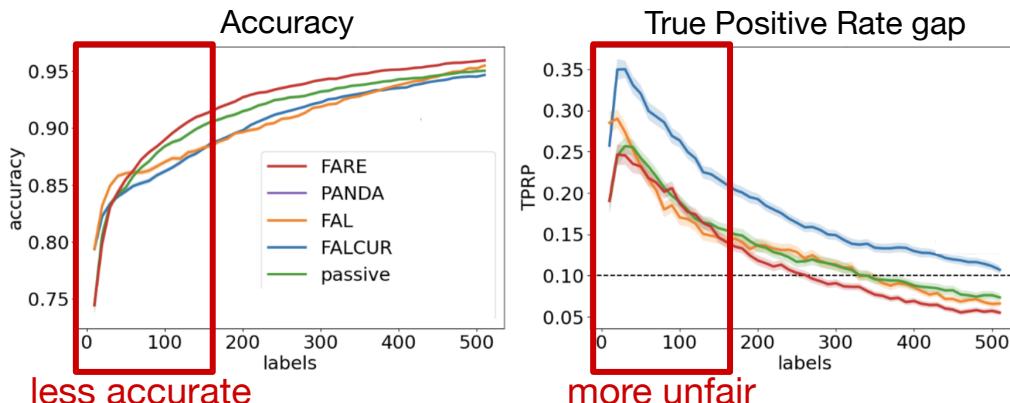
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worse accuracy AND fairness
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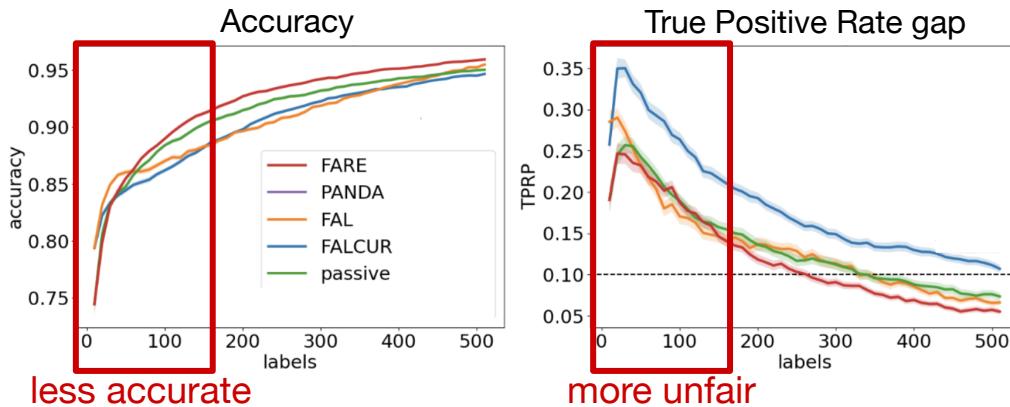
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worse accuracy AND fairness
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intersectional fairness amplifies data scarcity
e.g. avoid discriminating against Hispanic females
aged 30-40

Dataset: Communities & Crime
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Fairness – Outline

Fairness with partial group labels

Fairness with no group labels

Fairness in the low-label regime

Fairness with partial group labels

Problem setting: Fairness with partial group labels

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$\mathcal{D}_{\text{pred}} = \{(X_i, Y_i)\}_{i=1}^n$  **large dataset**
covariates X; class labels Y

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(X, Y) + sensitive attribute A i.e. group label

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Case study: In-processing mitigations with partial group labels

Reminder: $\text{OPT}_{\text{IP}} : \arg \min_f \mathcal{L}_{\text{pred}}(f; \mathcal{D}_{\text{pred}}) + \lambda \mathcal{L}_{\text{fair}}(f; \mathcal{D}_{\text{sensitive}})$

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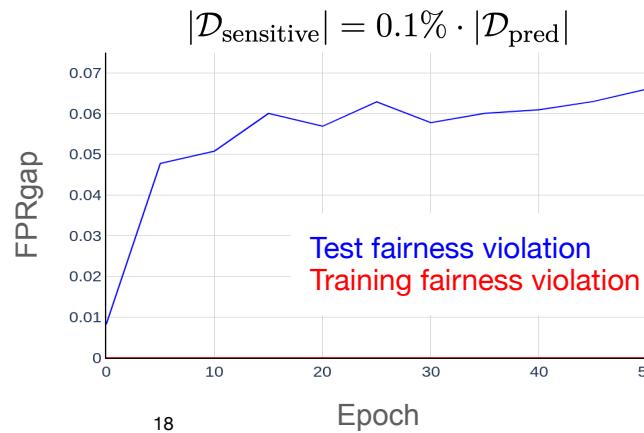
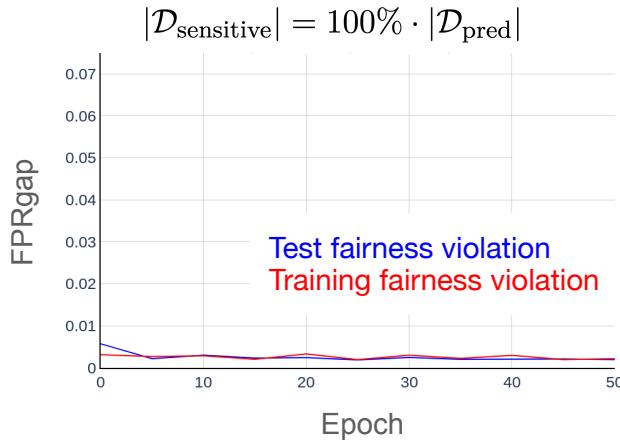
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 **overfitting!**

How to deal with partial group labels?

High level strategies

1. Use proxy for missing sensitive attributes
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Proxy for missing sensitive attributes

Strategies for missing sensitive attributes A

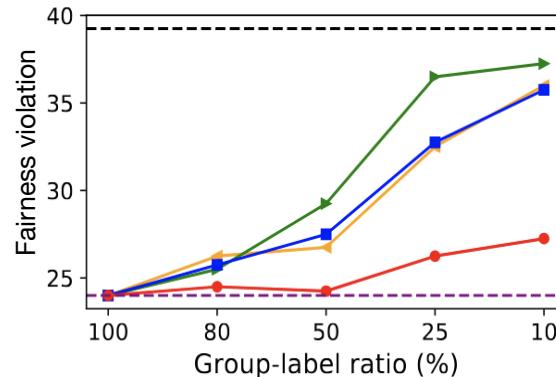
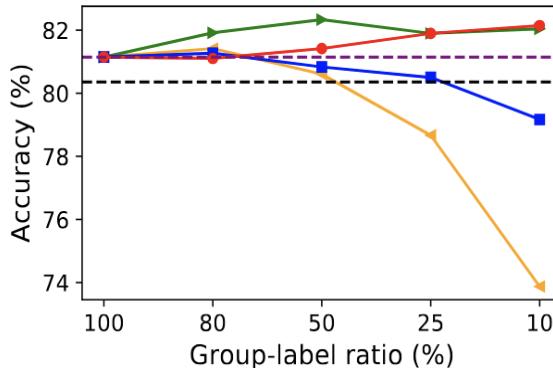
e.g. process data + in-processing fairness mitigation

Learning Fair Classifiers with Partially Annotated Group Labels

Sangwon Jung^{1*} Sanghyuk Chun^{2†} Taesup Moon^{1,3†}

¹ Department of ECE/ASRI, Seoul National University ² NAVER AI Lab

³ Interdisciplinary Program in Artificial Intelligence, Seoul National University



Dataset: UTKFace

Y = age group; A = ethnicity

Proxy for missing sensitive attributes

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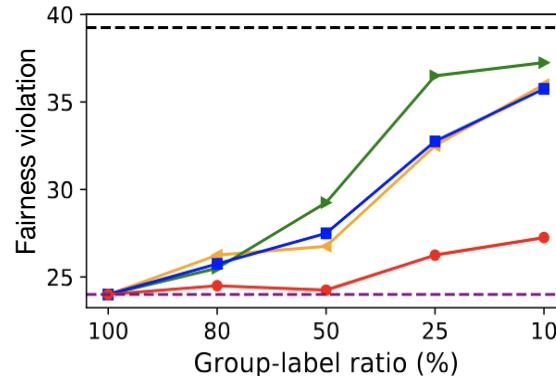
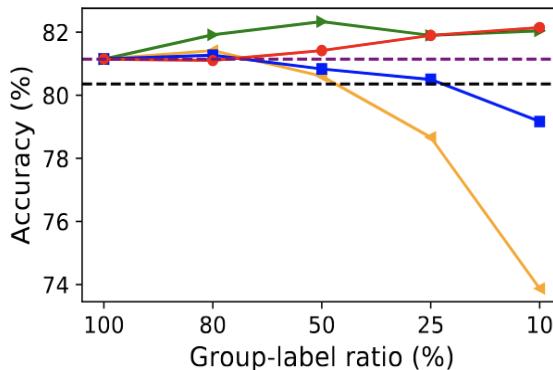
- drop samples with missing A

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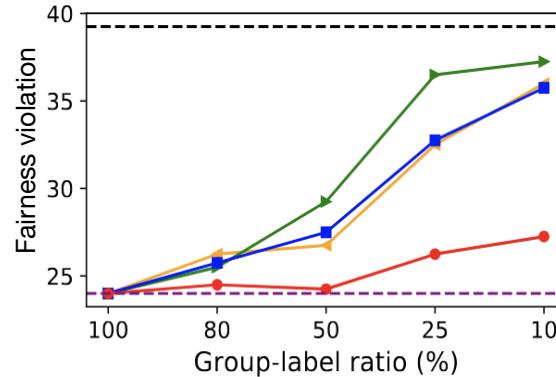
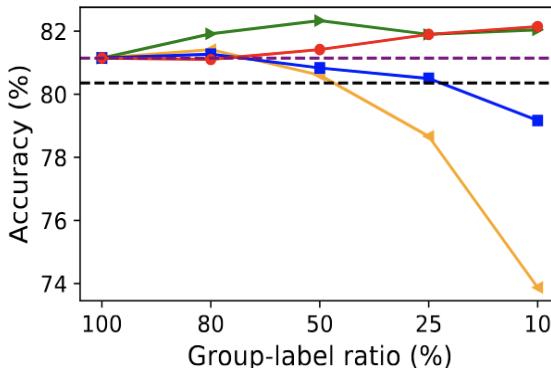
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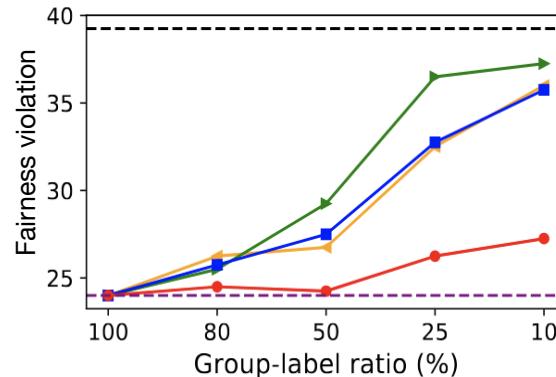
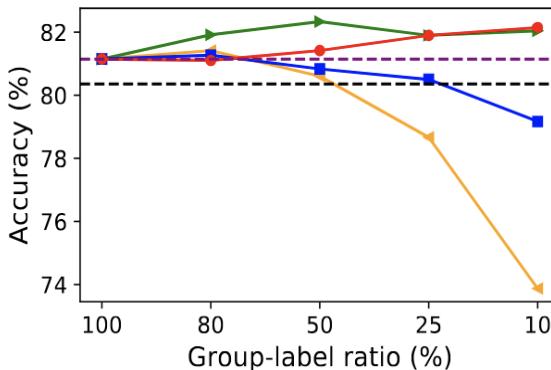
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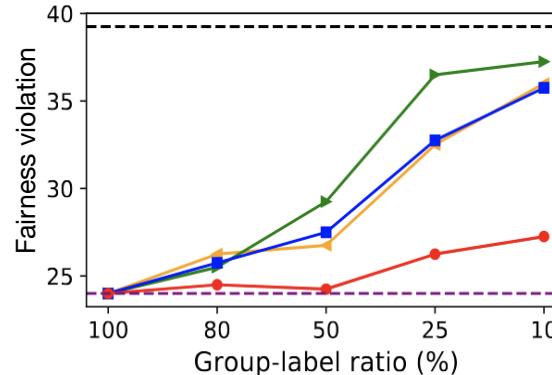
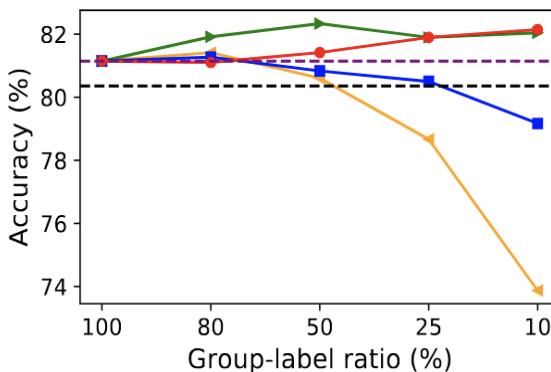
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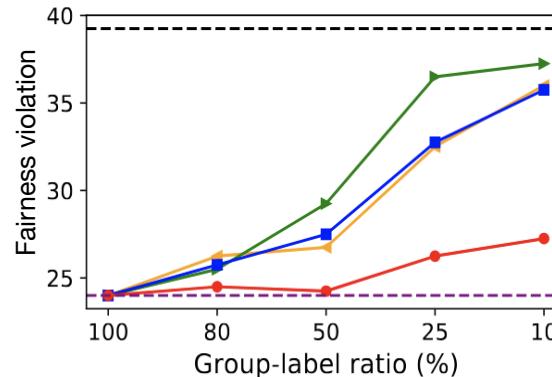
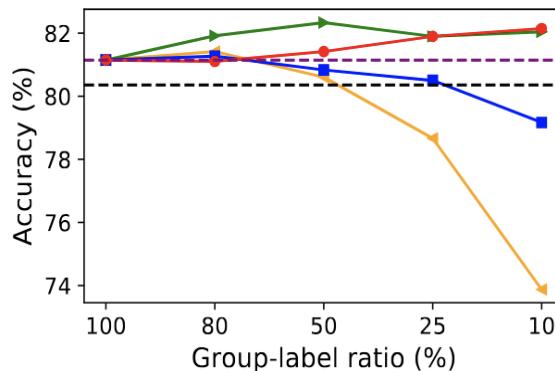
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→ **naive mitigations
are suboptimal**

Dataset: UTKFace

Y = age group; A = ethnicity

High-confidence group pseudo-labels

Predict missing sensitive attributes A:

$$\hat{a} = \begin{cases} \arg \max \hat{f}_A(x) & \hat{f}_A(x) > \tau \\ \text{draw from } P(A|Y=y) & \text{otherwise} \end{cases}$$

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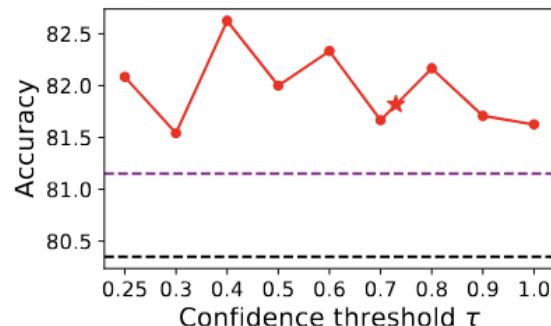
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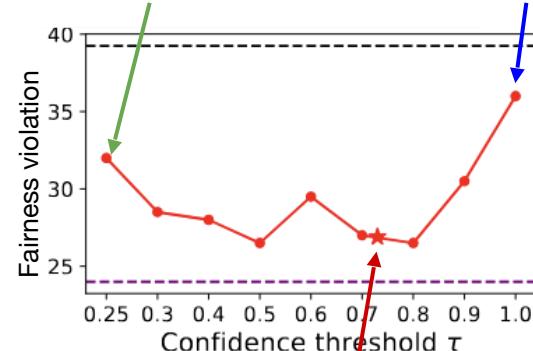
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Use validation set
(with group labels)

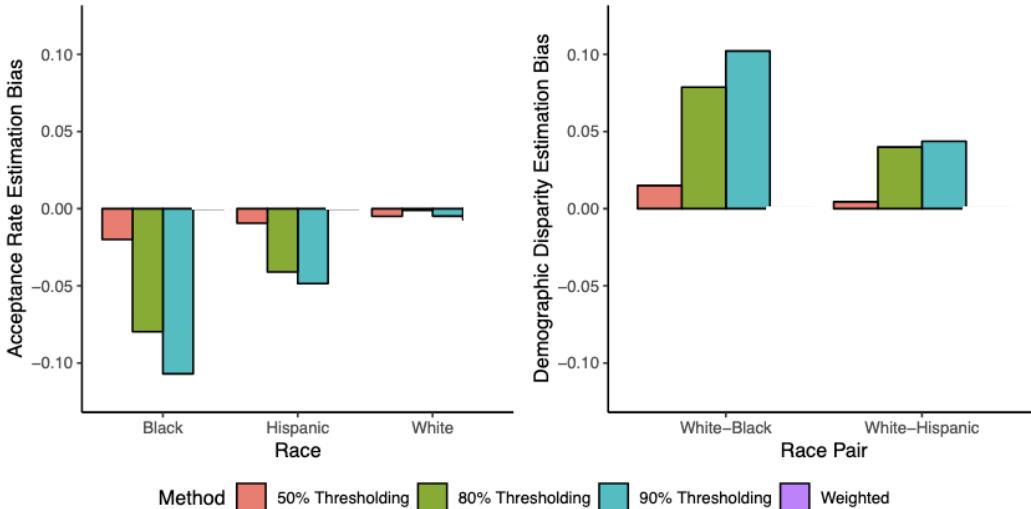


Suboptimal #1:
always impute
random label



Suboptimal #2:
always impute pseudo-
label from \hat{f}_A

Is thresholding confidence an optimal strategy?



Fairness Under Unawareness: Assessing Disparity When Protected Class Is Unobserved

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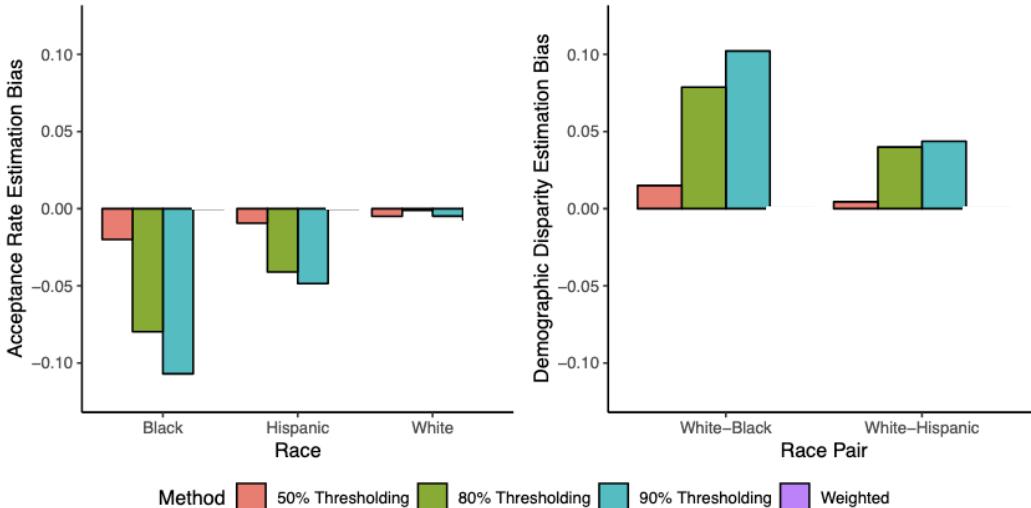
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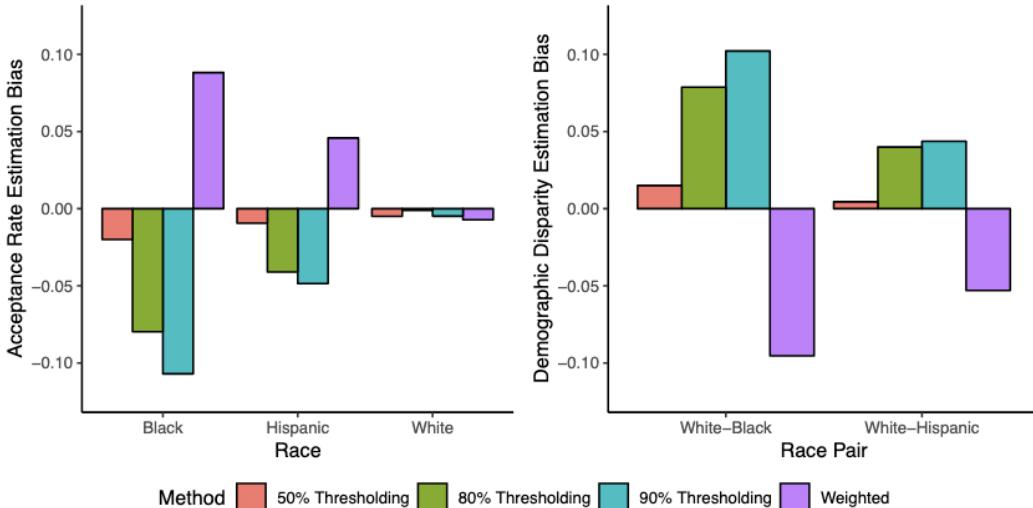
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 thresholding confidence can lead to poor fairness estimation

Dataset: HMDA
Y = 'was loan approved?'
A = ethnicity

Is thresholding confidence an optimal strategy?



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thresholding confidence can lead to poor fairness estimation

Weighted estimator also fails (but differently)

Dataset: HMDA
Y = 'was loan approved?'
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Summary: Using a proxy group label

Effective at mitigating unfairness

as long as sufficient group-labeled validation data is available

e.g. necessary to select hyperparameters like confidence threshold

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Statistically, often easy to predict the sensitive attribute from little data
but it can have ethical concerns and can amplify/hide biases in the data

Fairer machine learning in the real world: Mitigating discrimination without collecting sensitive data

Michael Veale  ¹ and Reuben Binns²

Fairness Under Unawareness:
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Improving Fairness in Machine Learning Systems:
What Do Industry Practitioners Need?

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How to deal with partial group labels?

High level strategies

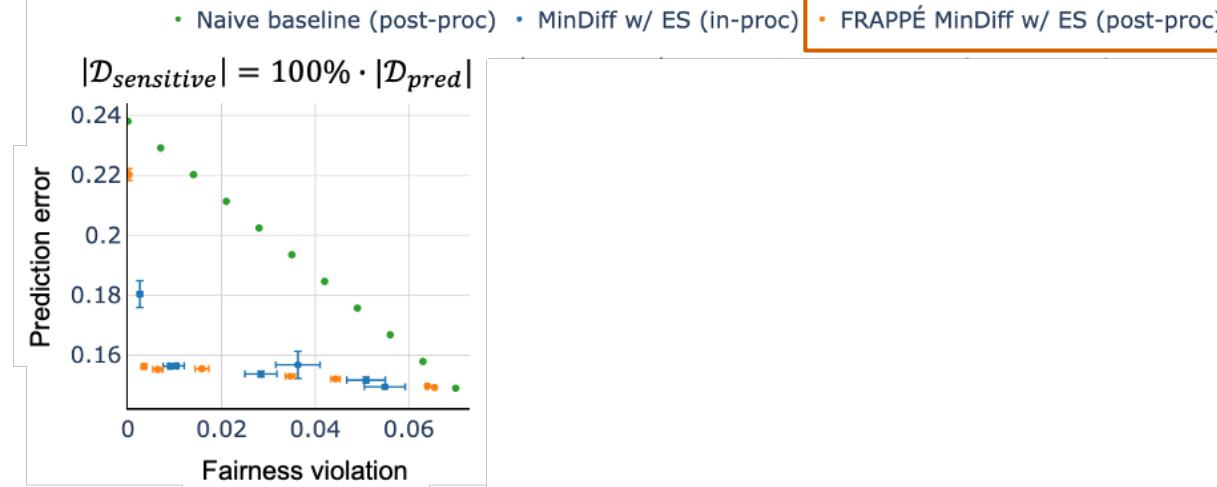
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Modular sample-efficient fairness mitigations

Setup: Equal Opportunity on Adult dataset

Naive baseline: “predict according to f_{base} with probability p , and predict 0 with probability $(1-p)$ ”



FRAPPÉ: A Group Fairness Framework for Post-Processing Everything

Alexandru Tifrea^{*1} Preethi Lahoti² Ben Packer² Yoni Halpern² Ahmad Beirami² Flavien Prost²

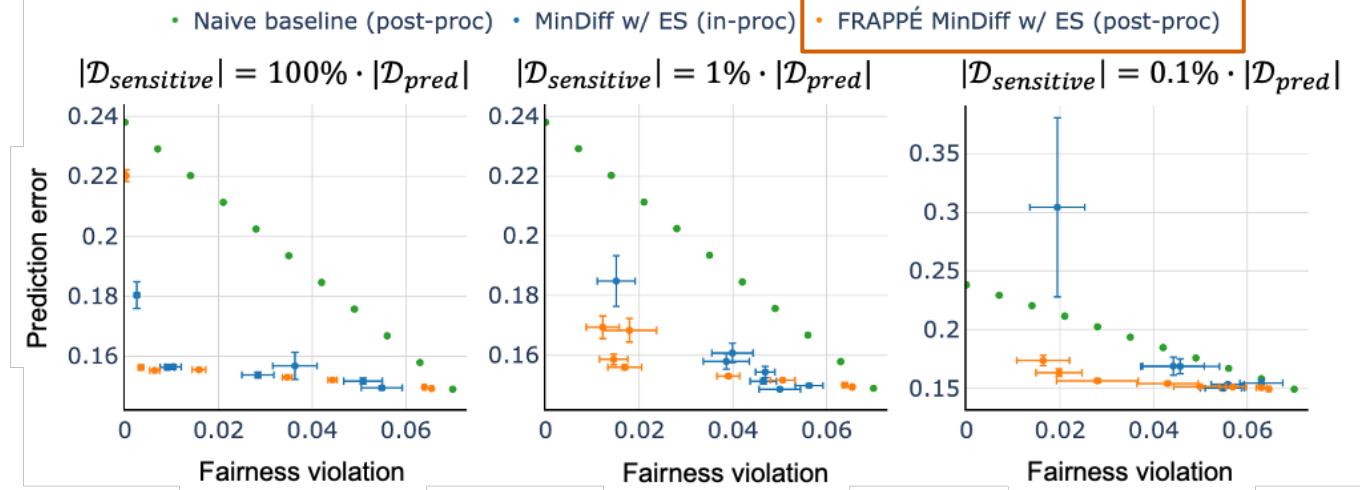
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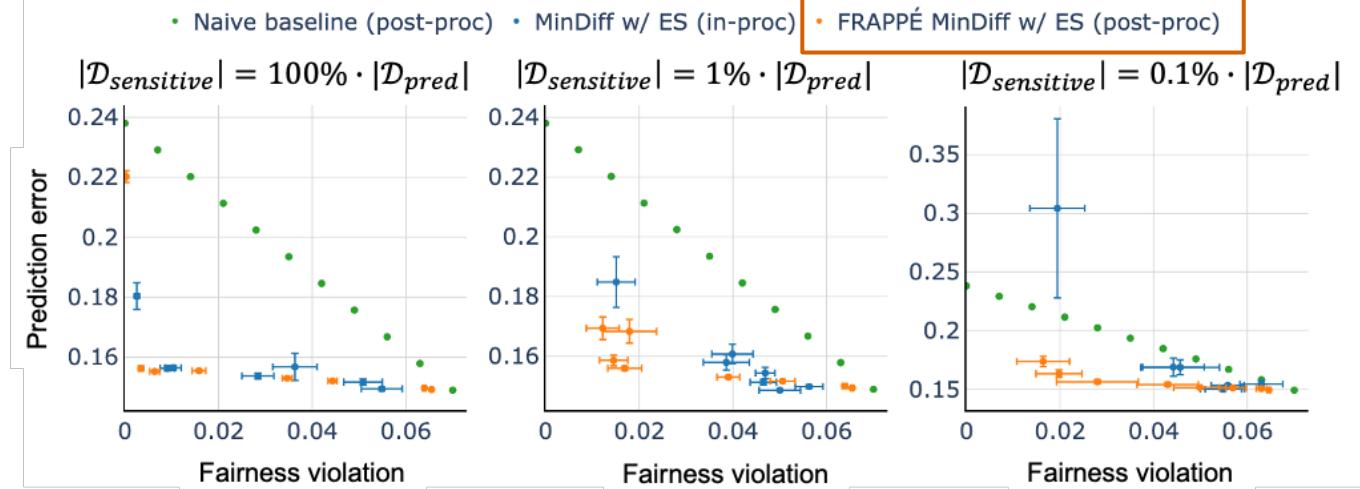
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computation time ~8x faster
than in-processing

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Accurate but unfair model:

$$f_{base} := \operatorname{argmin}_{\mathbf{f}} \mathcal{L}_{pred}(\mathbf{f}; \mathcal{D}_{pred})$$

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any notion of fairness

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related to \mathcal{L}_{pred} e.g. MSE, KL divergence etc

$$\mathcal{D}_{unlab} = \{x_i\}_{i=1}^N$$

unlabeled data

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Instances of modular multi-objective learning

LLM alignment

Asymptotics of Language Model Alignment

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Out-of-domain generalization

OVERPARAMETERISATION AND WORST-CASE GENERALISATION: FRIEND OR FOE?

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Adversarial robustness

Understanding and Mitigating the Tradeoff Between Robustness and Accuracy

Aditi Raghunathan^{*1} Sang Michael Xie^{*1} Fanny Yang² John C. Duchi¹ Percy Liang¹

Unlabeled Data Improves Adversarial Robustness

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Summary: Modular fairness mitigations

More sample efficient than in-processing

iff learning the fairness correction module is statistically efficient

e.g. $T(x)$ is not a complex function, $T(x)$ has low-dimensional structure (e.g. sparsity)

Summary: Modular fairness mitigations

More sample efficient than in-processing

iff learning the fairness correction module is statistically efficient

e.g. $T(x)$ is not a complex function, $T(x)$ has low-dimensional structure (e.g. sparsity)

Effective technique to induce any notion of fairness

iff fairness violations can be measured from observational data

e.g. $T(X)$ implicitly estimates $P(A|X)$ which might unidentifiable from observational data

Assessing Algorithmic Fairness with Unobserved
Protected Class Using Data Combination

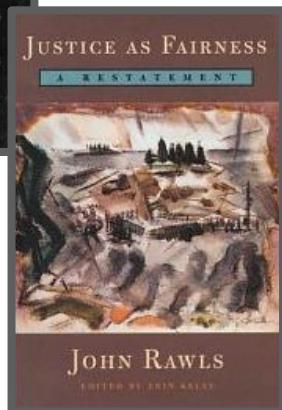
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Fairness with no group labels

Fairness as worst-group performance



Definition A hypothesis h^* satisfies Rawlsian max-min fairness if it maximizes the accuracy of the worst-off group

$$h^* = \arg \max_h \min_{a \in \mathcal{A}} \text{Acc}(h | A = a)$$

Mitigation strategies for worst-group fairness



If we know group labels:

- importance weighting (IW)
- group distributionally robust optimization (GDRO)

DISTRIBUTIONALLY ROBUST NEURAL NETWORKS
FOR GROUP SHIFTS: ON THE IMPORTANCE OF
REGULARIZATION FOR WORST-CASE GENERALIZATION

Shiori Sagawa*
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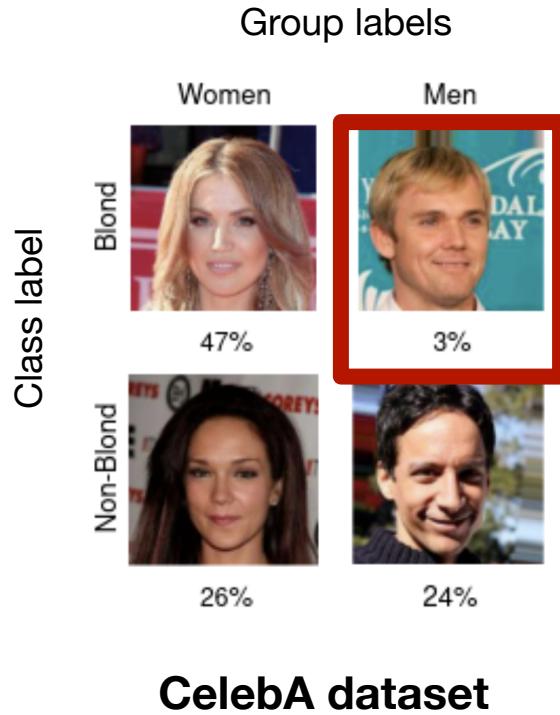
Pang Wei Koh*
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Percy Liang
Stanford University
pliang@cs.stanford.edu

CelebA dataset

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In the absence of group labels:

Two-stage method

- 1) identify worse-off group
- 2) employ e.g. IW/GDRO to improve worst-group error

Fairness via distributionally robust optimization (DRO)

$$\mathcal{R}_{erm}(\theta) := \mathbb{E}_P [\ell(\theta; Z)]$$

Fairness Without Demographics in Repeated Loss Minimization

Tatsunori B. Hashimoto^{1,2} Megha Srivastava¹ Hongseok Namkoong³ Percy Liang¹

Fairness via distributionally robust optimization (DRO)

$$\mathcal{R}_{\text{erm}}(\theta) := \mathbb{E}_P[\ell(\theta; Z)]$$

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determined by

*α_{\min} minority
group proportion*

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worst-case loss wrt the uncertainty set Q

$P = (\text{marginal})$ data distribution

$r = \text{radius of}$ uncertainty set

determined by α_{\min} minority group proportion

What if no group labels available?

A: pick a lower bound for α_{\min}

Detect worst-group using a biased classifier

DRO: upweights high-loss samples.

Alternative: Two-stage method

- 1) use **biased** classifier to identify error set
- 2) train fair classifier via IW / GroupDRO

Detect worst-group using a biased classifier

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Why are two-stage methods expected to work?



Majority group

Intuition: a biased classifier will predict based on the stronger correlation.
e.g. background

Detect worst-group using a biased classifier

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Why are two-stage methods expected to work?



Majority group



Minority group

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e.g. background



incorrect predictions where
spurious correlation does not hold
i.e. minority groups

How to train a biased classifier?

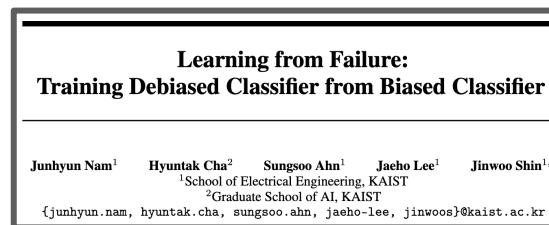
Setting 1: group labels available for validation set

How to train a biased classifier?

Setting 1: group labels available for validation set

Examples:

- heavy regularization
e.g. via early stopping
- custom loss function
e.g. amplify “easy” examples



Use worst-group validation error to select regularization strength, IW weights etc.

How to train a biased classifier?

Setting 2: no group labels at all

How to train a biased classifier?

Setting 2: no group labels at all

Examples:

- identify groups from training AND validation data with ensemble of biased classifiers to reduce noise
- post-hoc logit adjustment using $P(Y|\hat{Y}_{biased})$ as an estimate of $P(Y|A)$

**Boosting worst-group accuracy
without any group annotations**

Vincent Bardenhagen,* Alexandru Tifrea,* Fanny Yang
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**Group Robust Classification
Without Any Group Information**

Christos Tsirigotis*
Université de Montréal, Mila, ServiceNow Research Joao Monteiro
ServiceNow Research Pau Rodriguez
Apple MLR

David Vazquez
ServiceNow Research Aaron Courville†
Université de Montréal, Mila, CIFAR CAI Chair

How to train a biased classifier?

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		Corrupt-MNIST		Waterbirds		CelebA		Color MNIST		Adult		Poverty	
Tuning		Avg	Wg	Avg	Wg	Avg	Wg	Avg	Wg	Avg	Wg	Avg	Wg
No group labels	ERM	99.6	71.2	97.9	74.9	94.3	60.7	99.8	82.6	80.1	41.6	87.6	55.6
	Ours	99.0	96.5	97.5	78.5	88.0	78.9	99.3	96.6	81.2	68.0	86.3	50.0
Val group labels	ERM WG	99.5	79.8	97.6	86.7	93.1	77.8	99.7	84.4	78.9	61.2	87.7	51.5
	JTT	99.1	91.3	93.3	86.7	88.0	81.1	98.3	94.8	77.8	63.3	64.5	60.5

Similar average and worst-group accuracy for two-stage methods:

- with no group labels
- with validation group labels

DRO mitigations in the presence of outliers

Recall: Two-stage methods

- 1) use biased classifier to identify **error set**
- 2) train fair classifier via IW / GDRO

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The opposite of what robust statistics literature recommends!
e.g. can amplify outliers, noisy samples etc

Can we get both fairness and robustness to outliers?

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Robust Mixture Learning when Outliers Overwhelm Small Groups

Daniil Dmitriev^{1*}, Rares-Darius Buhai^{1*}, Stefan Tiegel¹, Alexander Wolters², Gleb Novikov³, Amartya Sanyal⁴, David Steurer¹, and Fanny Yang¹

Clustering algorithm that is

- applicable even for $|\text{Outliers}| \gg |\text{Minority group}|$
- computationally efficient
- information-theoretically optimal

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Fairness without Demographics through
Adversarially Reweighted Learning

Preethi Lahoti *
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Max Planck Institute for Informatics

Alex Beutel, Jilin Chen, Kang Lee, Flavien Prost,
Nithum Thain, Xuezhi Wang, Ed H. Chi
Google Research

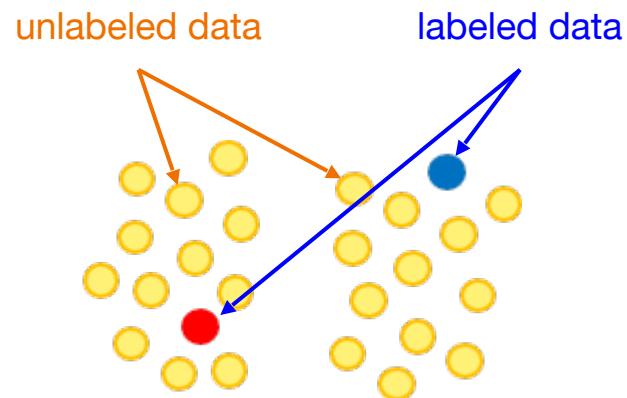
Clustering algorithm that is

- applicable even for $|\text{Outliers}| \gg |\text{Minority group}|$
- computationally efficient
- information-theoretically optimal

Idea: only upweight samples in the error set that are computationally identifiable using simple function class \mathcal{F} .

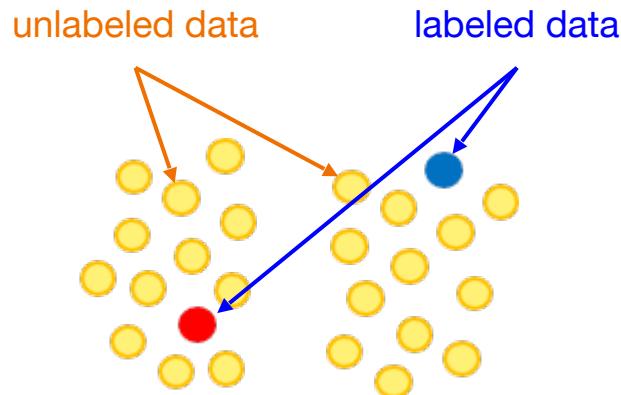
Fairness in the low-label regime

Low-label regime



Low-label regime

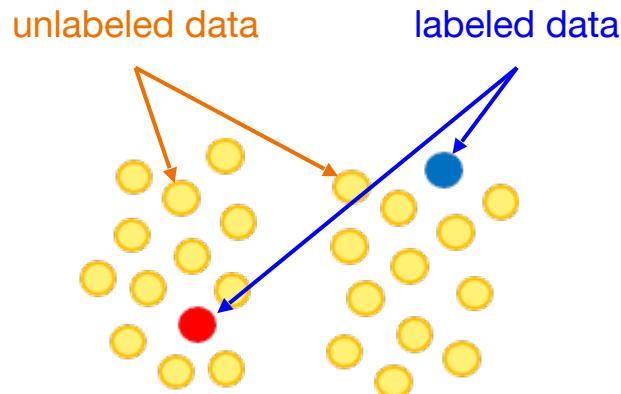
Research questions



- 1) How to acquire the labeled data?
- 2) How to learn from both labeled and unlabeled data?

Low-label regime

Research questions

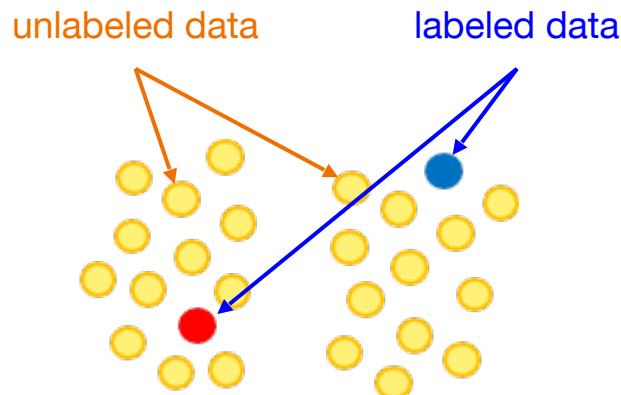


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active learning

Low-label regime

Research questions



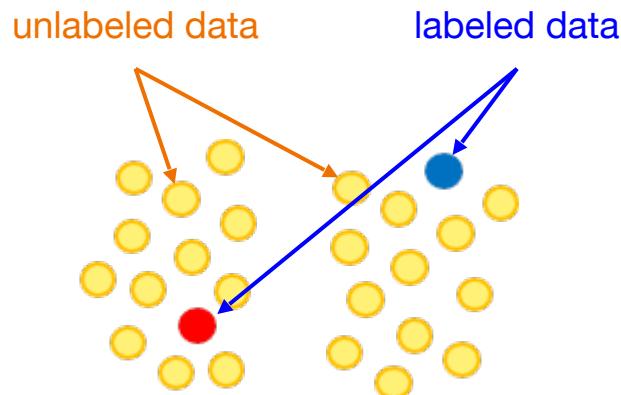
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active learning

**semi-supervised
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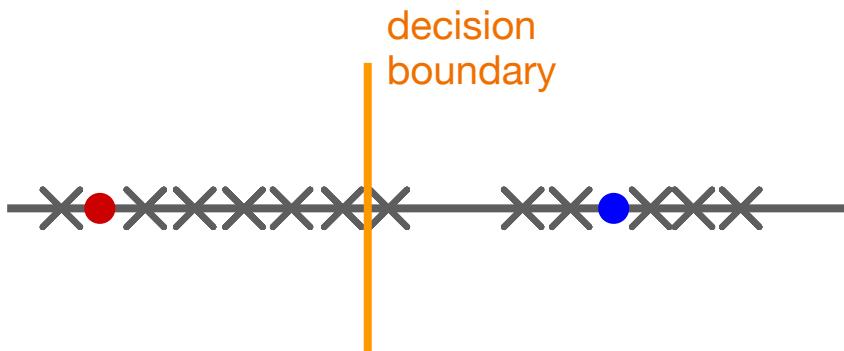
**semi-supervised
learning**

Fairness problems

- class imbalance
- group imbalance
(but potentially balanced classes)

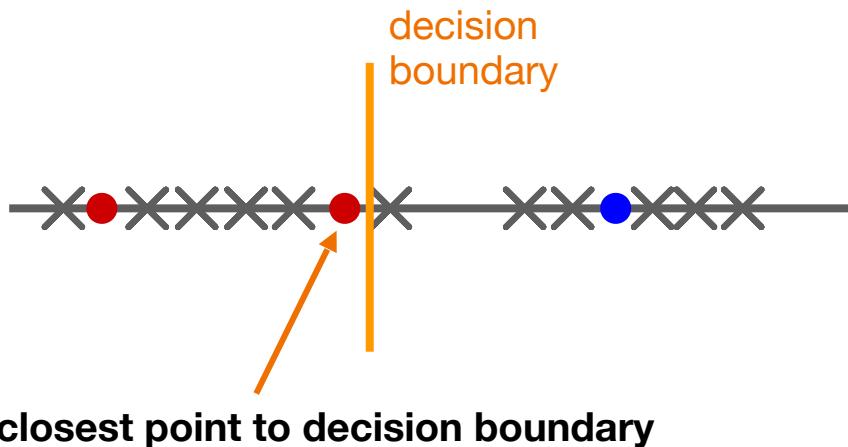
Uncertainty sampling-based active learning

Uncertainty sampling
“binary search to find decision boundary”



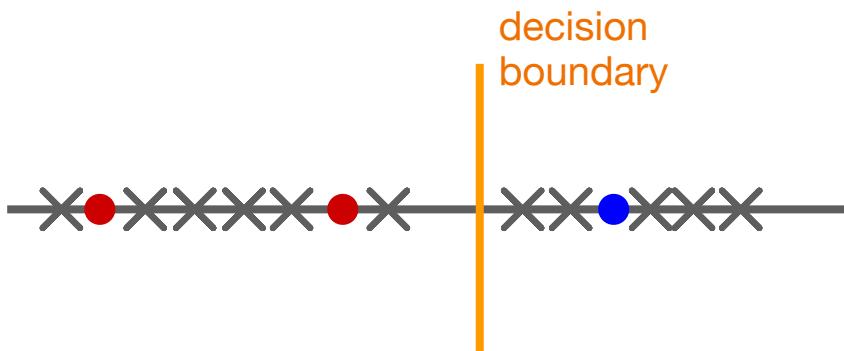
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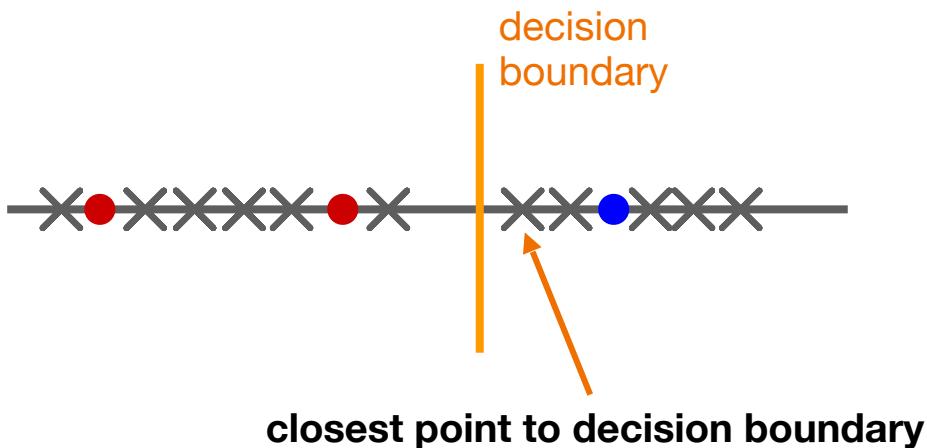
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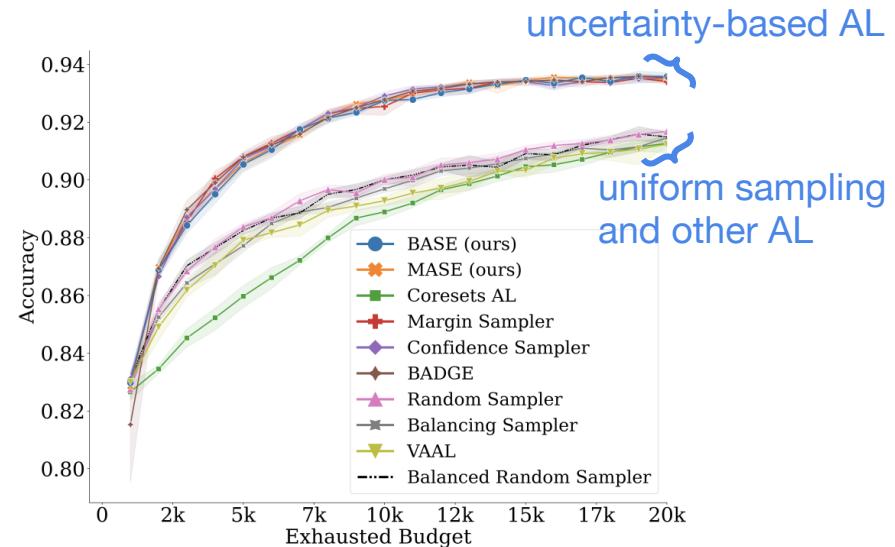
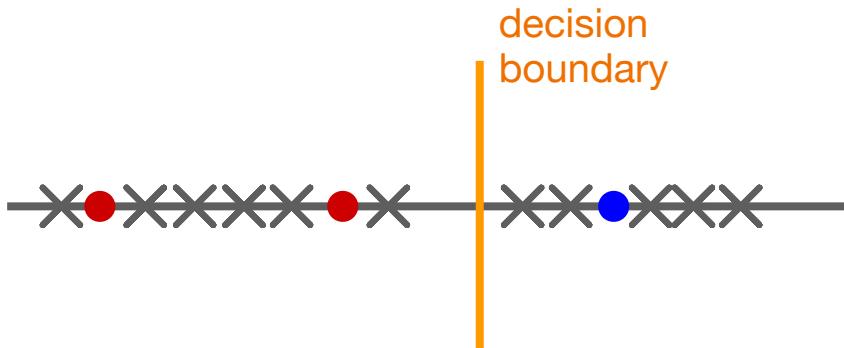
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U-AL is more label efficient than
uniform sampling or other AL

Standard active learning can improve fairness

Class-imbalanced classification

Learning on the Border:
Active Learning in Imbalanced Data Classification

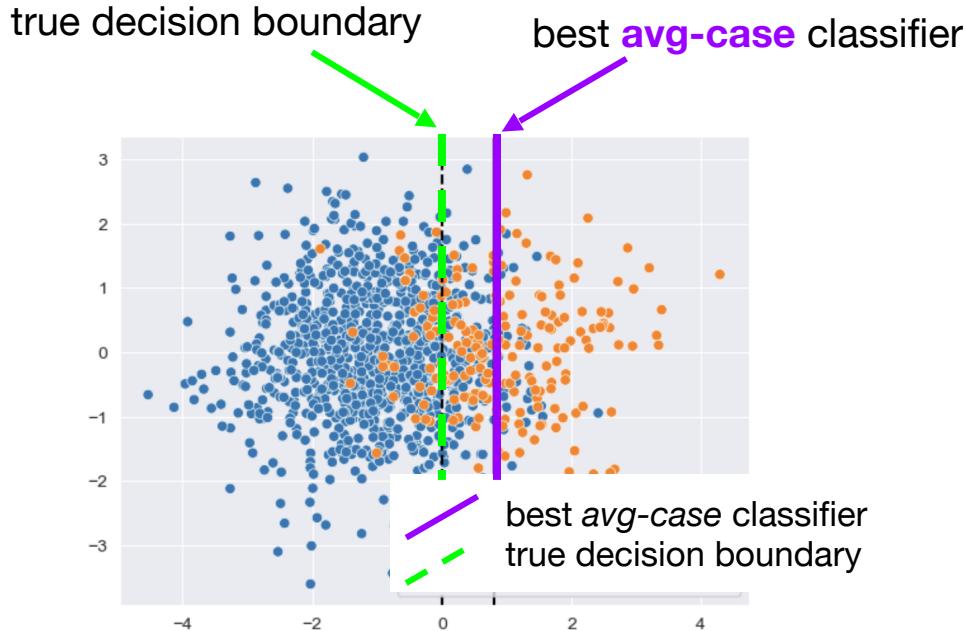
Şeyda Ertekin¹, Jian Huang², Léon Bottou³, C. Lee Giles^{2,1}



Focus on linear classification

Standard active learning can improve fairness

Class-imbalanced classification



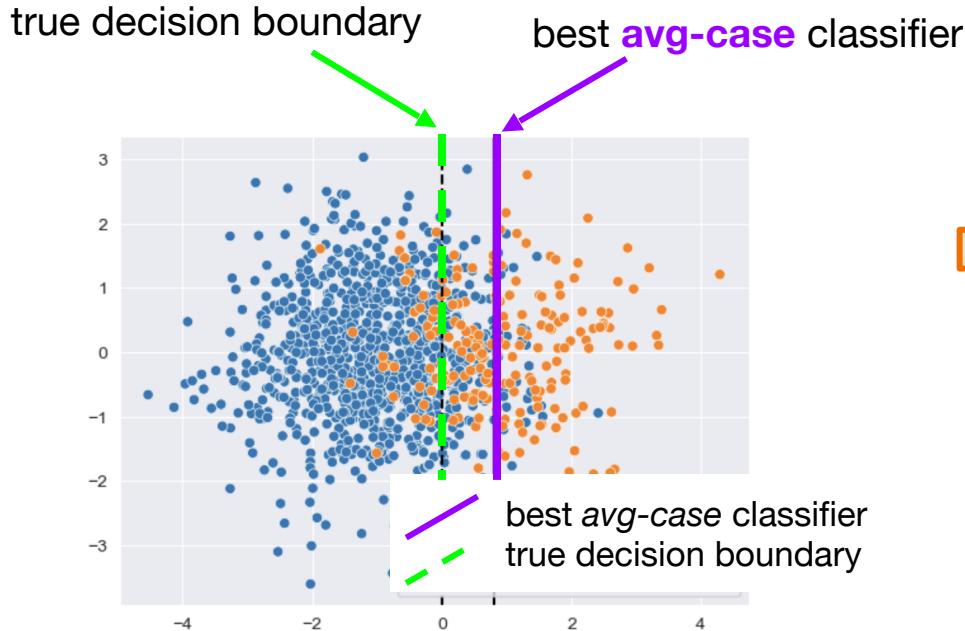
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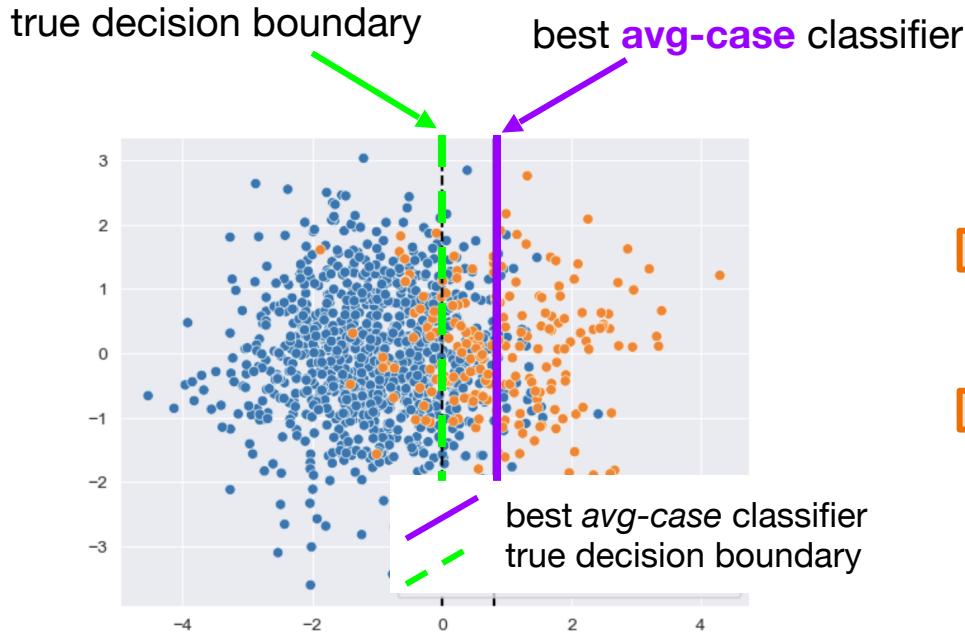
Şeyda Ertekin¹, Jian Huang², Léon Bottou³, C. Lee Giles^{2,1}

Decision boundary of biased classifier is closer to minority class

Focus on linear classification

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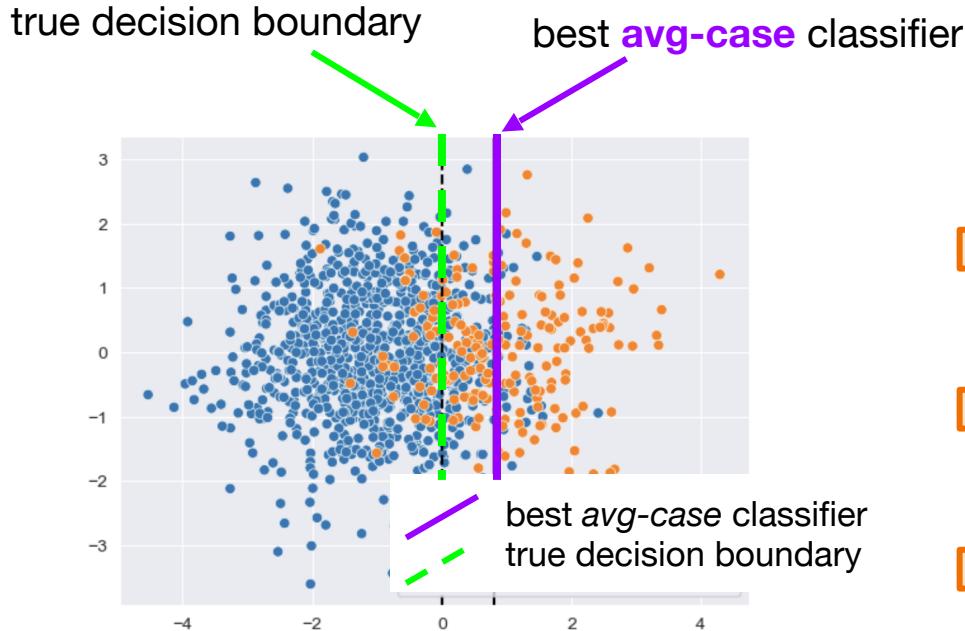
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Active Learning in Imbalanced Data Classification

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- ➡ Decision boundary of biased classifier is closer to minority class
- ➡ U-AL tends to select more minority points to be labeled

Standard active learning can improve fairness

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Active Learning in Imbalanced Data Classification

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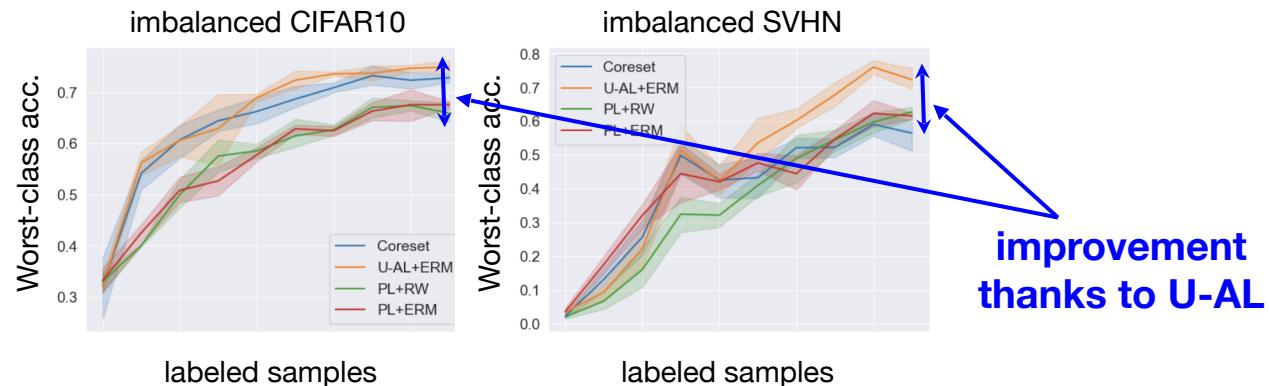
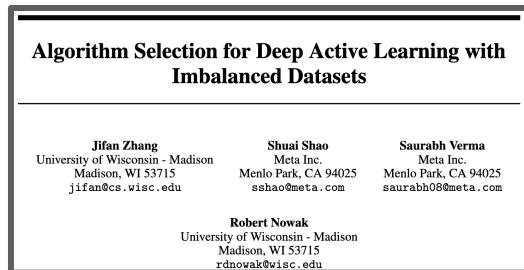
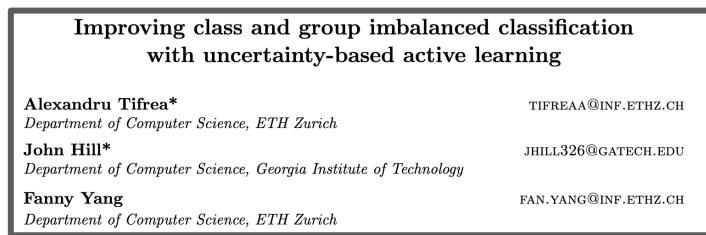
- Decision boundary of biased classifier is closer to minority class
- U-AL tends to select more minority points to be labeled
- U-AL collects a more balanced labeled set

Focus on linear classification

Standard active learning can improve fairness

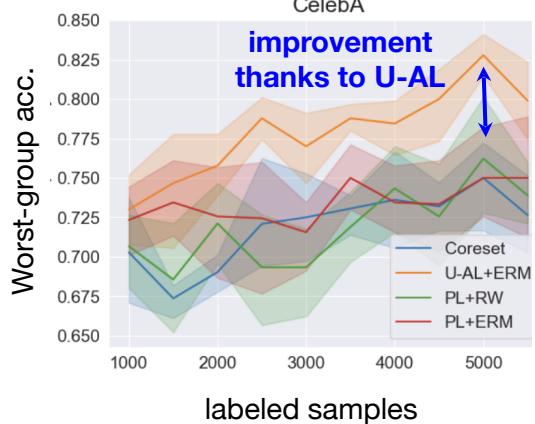
Class-imbalanced classification

U-AL also mitigates class imbalance in non-linear classification!



Standard active learning can improve fairness

Group-imbalanced classification



Improving class and group imbalanced classification
with uncertainty-based active learning

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CAN ACTIVE LEARNING PREEMPTIVELY MITIGATE
FAIRNESS ISSUES?

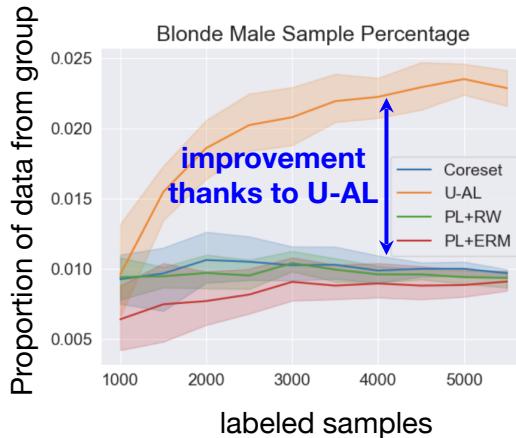
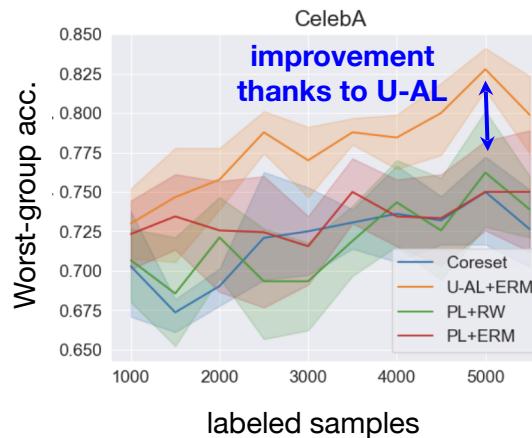
Frédéric Branchaud-Charron*, Parmida Atighehchian*, Pau Rodríguez,
Grace Abuhamad, Alexandre Lacoste

ServiceNow

{fr.branchaud-charron, parmida.atighehchian}@servicenow.com

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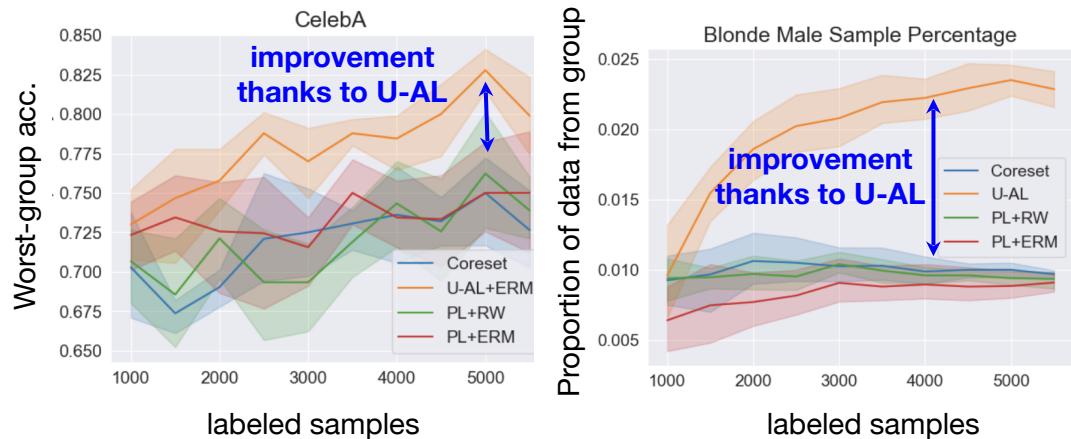
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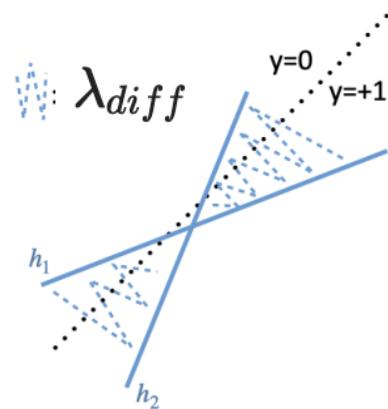
Takeaways

- no explicit group information used anywhere during sampling/learning!
- not *all* AL strategies help (e.g. coresset sampling)
- U-AL+ERM can be better than passive learning + reweighting

Using group labels for active learning

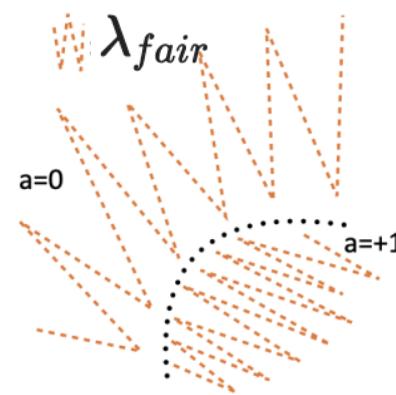
Acquire labels for samples selected according to:

$$P_{AL}(X) \sim \frac{1}{2} \lambda_{diff}(X) + \frac{1}{2} \lambda_{fair}(X)$$



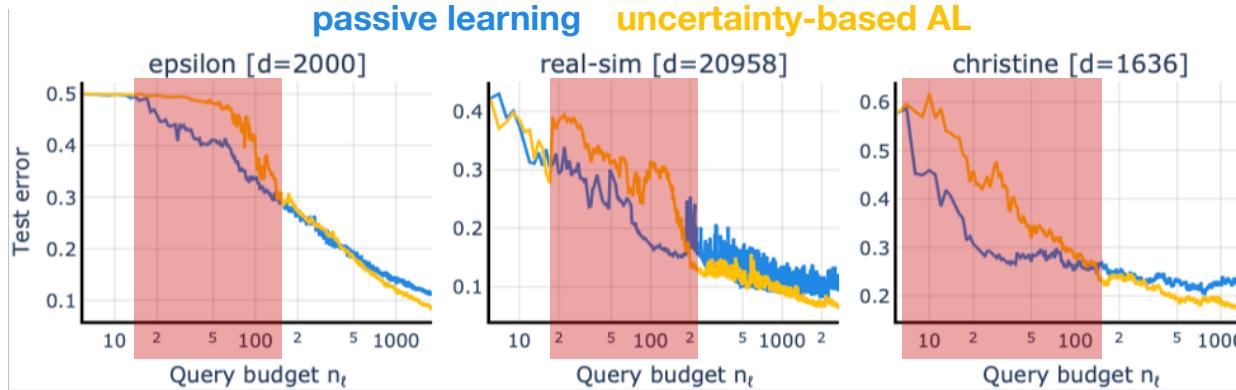
Informativeness criterion:
Disagreement region of ensemble

Fair Active Learning in Low-Data Regimes
Romain Camilleri, Andrew Wagenmaker, Jamie Morgenstern, Lalit Jain, Kevin Jamieson
University of Washington, Seattle, WA
`{camilr,ajwagen,jamiemmt,jamieson}@cs.washington.edu,lalitj@uw.edu`



Fairness criterion:
Uniform mass on all groups

Limitations of uncertainty-based AL



Err[U-AL] > Err[PL]

U-AL can be on par with or even worse than passive learning

- For high-dimensional data
- For data with lots of label noise

Margin-based sampling in high dimensions:
When being active is less efficient than staying passive

Alexandru Tifrea ^{*1} Jacob Clarysse ^{*1} Fanny Yang ¹

On the Relationship between Data Efficiency and Error
for Uncertainty Sampling

Stephen Mussmann ¹ Percy Liang ¹

Summary

A few examples of fair learning algorithms that

- (1) Have fewer data requirements than standard fairness mitigations
- (2) Leverage unlabeled data to improve fairness

Open questions

- Impact of class/group label noise
- Interplay between fairness and other evaluation metrics, beyond accuracy

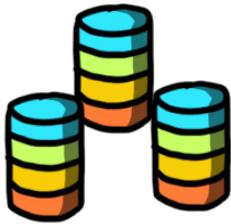


coming up in the next part

Privacy in Machine Learning

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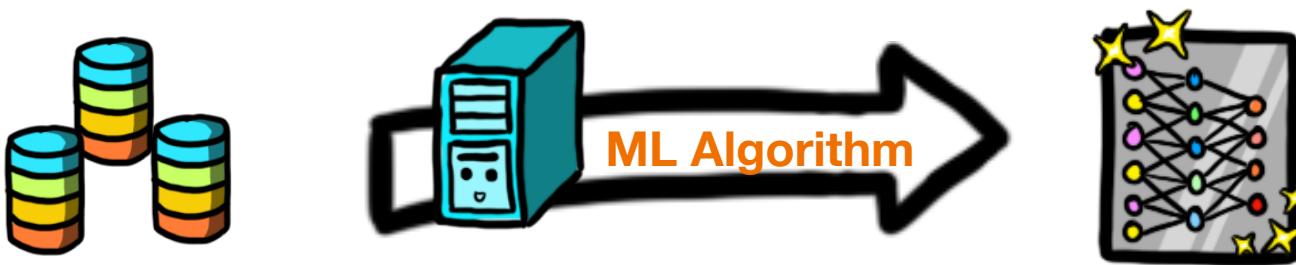
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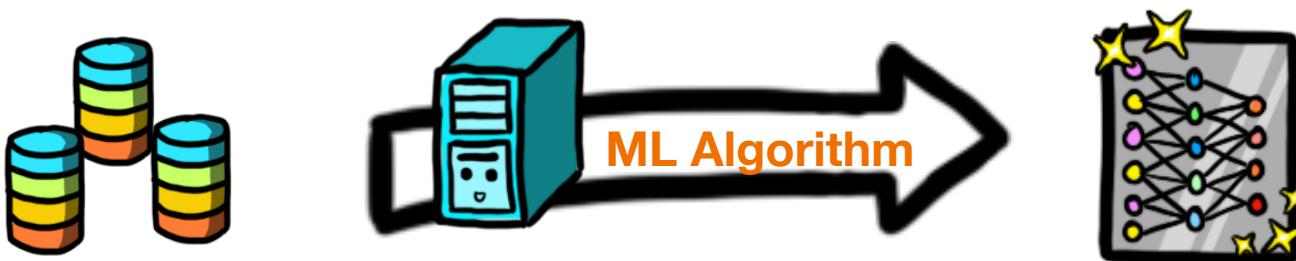
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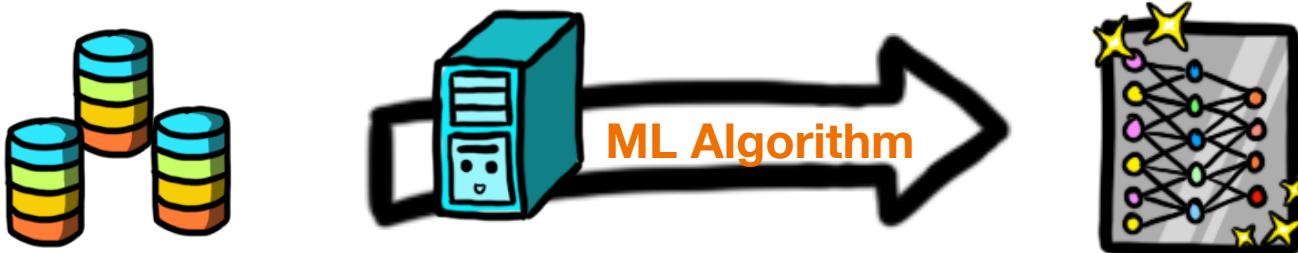


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Privacy can mean a lot of things but two things are important to define:

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Privacy can mean a lot of things but two things are important to define:

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- What can the privacy adversary observe ?

PETs in Machine Learning



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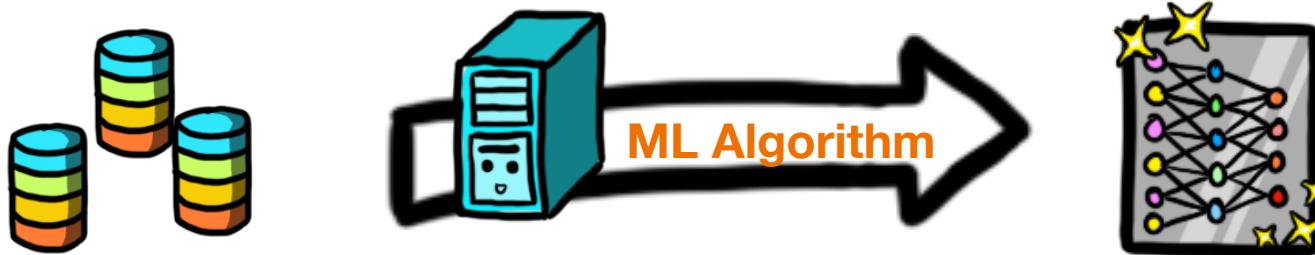
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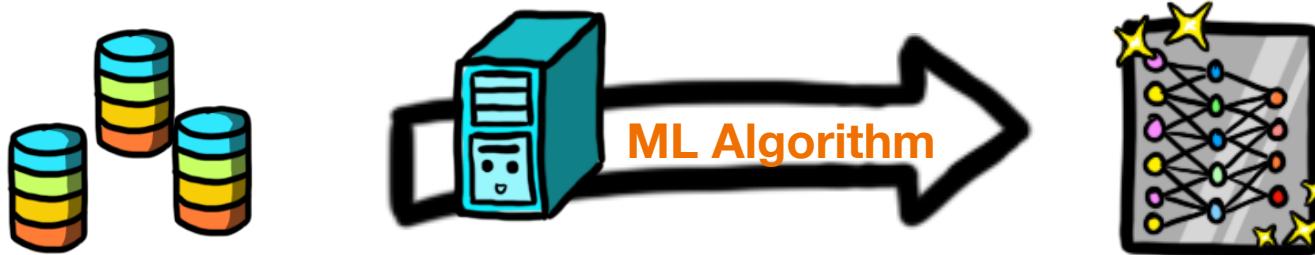
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“Data is a precious thing and will last longer than the systems themselves”

Sir Tim-Berners Lee

US Census and Privacy

Vulnerability of sparse data

WHOSE 2010 CENSUS RESPONSES CAN BE RECONSTRUCTED WITH CERTAINTY?

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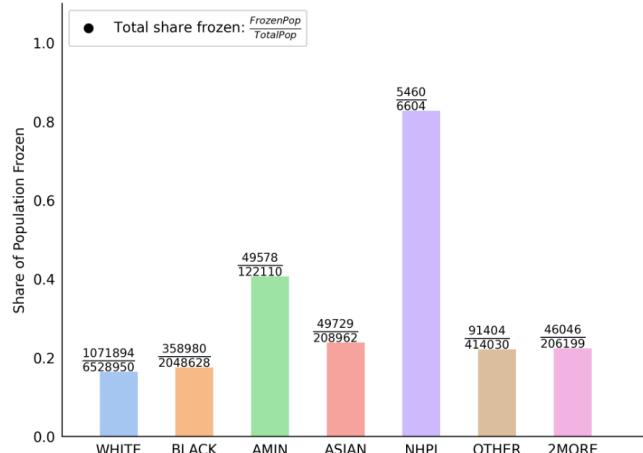
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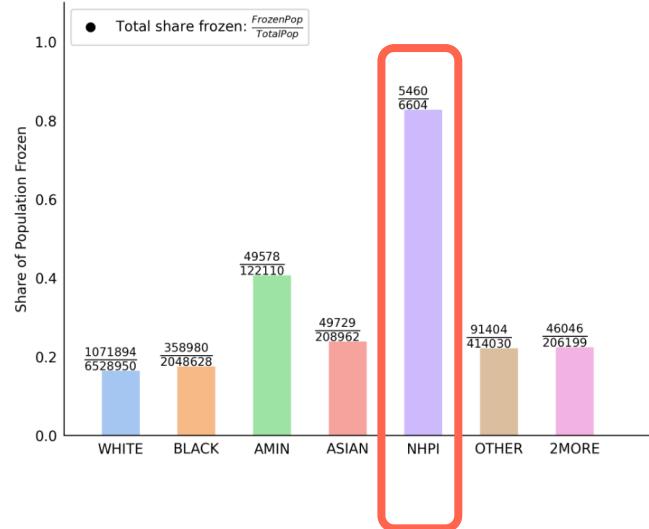
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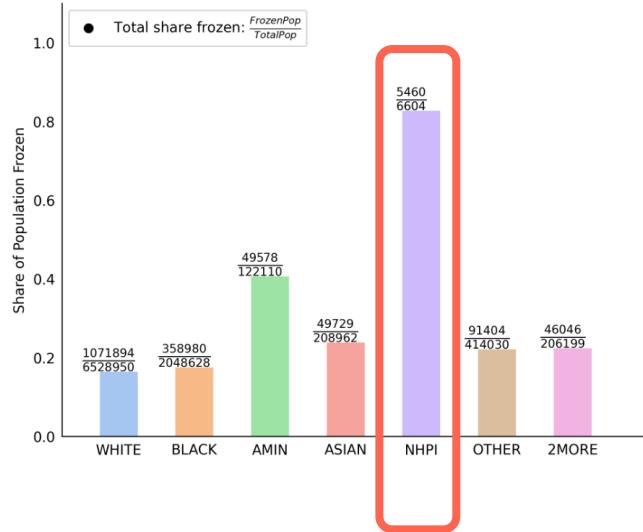
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Takeaway: Often privacy violations are stronger in smaller communities.

Cost of Privacy

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If the original dataset's privacy is to be protected, some accuracy needs to be sacrificed. The study of DP tries to control this trade-off.

Making an Algorithm Differentially Private

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- **Differential Privacy** noises the algorithm's output to limit the exposure of any single data point

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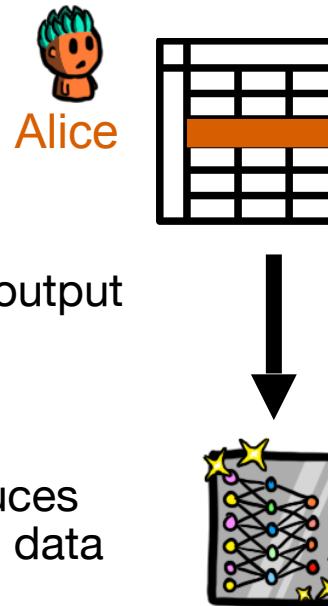
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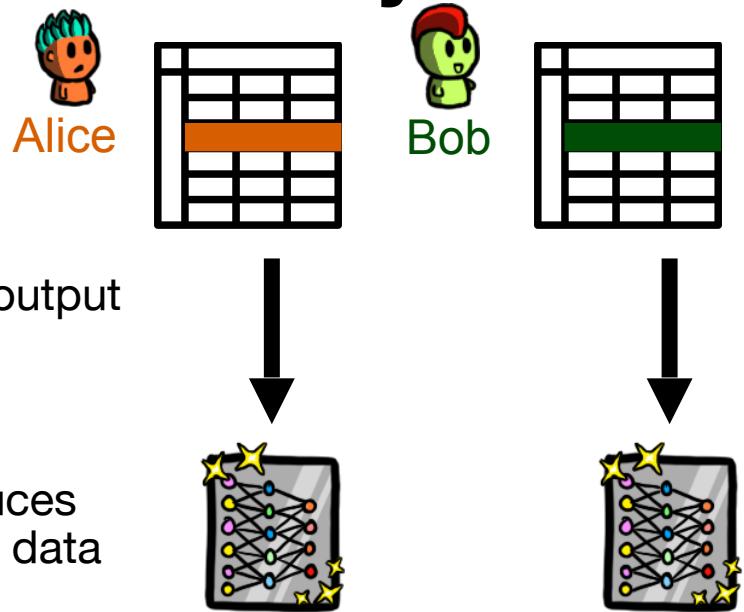
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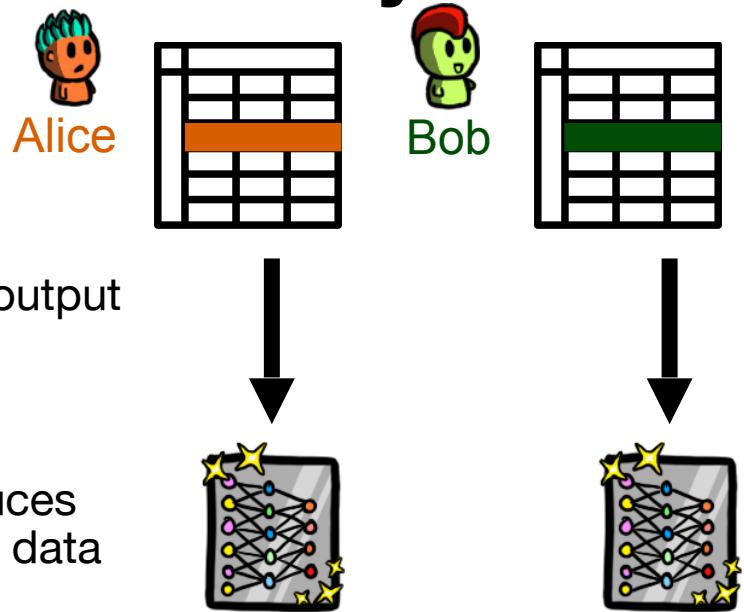
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The replacement of a single data record minimally impacts the trained model

How to make Machine Learning Private

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Differential Privacy (Defn.)

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- Neighbouring datasets S_1 and S_2
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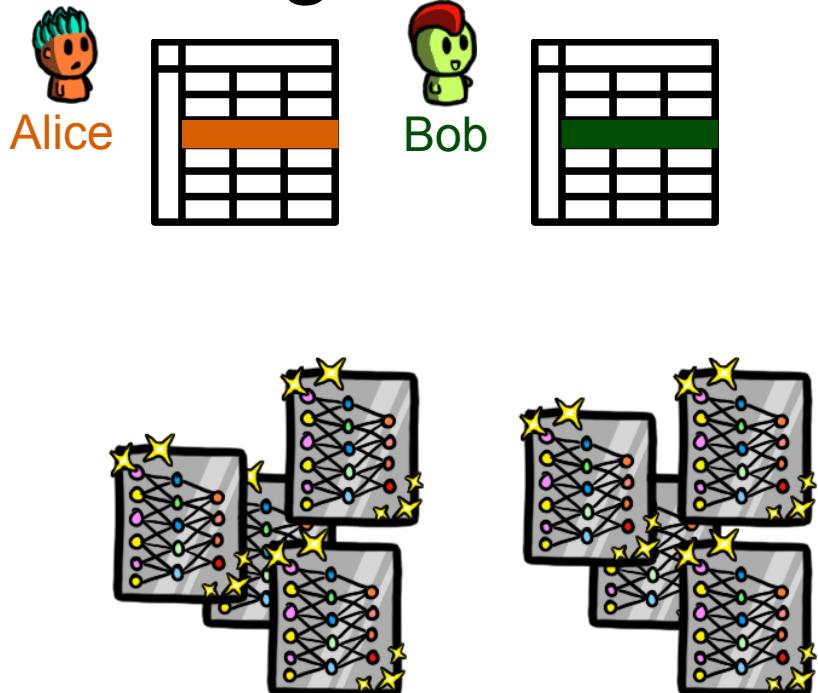
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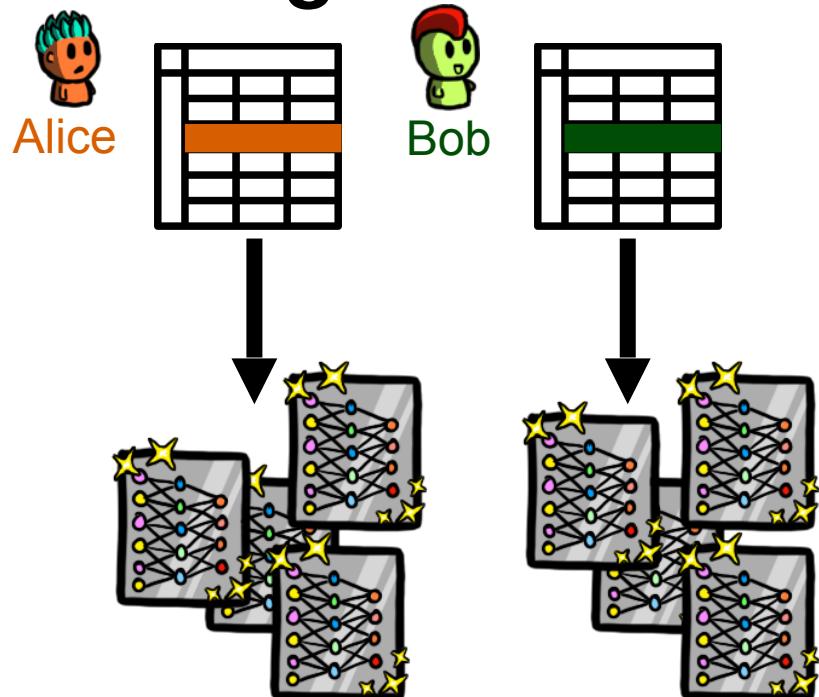
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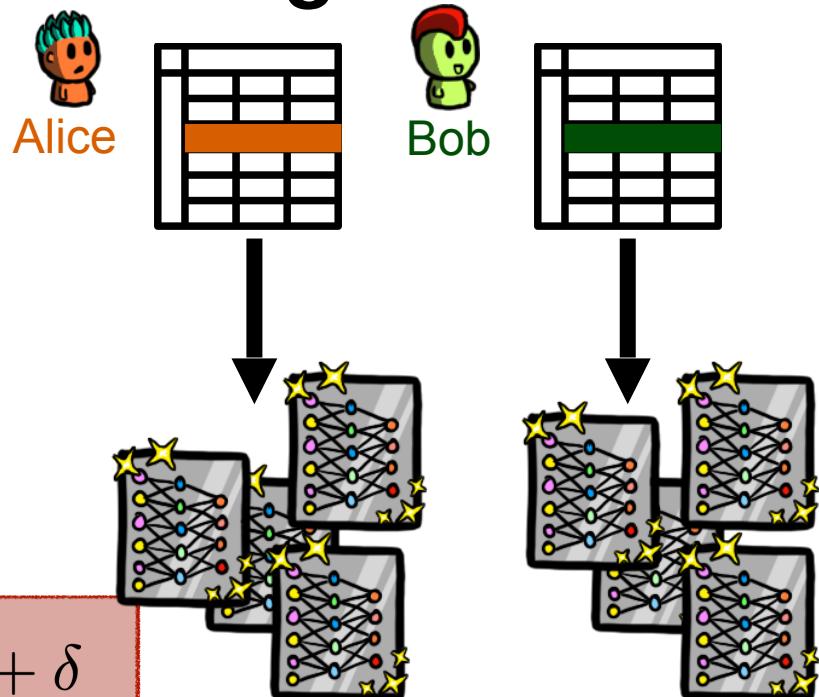
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Today, we will look at two ways in which data quality affects the performance of Differentially Private Algorithms

- *Good data requires less added noise* for the same level of privacy
- Some parts of data domain *incurs disproportionately higher loss* due to the Differential privacy than others

Differential Privacy and Disparate Impact

DP and Disparate Impact Examples in Practice

Publishing Wikipedia usage data with strong privacy guarantees

Temilola Adeleye¹, Skye Berghel², Damien Desfontaines², Michael Hay², Isaac Johnson¹, Cléo Lemoisson¹, Ashwin Machanavajjhala², Tom Magerlein², Gabriele Modena¹, David Pujo², Daniel Simmons-Marengo², and Hal Triedman¹

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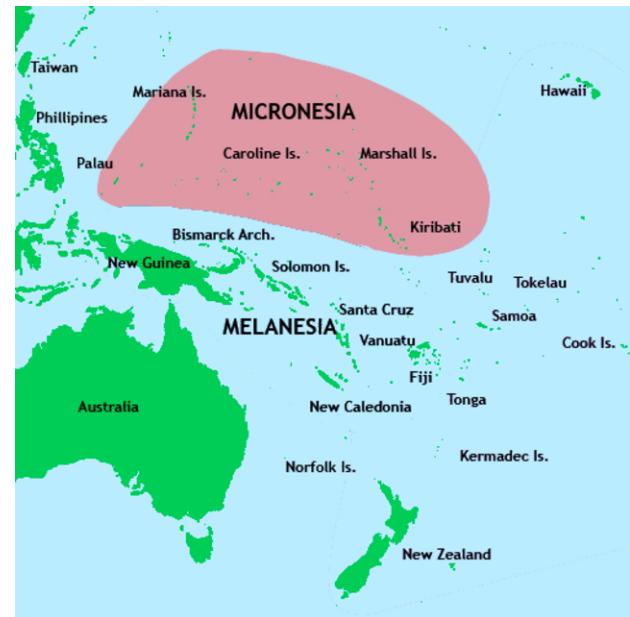
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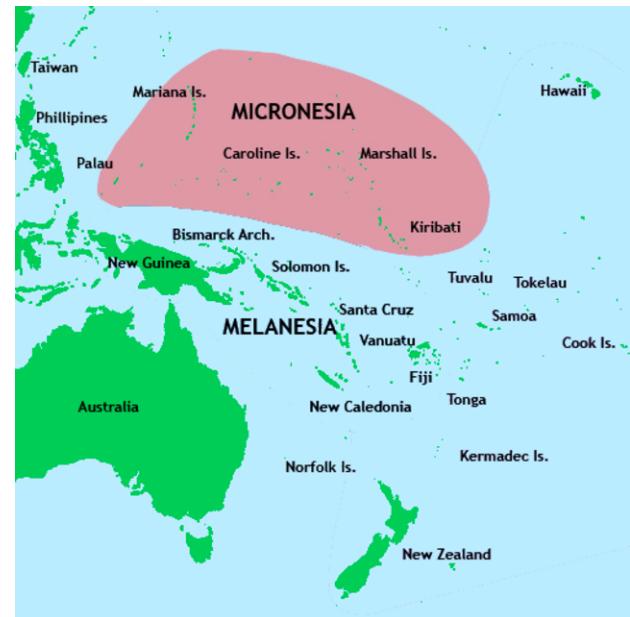
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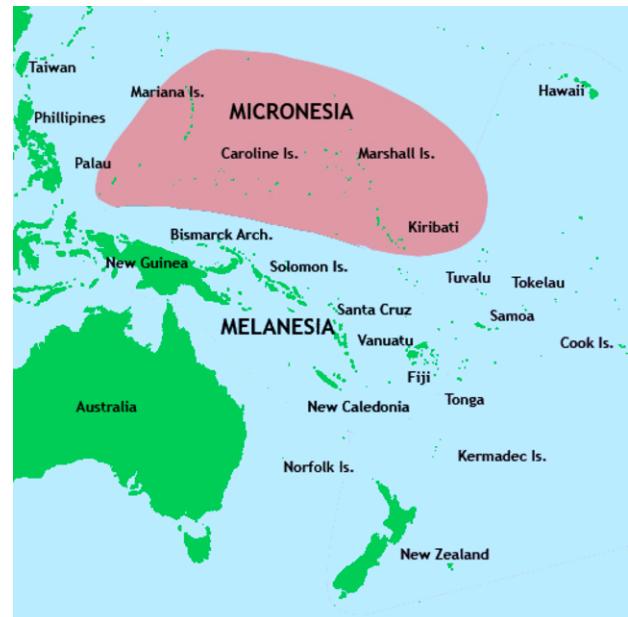
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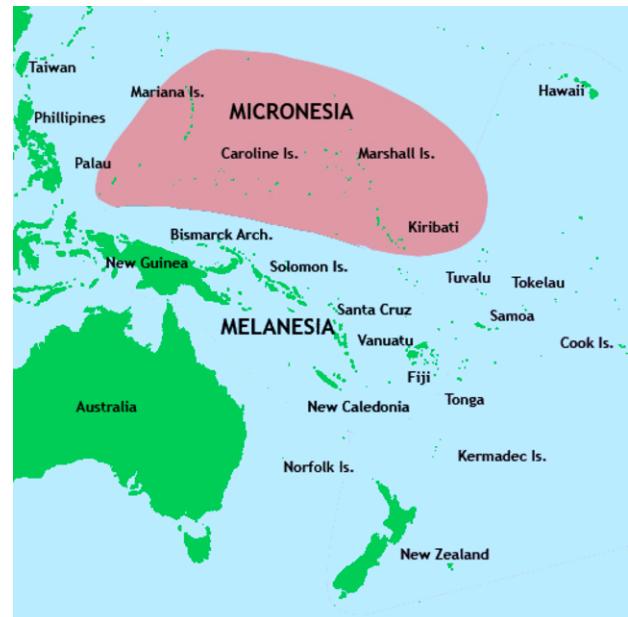
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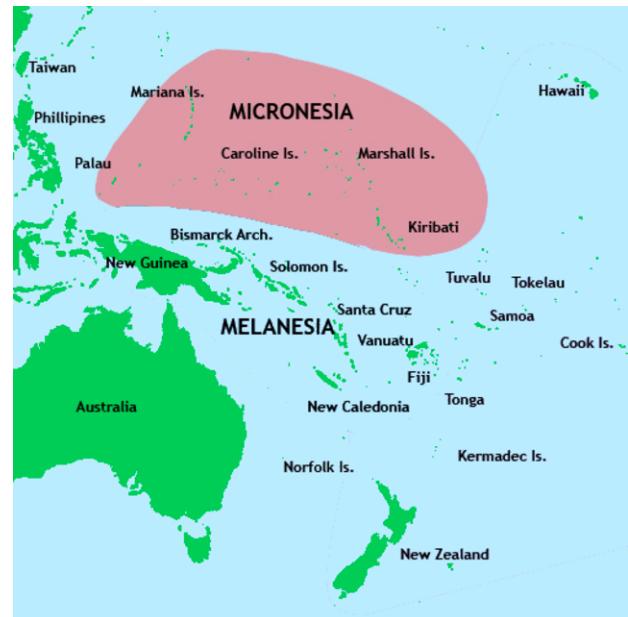
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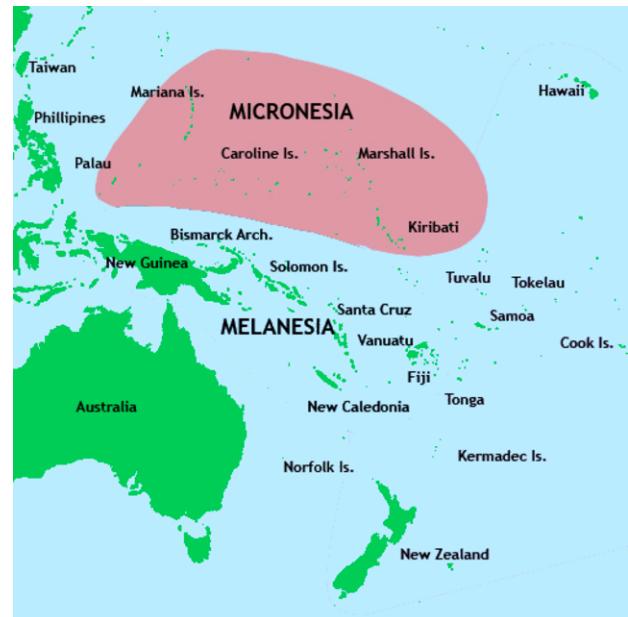
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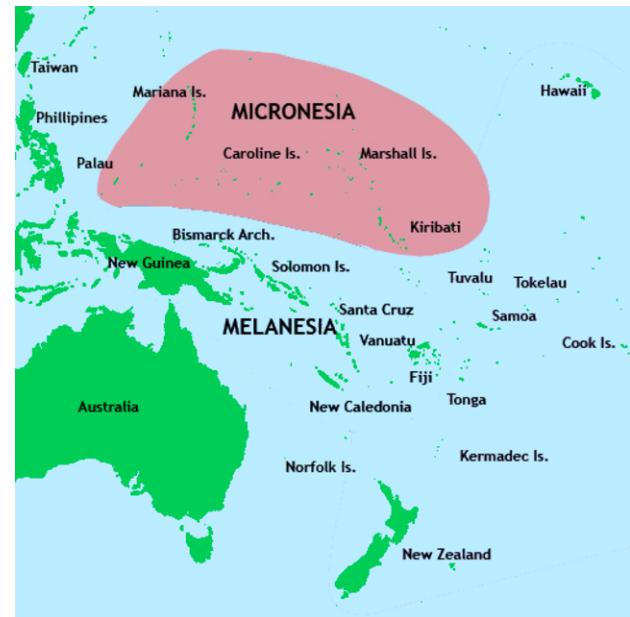
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The New York Times

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DP and Disparate Impact

Controlled experimental setting

How unfair is private learning?

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for each image

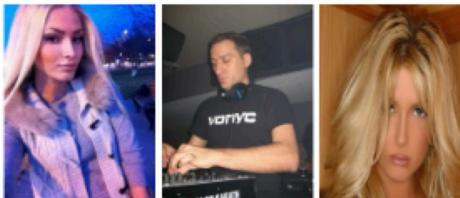
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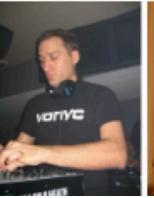
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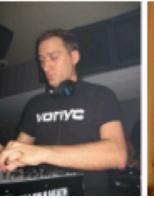
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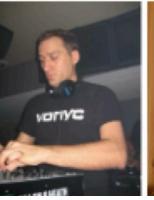
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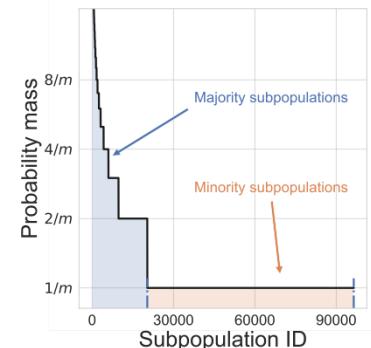


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- ...
- ...
- Subpopulation 2^{40}



How unfair is private learning?

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DP and Disparate Impact

Controlled experimental setting

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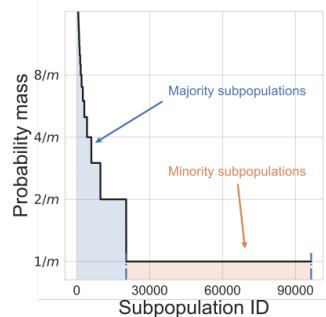
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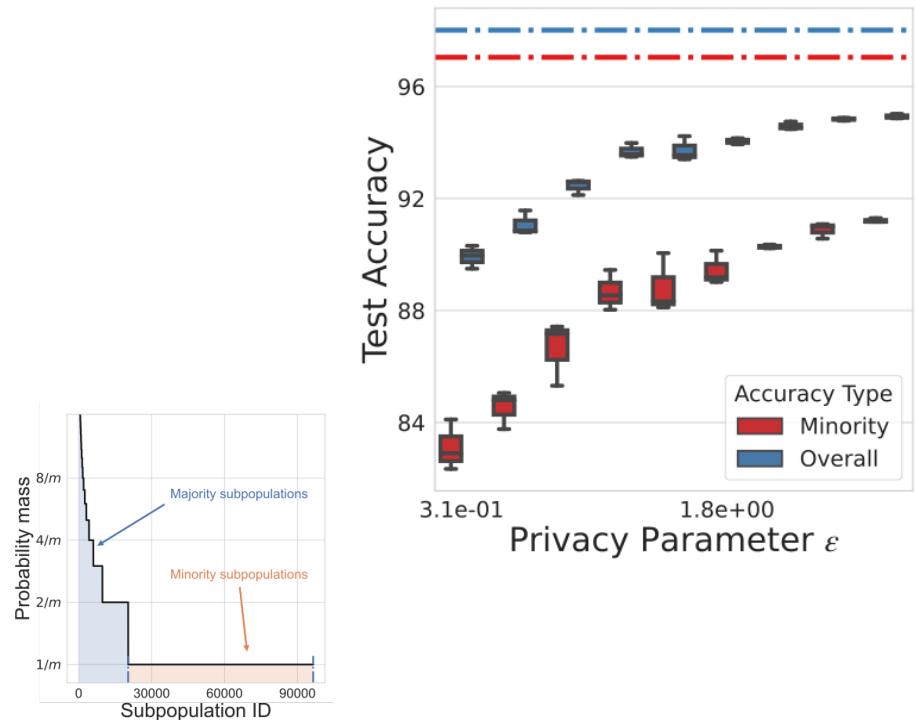
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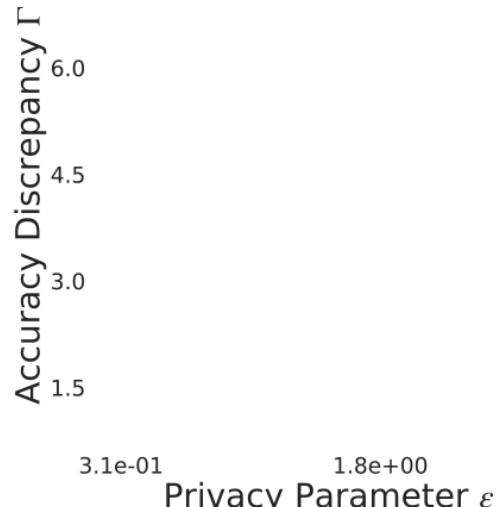
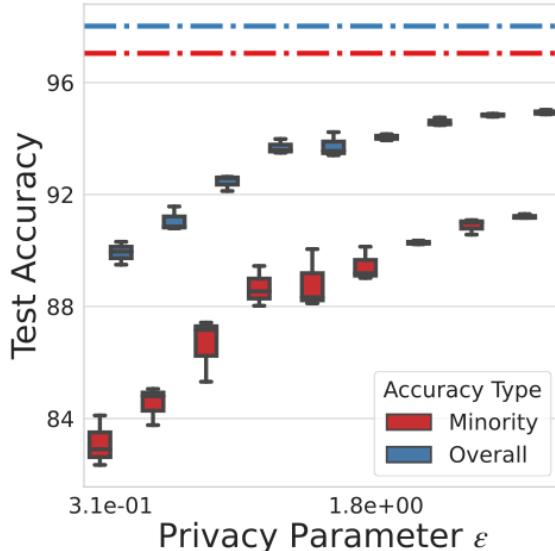
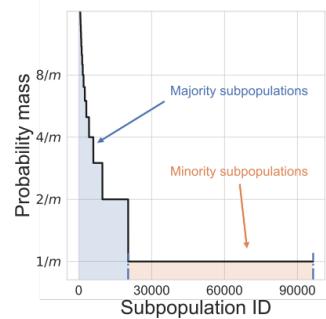
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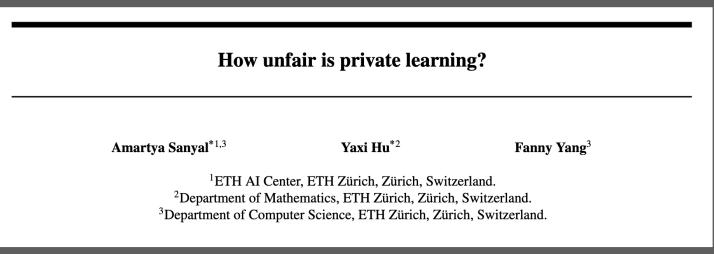
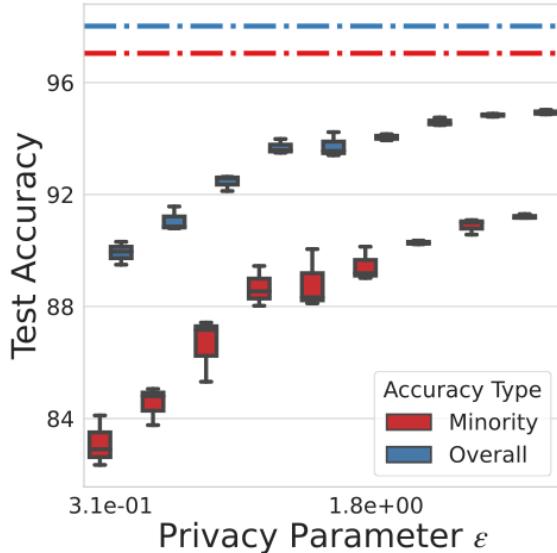
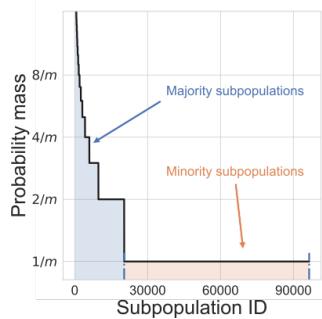
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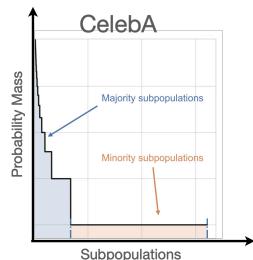
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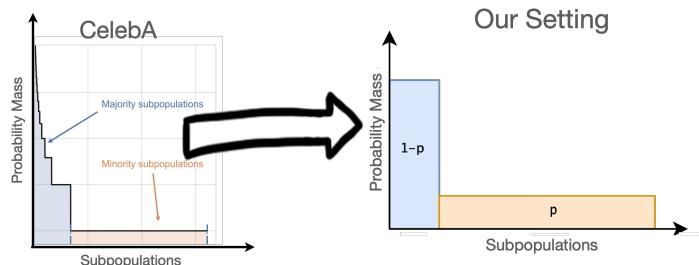
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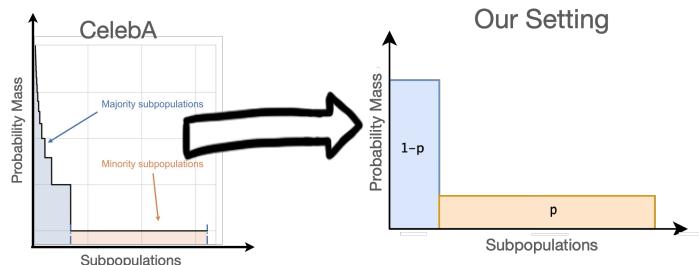
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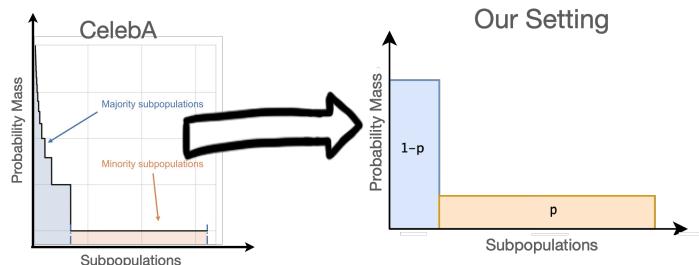
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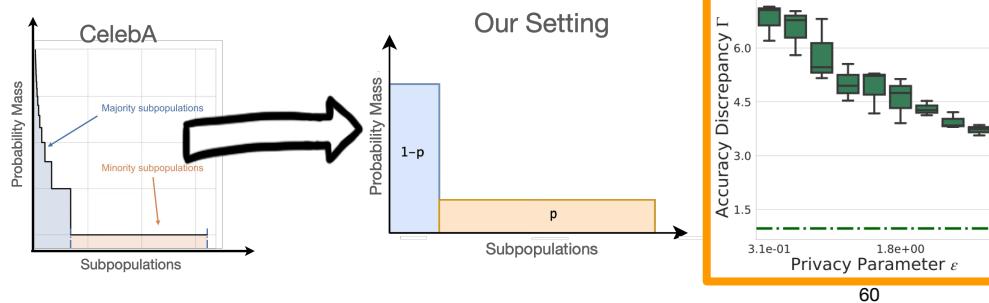
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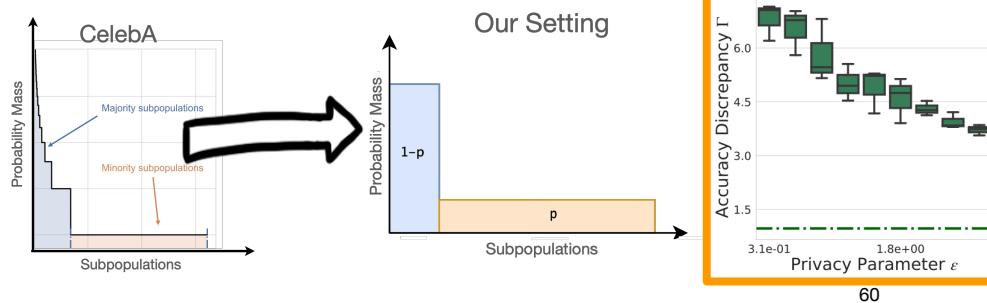
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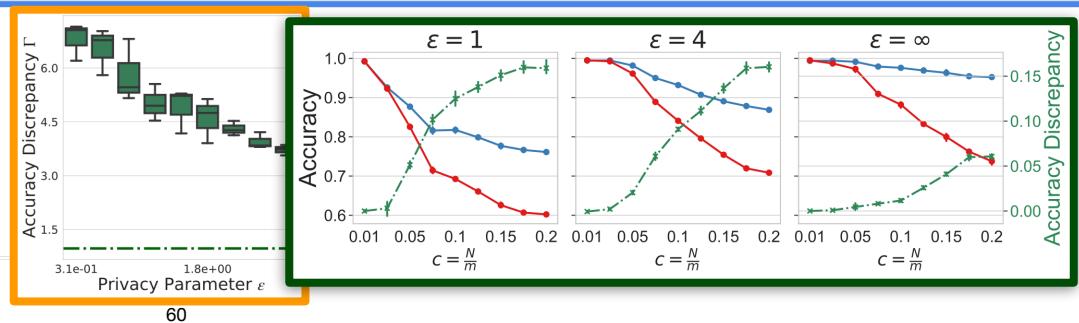
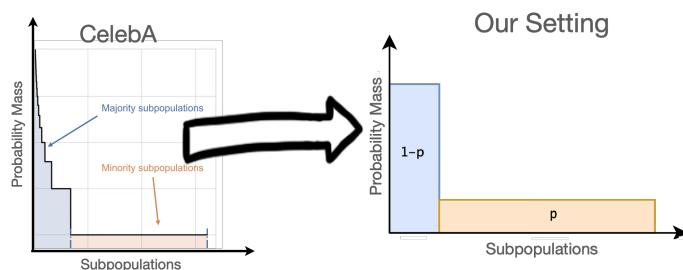
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DP and Disparate Impact

Fundamental Impossibility

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Fundamental Impossibility

On the Compatibility of Privacy and Fairness

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 - Obs 2. - Construct two datasets S_1, S_2 such that no classifier, except a constant classifier can be simultaneously fair on both.

DP and Disparate Impact

Other causes

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Differential Privacy Has Disparate Impact on Model Accuracy

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Differentially Private Empirical Risk Minimization under the Fairness Lens

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Removing Disparate Impact on Model Accuracy in Differentially Private Stochastic Gradient Descent

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Good data requires less noise

DP with “good” data

Favourable data properties

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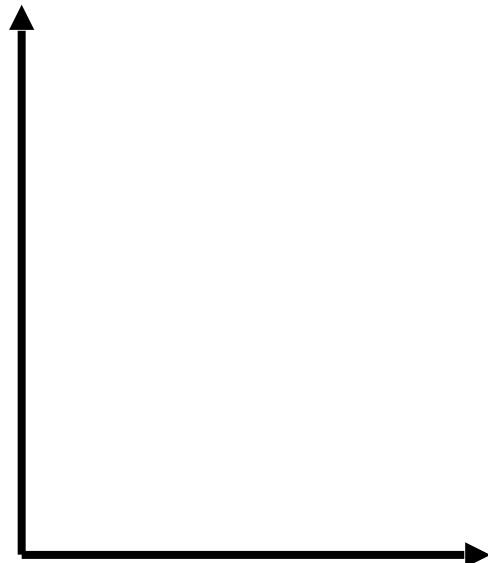
Naive DP Mean estimation

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- DP must protect against worst-case changes.
- A naïve DP estimator clips data to a ball of radius R
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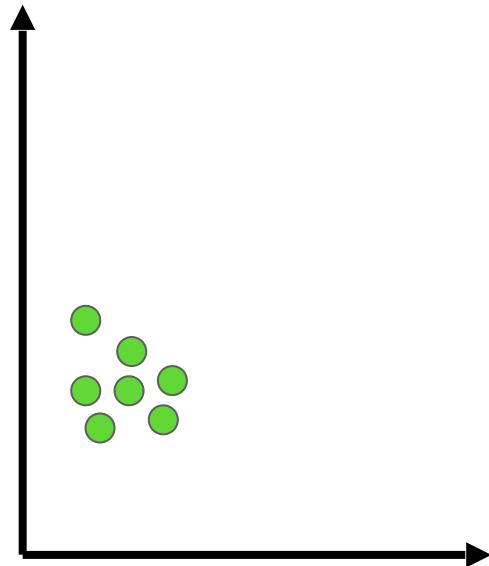
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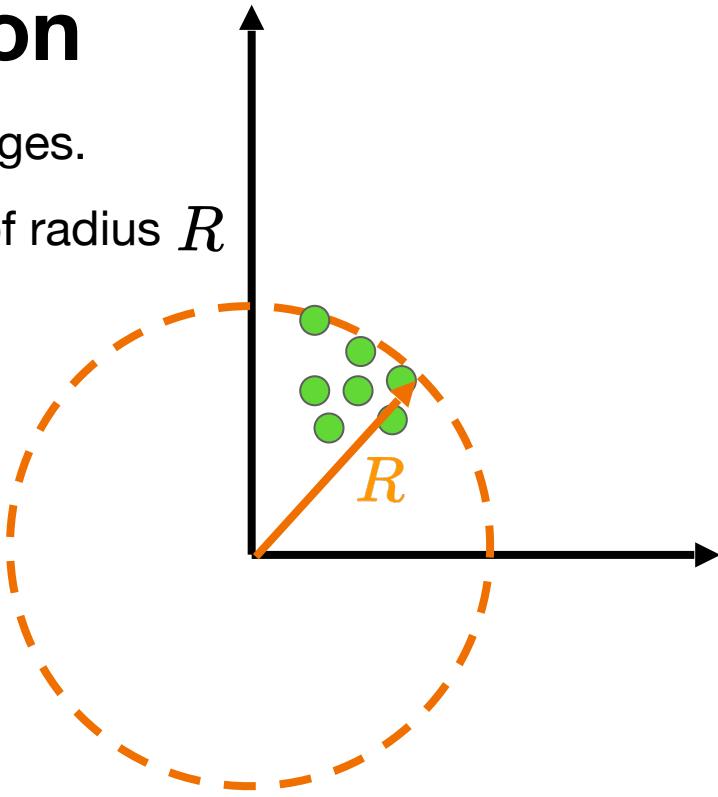
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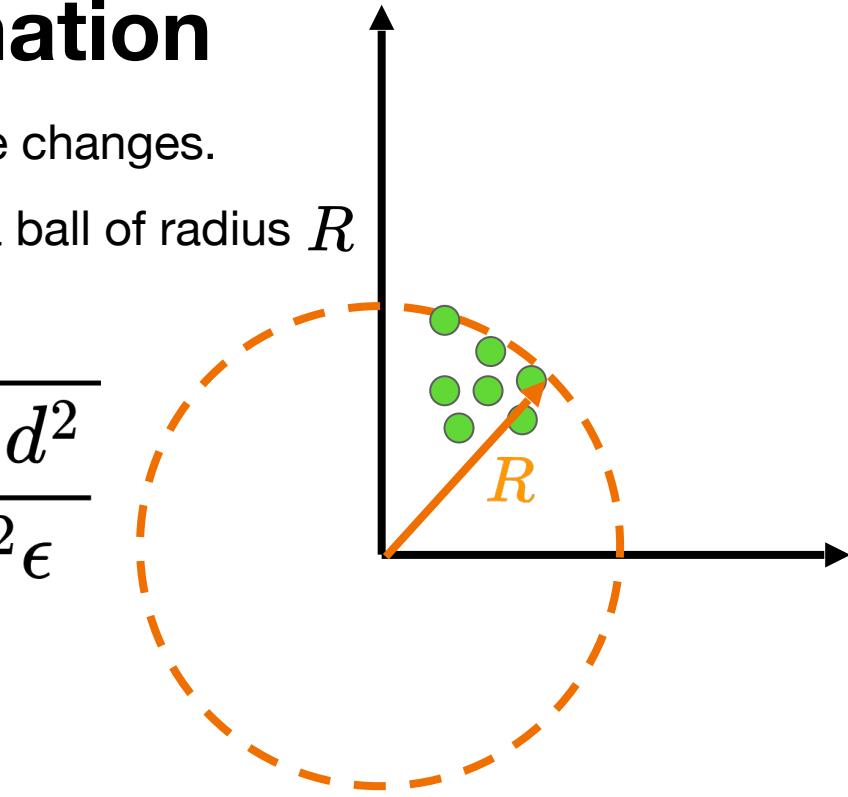
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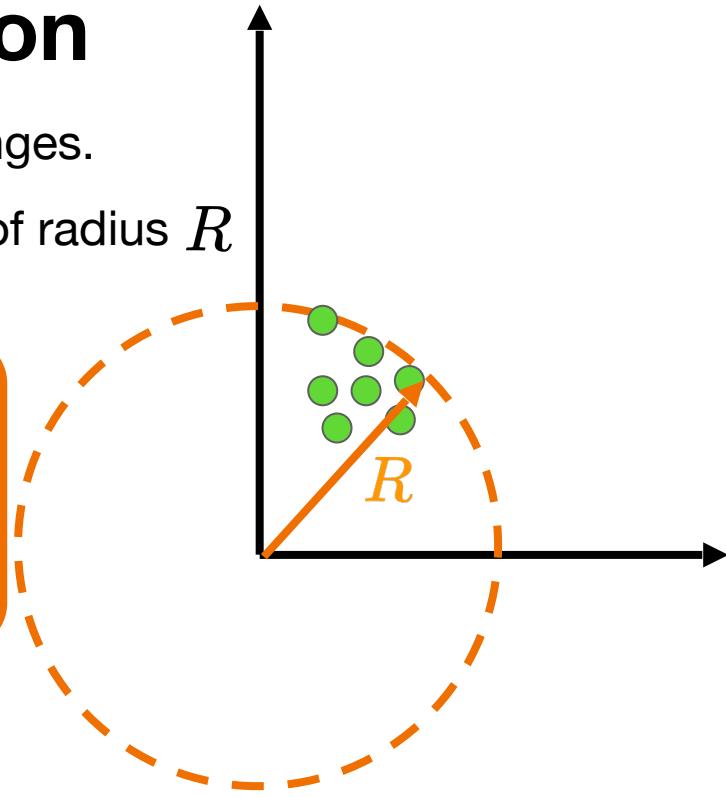
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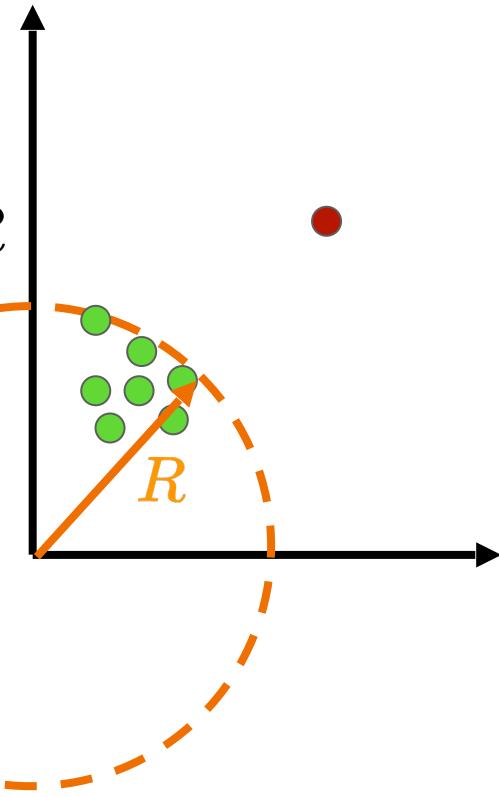
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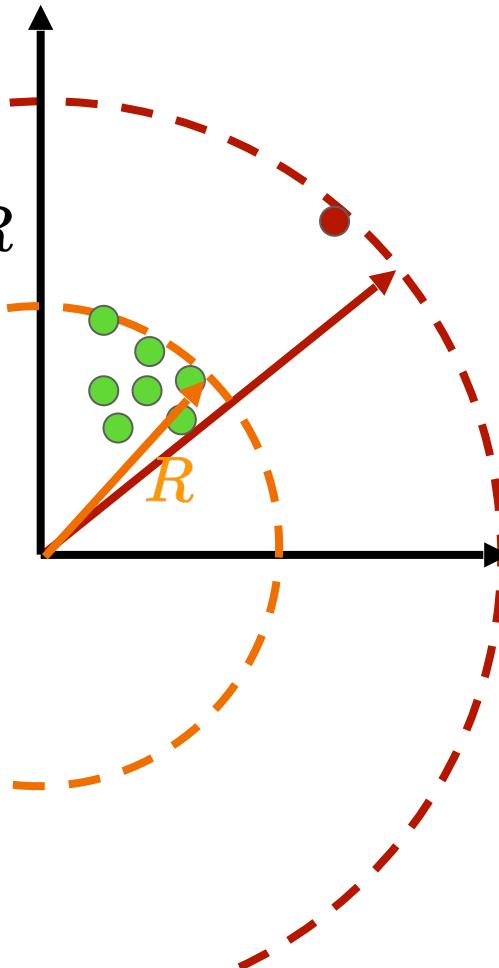
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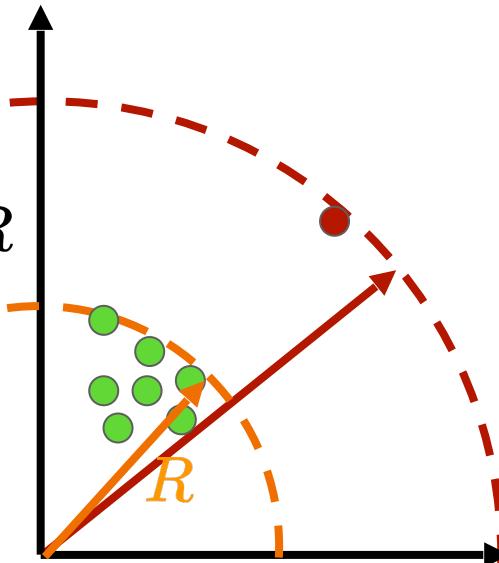
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- Heavy tails or outliers force R to be large.
- **Worst-case sensitivity leads to high noise and error.**

Friendly-Core estimation

FriendlyCore: Practical Differentially Private Aggregation

Eliad Tsfadia* Edith Cohen* Haim Kaplan* Yishay Mansour*
Uri Stemmer*

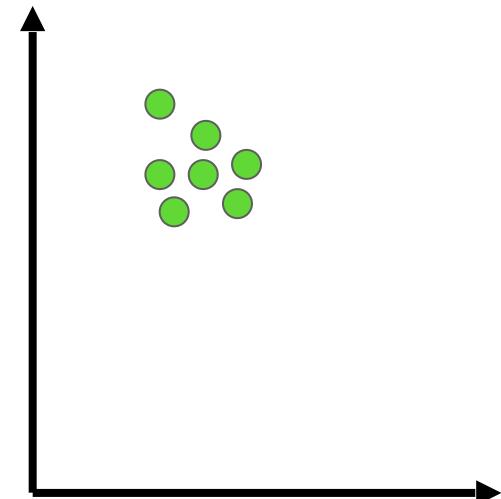
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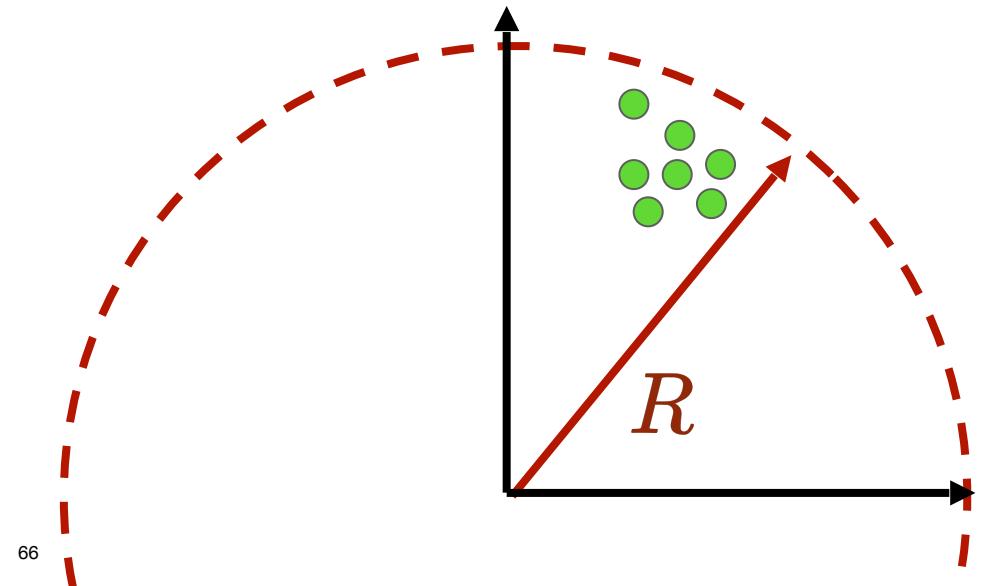


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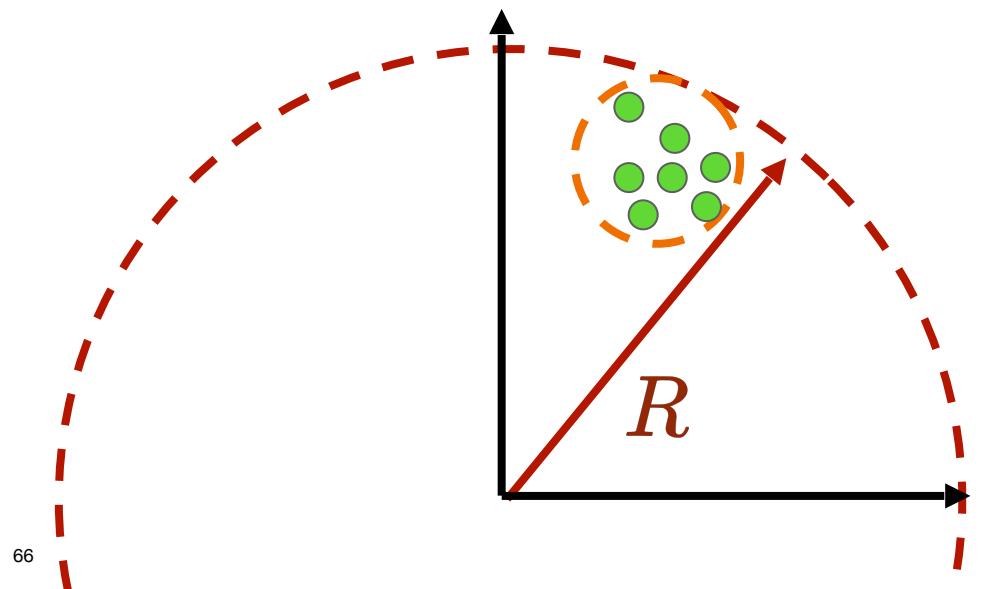
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- A dataset is friendly if every two points have a common neighbor within r



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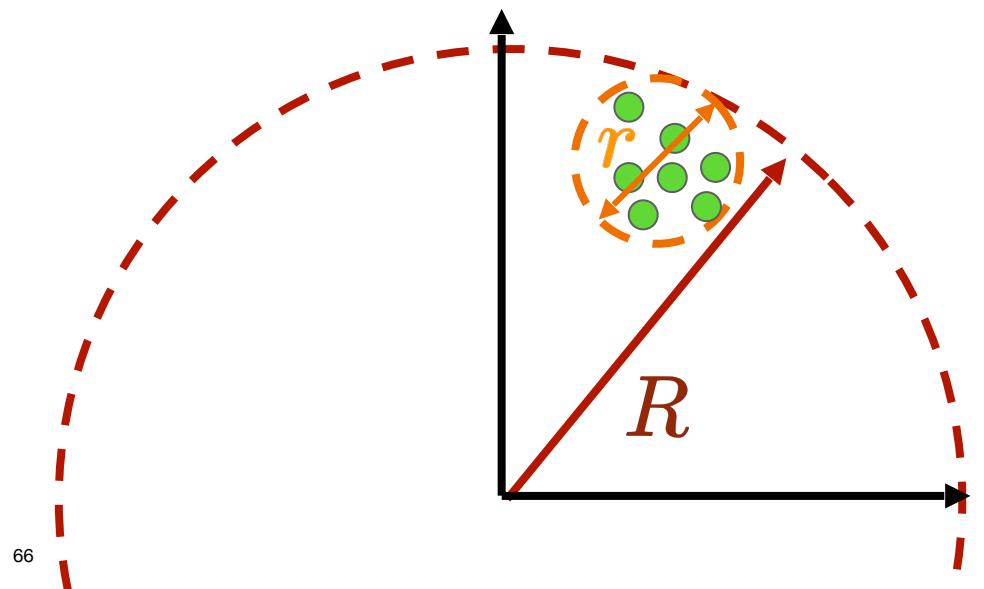
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Edith Cohen* Haim Kaplan* Uri Stemmer*

Yishay Mansour*

In many settings, most points lie in a ball of radius

- A dataset is friendly if every two points have a common neighbor within r



Friendly-Core estimation

FriendlyCore: Practical Differentially Private Aggregation

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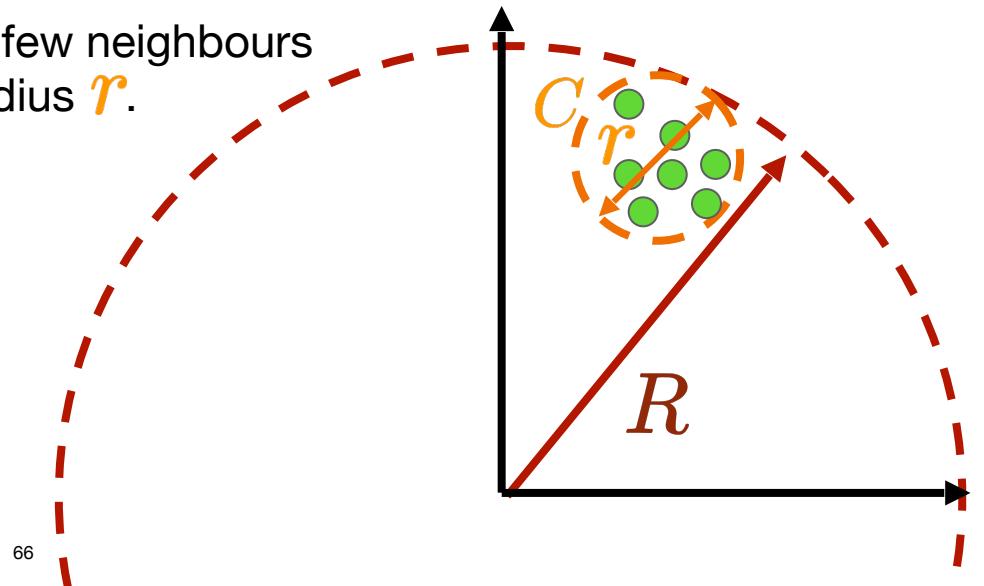
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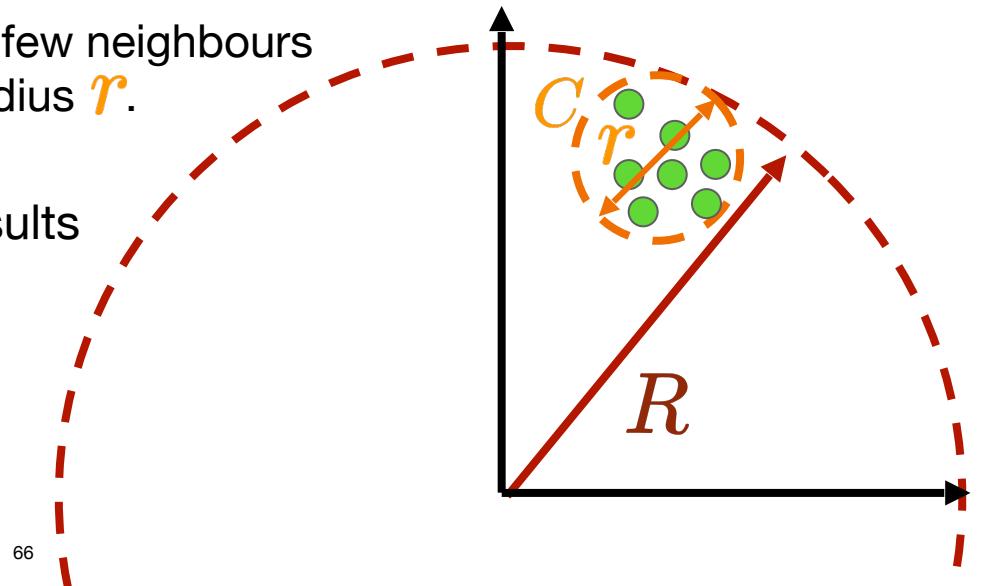
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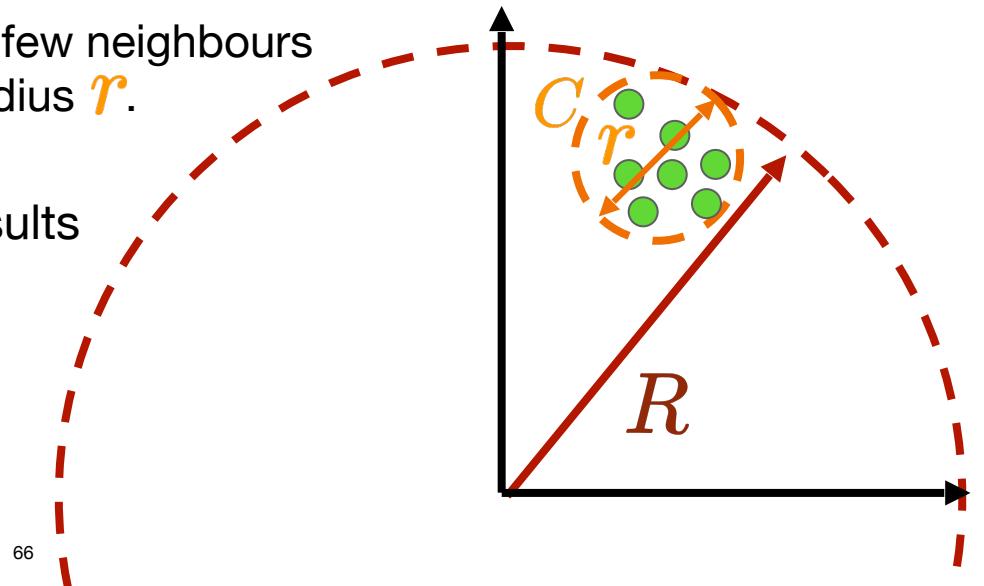
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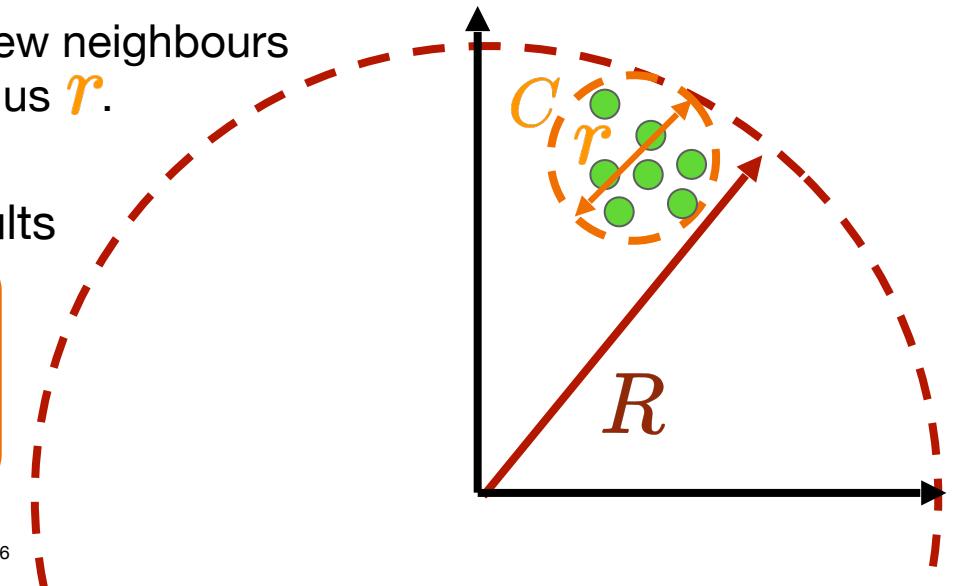
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DP geometric median

Private Geometric Median

Mahdi Haghifam*

Thomas Steinke†

Jonathan Ullman‡

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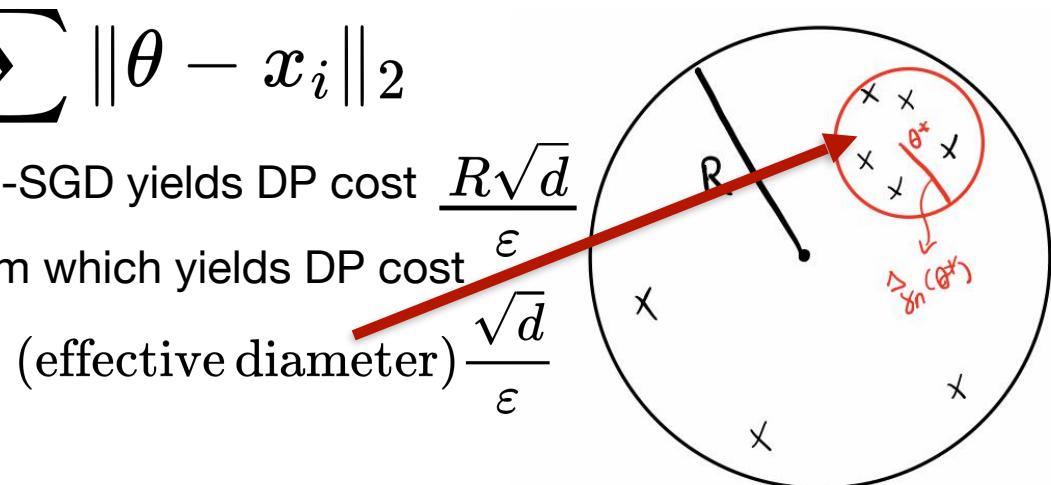
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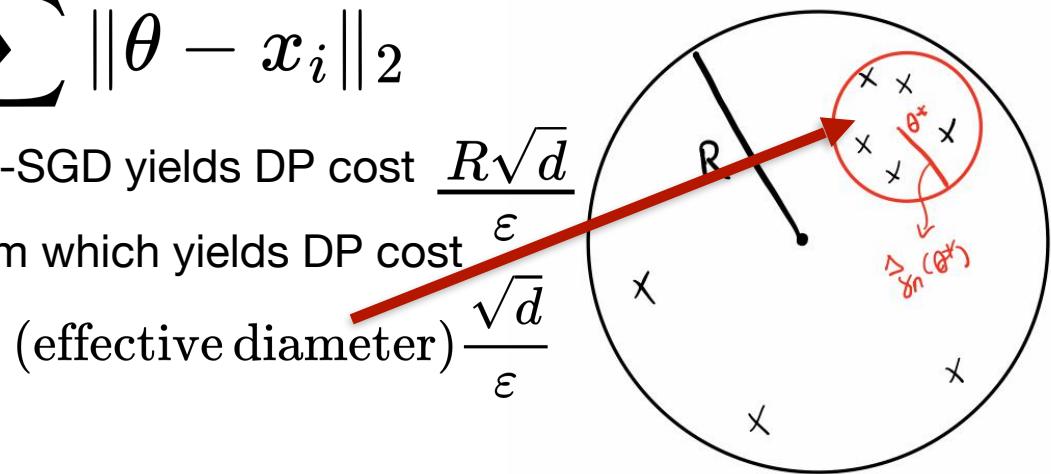
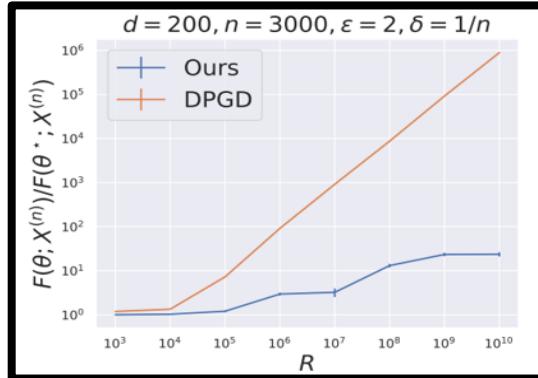
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DP Principal Component Analysis

DP Principal Component Analysis

DP-PCA: Statistically Optimal and
Differentially Private PCA

Xiyang Liu * Weihao Kong † Prateek Jain ‡ Sewoong Oh §

DP Principal Component Analysis

Lower bound for any data

DP-PCA: Statistically Optimal and
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Theorem 5.4 (Lower bound without Assumptions A.1–A.3) *Let $\tilde{\mathcal{P}}$ be the set of distributions satisfying Assumptions A.1–A.3 with $M = \tilde{O}(d + \sqrt{n\varepsilon/d})$, $V = O(d)$ and $\gamma = O(1)$. For $d \geq 2$, there exists a universal constant $C > 0$ such that*

$$\inf_{\hat{v} \in \mathcal{M}_\varepsilon} \sup_{P \in \tilde{\mathcal{P}}} \mathbb{E}_{S \sim P^n} [\sin(\hat{v}(S), v_1)] \geq C\kappa \min \left(\sqrt{\frac{d \wedge \log((1 - e^{-\varepsilon})/\delta)}{\varepsilon n}}, 1 \right). \quad (13)$$

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Theorem 5.5 (Lower Bound, Gaussian distribution). *Let \mathcal{M}_ε be the set of distributions satisfying Assumptions A.1–A.3 with $M = \tilde{O}(d + \sqrt{n\varepsilon/d})$, $V = O(d)$ and $\gamma = O(1)$ is denoted by $\tilde{\mathcal{P}}$. Let $\mathcal{P}_{(\lambda_1, \lambda_2)}$ be the set of Gaussian distributions with (λ_1, λ_2) as the first and second eigenvalues of the covariance matrix is denoted by $\mathcal{P}_{(\lambda_1, \lambda_2)}$. There exists a universal constant $C > 0$ such that*

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Lower bound for sub-gaussian

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Theorem 5.4 (Lower bound without Assumption A.1) Let \mathcal{M}_ε be the set of distributions satisfying Assumption A.1 that map n i.i.d. samples to an estimate $\hat{v} \in \mathbb{R}^d$. A set of distributions satisfying Assumptions A.1–
 $\gamma = O(1)$ is denoted by $\tilde{\mathcal{P}}$. For $d \geq 2$, there exists a

- Similar results known about other problems including PCA.
- Key takeaway:
 - Privacy guaranteed for **ALL** datasets.
 - **When data quality is high, utility is better.**

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DP SGD

Deep Learning with Differential Privacy

October 25, 2016

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Algorithm 1 Differentially private SGD (Outline)

Input: Examples $\{x_1, \dots, x_N\}$, loss function $\mathcal{L}(\theta) = \frac{1}{N} \sum_i \mathcal{L}(\theta, x_i)$. Parameters: learning rate η_t , noise scale σ , group size L , gradient norm bound C .

Initialize θ_0 randomly

for $t \in [T]$ **do**

 Take a random sample L_t with sampling probability L/N

Compute gradient

 For each $i \in L_t$, compute $\mathbf{g}_t(x_i) \leftarrow \nabla_{\theta_t} \mathcal{L}(\theta_t, x_i)$

Clip gradient

$\bar{\mathbf{g}}_t(x_i) \leftarrow \mathbf{g}_t(x_i) / \max(1, \frac{\|\mathbf{g}_t(x_i)\|_2}{C})$

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1. DP-PCA requires **additional time**

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Algorithm 1 Differentially private SGD (Outline)

Input: Examples $\{x_1, \dots, x_N\}$, loss function $\mathcal{L}(\theta) = \frac{1}{N} \sum_i \mathcal{L}(\theta, x_i)$. Parameters: learning rate η_t , noise scale σ , group size L , gradient norm bound C .

Initialize θ_0 randomly
for $t \in [T]$ do

(1) Take a random sample L_t with sampling probability L/N

(2) Compute gradient
For each $i \in L_t$, compute $\mathbf{g}_t(x_i) \leftarrow \nabla_{\theta_t} \mathcal{L}(\theta_t, x_i)$

(3) Clip gradient
 $\bar{\mathbf{g}}_t(x_i) \leftarrow \mathbf{g}_t(x_i) / \max(1, \frac{\|\mathbf{g}_t(x_i)\|_2}{C})$

(4) Add noise
 $\tilde{\mathbf{g}}_t \leftarrow \frac{1}{L} (\sum_i \bar{\mathbf{g}}_t(x_i) + \mathcal{N}(0, \sigma^2 C^2 \mathbf{I}))$

(5) Descent
 $\theta_{t+1} \leftarrow \theta_t - \eta_t \tilde{\mathbf{g}}_t$
Output θ_T and compute the overall privacy cost (ϵ, δ) using a privacy accounting method.

DP SGD

- DP-SGD is the standard workhorse for DP Machine Learning algorithms.
- As we saw earlier, the added noise scales with dimensionality of params
- To avoid this, they conduct DP-PCA on data before doing DP-SGD.

But,

1. DP-PCA requires **additional time**
2. DP-PCA incurs **additional privacy cost**

Deep Learning with Differential Privacy

October 25, 2016

Martín Abadi*
H. Brendan McMahan*

Andy Chu*
Ilya Mironov*
Li Zhang*

Ian Goodfellow†
Kunal Talwar*

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(5) $\theta_{t+1} \leftarrow \theta_t - \eta_t \tilde{\mathbf{g}}_t$

Output θ_T and compute the overall privacy cost (ϵ, δ) using a privacy accounting method.

PILLAR

Leveraging intrinsic low dimensionality

PILLAR: How to make semi-private learning more effective

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PILLAR

Leveraging intrinsic low dimensionality

Idea 1: Use identically distributed **public unlabelled data** to find low rank subspace for projection



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- But natural data is not inherently low rank in pixel space

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Idea 2: Use any **public unlabelled pre-training** data for representation learning.



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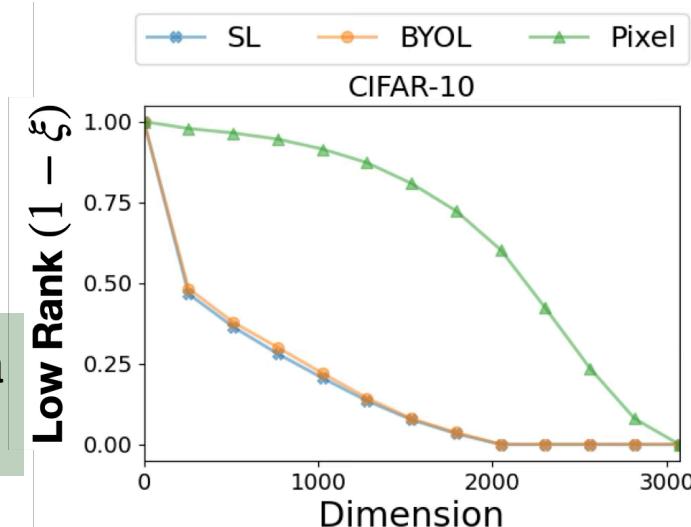
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$$1 - \xi = \text{low rank reconstruction error}$$

70

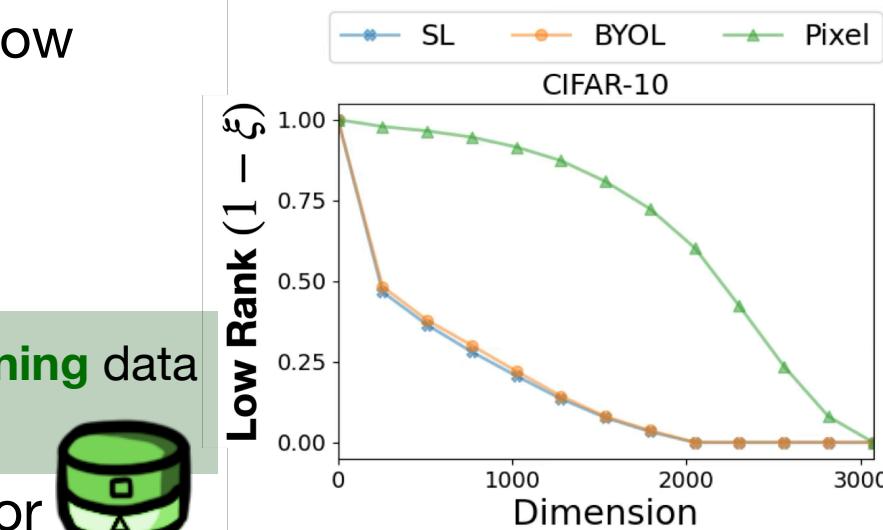
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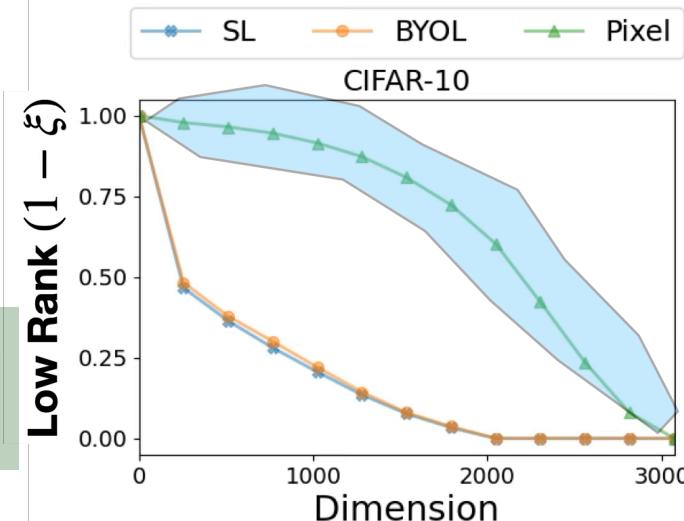
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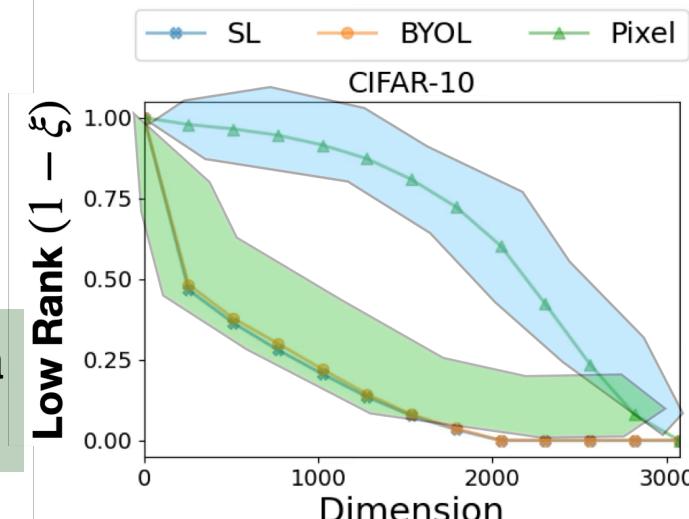
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PILLAR for Chest X-Ray Classification

Leveraging intrinsic low dimensionality

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Public
unlabelled
pre-training



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PILLAR for Chest X-Ray Classification

Leveraging intrinsic low dimensionality

Private labelled



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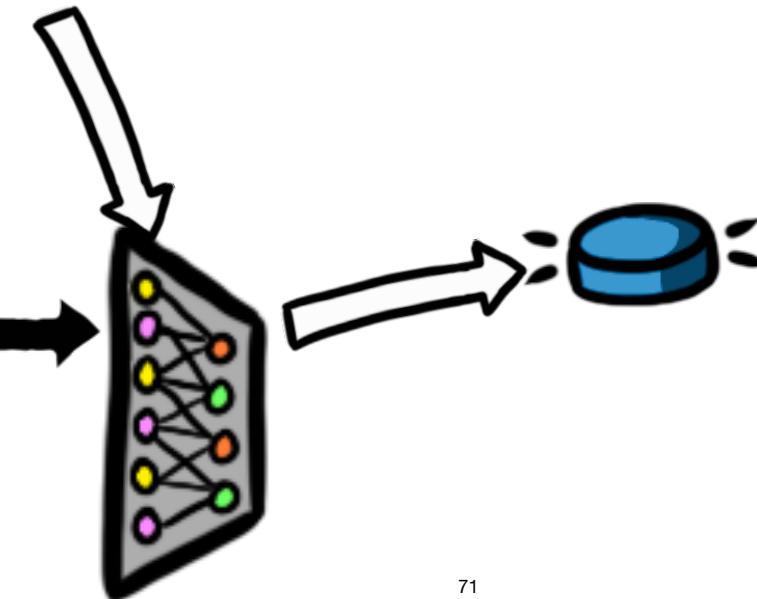
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PILLAR for Chest X-Ray Classification

Leveraging intrinsic low dimensionality

Private labelled



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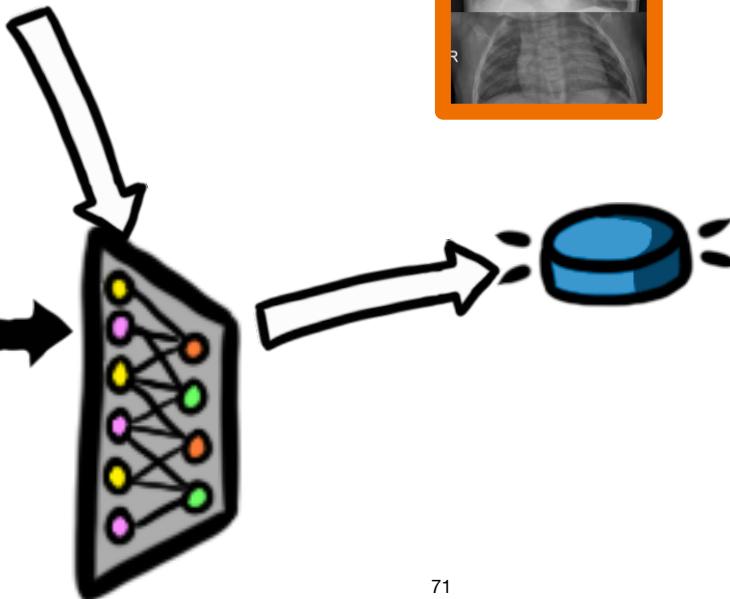
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Public unlabelled



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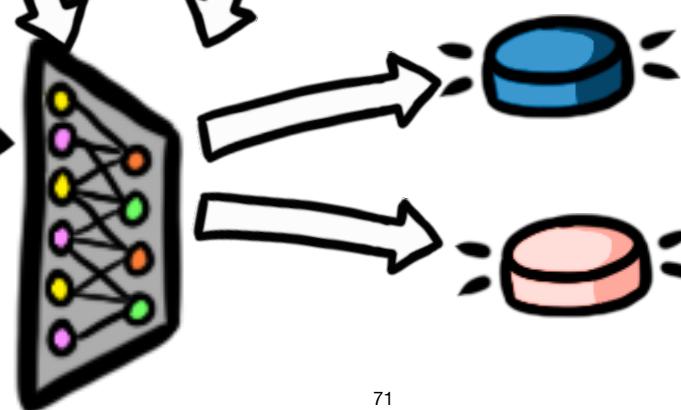
Private labelled



Public unlabelled



Public
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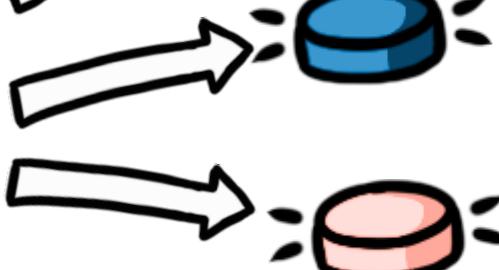
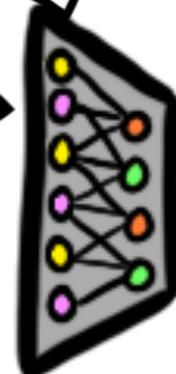
Private labelled



Public unlabelled



Public
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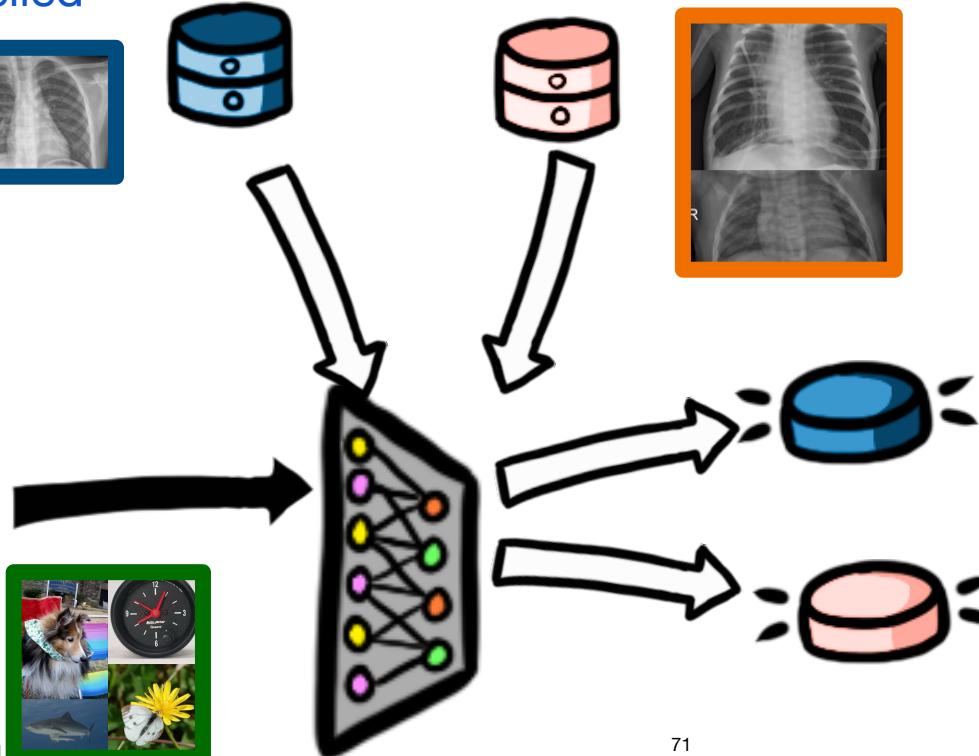
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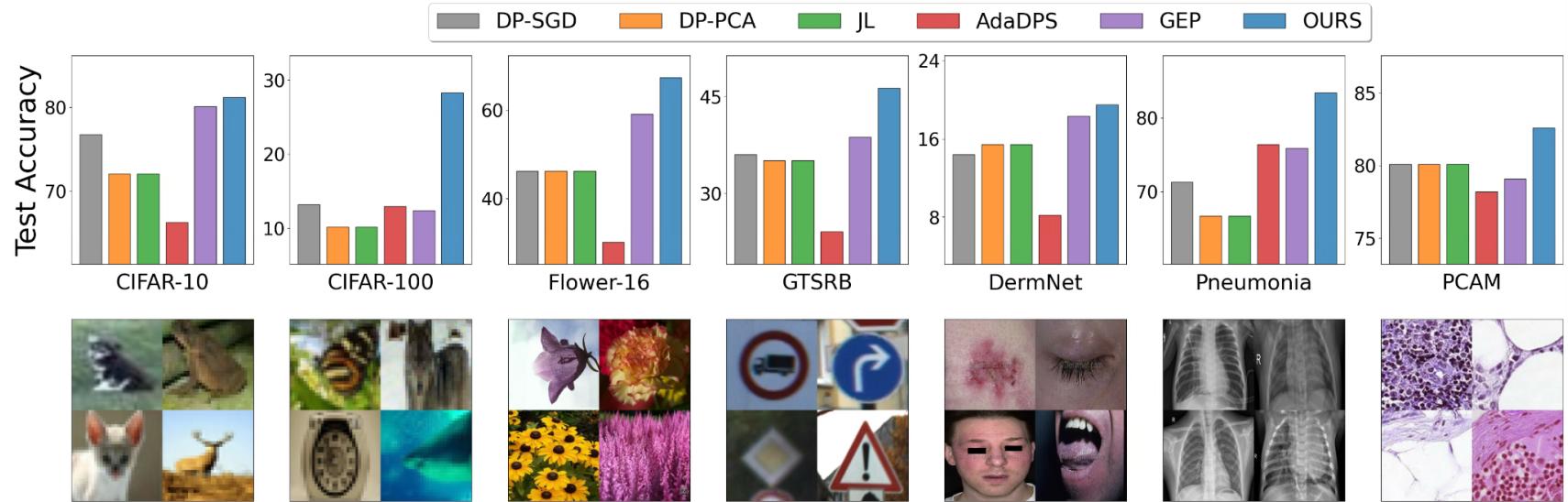
Public
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pre-training



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Other approaches to leverage unlabelled data



- GEP works in the gradient space
- AdaDPS use public data for gradient pre-conditioning

Next



Robustness in Machine Learning

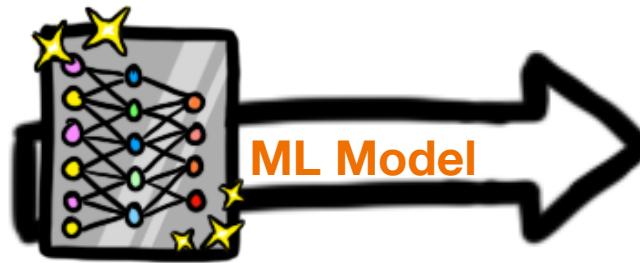
Adversarial Robustness in Machine Learning

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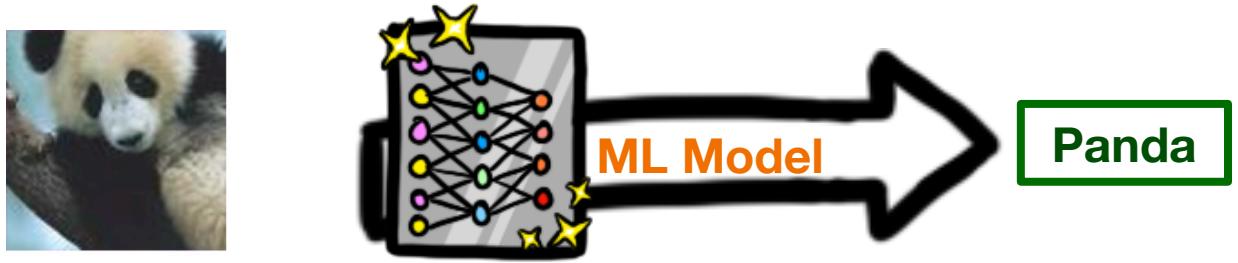
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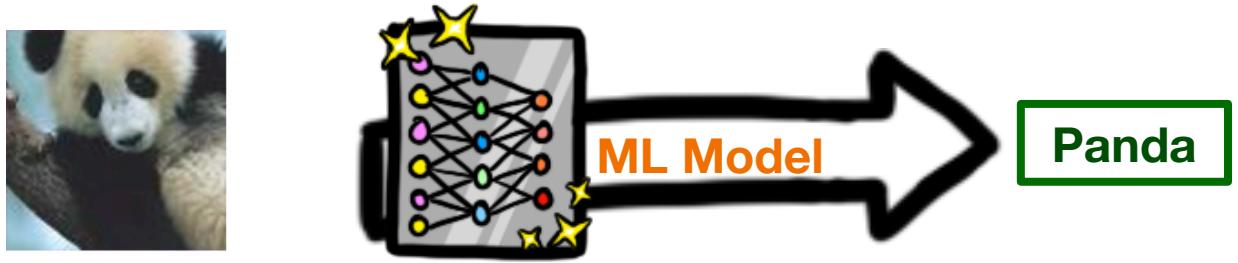
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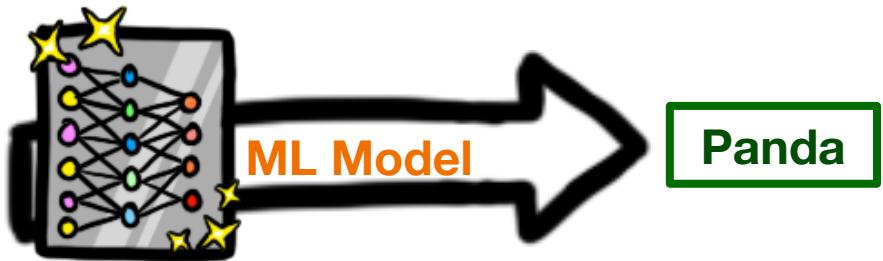
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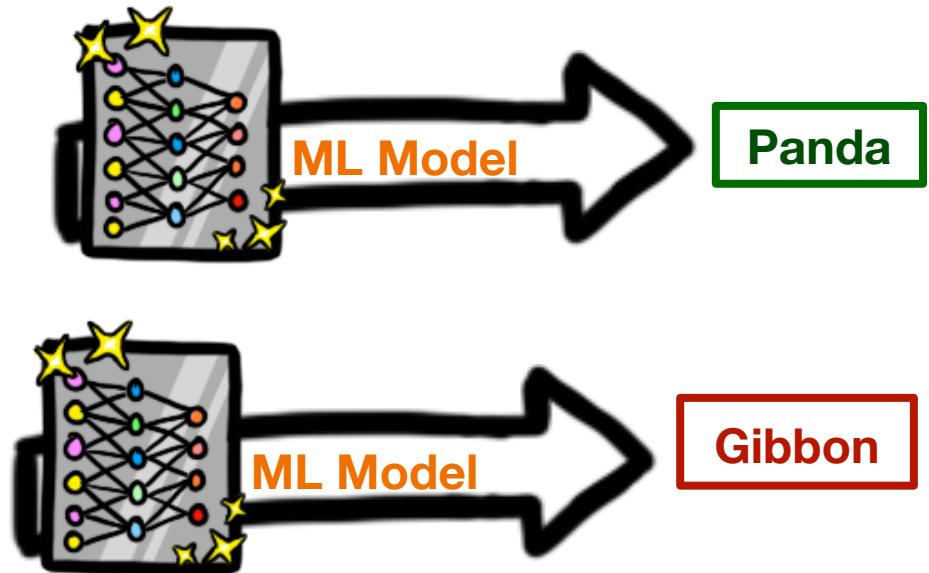
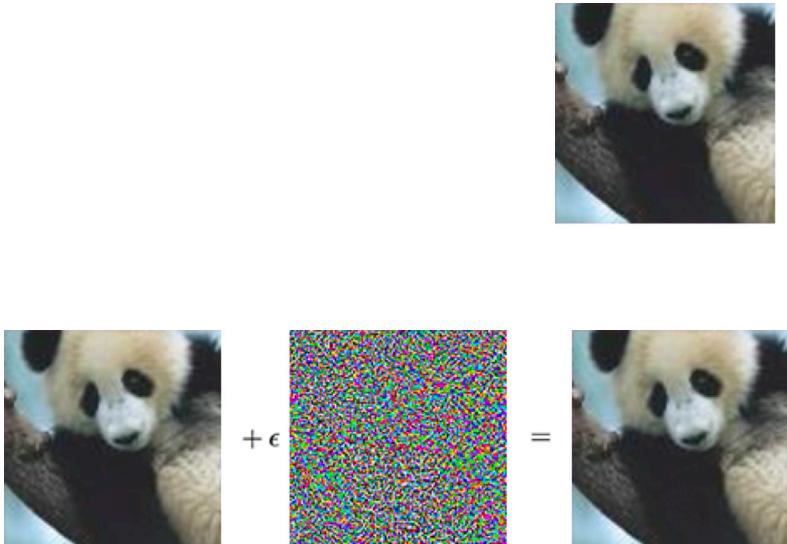
Adversarial Robustness in Machine Learning



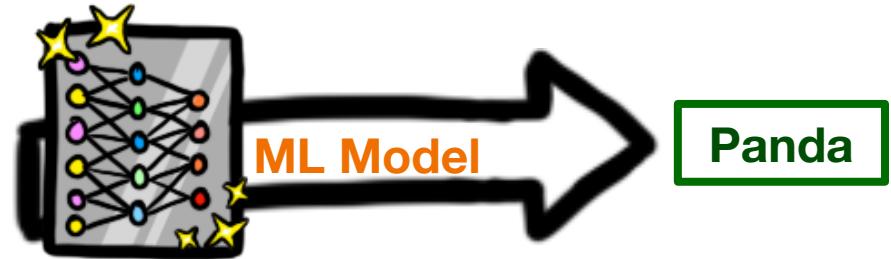
$$\begin{matrix} \text{Original Image} \\ + \epsilon \\ \text{Noisy Image} \end{matrix} = \text{Adversarial Image}$$



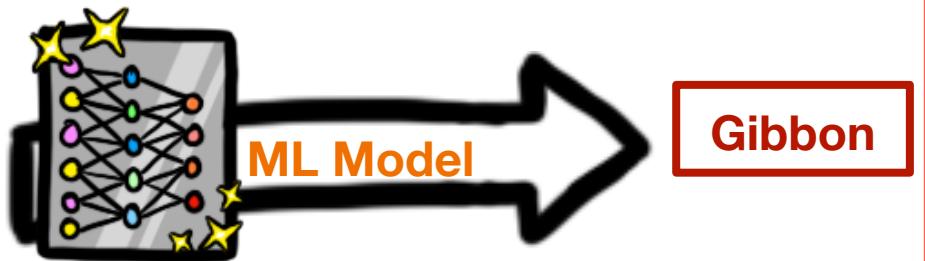
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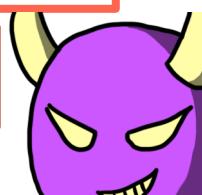
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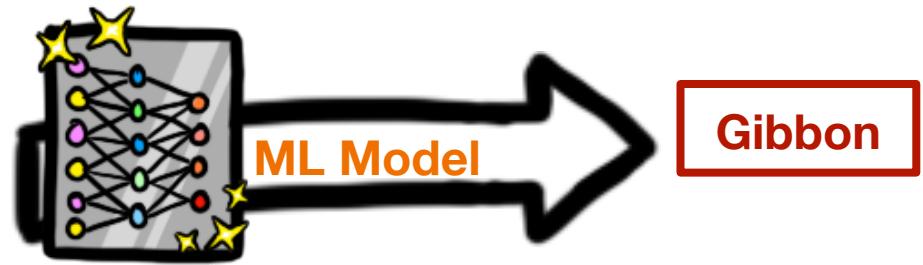
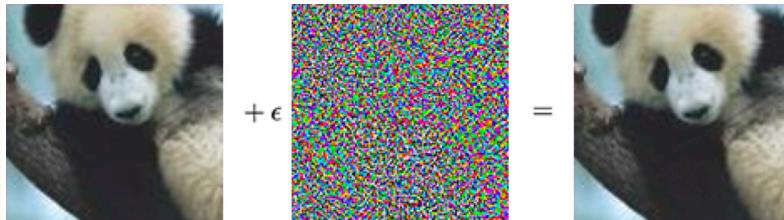
$$\begin{matrix} \text{Image of a Panda} & + \epsilon & = \text{Image of a Panda with noise} \end{matrix}$$



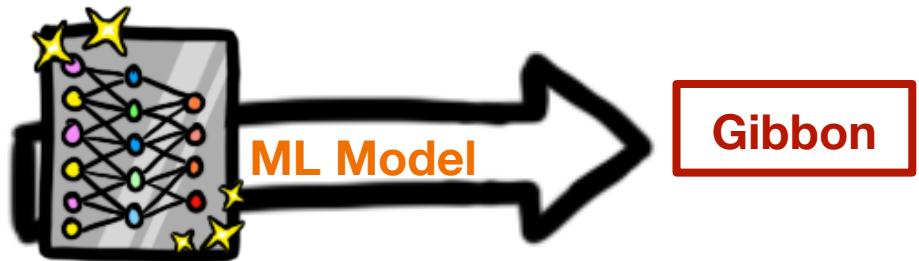
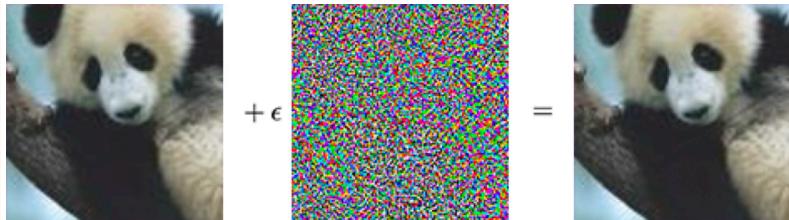
Adversarial Example



Adversarial Robustness in Machine Learning

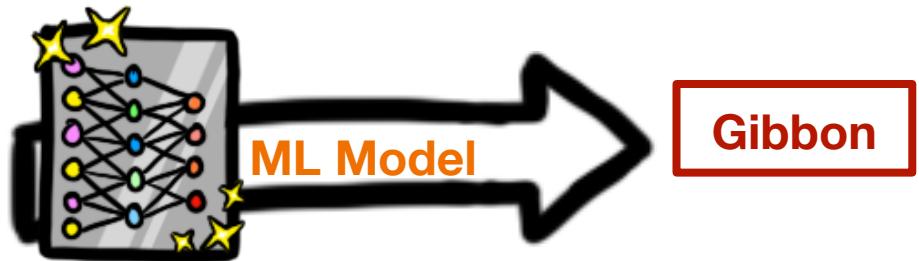
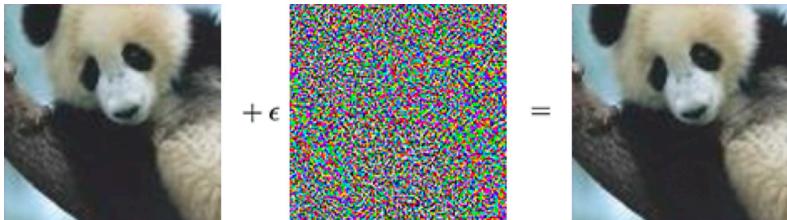


Adversarial Robustness in Machine Learning



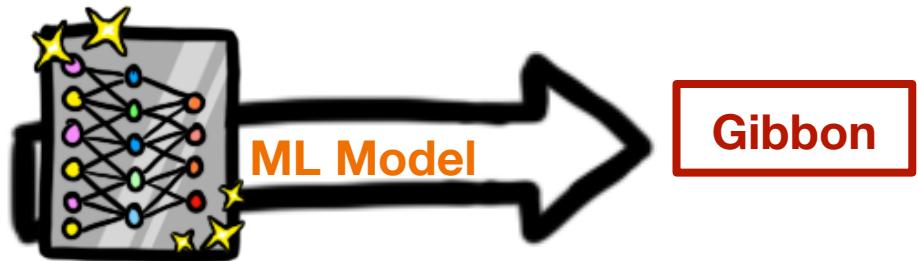
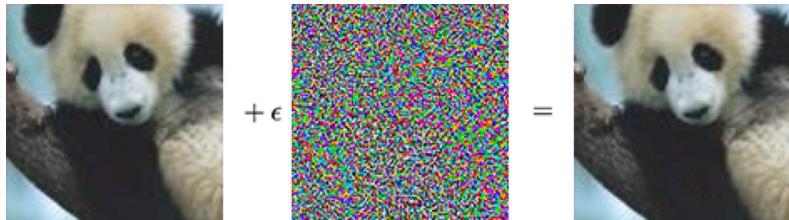
For any distribution \mathcal{P} over $\mathbb{R}^d \times \{0, 1\}$ and any binary classifier $f : \mathbb{R}^d \rightarrow \{0, 1\}$

Adversarial Robustness in Machine Learning



For any distribution \mathcal{P} over $\mathbb{R}^d \times \{0, 1\}$ and any binary classifier $f : \mathbb{R}^d \rightarrow \{0, 1\}$
the γ -adversarial error is defined as

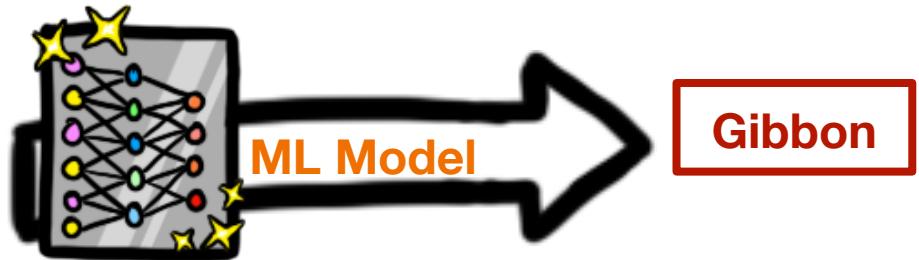
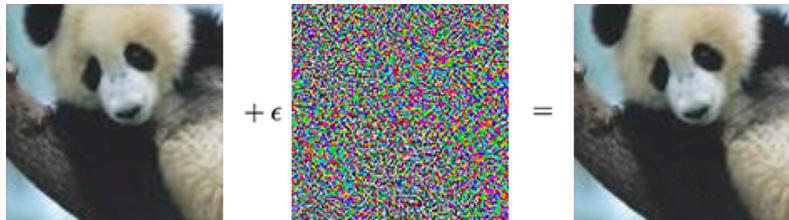
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$$\Pr_{(x,y) \sim \mathbb{P}}[\text{exists } z \in \mathcal{B}_\gamma(x) : f(z) \neq y]$$

Adversarial Robustness in Machine Learning

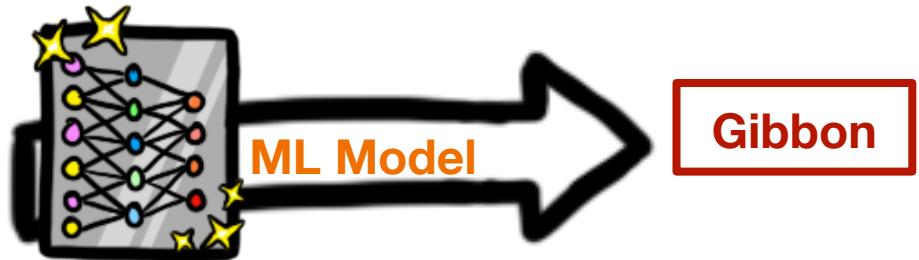
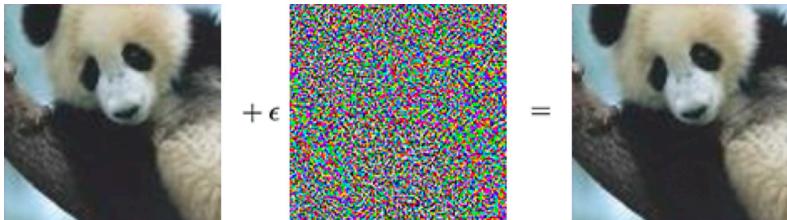


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$$\Pr_{(x,y) \sim \mathbb{P}} [\text{exists } z \in \mathcal{B}_\gamma(x) : f(z) \neq y]$$

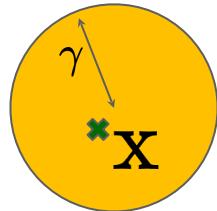
\mathbf{x}^*

Adversarial Robustness in Machine Learning



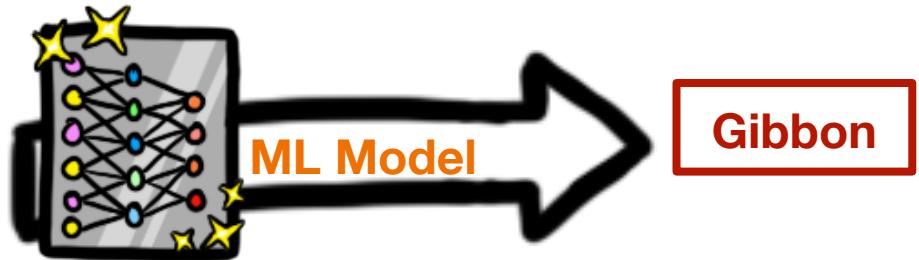
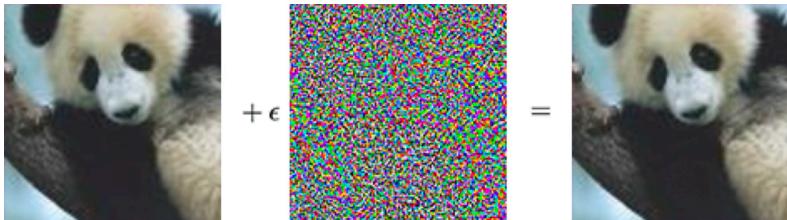
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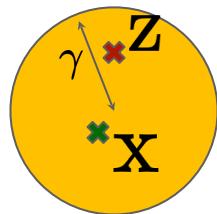


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Label Noise is ubiquitously interpolated

UNDERSTANDING DEEP LEARNING REQUIRES RE-THINKING GENERALIZATION

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Learning from Noisy Labels with Deep Neural Networks: A Survey

Hwanjun Song, Minseok Kim, Dongmin Park, Yooju Shin, Jae-Gil Lee

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- Trained long enough, NNs fit label noise

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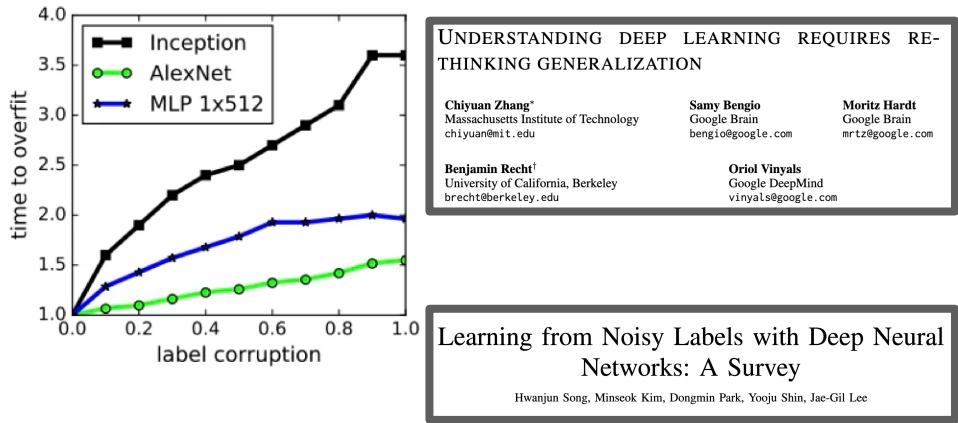
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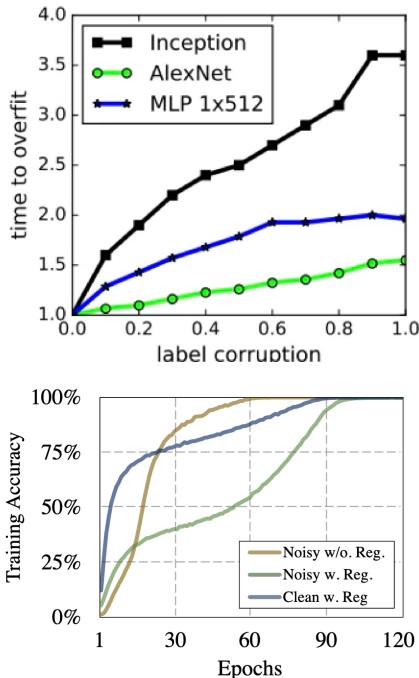
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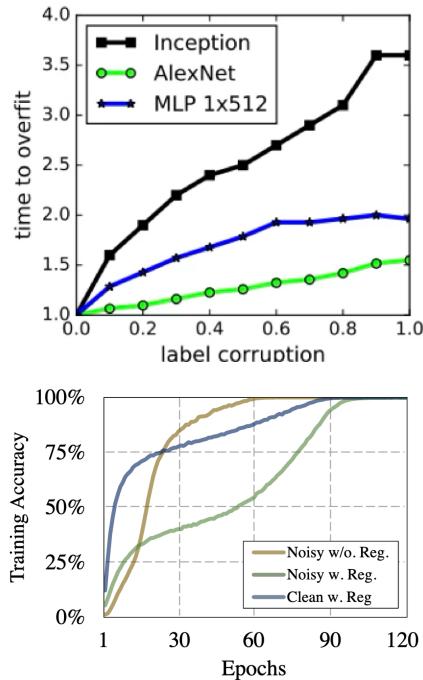
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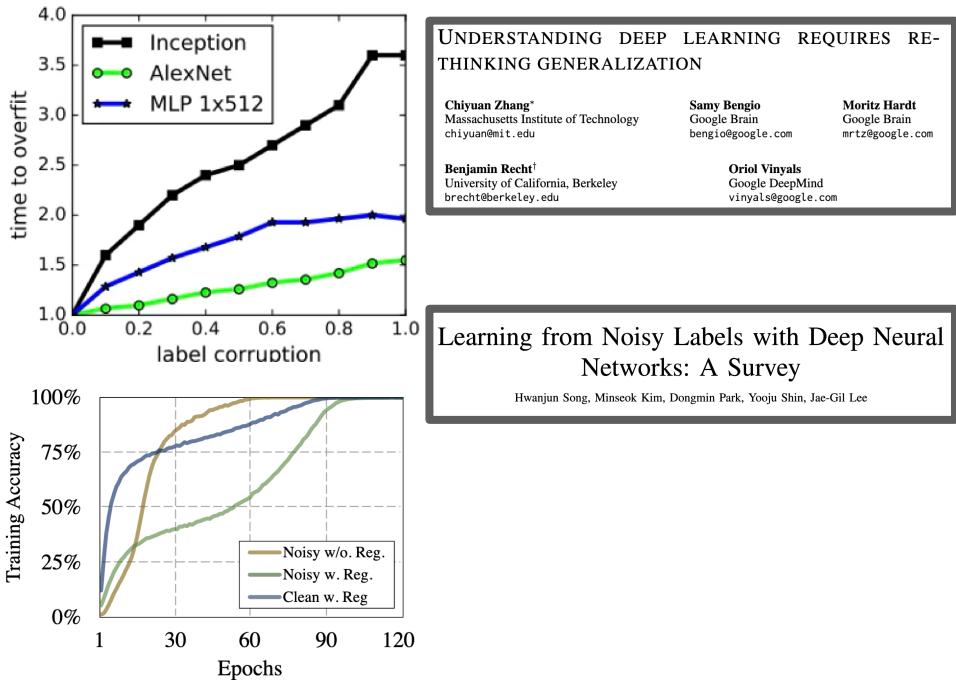
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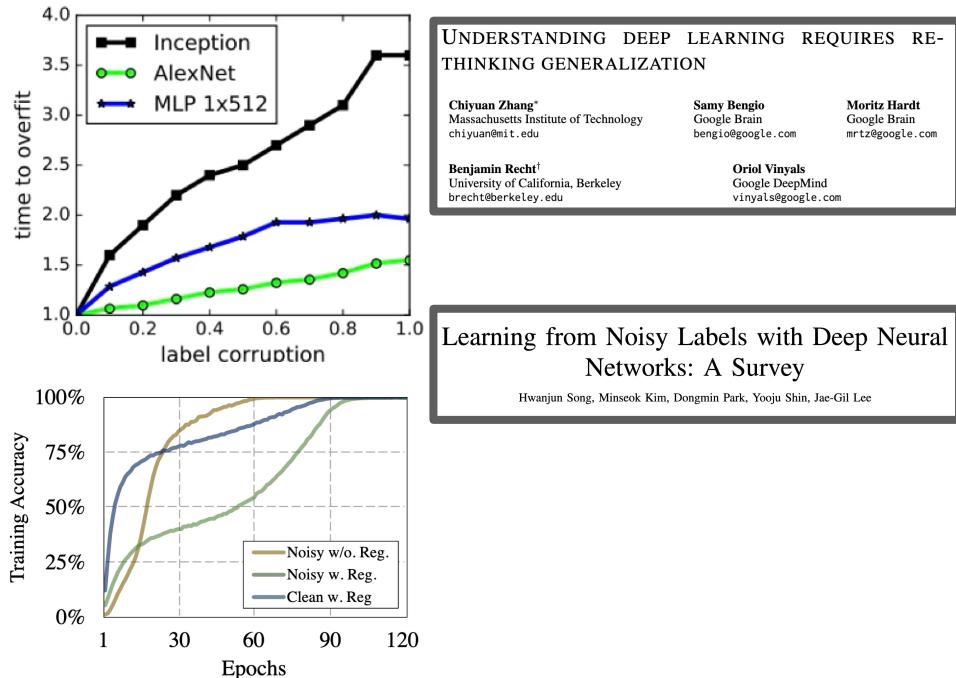
Label Noise is ubiquitously interpolated

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- Define a model with 100% training acc: **Interpolator**



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Question: What about **Robust Accuracy** ?

Lower bound on Adversarial error

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A LAW OF ADVERSARIAL RISK, INTERPOLATION, AND LABEL NOISE

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Lower bound on Adversarial error

Let

- μ be any distribution on \mathbb{R}^d ,
- $\eta \in (0, 1)$ be the uniform label noise rate,
- $\mathcal{C} \subset \mathbb{R}^d$ be any region, and
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Theorem If the noisy dataset size $m = \Omega\left(\frac{N(\mathcal{C}, \epsilon, \|\cdot\|)}{\mu(\mathcal{C})\eta}\right)$, for all interpolators h

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$$\text{Adv. Error}_\epsilon(h) \geq \mu(\mathcal{C})$$

Lower bound on Adversarial error

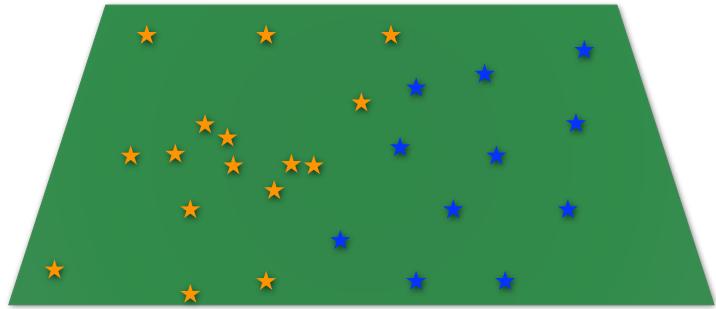
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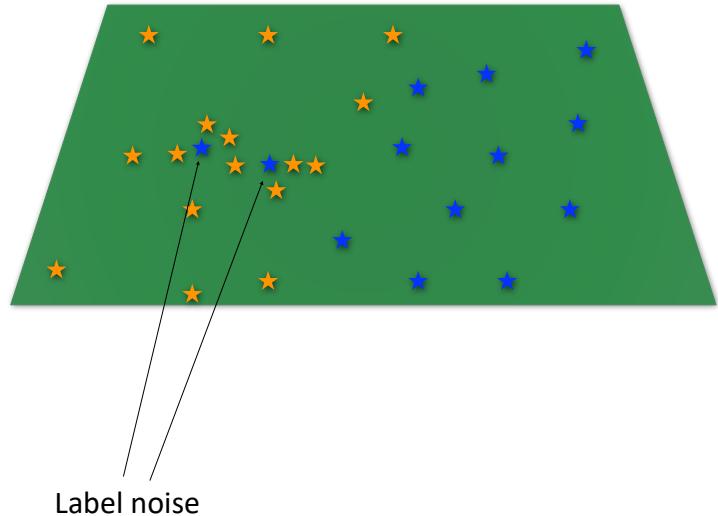
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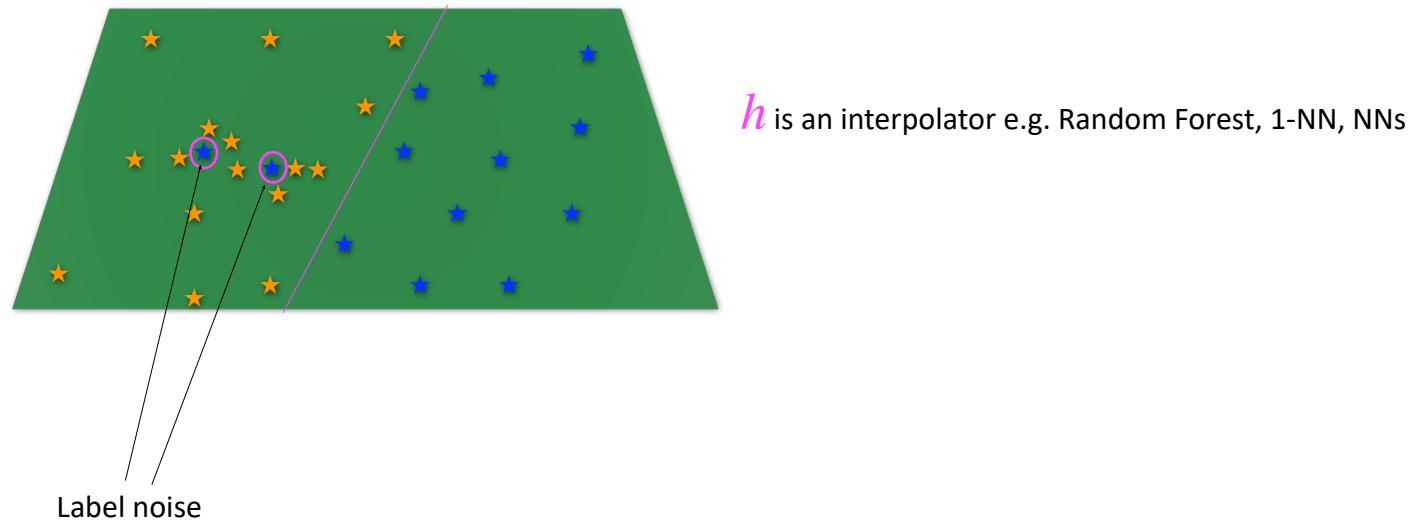
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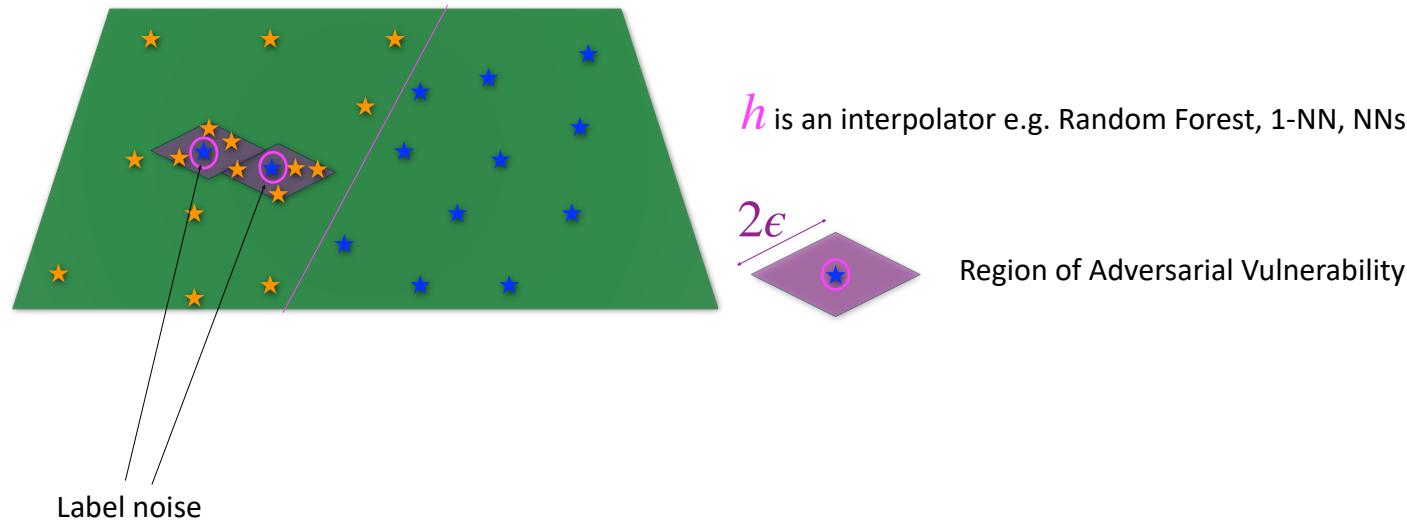
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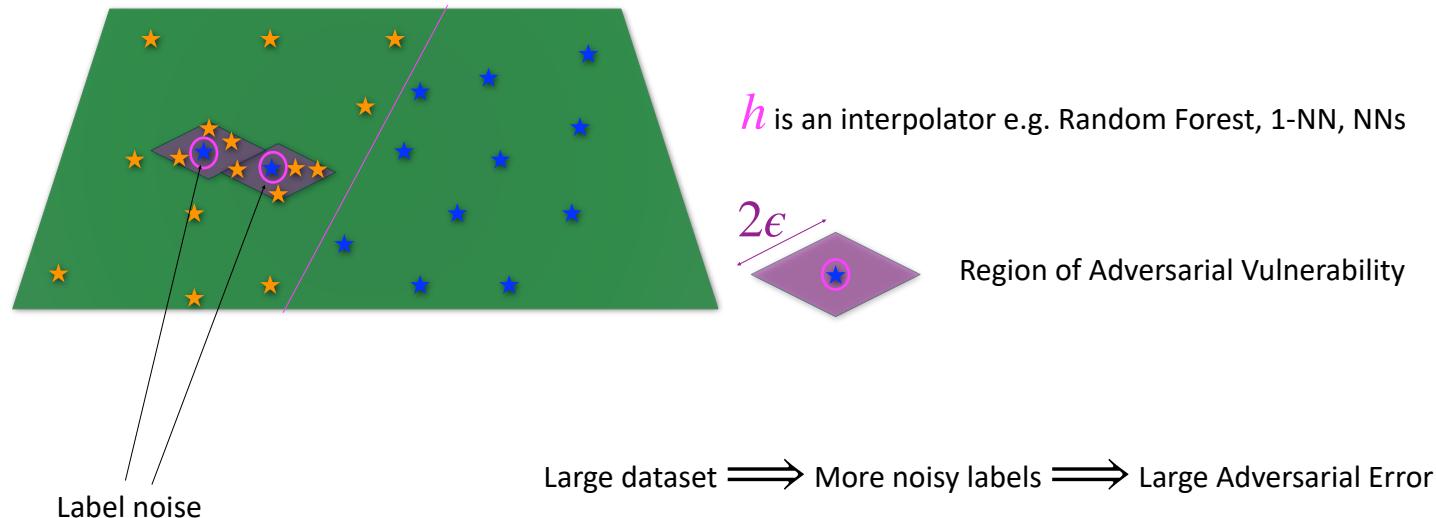
Lower bound on Adversarial error



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Lower bound on Adversarial error



Adversarial training

Towards Deep Learning Models Resistant to Adversarial Attacks

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Adversarial training

Adversarial Training replaces (or augments) clean data with corresponding adversarial examples during SGD.

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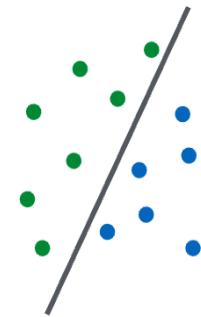
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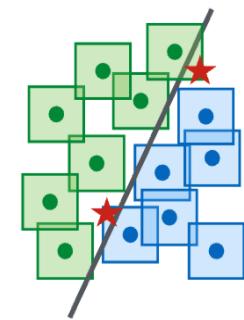
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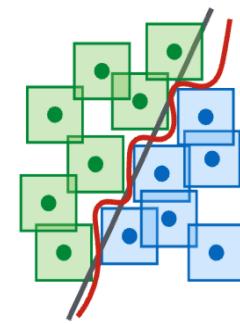
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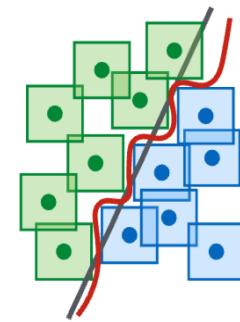
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Naturally, complex models can fit the augmented data better.



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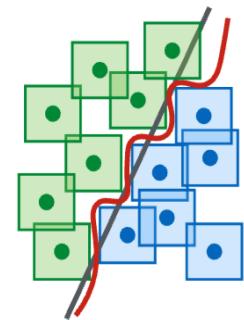
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Robust overfitting is when train robust error decreases but test robust error increases.

Overfitting in adversarially robust deep learning

Leslie Rice *¹ Eric Wong *² J. Zico Kolter¹

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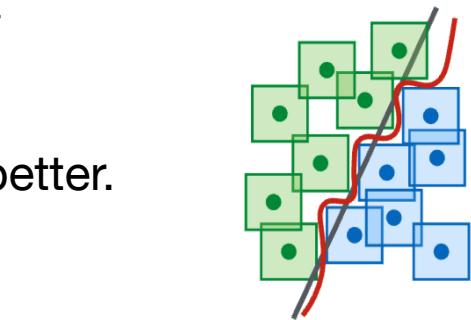
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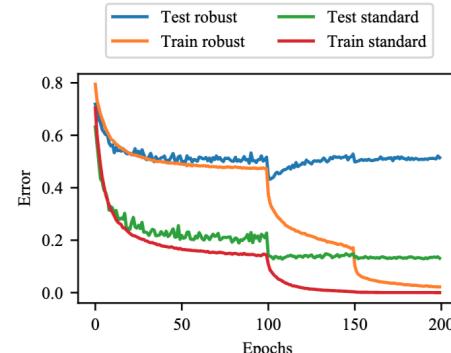
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Robust Overfitting and label noise

Label Noise in Adversarial Training: A Novel Perspective to Study Robust Overfitting

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Robust Overfitting and label noise

- One of explanations given for Robust overfitting is that adversarial training implicitly adds label noise.

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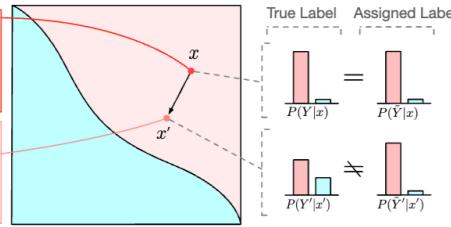
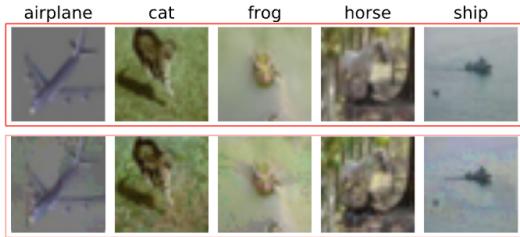
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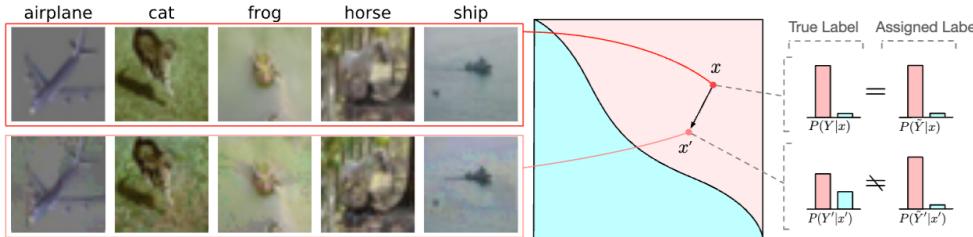
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Data Quality Matters For Adversarial Training: An Empirical Study

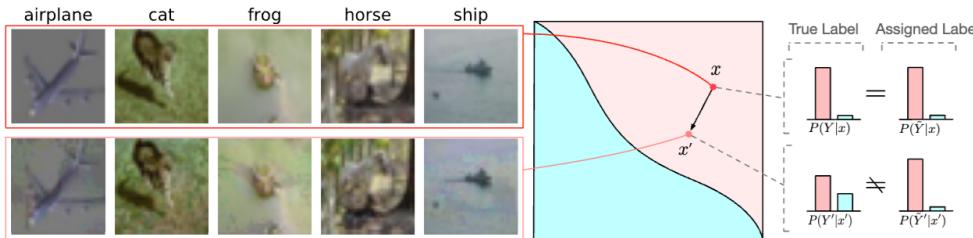
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- Larger perturbation radius causes more overfitting

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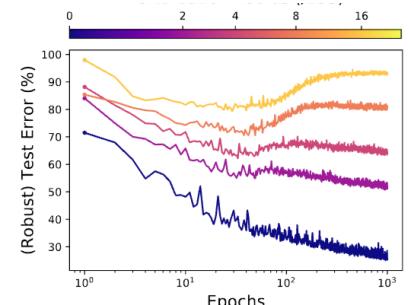
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Improving Robust generalisation

Adversarially Robust Generalization Requires More Data

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Interpolation can hurt robust generalization even when
there is no noise

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Reinhard Heckel^{2,3} and Fanny Yang¹

¹*ETH Zurich*, ²*Rice University*, ³*Technical University of Munich*

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Exists simple distribution in d dim where robust generalisation requires \sqrt{d} times more data.

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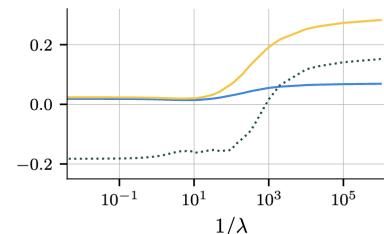
Aleksander Madry
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Interpolation can hurt robust generalization even when there is no noise

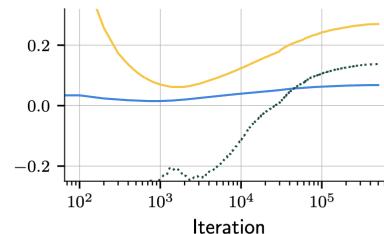
Konstantin Donhauser^{*1}, Alexandru Tifrea^{*1}, Michael Aerni¹
Reinhard Heckel^{2,3} and Fanny Yang¹

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— Standard risk — Robust risk ... Normalized robust margin



(a) Benefit of ridge regularization

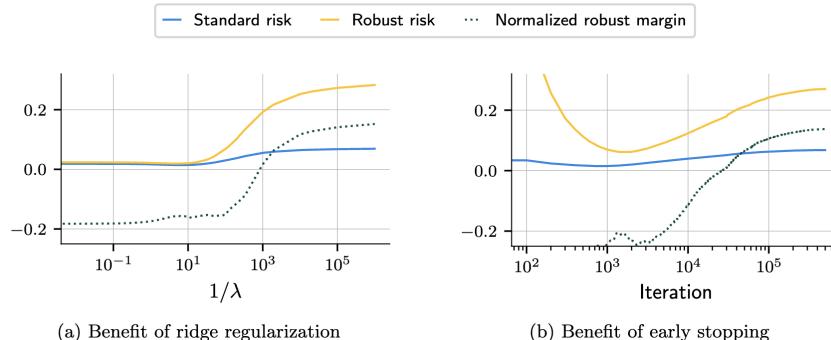
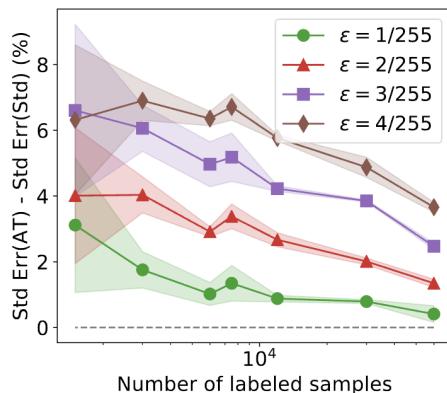


(b) Benefit of early stopping

Improving Robust generalisation

Exists simple distribution in d dim where robust generalisation requires \sqrt{d} times more data.

- Clearly, more data helps to avoid robust overfitting
- Regularisation and early-stopping also helps.



Adversarially Robust Generalization Requires More Data

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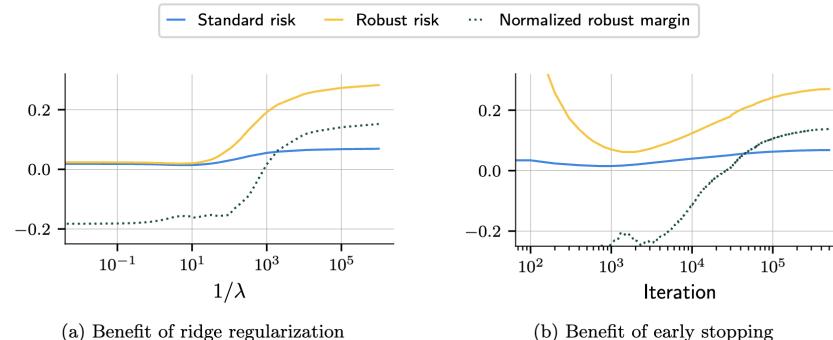
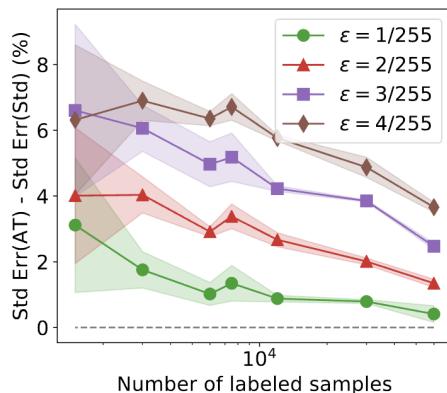
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What about unlabelled data ?

Improving Robust generalisation

With unlabelled data

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REQUIRES MORE UNLABELED DATA

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Unlabeled Data Improves Adversarial Robustness

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Recipe: Use adversarial training on pseudo-labels on the unlabelled data

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Improving Robust generalisation

With unlabelled data

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Method	Robust Test Acc.	Standard Test Acc.
Standard Training	0.8%	95.2%
PG-AT (Madry et al., 2018)	45.8%	87.3%
TRADES (Zhang et al., 2019)	55.4%	84.0%
Vanilla Supervised		
Standard Self-Training	0.3%	96.4%
Robust Consistency Training (Carmon et al., 2019)	56.5%	83.2%
Semisupervised with same unlabeled data		
RST + PG-AT (this paper)	58.5%	91.8%
RST + TRADES (this paper) (Carmon et al., 2019)	63.1%	89.7%

Understanding and Mitigating the Tradeoff Between Robustness and Accuracy

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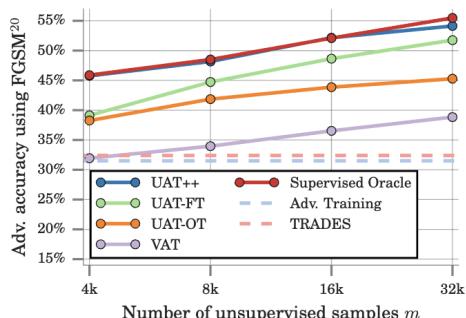
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Are Labels Required for Improving Adversarial Robustness?

Jonathan Uesato* Jean-Baptiste Alayrac* Po-Sen Huang*

Robert Stanforth Alhussein Fawzi Pushmeet Kohli

DeepMind
{juesato,jalayrac,poeshuang}@google.com

Distributional Robustness in Machine Learning

Robustness to Distribution Shift

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- **Adversarial Robustness** measures performance against the worst shift between train and test set.

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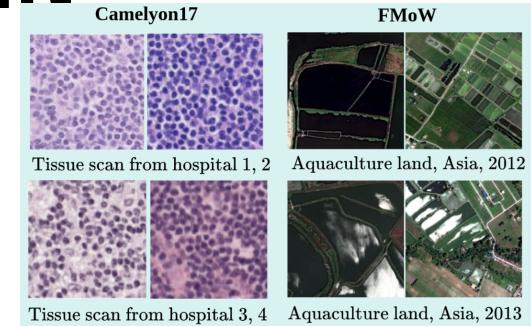
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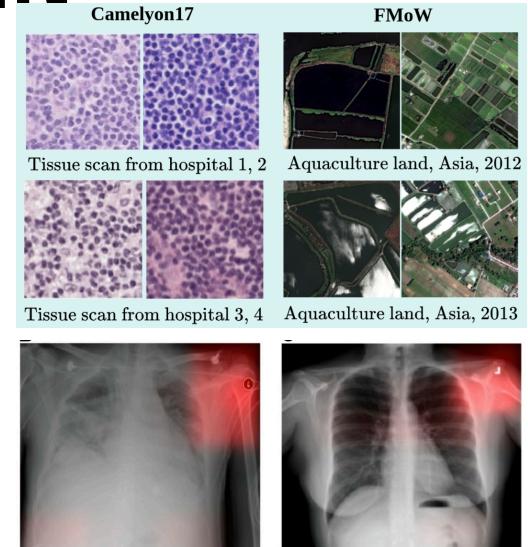
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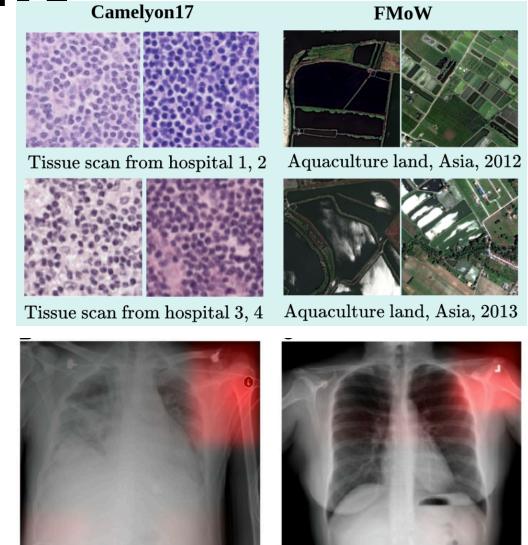
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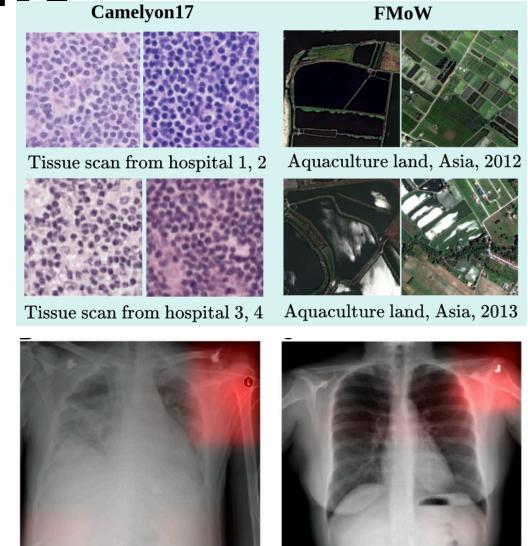
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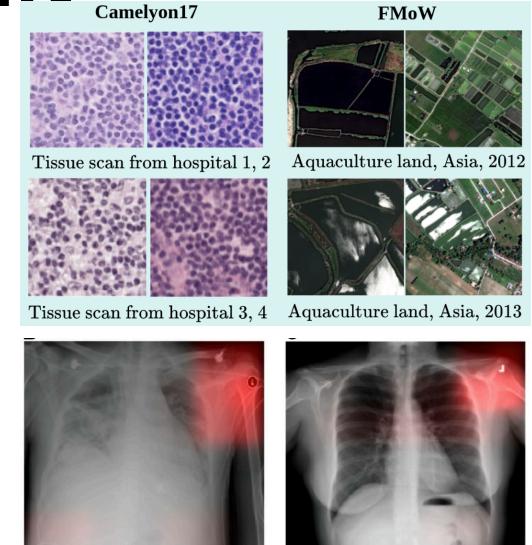
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- Goal is to allow for a graceful degradation with increasing shift



Robustness to Distribution Shift

Rich body of existing literature

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We will not even attempt to be exhaustive

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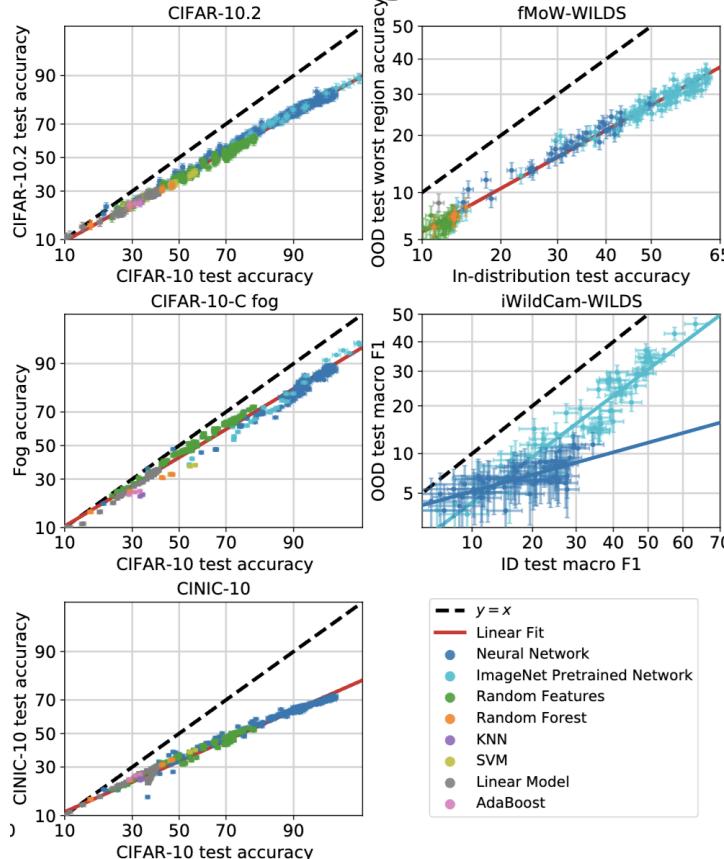
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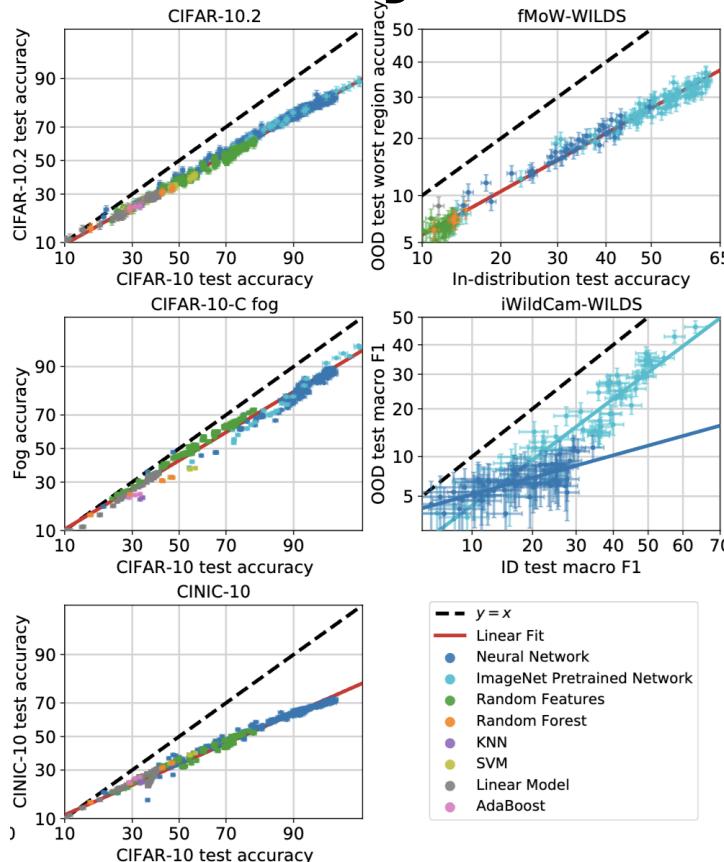
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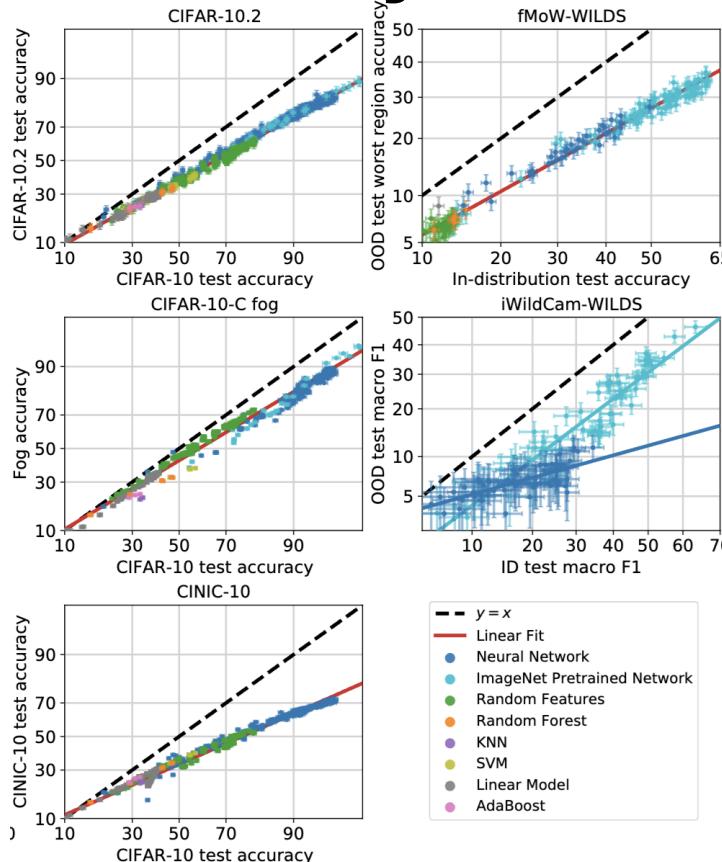


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Shiori Sagawa† Pang Wei Koh† Vaishaal Shankar* Percy Liang†
Yair Carmom‡ Ludwig Schmidt§

- **Accuracy-on-the-line phenomenon:** ID and OOD accuracy are positively correlated.

Accuracy-on-the line

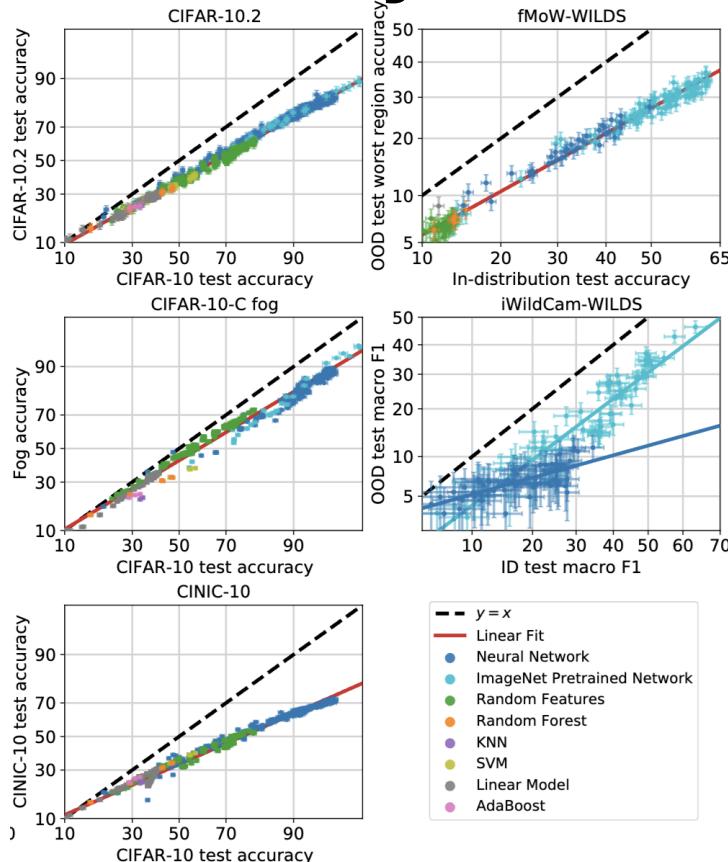


Accuracy on the Line: On the Strong Correlation
Between Out-of-Distribution and In-Distribution Generalization

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- Indicates that improving ID accuracy also improves OOD accuracy.

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- **Accuracy-on-the-line phenomenon:** ID and OOD accuracy are positively correlated.
- Indicates that improving ID accuracy also improves OOD accuracy.
- Holds for a wide variety of models and datasets

Label Noise and Distribution Shift

Accuracy on the wrong line: On the pitfalls of noisy data for
out-of-distribution generalisation

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- Question: Is **Accuracy-on-the-line** robust to noisy or low quality labels ?

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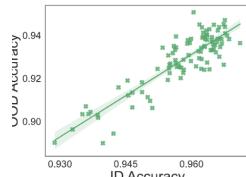
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Label Noise and Distribution Shift

- Question: Is **Accuracy-on-the-line** robust to noisy or low quality labels ?



(b) Noiseless dataset

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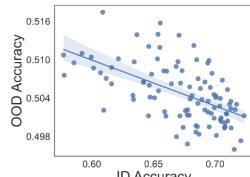
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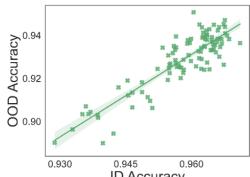
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Label Noise and Distribution Shift

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(a) Noisy dataset



(b) Noiseless dataset

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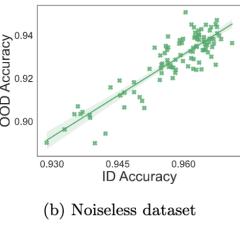
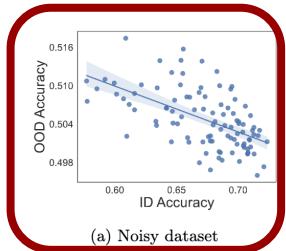
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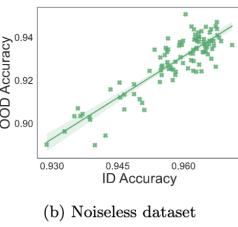
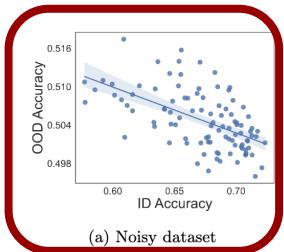
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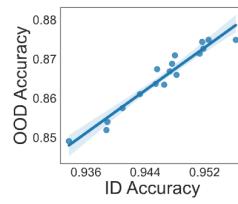
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Accuracy-on-the-wrong line



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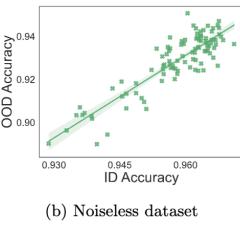
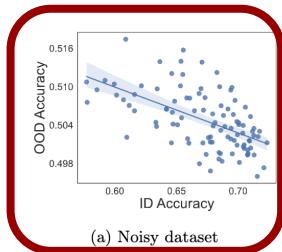
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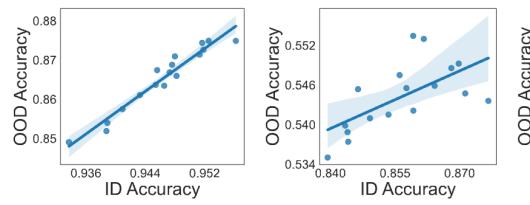
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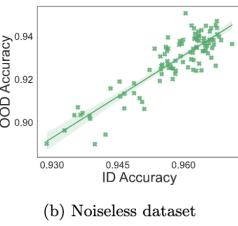
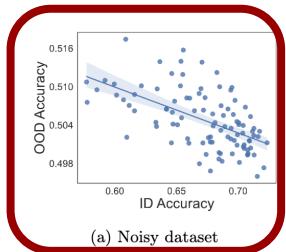
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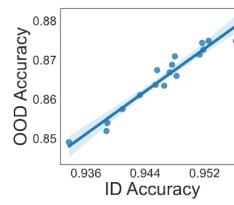
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Label Noise and Distribution Shift

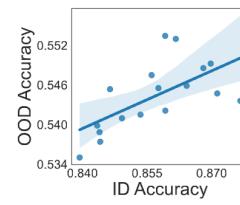
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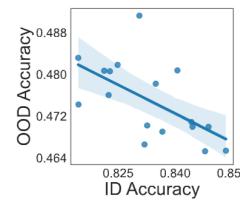
Accuracy-on-the-wrong line



(a) $\eta = 0.$



(b) $\eta = 0.15$



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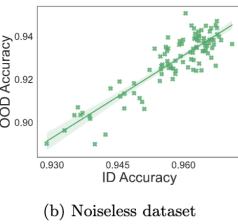
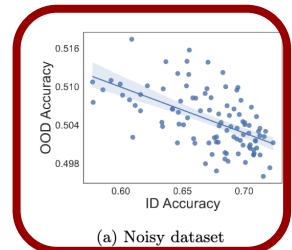
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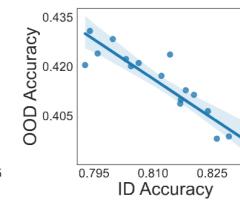
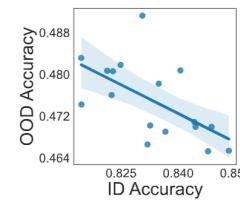
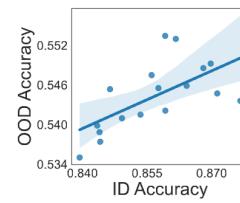
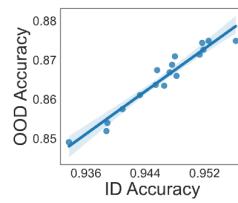
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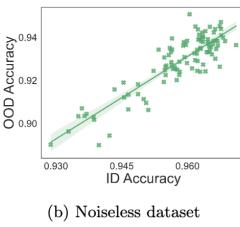
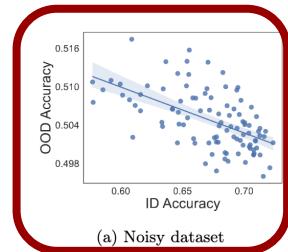
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Accuracy-on-the-wrong line

Two sufficient factors for Accuracy-on-the-wrong-line

Accuracy on the wrong line: On the pitfalls of noisy data for out-of-distribution generalisation

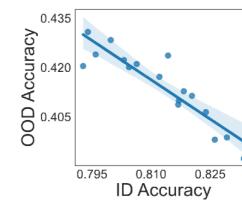
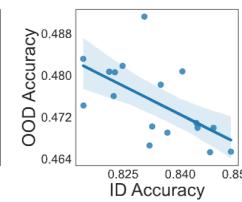
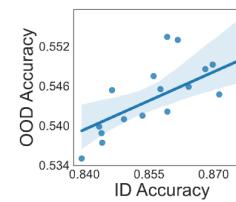
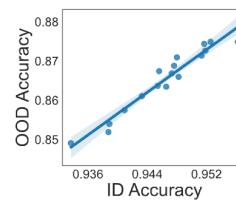
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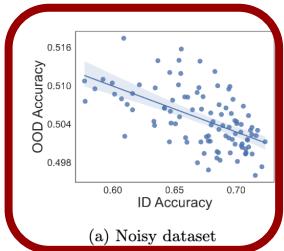
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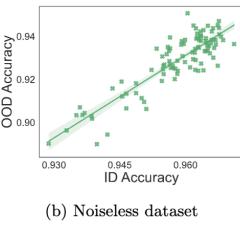
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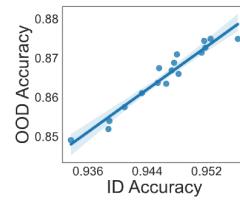
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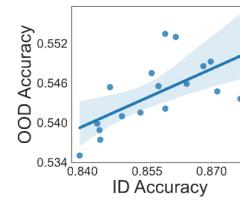
(a) Noisy dataset



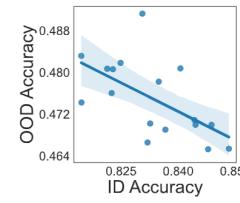
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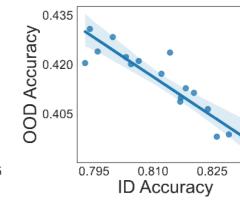
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Accuracy-on-the-wrong line

Two sufficient factors for Accuracy-on-the-wrong-line

- Inject and fit **random label noise** in the training data
- Presence of multiple “**nuisance features**” i.e. irrelevant features

Theory

Theory

Let the data satisfy the following

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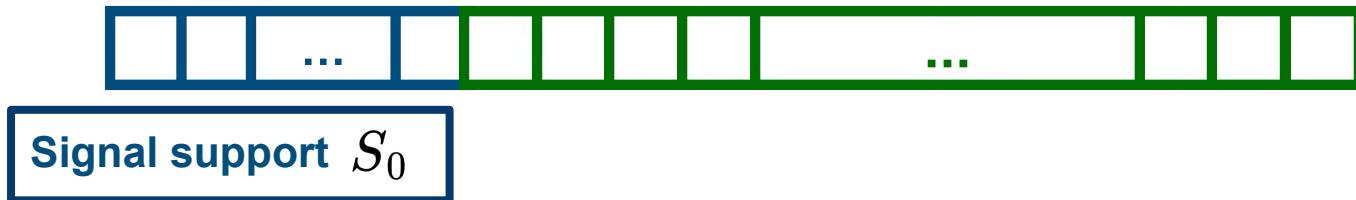
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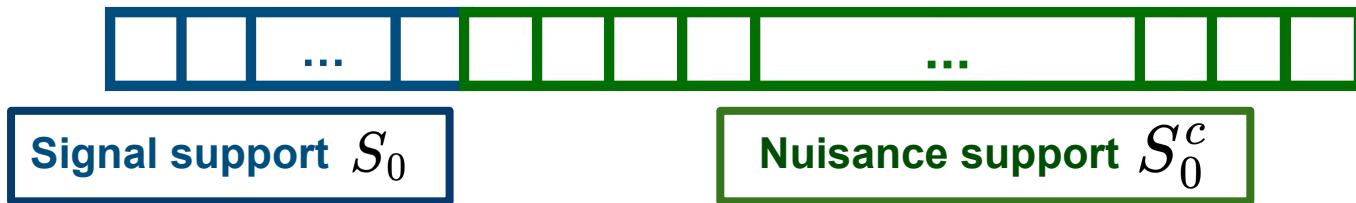
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Signal support S_0

Nuisance support S_0^c

Data is labelled as $y = \langle \theta^*, x \rangle$
where θ^* is supported on S_0

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S_0 - oblivious shift distribution Δ only
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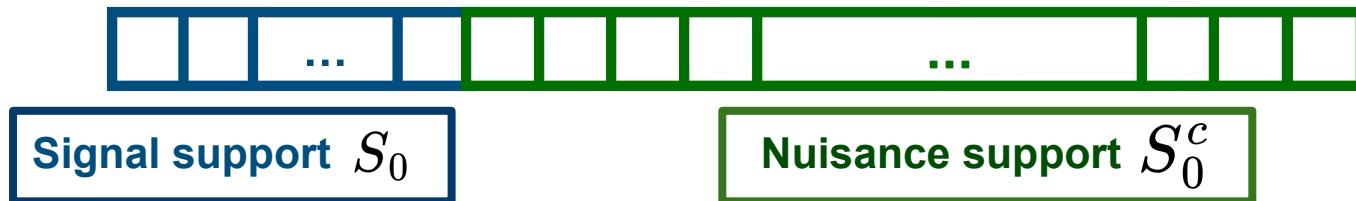
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Informal Theorem For all x s.t. $\langle \theta^*, x \rangle > 0$, we have

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Informal Theorem For all x s.t. $\langle \theta^*, x \rangle > 0$, we have

$$\Pr_{\delta \sim \Delta} [\langle \hat{\theta}, x + \delta \rangle < 0] \geq 1 - \exp(-|S_0^c|\tau^2)$$

Using unlabelled data

HOW ROBUST IS UNSUPERVISED REPRESENTATION
LEARNING TO DISTRIBUTION SHIFT?

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Using unlabelled data

- **Pre-trained representations** are a common strategy against this problem.
- But representations from supervised training often suffer from problems like **simplicity bias**.

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Solution - Use **Unlabelled data** & **unsupervised representation** learning

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Experimental setup

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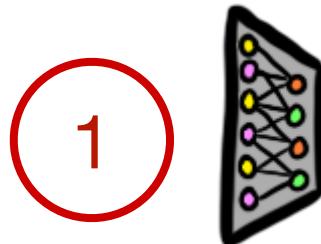
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Pre-train representation learning on **ID data**
with labelled (SL) or unlabelled data (AE/SSL)

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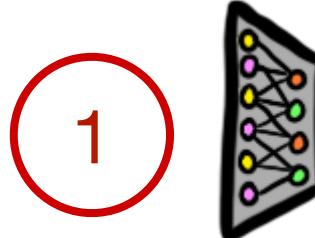
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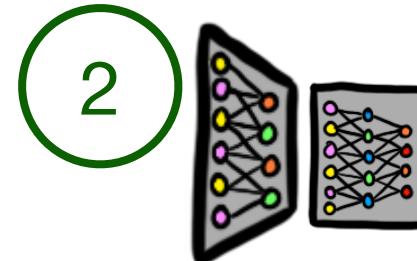
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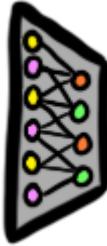
Pre-train representation learning on **ID data** with labelled (SL) or unlabelled data (AE/SSL)

Train a small ML model on top of the features using **Dist X (ID or OOD)**



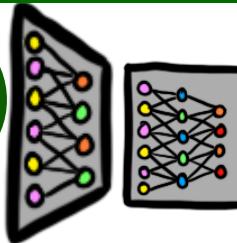
Using unlabelled data

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Train a small ML model on top of the features using **Dist X**

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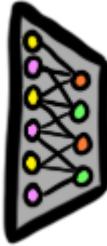
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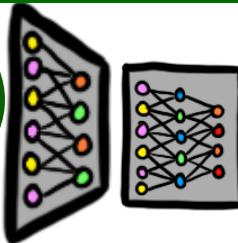
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Train a small ML model on top of the features using Dist X

2



Pre-train representation learning on ID data with labelled (SL) or unlabelled data (AE/SSL)

Dist X → OOD. Test on OOD.

HOW ROBUST IS UNSUPERVISED REPRESENTATION LEARNING TO DISTRIBUTION SHIFT?

Yuge Shi*

Department of Engineering Science
University of Oxford

Imant Daunhawer & Julia E. Vogt

Department of Computer Science
ETH Zurich

Philip H.S. Torr

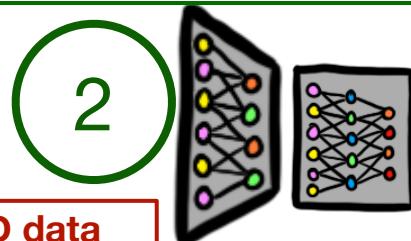
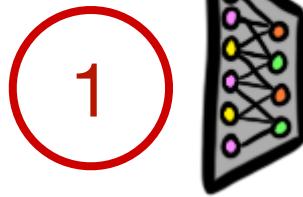
Department of Engineering Science
University of Oxford

Amartya Sanyal

Department of Computer Science & ETH AI Center
ETH Zurich

Using unlabelled data

Train a small ML model on top of the features using Dist X



Pre-train representation learning on ID data
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How robust is unsupervised representation learning to distribution shift?

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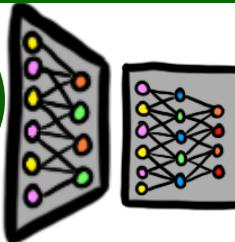
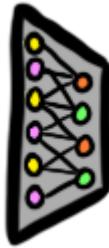
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Shift Sensitivity = Diff between

1. Dist X → OOD. Test on OOD.
2. Dist X → ID. Test on ID.

Captures robustness of

How Robust is Unsupervised Representation Learning to Distribution Shift?

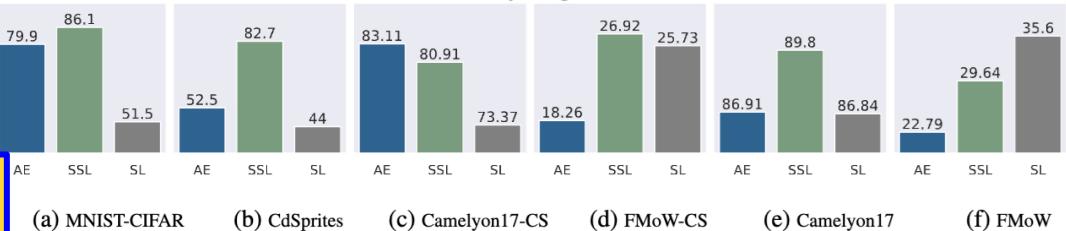
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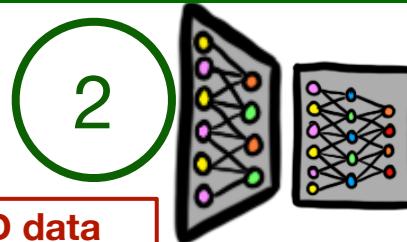
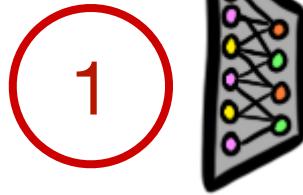
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OOD Accuracy (higher is better)



Using unlabelled data

Train a small ML model on top of the features using Dist X



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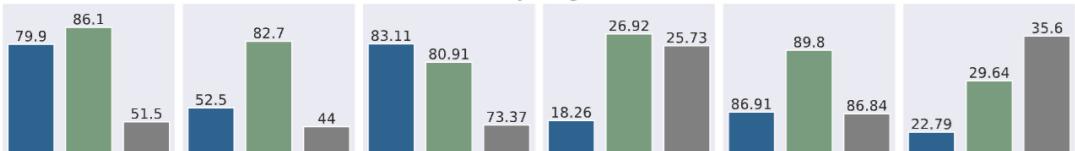
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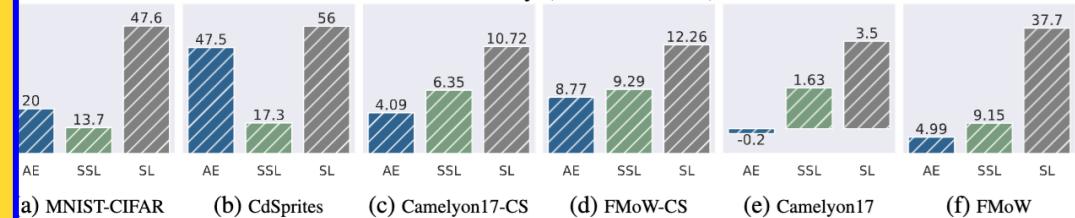
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OOD Accuracy (higher is better)



Shift Sensitivity (lower is better)

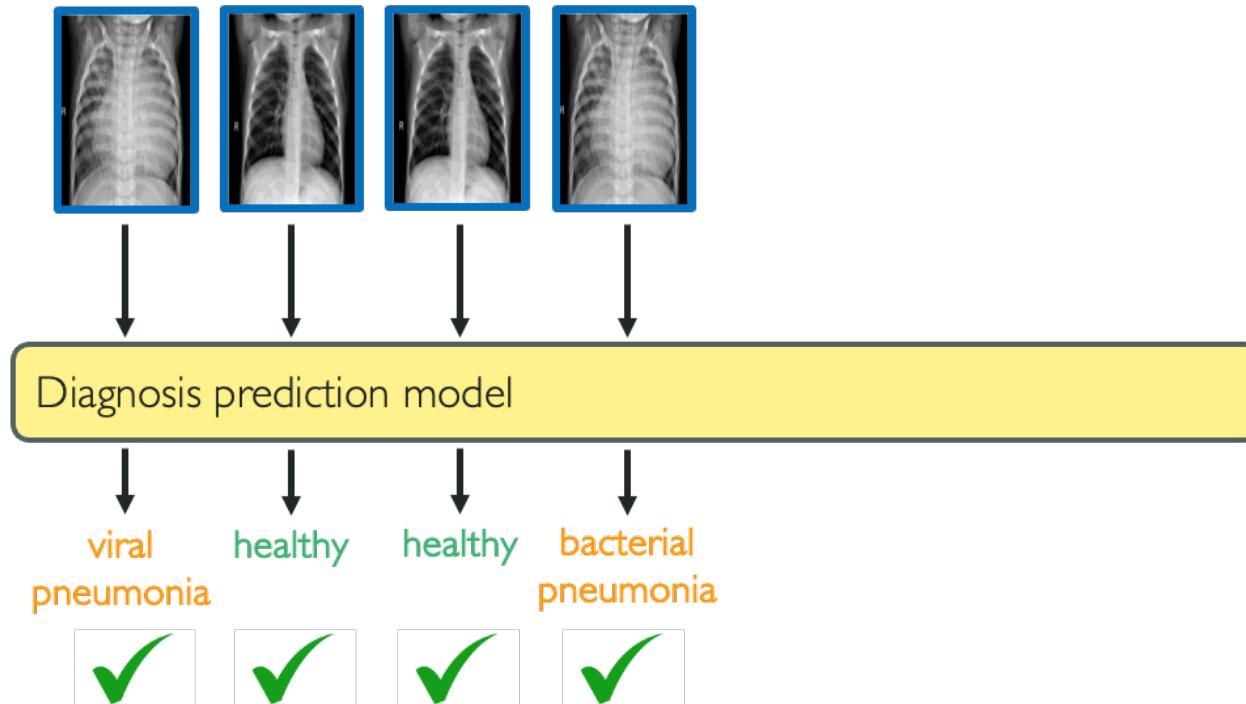


Out-of-distribution detection

**What if we cannot predict reliably
outside of the training distribution?**

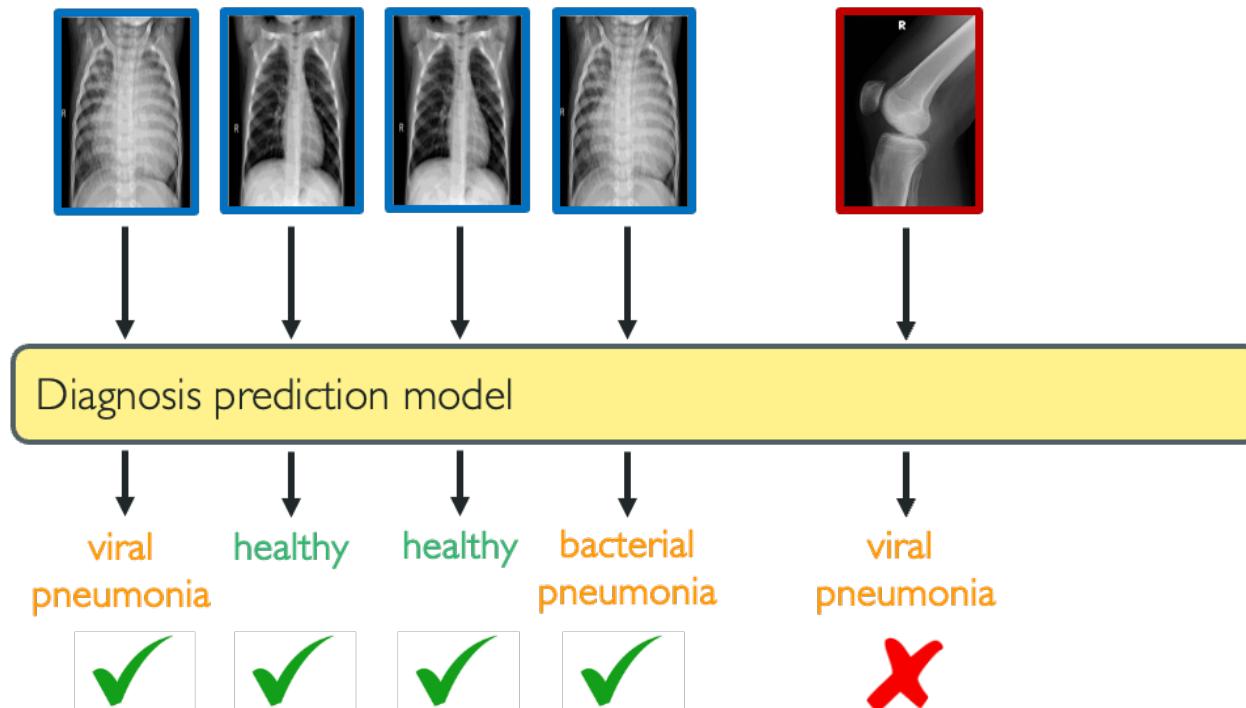
When can't we predict on OOD data?

Novel classes



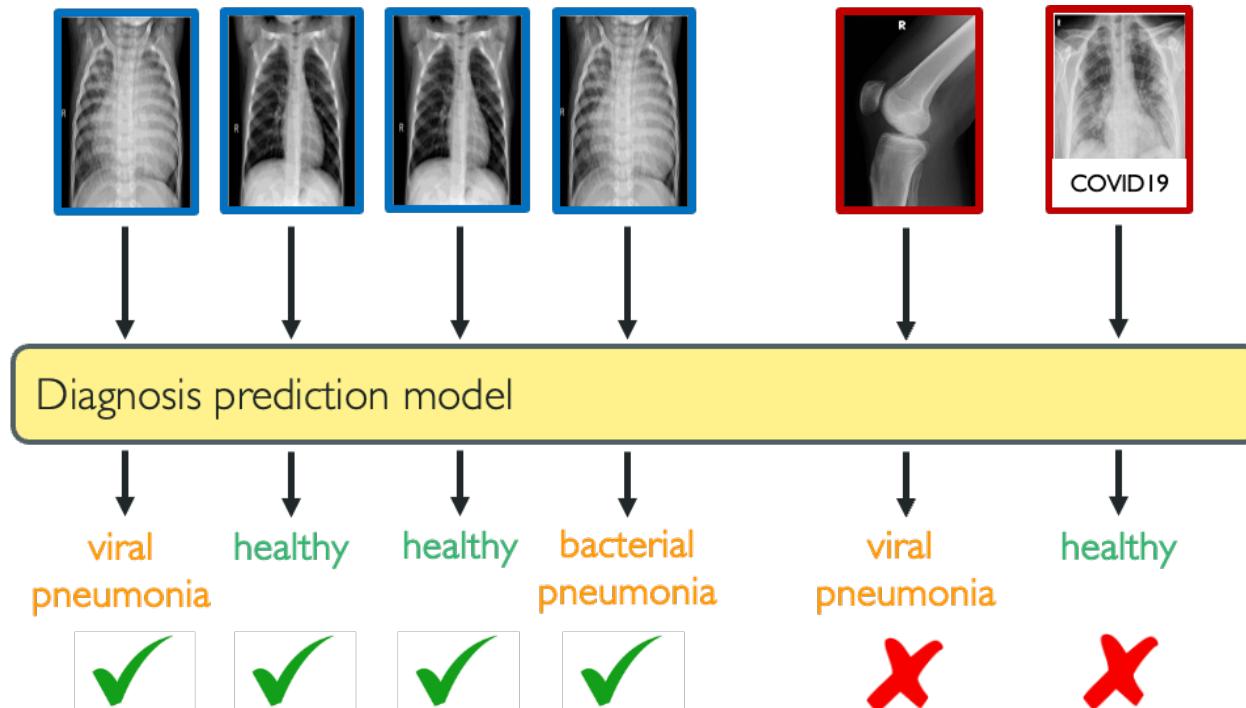
When can't we predict on OOD data?

Novel classes



When can't we predict on OOD data?

Novel classes



When can't we predict on OOD data?

Strong distribution shifts

$\mathbb{P}(X, Y)$ determined by (θ^*, θ_e)

The diagram shows the expression $\mathbb{P}(X, Y) \text{ determined by } (\theta^*, \theta_e)$. Two arrows point from the text "invariant parameters" and "domain-specific parameters" to the respective parameters θ^* and θ_e in the equation.

invariant parameters domain-specific parameters

When can't we predict on OOD data?

Strong distribution shifts

$\mathbb{P}(X, Y)$ determined by (θ^*, θ_e)

invariant
parameters

domain-specific
parameters

$$\theta^*$$

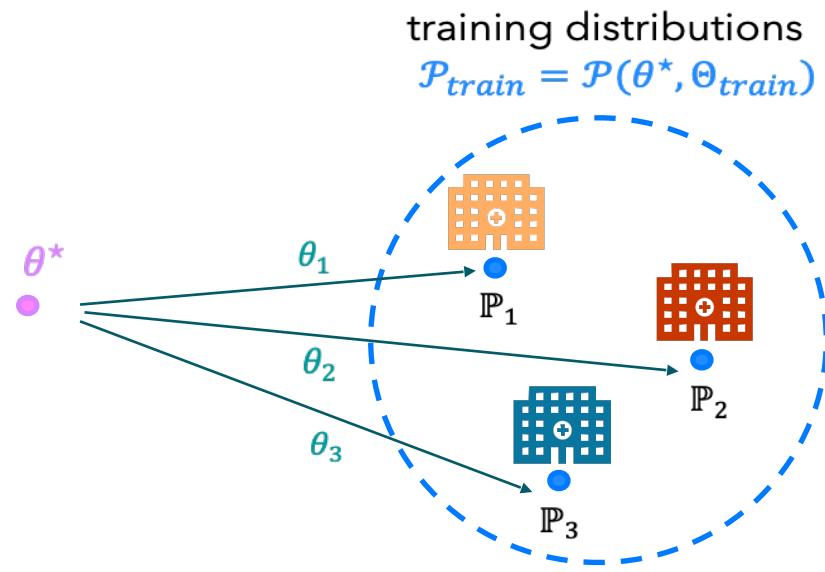

When can't we predict on OOD data?

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When can't we predict on OOD data?

Strong distribution shifts

$\mathbb{P}(X, Y)$ determined by (θ^*, θ_e)

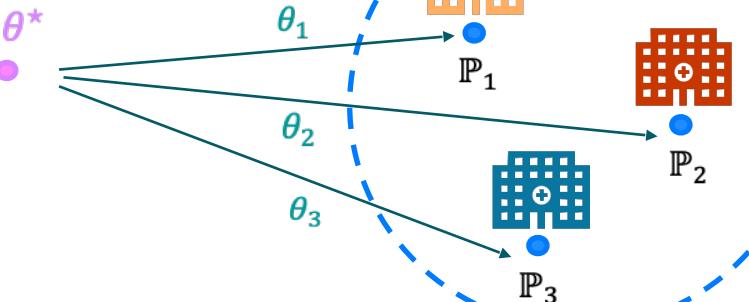
invariant
parameters

domain-specific
parameters

Model
 β

training distributions
 $\mathcal{P}_{train} = \mathcal{P}(\theta^*, \Theta_{train})$

θ^*



When can't we predict on OOD data?

Strong distribution shifts

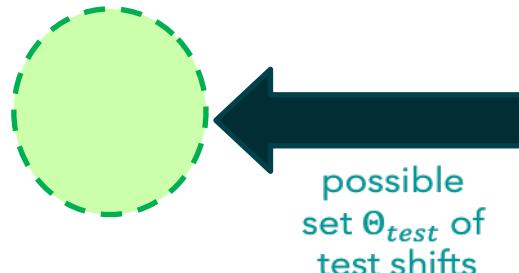
$\mathbb{P}(X, Y)$ determined by (θ^*, θ_e)

invariant
parameters

domain-specific
parameters

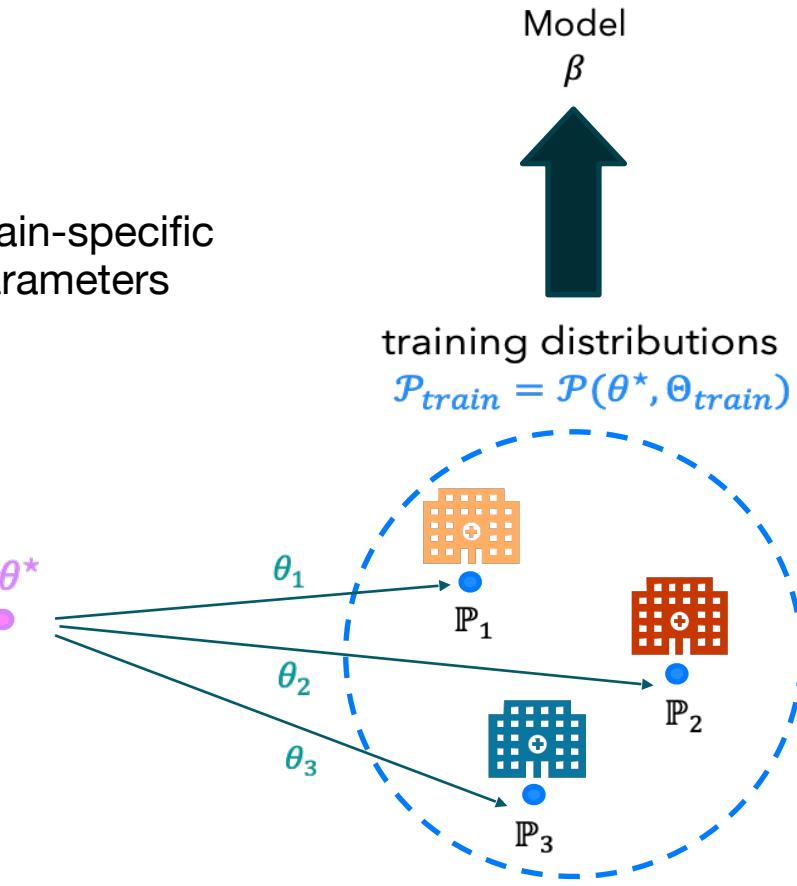
possible test distributions

$$\mathcal{P}_{test} = \mathcal{P}(\theta^*, \Theta_{test})$$



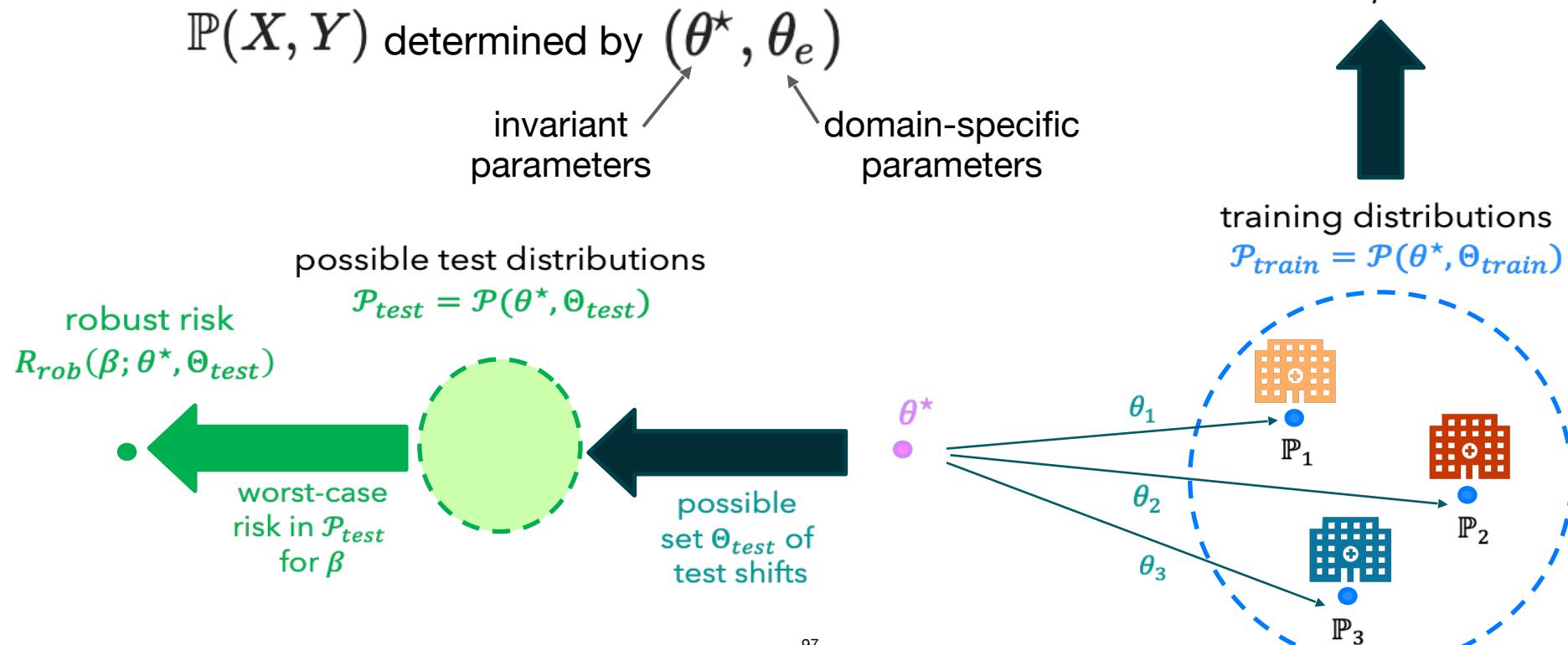
$$\theta^*$$

possible
set Θ_{test} of
test shifts



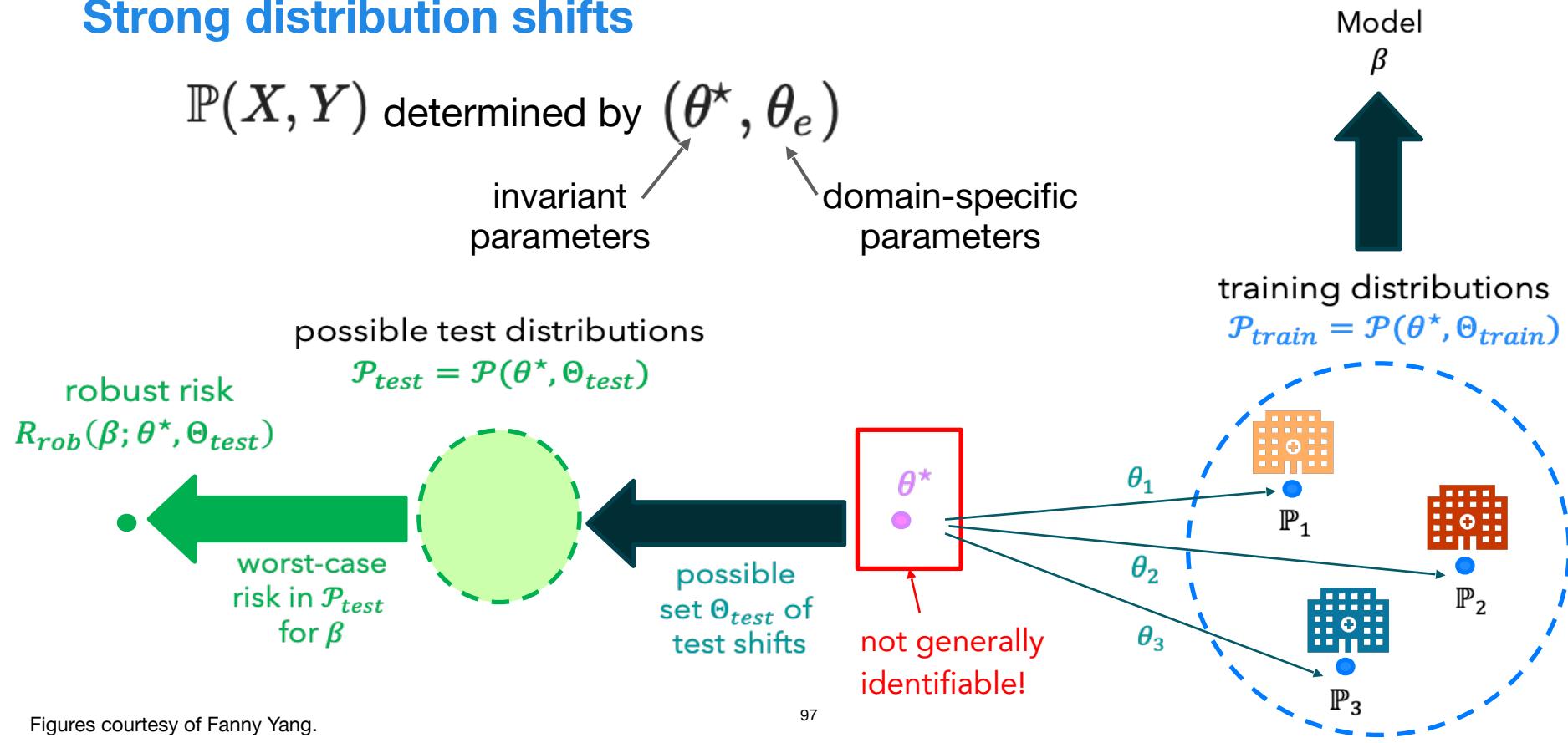
When can't we predict on OOD data?

Strong distribution shifts



When can't we predict on OOD data?

Strong distribution shifts



Impossibility result for distribution shifts

Achievable distributional robustness when the robust risk is only partially identified

Julia Kostin¹, Nicola Gnecco^{*2}, and Fanny Yang¹

¹Department of Computer Science, ETH Zurich

²Department of Mathematics, Imperial College London

Mean shifts during test time assumed to lie in $\Theta_{test} = \{\theta_{test}: \theta_{test}\theta_{test}^\top \leq \gamma M_{seen} + \gamma' M_{unseen}\}$

Test time shifts assumptions

Covariance with range in span of **seen shift directions** $range(M_{seen}) \subset span \{\theta_e\}_{e \in [k]}$

Projection matrix onto **unseen direction**: $range(M_{seen}) \perp span \{\theta_e\}_{e \in [k]}$

Impossibility result for distribution shifts

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Main theoretical result

Information-theoretic lower bound on robust risk.

Corollary

- **No “unseen” shifts:** Existing OOD generalization algorithms (e.g. anchor regression) are optimal.
- **No “seen” shifts:** Anchor regression is not better than ordinary least squares.

**What if we cannot predict reliably
outside of the training distribution?**

What if we cannot predict reliably outside of the training distribution?

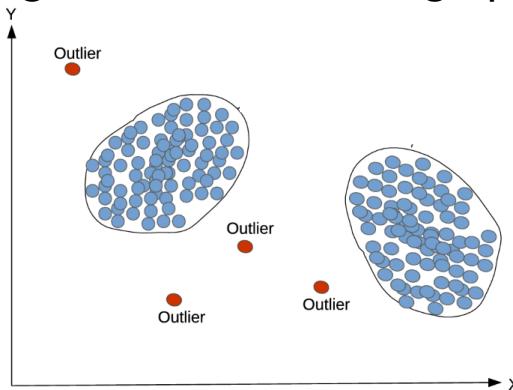
**A: Flag out-of-domain samples
and abstain.**

Traditional OOD detection methods

Unsupervised OOD i.e. only observe in-distribution samples.

Examples:

Density estimation
e.g. in NN embedding space



Predictive uncertainty
e.g. ensembles

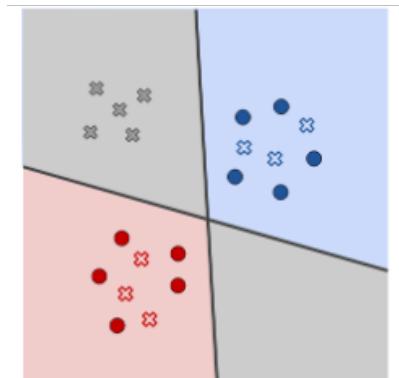


Figure sources: <https://link.springer.com/article/10.1007/s10044-021-00998-6>, <https://arxiv.org/abs/2012.05825>

Limitations of unsupervised OOD detection

Limitations of unsupervised OOD detection

Challenge #1: Unsupervised OOD detection can be ill-defined

Perfect Density Models Cannot Guarantee Anomaly Detection

Charline Le Lan ^{1,2,*} and Laurent Dinh ²

¹ Department of Statistics, University of Oxford, Oxford OX1 3LB, UK
² Google Research, Montreal H3B 2Y5, CA

Limitations of unsupervised OOD detection

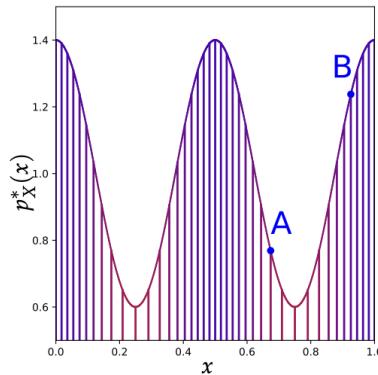
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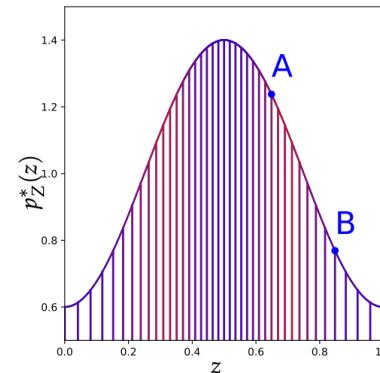
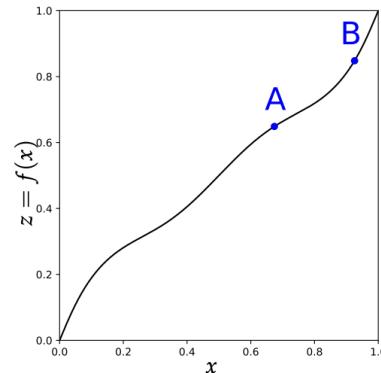
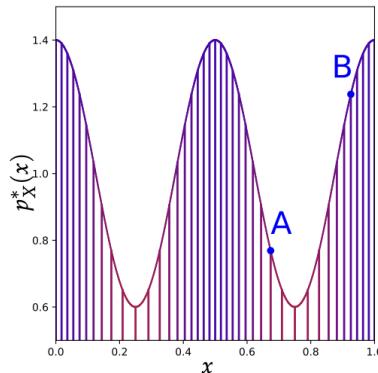
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invertible change of representation

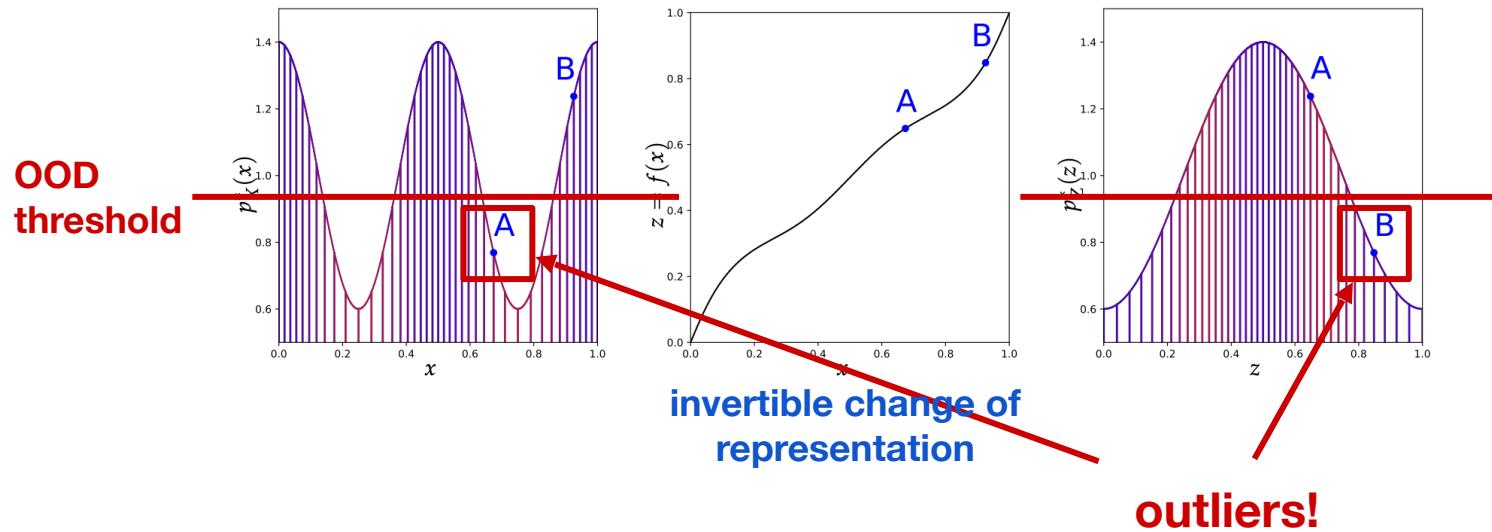
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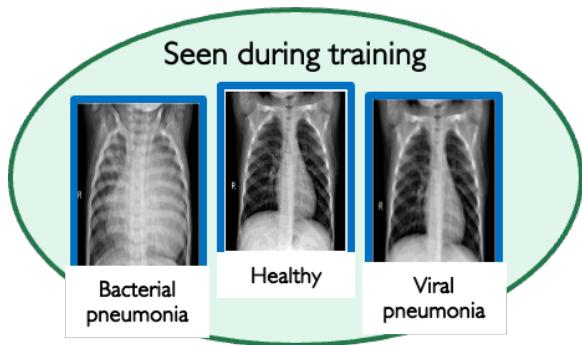
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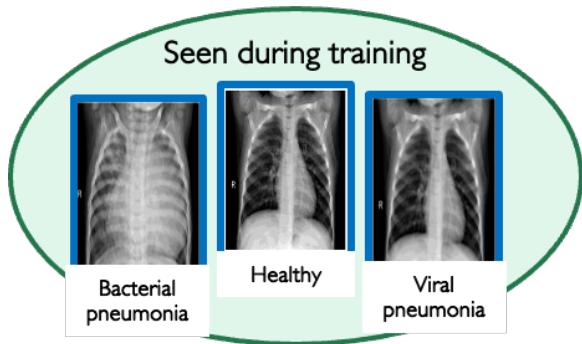
Limitations of unsupervised OOD detection

Challenge #2: finite samples + curse of dimensionality



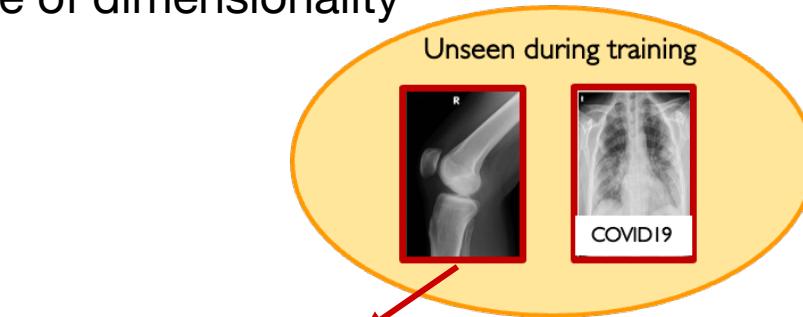
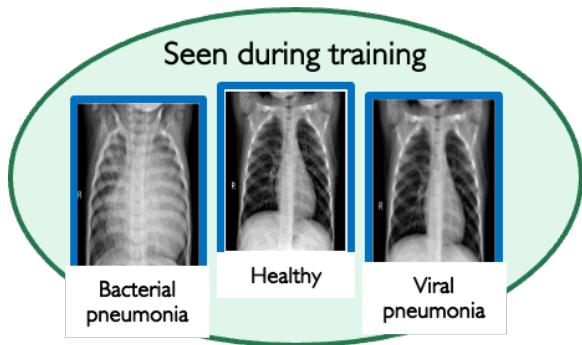
Limitations of unsupervised OOD detection

Challenge #2: finite samples + curse of dimensionality

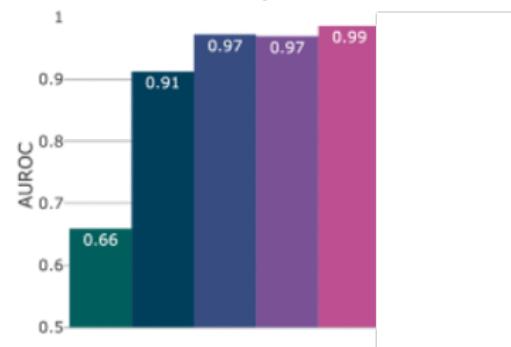


Limitations of unsupervised OOD detection

Challenge #2: finite samples + curse of dimensionality

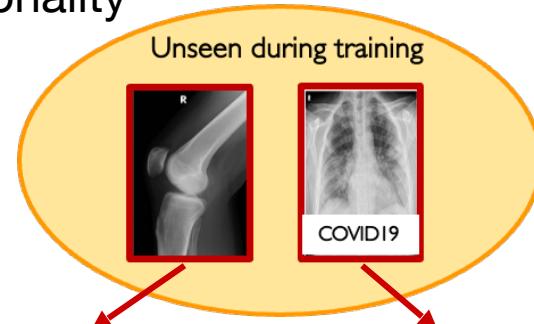
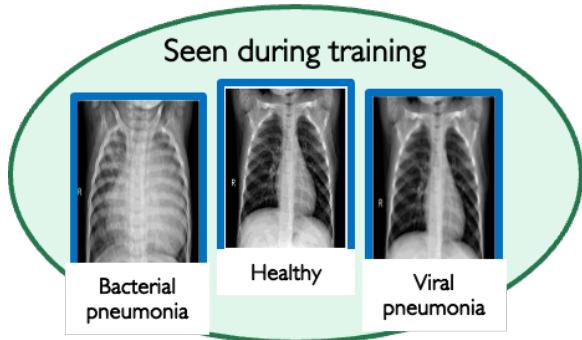


Far OOD (“easy”)
i.e. OOD = new dataset



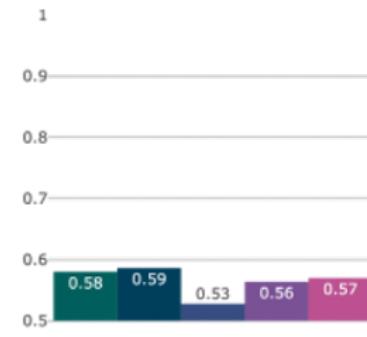
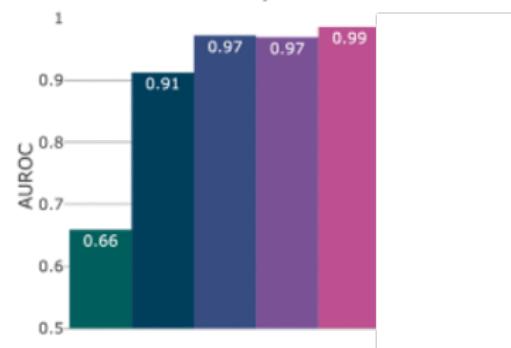
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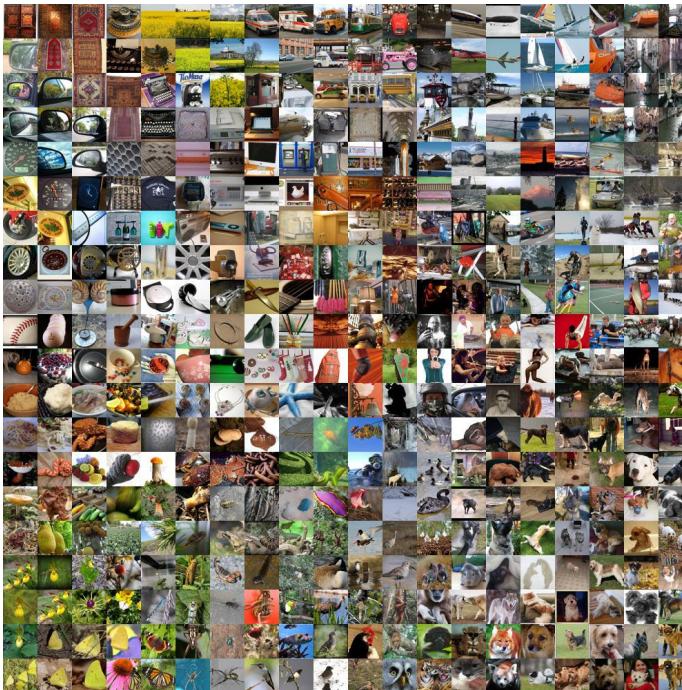
Far OOD (“easy”)
i.e. OOD = new dataset

Near OOD (“hard”)
i.e. OOD = new classes



Diverse pre-training data

Pre-train on ImageNet21k



Exploring the Limits of Out-of-Distribution Detection

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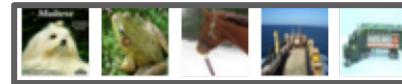
Balaji Lakshminarayanan
Google Research, Brain Team
balajiln@google.com

Diverse pre-training data

Pre-train on ImageNet21k



Fine-tune on CIFAR10



Unsup. method:
Pretrained method:

Outliers: CIFAR100



AUROC
0.80
0.97

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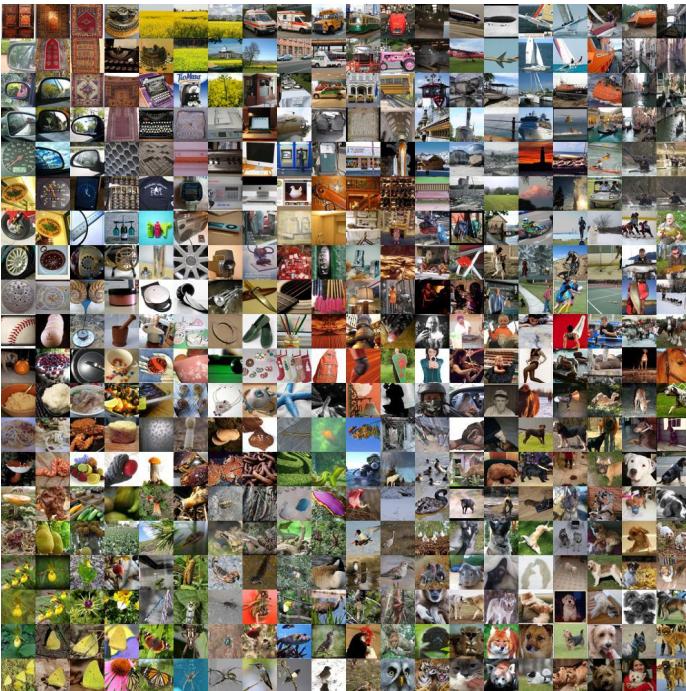
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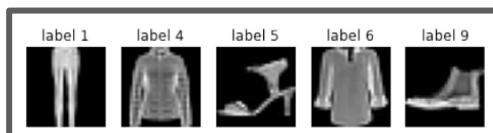
Fine-tune on CIFAR10



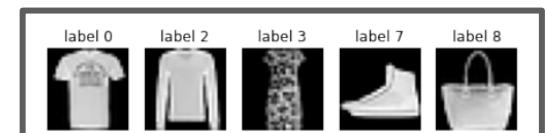
Unsup. method:
Pretrained method:

AUROC
0.80
0.97

Fine-tune on
5-class FashionMNIST



Outliers: remaining
FashionMNIST classes



Unsup. method:
Pretrained method:

AUROC
0.82
0.87

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Using proxy OOD data

Natural proxy OOD data

DEEP ANOMALY DETECTION WITH OUTLIER EXPOSURE

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Mantas Mazeika
University of Chicago
mantas@ttic.edu

Thomas Dietterich
Oregon State University
tgd@oregonstate.edu

Known outliers: TinyImages dataset
(superset of CIFAR10/100)



Synthetic proxy OOD data

CSI: Novelty Detection via Contrastive Learning on Distributionally Shifted Instances

Jihoon Tack^{*†}, Sangwoo Mo^{*‡}, Jongheon Jeong[‡], Jinwoo Shin^{†‡}

^{*}Graduate School of AI, KAIST

[‡]School of Electrical Engineering, KAIST

Known outliers: synthetic image transformations



(a) Original

(b) Cutout

(c) Sobel

(d) Noise

(e) Blur

(f) Perm

(g) Rotate

Using proxy OOD data

DEEP ANOMALY DETECTION WITH
OUTLIER EXPOSURE

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Known outliers: TinyImages dataset
(superset of CIFAR10/100)



In-distribution data:
5-class CIFAR10



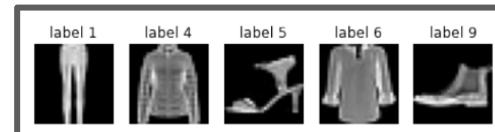
Outliers: remaining
CIFAR10 classes



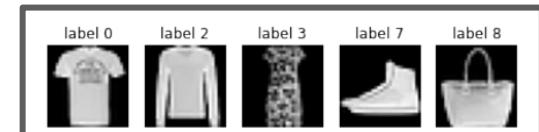
AUROC
0.82

Outlier exposure method:

In-distribution data:
5-class FashionMNIST



Outliers: remaining
FashionMNIST classes



AUROC
0.66

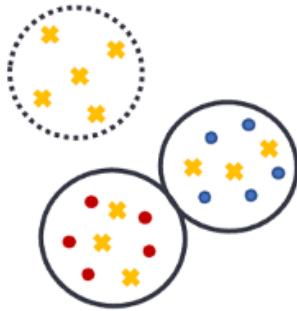
Outlier exposure method:

Semi-supervised OOD detection

Leveraging unlabeled data

Semi-supervised novelty detection using
ensembles with regularized disagreement

Alexandru Tifrea, Eric Stavarache, Fanny Yang
Department of Computer Science
ETH Zurich, Switzerland



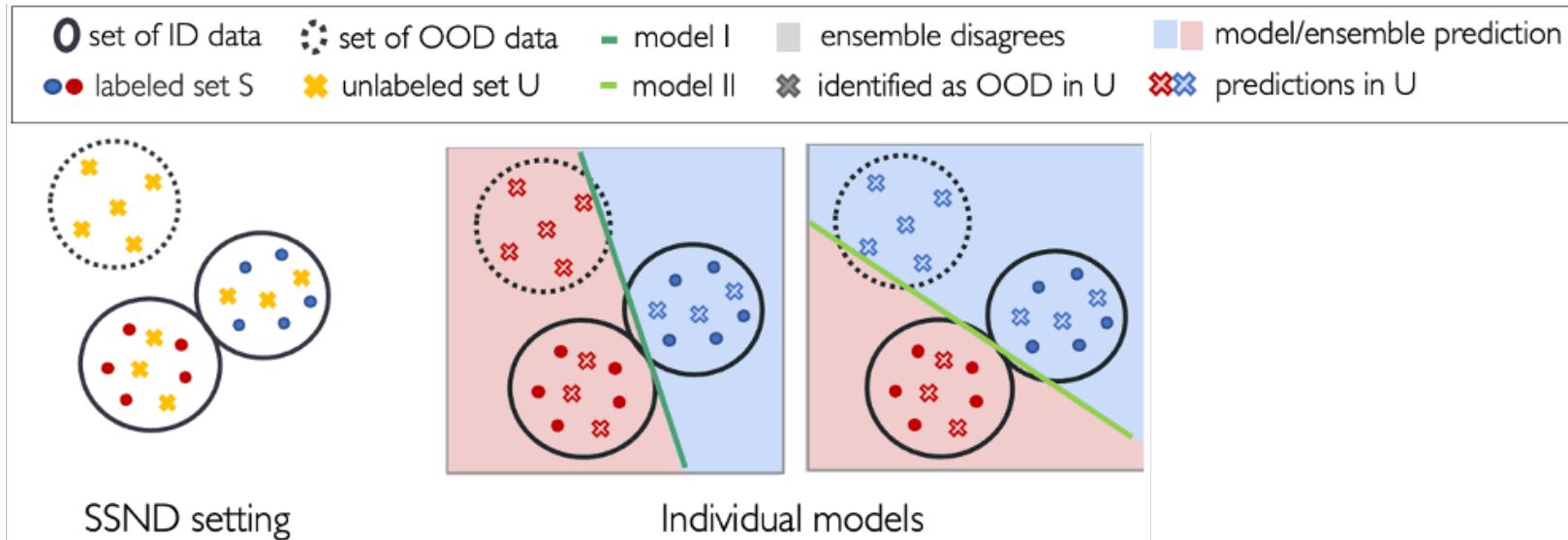
SSND setting

Semi-supervised OOD detection

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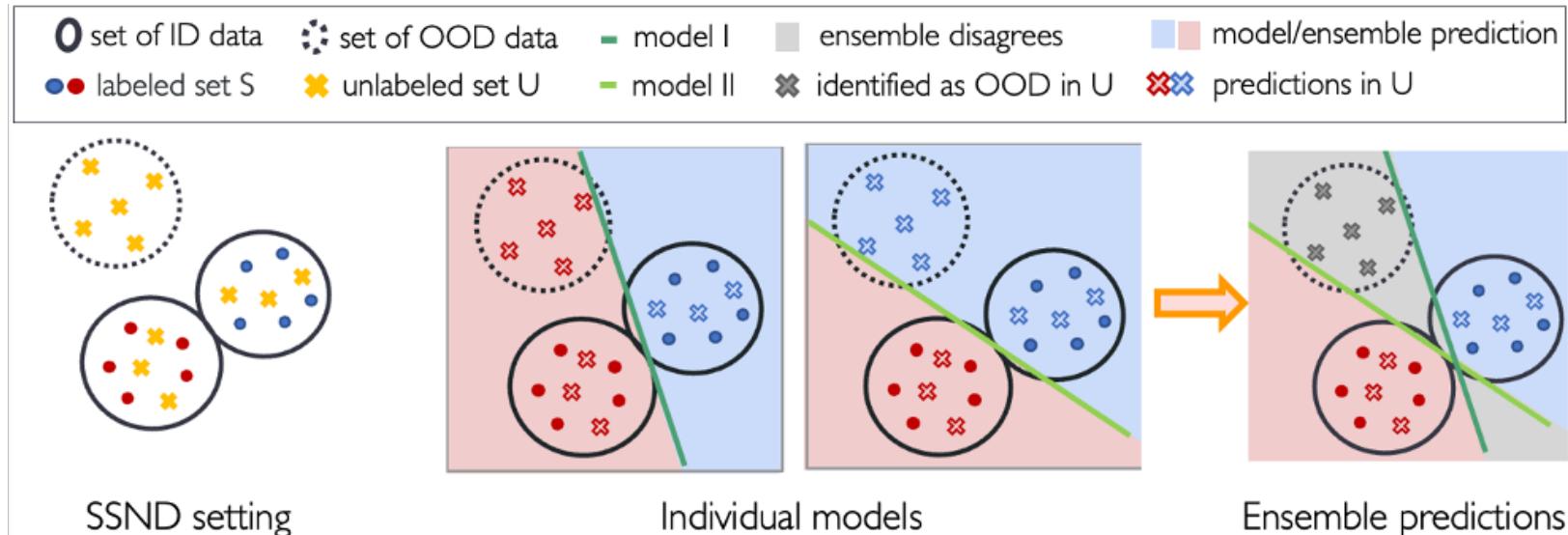


Semi-supervised OOD detection

Leveraging unlabeled data

Semi-supervised novelty detection using ensembles with regularized disagreement

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Department of Computer Science
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sample x is flagged as OOD if “**disagreement**” $>$ threshold

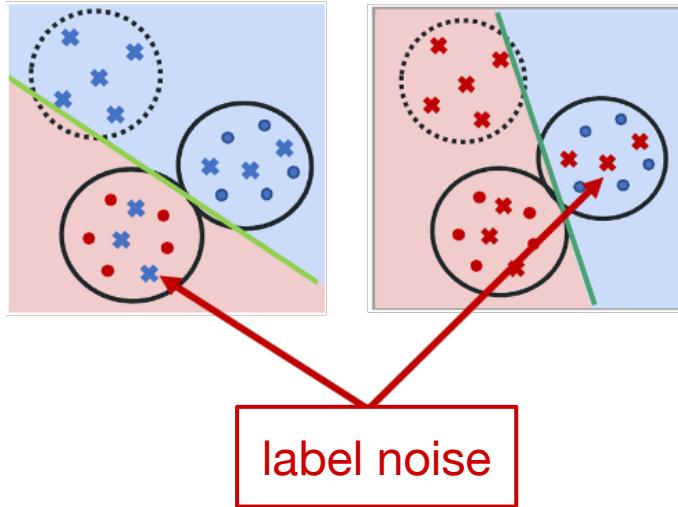
e.g. average pairwise TV distance between predictive distributions of the models in ensemble

Semi-supervised OOD detection

Key ingredient: Appropriate regularization

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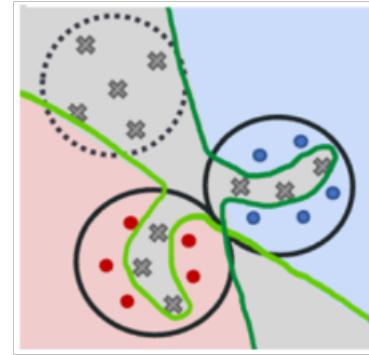
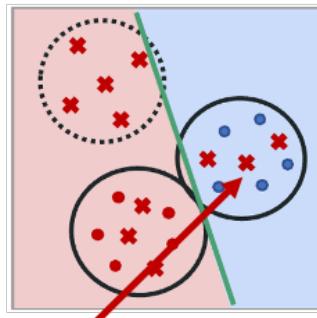
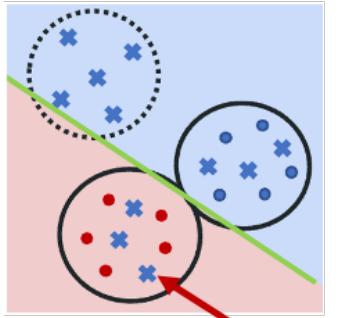


Semi-supervised OOD detection

Key ingredient: Appropriate regularization

Semi-supervised novelty detection using
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label noise

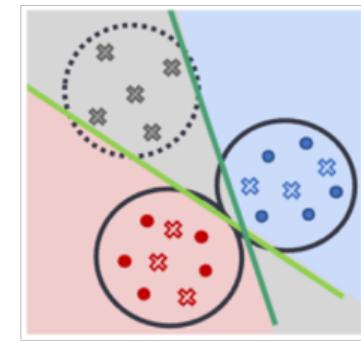
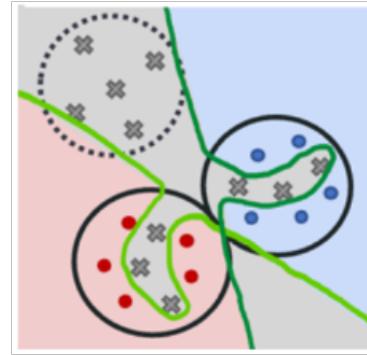
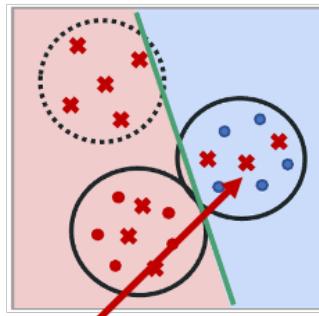
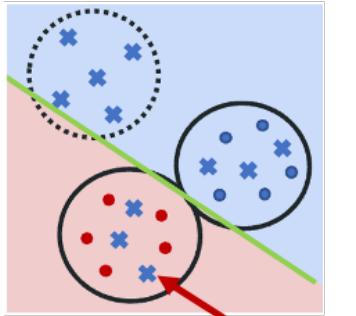
Too much diversity

Semi-supervised OOD detection

Key ingredient: Appropriate regularization

Semi-supervised novelty detection using ensembles with regularized disagreement

Alexandru Tifrea, Eric Stavarache, Fanny Yang
Department of Computer Science
ETH Zurich, Switzerland



label noise

Too much diversity

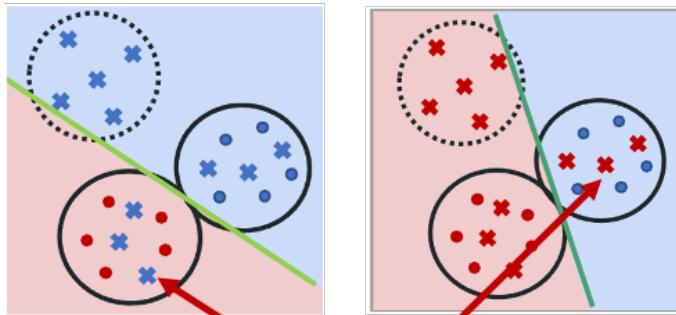
Right amount of diversity

Semi-supervised OOD detection

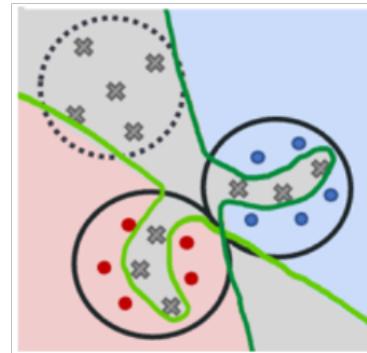
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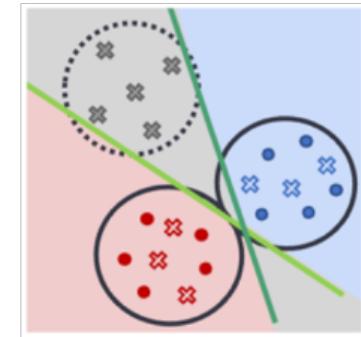
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label noise



Too much diversity



Right amount of diversity

Idea: regularization with strength chosen using ID validation set

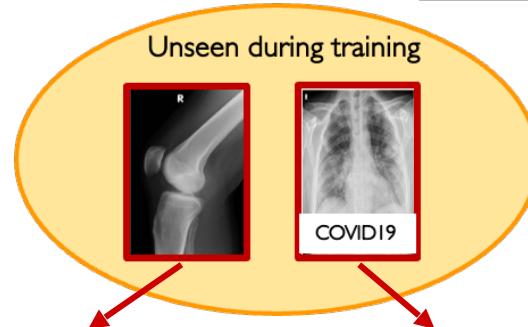
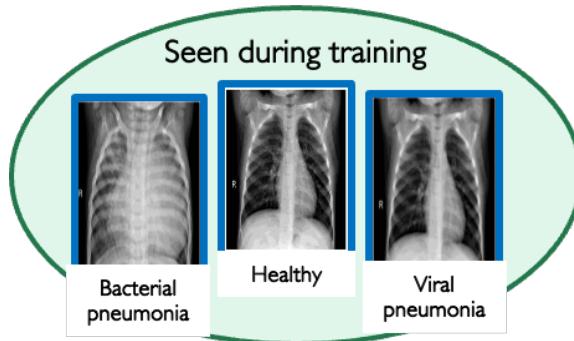
i.e. control FPR (ID samples incorrectly flagged as OOD)

Semi-supervised OOD detection

Performance on near OOD data

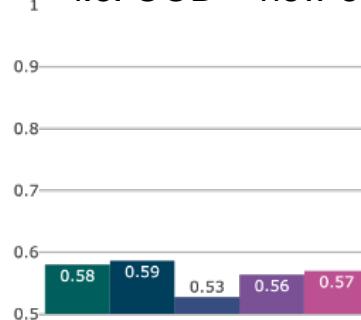
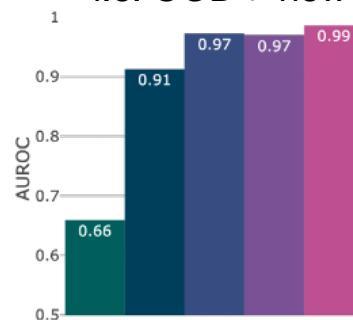
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Far OOD (“easy”)
i.e. OOD = new dataset

Near OOD (“hard”)
i.e. OOD = new classes

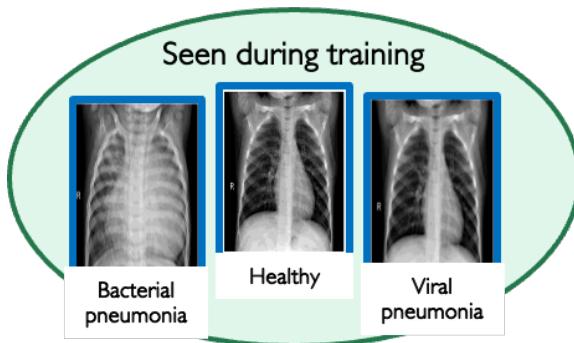


Semi-supervised OOD detection

Performance on near OOD data

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semi-sup. OOD detection

Far OOD ("easy")
i.e. OOD = new dataset



Near OOD ("hard")
i.e. OOD = new classes



Limitations of semi-supervised OOD detection

Challenge #1: not suitable for real-time applications

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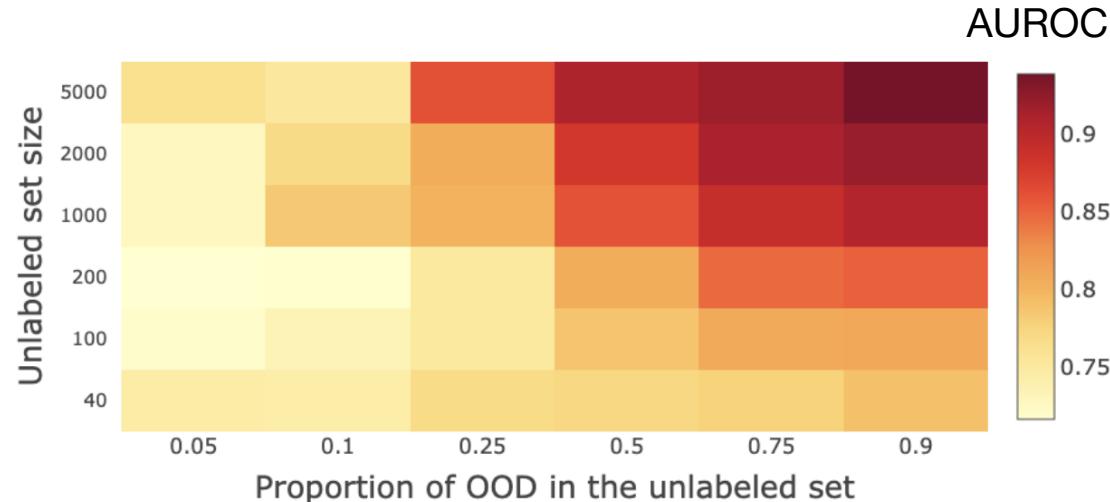
Limitations of semi-supervised OOD detection

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Challenge #1: not suitable for real-time applications

Challenge #2: not suitable for anomaly detection i.e. singleton outliers



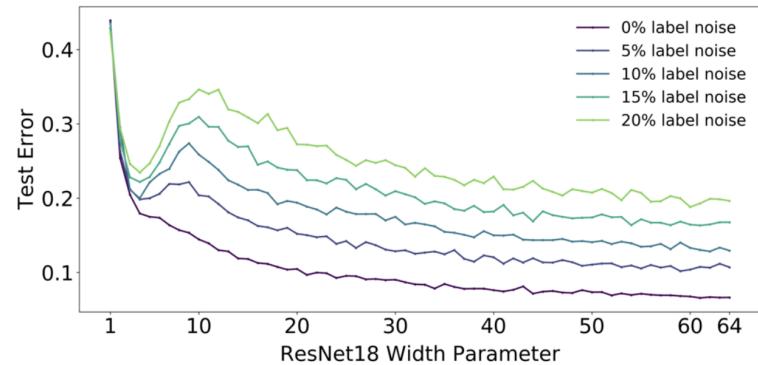
Outlook and future directions

Summary: Trustworthy ML under imperfect data

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If accuracy alone is the goal:

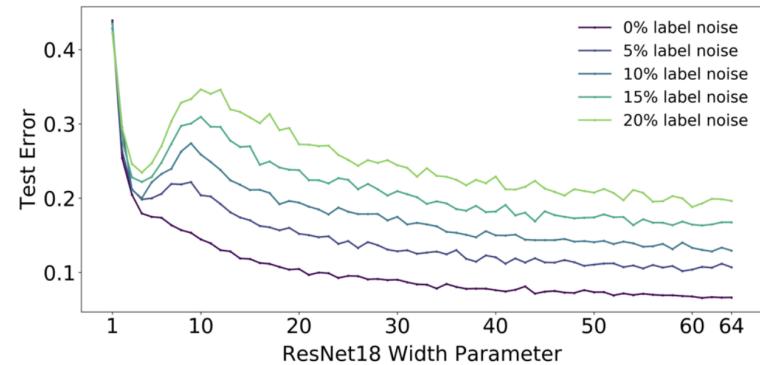
benign overfitting of label noise



Summary: Trustworthy ML under imperfect data

If accuracy alone is the goal:

benign overfitting of label noise



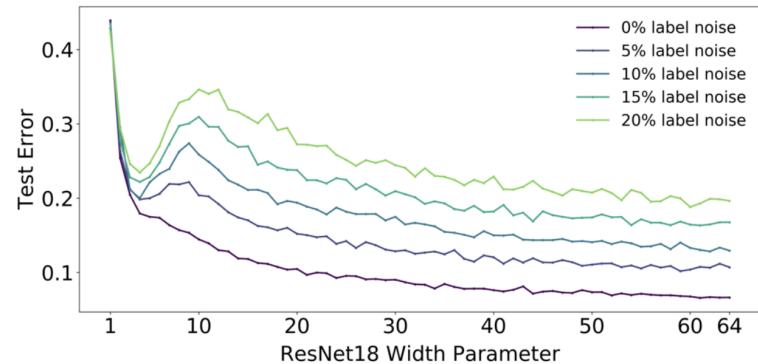
If we care about trustworthiness:

This tutorial: Several examples of trustworthy learning algorithms that work well under label noise, missing data etc.

Summary: Trustworthy ML under imperfect data

If accuracy alone is the goal:

benign overfitting of label noise



If we care about trustworthiness:

This tutorial: Several examples of trustworthy learning algorithms that work well under label noise, missing data etc.

Open questions

- What other data-related limitations do existing trustworthy algorithms suffer from?
- How to improve trustworthiness in other difficult problem settings?

Summary: Trustworthy ML and unlabeled data

Summary: Trustworthy ML and unlabeled data

If accuracy alone is the goal:

SSL cannot be simultaneously better than both unsupervised and supervised learning

Can semi-supervised learning use all the data effectively? A lower bound perspective

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Summary: Trustworthy ML and unlabeled data

If accuracy alone is the goal:

SSL cannot be simultaneously better than both unsupervised and supervised learning

If we care about trustworthiness:

This tutorial: Several examples where unlabeled data can help to overcome limitations of supervised learning.

Can semi-supervised learning use all the data effectively? A lower bound perspective

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Summary: Trustworthy ML and unlabeled data

If accuracy alone is the goal:

SSL cannot be simultaneously better than both unsupervised and supervised learning

If we care about trustworthiness:

This tutorial: Several examples where unlabeled data can help to overcome limitations of supervised learning.

Open questions

- How fundamental are the improvements to trustworthiness due to unlabeled data?
- What other kinds of (potentially noisy) side information can be used to improve trustworthiness?

Can semi-supervised learning use all the data effectively? A lower bound perspective

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Thank you!