

## Distinguishing characteristics of FAs

Step 3: Data

→ Does not require any auxiliary information

## Applicability areas by domain

AI Production System:

16/9/19

First Order

Syntax:  $\rightarrow C$

&

Components

Eg: ↑

R ↑

To

control strategy

irrevocable

tentative

backtracking

graph search  
control

Algo.

### ① Procedure Production



Step 1: Data is initial database

Step 2: Until data satisfies the termination

condition to begin, select some

rule R in the set of rules, that can  
be applied to data

Step 3: Data is the result of applying R to data.

1	5	7
2	3	4
6	0	5

possible:  
top()  
left()  
right()

## First Order Predicate Logic (FOL)

Syntax: alphabet of symbols

& how wff is formed  
(well-formed formula)

Components:  
predicate symbol  
" "  
var  
" "  
function  
" "  
constant

→ does not allow  
quantification  
over predicates  
/ functions.

1/19

actives

Eg: Nielson wrote Principles of A.I.

predicate  
↓  
represents a relation

Represented as: write(Nielson, Principles of AI)  
→ TRUE

To get who wrote it?

write(x, Principles of AI).

write(x, y) → Who wrote something?

→ Inf. Search needed.

action

some

it can

→ John's brother & John's sister are sibling

to each other. brother(x, John)

sibling(John's brother, John's sister)

sister(x,

John)



Or  $\text{sibling}(\text{brother}(\text{John}), \text{sister}(\text{John}))$

predicative  
return T/F

func<sup>n</sup>  
func<sup>n</sup>

return value

$\rightarrow (\exists x$

$\rightarrow \cancel{\forall} Fc$   
suc

$\rightarrow$  The house is yellow.

$\text{yellow}(h1)$  OR  $\text{color}(h1, \text{yellow})$

↓  
predicative

$\forall C$

### CONNECTIVES :

~~$\exists$~~

$\rightarrow$  John lives in a yellow house

$\text{color}(h1, \text{yellow}) \wedge \text{live}(h1, \text{John})$

$\forall(x)$

$\rightarrow$  John plays chess or badminton

$\text{play}(\text{John}, \text{chess}) \vee \text{play}(\text{John}, \text{badminton})$

$\rightarrow$  If the car belongs to John, then it is grey

$\text{belong}(c1, \text{John}) \Rightarrow \text{color}(c1, \text{grey})$

$\rightarrow$  All elephants are grey

$\forall(x) \text{elephant}(x) \Rightarrow \text{color}(x, \text{grey})$

$\rightarrow$  There is a person who wrote P.A.I

$\exists(p) \text{person}(p) \Rightarrow \text{wrote}(p, \text{PAI})$

$PL < FOPL < \underline{SOPL}$

2<sup>nd</sup> order P.L.

(John))

$$\neg (\exists(x) P(x)) \Rightarrow \forall(x) \neg P(x)$$

$\rightarrow$  ~~For every set  $x$ , there is a set  $y$  such that cardinality of  $y$  is greater than~~

(h), yellow)

that of  $x$

$$\forall(x) \neg (\exists(y) \xrightarrow{\text{set}(x) \wedge \text{set}(y)} \neg (\text{card}(y) > \text{card}(x)))$$

$$\neg \forall(x) (\text{card}(x) \wedge \exists(y))$$

(John)

(John, badminton)  
is grey

I, grey)

grey)

$$\forall(x) \left( \text{set}(x) \Rightarrow \neg \exists(y) \exists(m) \exists(n) (\text{set}(y) \wedge \text{card}(y, n) \wedge \text{card}(x, m) \wedge \text{greater}(n, m)) \right)$$

(P, PAI)

## Most General Unifier

23/10/19

$$(\forall x) \{ P(x) \Rightarrow \{ (\forall y) [P(y) \Rightarrow P(f(x,y))] \}$$

$$\wedge \sim (\forall y) [\sim Q(x,y) \Rightarrow P(y)]$$

Steps

- ① Eliminate  $\Rightarrow$
- ② Reduce scope of negation
- ③ Standardize variables
- ④ Eliminate  $\exists$
- ⑤ Convert to Prenex
- ⑥ Put matrix in CNF
- ⑦ Eliminate  $\forall$
- ⑧ Separate into clauses
- ⑨ Rename Var

(Replace  $x_1, x_2$   
with set of  
well formed formula):  
 $\{x_1, x_2\}$

$$① A \Rightarrow B \quad \text{to} \quad \sim A \vee B$$

$$\forall x \{ \sim P(x) \vee (\forall y) [\sim P(y) \vee P(f(x,y))] \}$$

$$\wedge \sim (\forall y) [\sim Q(x,y) \vee P(y)] \}$$

( $\forall x$ )

② ( $\forall x$ )  $\{ \sim$

A  
op

③ dummy

( $\forall x$ ) {

④

Note:

$$\begin{aligned}
 & (2) (\forall x) \{ \sim P(x) \vee (\exists y) [\sim P(y) \vee P(f(x, y))] \} \\
 & \quad \wedge (\exists y) [Q(x, y) \wedge \sim P(y)] \\
 & \quad \text{After applying NOT, } \uparrow \quad \text{After changing to } \exists \quad \& \quad \text{then applying De Morgan's Law}
 \end{aligned}$$

(3) dummy variable  $\Rightarrow$  same variable name should not be used anywhere else

$$\begin{aligned}
 & (\forall x) \{ \sim P(x) \vee (\exists y) [\sim P(y) \vee P(f(x, y))] \} \\
 & \quad \wedge (\exists w) [Q(x, w) \wedge \sim P(w)]
 \end{aligned}$$

$$\begin{aligned}
 & \text{E.g. } (\forall x) [P(x) \Rightarrow (\exists z) Q(z)] \\
 & \quad \downarrow \\
 & \quad (\forall x) [P(x) \Rightarrow (\exists w) Q(w)]
 \end{aligned}$$

$$\begin{aligned}
 & (4) \quad \left\{ \begin{array}{l} \text{E.g. } (\forall y) [(\exists x) P(x, y)] \\ \quad \Downarrow \\ \quad \text{i.e. there exists an } x \\ \quad \text{s.t. } x \text{ & } y \text{ are related} \\ \quad \text{So write } x = f(y) \\ \quad (\forall y) [P(f(y), y)] \end{array} \right.
 \end{aligned}$$

$$\begin{aligned}
 & (\forall x) \{ \sim P(x) \vee (\exists y) [\sim P(y) \vee P(f(x, y))] \} \\
 & \quad \wedge [Q(x, h(x)) \wedge \sim P(h(x))]
 \end{aligned}$$

Note: If  $(\exists u)$  is not prefixed with  $(\forall y)$   $\Rightarrow$  so  $x$  is represented by a quantifier operator (represented in capital letters)

~~Skolem  
const~~

$$\text{ie. } (\exists x) P(x) \rightsquigarrow P(\underline{\underline{x}})$$

Process is called skolemization

( $\forall x$ ) ( $\forall$

- ⑤  $\forall$   $\rightarrow$  all  $\forall$  are at the front of the expression.

Only quantifier part (prefix), Quantifier free part (matrix)

$$(\forall x)(\forall y) \left\{ \neg P(a) \vee \left\{ \begin{array}{l} [ \neg P(y) \vee P(f(a,y)) ] \\ \wedge [ Q(a, h(x)) \wedge \neg P(h(x)) ] \end{array} \right\} \right\}$$

- ⑥  $x_1 \vee x_2 \vee x_3 = (x_1 \vee x_2) \vee x_3 \Rightarrow$  Conjunctive Normal form

$$(\forall x)(\forall y) \left\{ \neg P(x) \vee \neg P(y) \vee P(f(x,y)) \right\}$$

$(\forall x)(\forall y)$

$$A + B \cdot C = (A+B)(A+C)$$

$$\left\{ \neg P(x) \vee \neg P(y) \vee P(f(x,y)) \right\}$$

set of wff :

7

8

$$A \vee (B \wedge C) \\ = (A \vee B) \wedge (A \vee C)$$

$$(\forall x)(\forall y) \{ \sim P(x) \vee [ \sim P(y) \vee P(f(x,y)) ] \}$$

$$\wedge \left[ \begin{array}{c} \sim P(x) \vee [ Q(x, h(x)) \wedge \sim P(h(x)) ] \\ \hline A \end{array} \right] \quad \left[ \begin{array}{c} \sim P(y) \vee [ Q(y, h(y)) \wedge \sim P(h(y)) ] \\ \hline B \end{array} \right] \quad \left[ \begin{array}{c} \sim P(f(x,y)) \vee [ Q(f(x,y), h(f(x,y))) \wedge \sim P(h(f(x,y))) ] \\ \hline C \end{array} \right]$$

$$\wedge [ \sim P(x) \vee Q(x, h(x)) ]$$

$$\wedge [ \sim P(x) \vee \sim P(h(x)) ]$$

form

~~(f(x,y))~~ ⑦ Just remove ~~x~~

+ c) ⑧ Clauses: (Those with only  $\vee$  & are separated by  $\wedge$ )

set of wff:  $\{ (\sim P(x) \vee \sim P(y) \vee P(f(x,y))) \}$

$$, (\sim P(x) \vee Q(x, h(x)))$$

$$, (\sim P(x) \vee \sim P(h(x))) \}$$

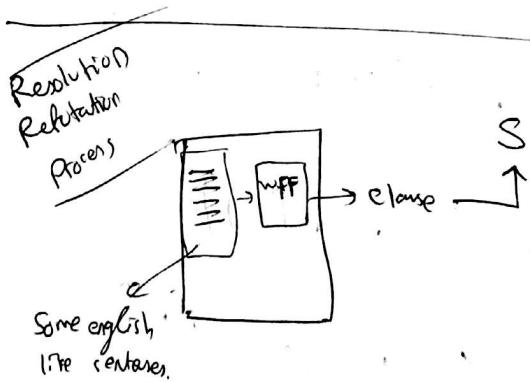
$$\begin{aligned}
 \textcircled{9} \quad & \left\{ \begin{array}{l} \neg P(x_1) \vee \neg P(y) \vee P(f(x_1, y)) \\ , \neg P(x_2) \vee Q(x_2, h(x_2)) \\ , \neg P(x_3) \vee P(h(m_3)) \end{array} \right\}
 \end{aligned}$$

Prod  
—  
C

Let  
Procedure

- Step 1 (1)  
2 (2)  
3 (3)  
4 (4)

Parent Clauses	Resolvent	Comments
$P \text{ and } \neg P \vee Q$	$(P, \neg P \vee Q)$ $Q$	Modus Ponens
$P \vee Q \text{ and } \neg P \vee Q$	$(P \vee \neg P \vee Q, Q)$ $Q'$	Merge
$P \vee Q \text{ and } \neg P \vee \neg Q$	$(P \vee \neg P \text{ and } Q \vee \neg Q) = 1$	Tautology
$\neg P \text{ and } P$	NIL	Empty Clause → sign of contradiction
$\neg P \vee Q \text{ and } \neg Q \vee R$	$P \Rightarrow R$ $(\because P \Rightarrow Q \text{ &} Q \Rightarrow R)$	Method due to chaining (Transitive)



Task is to find out whether w logically follows from S.

Pro

- Eg: (1)  
(2)  
(3)

## Production System for Resolution Refutation

Let  $S$  is a set of clauses (best-set)

### Procedure Resolution

Step 1 ① Clauses ( $\rightarrow S$ ) until ~~NIL is a~~

② until NIL is a member of clauses do

③ begin

④ select two distinct resolvable clauses  $C_i \& C_j$  in Clauses (from Clause-set)

⑤ Compute a Resolvent ( $R_{ij}$ ) of  $C_i \& C_j$ .

⑥ Clauses  $\rightarrow$  the set produced by adding  $R_{ij}$  to Clauses.

⑦ end

- Eg:
- ① Whoever can read, is literate
  - ② Dolphins are not literate
  - ③ Some dolphins are intelligent

Prove that some who are intelligent cannot read.

Ans  
by.  
from S.

$\begin{array}{l} A \\ \hline S \\ \hline \end{array}$ 
 (1)  $(\forall x) \text{ Read}(x) \Rightarrow \text{Literate}(x)$   
 (2)  $(\forall y) \text{ Dolphin}(y) \Rightarrow \sim \text{Literate}(y)$   
 (3)  $(\exists z) \text{ Dolphin}(z) \wedge \text{Intelligent}(z)$

$W = \neg (\exists w) \text{ Intelligent}(w) \wedge \sim \text{Read}(w)$

$S = \left\{ \begin{array}{l} \sim R \\ \sim I \\ I \\ \sim \end{array} \right.$

Break to clause form

- (1)  $\sim R(x) \vee L(x)$
- (2)  $\sim D(y) \vee \sim L(y)$
- (3)  $D(\epsilon) \wedge I(\epsilon)$   
since separated by AND  
so 2 clauses

$$\boxed{S \cup \sim W = S \cup W}$$

There exist, but  
NO  $\forall$ .  
So replace variable  
by a const C

(∴ we need to refute)

$$\overline{W} = (\forall w) \sim I(w) \vee R(w)$$

So clauses  $\rightarrow (\sim I(w) \vee R(w))$

So we get 5 clauses.

Tree  
~~open~~

$\sim R(x) \vee L($

NF

$\rightarrow \text{Literate}(x)$

$\rightarrow \sim \text{Literate}(y)$

$\wedge \text{Intelligent}(z)$

$\wedge \sim \text{Read}(w)$

$$\frac{S \cup \sim W}{S \cup W}$$

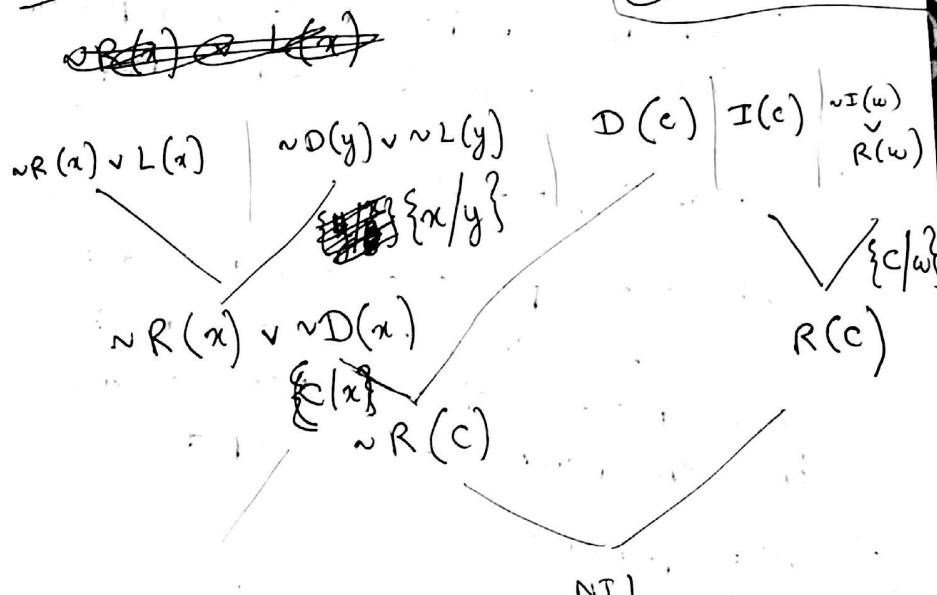
There exist, but  
NO  $\vdash$ .  
So replace variable  
by a const C

$$S = \left\{ \begin{array}{l} \sim R(x) \vee L(x), \\ \sim D(y) \vee \sim L(y), \\ D(c), \\ I(c), \\ \sim I(w) \vee R(w) \end{array} \right\}$$

give separate variable  
for diff clauses  
multiple clause entries  
from same  
give same name

- A variable can  
be replaced by  
another variable,  
① const - symbol  
② func - symbol

Tree



$$\frac{R(w)}{\sim \vee R(w)}$$

$\{ \_ / \_ \}$   
replaced by which was replaced.

To write beside lines.

variable  $\rightarrow$  small letters  
const  $\rightarrow$  Capital letters



## Control Strategy for Resolution Refutation

8/11/19

~ Q

~ C

### ① Breadth First

Compute all 1<sup>st</sup> level resolvent;  
then level 2, level 3 ... — Complete,  
inefficient

uttera provding  
goal wff if it  
~ exists

### ② Linear input form

Each resolvent has at least 1 parent  
belonging to the base set — Not  
Complete

initial set of  
clauses from pre  
base set

### ③ Set of Support

At least 1 parent of each resolvent is  
selected from among the clauses, resulting  
from negation of goal wffs or from  
their descendants — Complete

~ Q (x)

If we follow  
②

### ④ Unit Preference

try to select a single literal clause  
(unit) to be a parent

### ⑤ Ancestry filtered from

each resolvent has a parent that is  
either in base set or ancestor of other  
parent

T  
☆

### ⑥ Combination

ion

8/11/19

$$\sim Q(x) \vee \sim P(x) \quad Q(y) \vee \sim P(y)$$

$$\sim Q(w) \vee P(w) \quad Q(u) \vee P(A)$$

resolvent ;  $\sim$  exists

- Complete,  
inefficient

least 1 parent

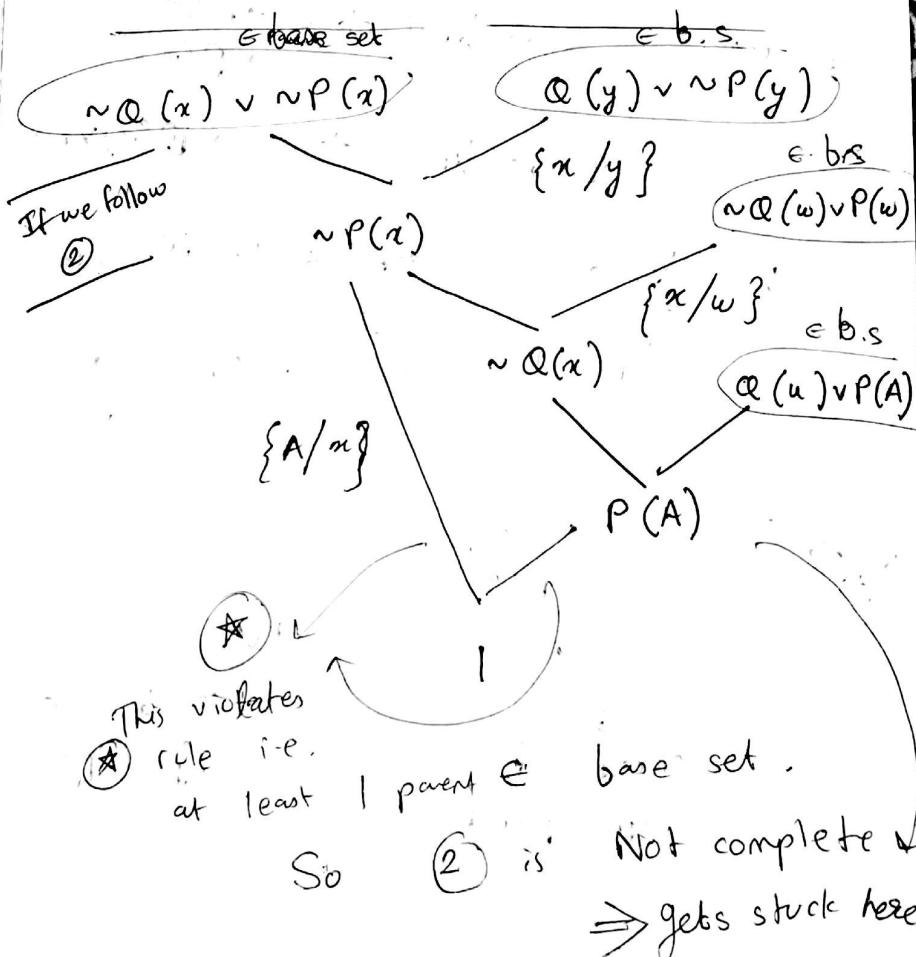
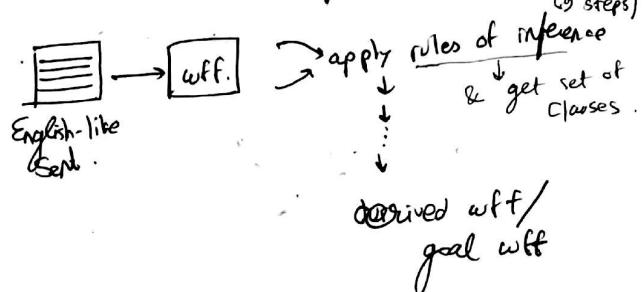
set - Not  
Complete  
in form  $\{P\}$   
we sel

If resolvent is  
clauses, resulting  
wffs or from  
complete

literal clause

at that is  
either of other

when providing  
goal wff if it



If we follow  
③

See eg of  
dolphin



$$\equiv | c_1 \\ c_2 \\ c_3$$

$$gal \text{ aff} \xrightarrow{\text{negation}} \equiv | c_4 \\ c_5$$

$$S_0, \quad c_1 \quad c_4$$

Eg: If  
Jo

A.

when we  
use via  
there shou  
a q

Clause

If we follow  
④

Single literal clause:  $\rightarrow P(A)$   
 $\rightarrow P(x)$

Double literal clause:  $\rightarrow \neg P(x) \vee P(x)$

We try to select single literal clause

(may not be present)

↓  
so no. of steps will be reduced.

If we follow  
⑤

$\sim P(x)$

$P(A)$

can be done  
(prev. pg.)

ancestor of  
other parent.

Result

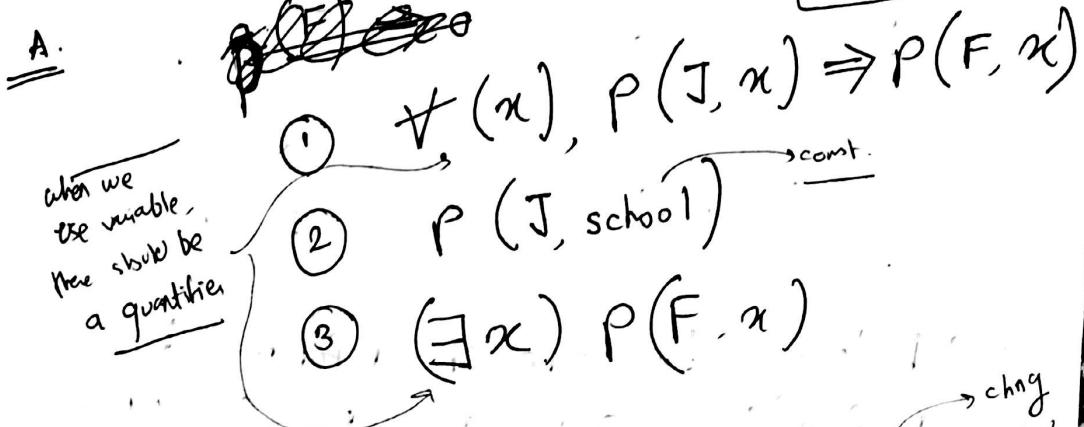
By

u



Eg: If Fido goes wherever John goes & if John is at school, where is Fido?

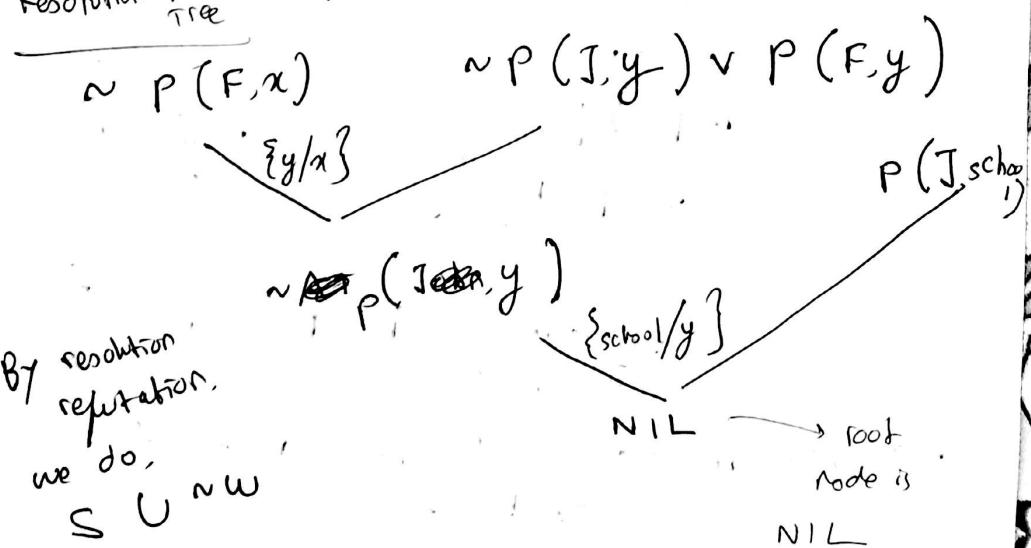
OR use AT instead of P



Clause forms

- 1)  $\neg P(J, x) \vee P(F, x)$  → changing to new variable  $y$  (to avoid clash)
- 2)  $P(J, \text{school})$
- 3) Negating  $\rightarrow \neg [\exists x] \neg P(F, x)$   
 $\downarrow$   
 $(\forall x) \neg P(F, x)$

Resolution Refutation Tree



How to get answer?

→ Append to each clause, curving from negation of goal wff, its own negation

$$\neg \cancel{P(F, x)} \quad \vee \quad P(F, x)$$

→ Following the str of refutation tree, perform the same resolution as before until some clause is obtained at the root.

So,

$$\neg P(F, x) \vee p(F, x)$$

This is added now

$$\neg P(J, y) \vee P(F, y)$$

MODIFIED PROOF TREE

$$\neg P(J, y) \\ \vee P(F, y)$$

$$P(J, \text{school})$$

ANS: of the given ques

$$P(F, \text{school})$$

→ Use the clause at the root as an answer statement

AND-OR graph

all the nodes need to be processed

- hypergraph
- hyperarc
- K. connector
- Formulation
- 2 person
- plore

- Iterative
- Adversarial
- Static
- f(x)

• Root  $\rightarrow d$   
t

- my
- el
- Arc
- In

6/11/19 (II)

arising from  
own negation



$(F, x)$

tree  
as before  
but at the

row

$y) \vee P(F,y)$

(J, school)

school

as an

AND-OR graph

all the  
nodes need to  
be processed

one of the ...

→ hypergraph

→ hyperarc

→ K. connector

→ Formulating game playing as search

→ 2 person, perfect info

players move alternately, no chance factor

→ Iterative methods

→ Adversary

→ Static

adversarial person vs such game.

eval func

place for placing  
rover with a plan  
B hv a complete plan  
to win.

Evaluation func' of win.

Tic-Tac-Toe

$f(x) = \text{large}$

true (my winning cond<sup>n</sup>)

= large - ve (my losing cond<sup>n</sup>)

=  $+\infty$

=  $-\infty$ , (draw cond<sup>n</sup>)

= 0

$f(x) =$

weighted features.

### Game Tree

- Root → decision, on what is the best single move
- To make next

- my turn → MAX

- else → MIN

- Arrows → possible legal moves.

- In each level - MAX/MIN

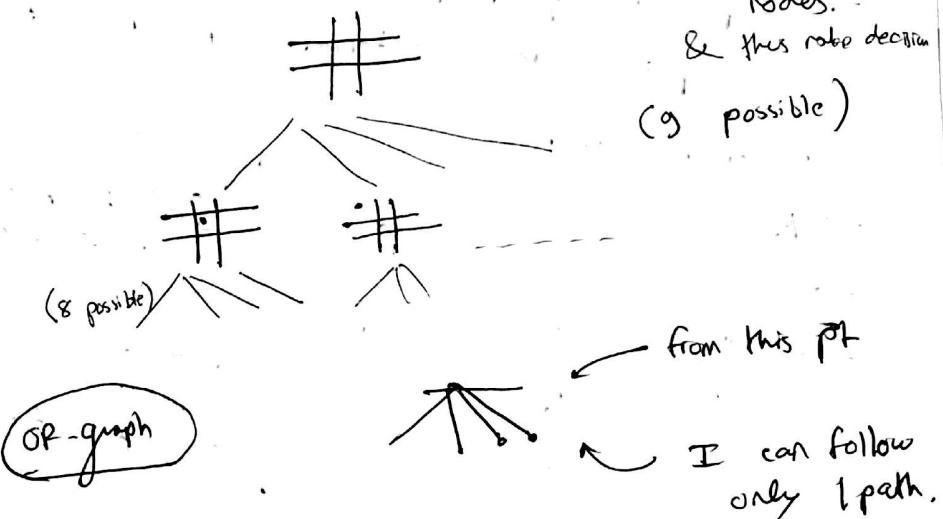
- Nodes corresponding to MIN's next move have successors that are like AND nodes (all nodes)
- Nodes --- to MAX's = --- (any one like - nodes of the nodes)

Game - # nodes in complete game tree

checkers :  $10^{90}$

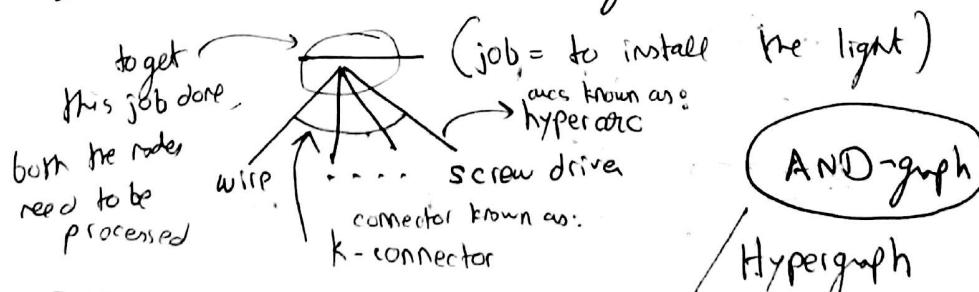
chess :  $10^{120}$

bcs hv to ensure  
that win is mine  
from all possible  
nodes.  
& thus rite decision  
(9) possible



So, only one of the nodes  
need to be  
processed

Eg: If I have a wire and a screwdriver,  
I could install the light.



So, OR graph

Eg:  
I e

So,

Again,

Can

AN

A.

Hypergraph

MIN's next move  
 like AND nodes (all the nodes)  
 OR nodes (any one of the nodes)  
 game tree

bcoz hv to ensure  
 that win is mine  
 from all possible  
 nodes.  
 & thus rite decision  
 (9 possible)

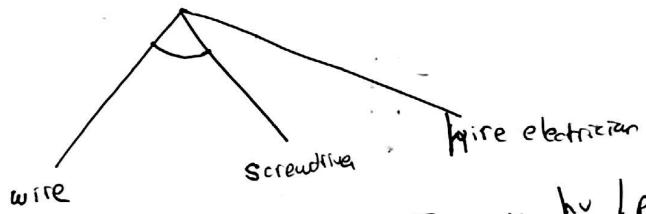
- from this pt
- I can follow only 1 path.
- of the nodes need to be processed
- a screwdriver,
- 2) the light)

AND-graph  
 / Hypergraph

So, OR-graph can be differentiated from AND-graph by the help of a connector.

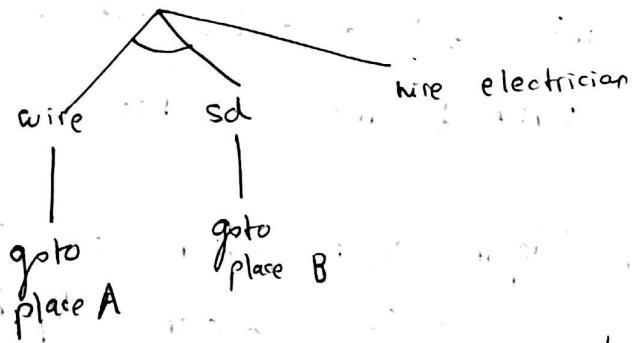
Eg: If I have a wire & a screwdriver,  
 I could install the light  
 else, hire an electrician.

So,

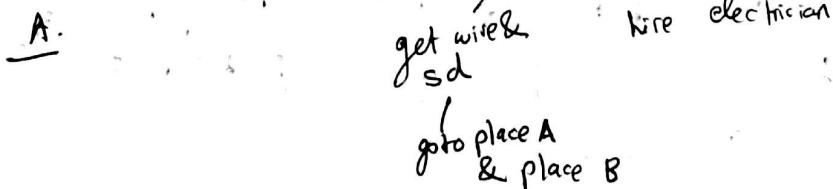


So, in 1 single graph, I can hv 1 part  
 as AND & one as OR

Again, this can be extended to



Can this be converted to a graph w/o  
 AND? (using only OR)

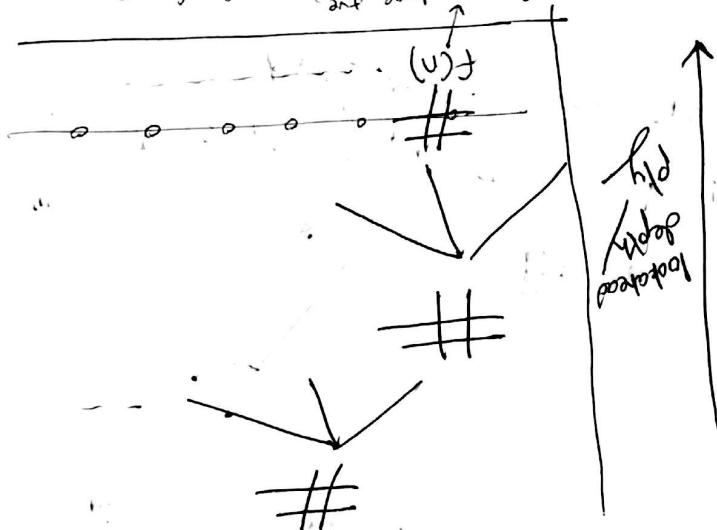


For each of these so called leafy acids some surface oxidation may occur but the carboxylic acid group remains intact.

The depth up to which one could release is called lookahead depth /  $\delta$

which to move the curves  
moves by a certain extent to decide

Lid to  
seal + cool  
at my  
room temp



To generate 10<sup>40</sup> nodes in a complete tree  
it will take yrs to complete ←

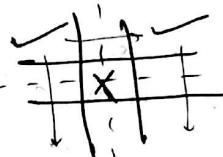
This concept can be used for formulating a game where 2 persons are involved.

planning

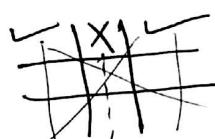
tree  
shape

Eg: For tic-tac-toe, static eval func<sup>may be</sup> ~~as equal~~  
~~determined by~~ no. of open rows / col / diag to form 3-consecutive (no. of 3-lengths open for me)

Eg:



$$\checkmark \rightarrow 3$$



$$X \rightarrow 2$$

$$\checkmark \rightarrow 4$$

$$X \rightarrow 1$$

So, one possibility, static eval func<sup>"</sup>

$$= \left( \begin{array}{l} \text{No. of 3 len open for me} \\ - \text{No. of 3 len open for opponent} \end{array} \right)$$

For chess

$f(x) =$  weighted features

$$= w_1 f_1 + w_2 f_2 + \dots$$

can be weight of pieces

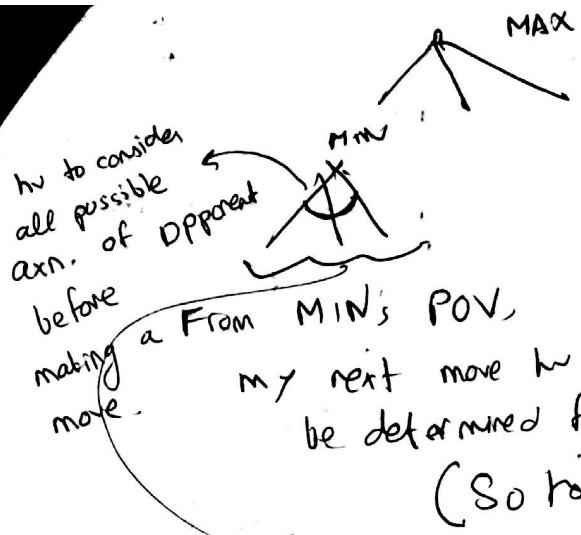
AND can also include its pos<sup>n</sup> on board

current move)

foresee

ply

leaf nodes performed over is wrt root node



→ At

(5) Pick ch de

Eg. (Oppos m

D 100

ne + f

How to compute?

→ At MIN node, backed up value is  
the min of the values associated  
with its children

So ch a

## Searching GameTree using Minimax Algo

Step ①: Create start node as a max node  
(my turn to move)  
with current board configuration

(start from here, go up)

② Expand nodes down to some depth  
(ply) of lookahead in the game

③ Apply evaluation func<sup>n</sup> at each of  
the leaf nodes

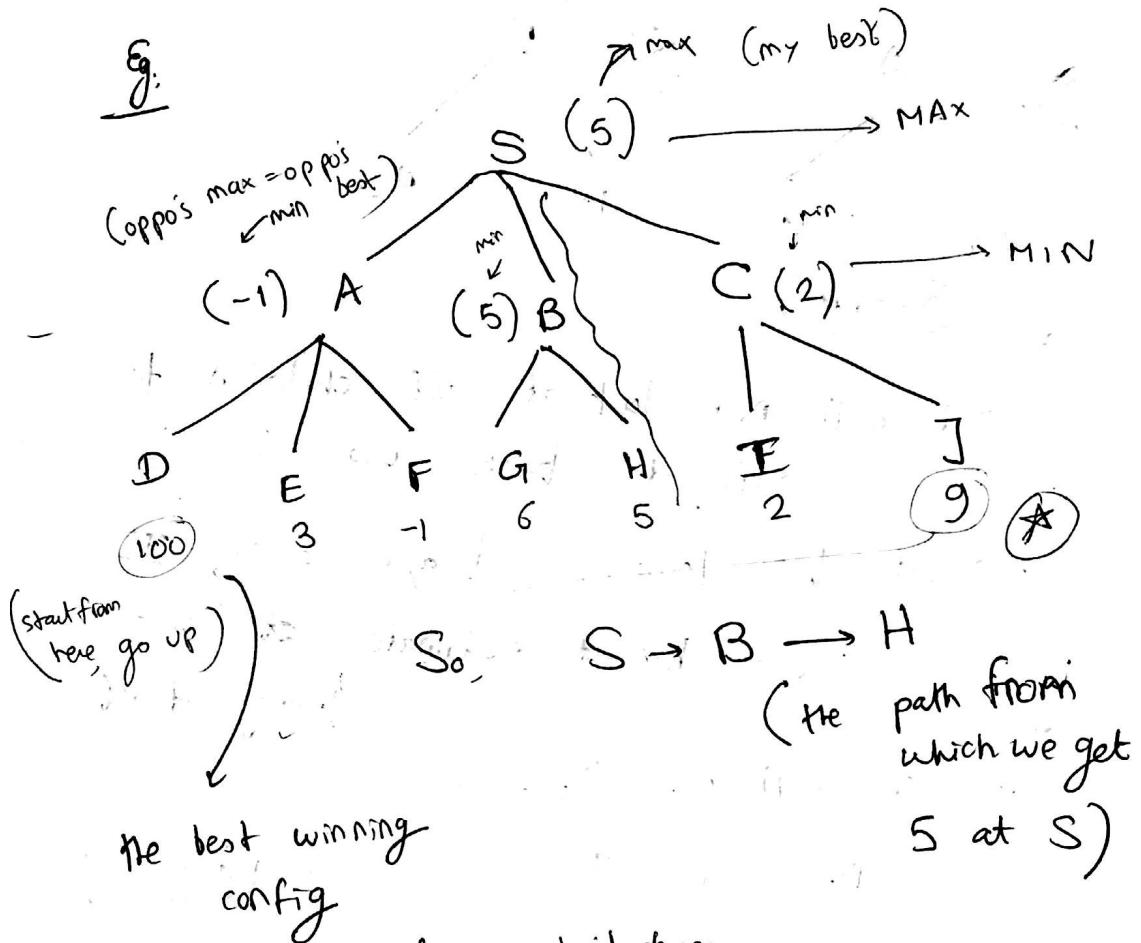
④ Back up values for each of the  
non-leaf nodes until a value is  
computed for the root.

How to compute?  
→ At MIN node, backed up value is  
the min of the values associated  
with its children

→ At MAX node,  $\max$  of the values

- (5) Pick the operator associated with the child node, whose backed up value determined the value at the root.

e.g.



But my algo didn't choose this, bcos here in  $(-1) \rightarrow$  when oppo gives his best, I lose.

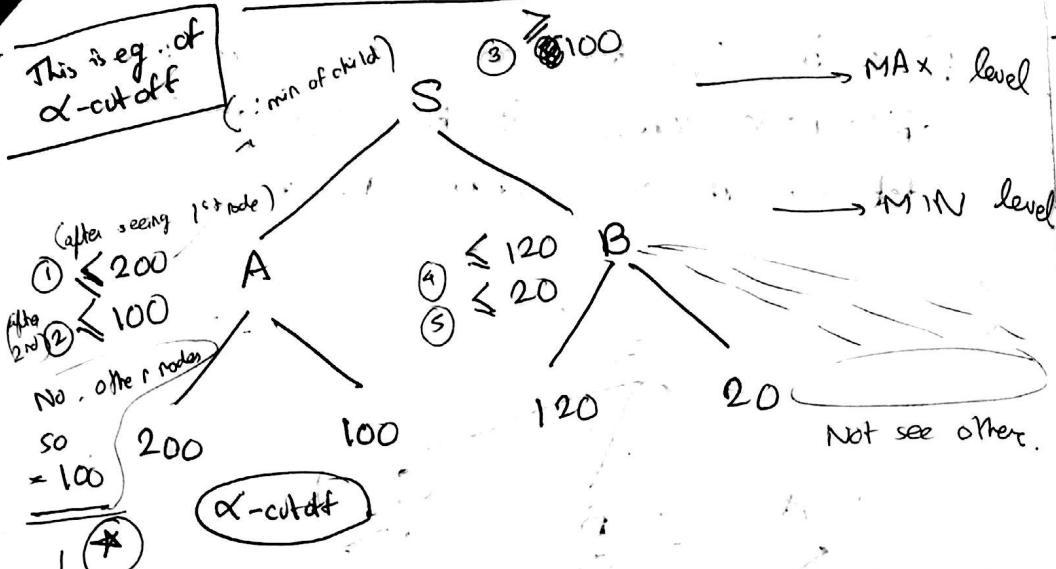
But in  $S \rightarrow B \rightarrow G$ , I win irrespective of opponent config

\* Not chosen 9 also

2 is  $\approx 0$ . So as we go deep, it's possible that we lose when we go more down.

So choose such a place which can beaten scores altogether.

## Alpha-Beta Pruning Algorithm:



→ I will not look at all children to calculate backed up value

→ But by looking 1 after another, I can have an estimate ~~w/o~~ w/o looking at all

Now I will not look at B.

Now after  $\textcircled{1}$ ,  $S > 100$  ( $\because \alpha$ )

After  $\textcircled{3}$  &  $\textcircled{4}$ , at  $S$ , its  $> 100$  &  $> 120$

After  $\textcircled{5}$ , no matter how many nodes we see, it'll always be  $\leq 20$

So I can prune other children at B

which has no effect at S  
(when becomes  $\geq 20$ )

Thm:

→ MAX level

→ MIN level

at see other.

draw to

live

then I

w/o  
ing at all

100 ( $\because \alpha$ )

its  $\geq 100$   
 $\& \geq 120$

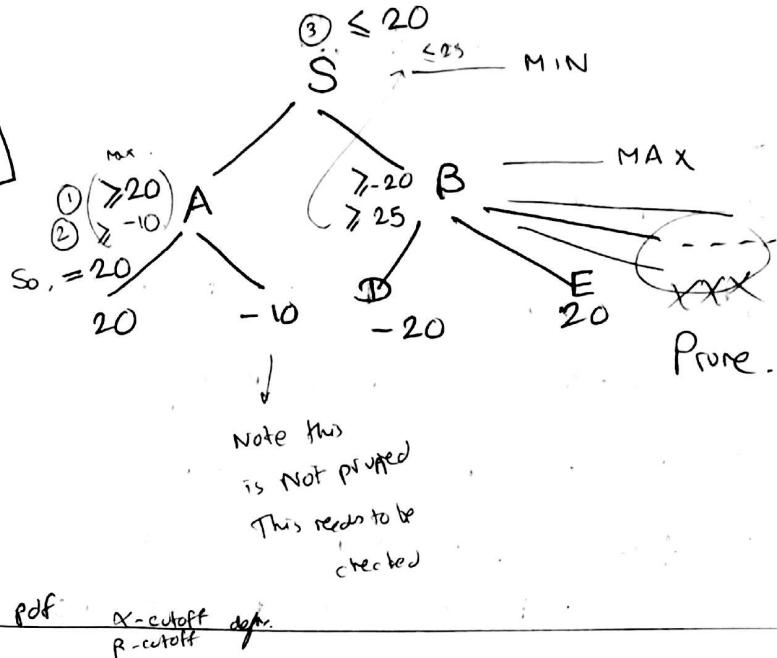
on my node

it'll

be  $\leq 20$

effect at S  
(when becomes  
 $\geq 20$ )

Eg. of  $\beta$ -  
cutoff



In chess - branching factor = 35  
After  $\alpha$ - $\beta$  pruning, it reduces to 6.

Worst case : No pruning

Best case :  $(2b)^{d/2}$

when is it best case?

Horizon effect

I see till depth d

If I see till depth  $d+1$ , situation is entirely different

# Uncertainty Handling

7/11/19

## Reasoning based on PL

- Reasoning based on PL operates under:  
Certain, complete, unchanging, consistent facts
- Given facts, rules → confident conclusions
- Derived truth → never contradicts, given that no contradictions exist on axioms.
- Real life → imprecise, incomplete, uncertain

## Limitations of PL

- Limited in expressive power (more or less - -)
- Only the True/False Statements
- No way to produce new knowledge about the world; only what is derivable.

## Uncertain Situation

- Uncertain knowledge - Heuristic knowledge - certain sets of evidences probably imply certain conclusions
- Uncertain data - domain knowledge is certain, but not data - to infer a specific cause from an observed effect, we may have to rely on questionable test result.

- Incomplete processing
- Random
- PL is

## NMR

- Human

absolute  
char

truth value  
will not  
depend on  
other sent. - b  
&  
truth info  
never changing  
over a time  
pre

→ A  
pre

→ F

(

7/11/19

→ Incomplete info - decisions are taken in course of processing incrementally acquired info.

→ Randomness - knowledge & info is complete, data is certain but domain is inherently random - stochastic domain

→ PL is monotonic (# facts known to be T at any time)

ex:

consistent facts

inconsistencies

cts. given that no s.

to uncertain

or less →

about the

- certain

fair conclusions

> certain, but come from an questionable

## NMR systems

→ Human problem solver often augment

absolute truths with beliefs that are subject to change given further info; Tentative beliefs

truth value will not depend on other sent. & truth info never chng over a time

→ based on default assumptions. Not one made in the light of lack of evidence to the contrary

→ An NMR system tracks a set of beliefs &

revises those beliefs when new knowledge is observed/derived

→ NMR system - a set of premises (immutably T),

tentative beliefs (potentially incorrect),

dependency record for each tentative belief

(tracks beliefs v/s. justifications)



how to store a belief  
stmt. & its set  
of justifications  
(dependency record)

## NMR systems

- In NMR, new facts became known which contradicted & invalidated old knowledge  $\rightarrow$  old knowledge was retracted causing other dependent know... to become invalid  $\rightarrow$  thereby requiring further retractions  $\rightarrow$  shrinkage or non-monotonic growth at times
- Methods to accurately represent, and deal with different forms of uncertainty

9 diff approaches

① TMS (truth maintenance systems) — permits addition of changing (even contradictory) statements to KB (knowledge base)

② Modal & temporal logic — permit representation & reasoning about necessary & possible situations, temporal & other related situations  
(can get idea in Patterson book)

③ Fuzzy logic — deals with vague & imprecise info

④ Reasoning based on Probability

→ Since a  
it is  
but  
true

→ So, a  
any  
indi

→ B  
an

de

→ P

→ P

→ D

→ Ma

be

which  
→ of  
dependent  
wiring

→ Since an NMRs include tentative knowledge, it is possible to add new piece of knowledge that will cause a previously believed tentative truth to become F.

stone

→ So, when a belief in an NMRs is revised, then any beliefs that rest on it, directly/indirectly, must also be revised.

deal with

→ Brief revision - propagates the effect of any change in belief; through dependency directed backtracking; when any inconsistency arises, as a result of newly added justification, dependency directed backtracking is invoked to restore consistency

- NMRs → useful for planning & design (requiring large no. of tentative assumptions)  
→ NMRs → consumes memory, time

representations

possible

situations

imprecise  
info

### TMS

- Doyle, 1979  
→ Main job → maintain consistency in knowledge base (KB) being used by any problem solver & not to perform as inference fn; As such it frees the problem solver from any concern of consistency



TMS...

IE

KB

IT T /

→ TMS maintains currently active belief set.  
Updating is incremental; after each inference  
info. is exchanged between IE & TMS.

IE tells TMS what deductions it has made.  
TMS asks questions about current beliefs &  
reasons for failure. It maintains a consistent  
set of beliefs for IE.

→ TMS operates as KBMS & is called  
every time the reasoning system generates a  
new Truth value. TMS, using belief  
revision, takes any action required to  
modify dependent beliefs to maintain consistency.

Structure

→

TMS

In TMS,

Node → one unit of knowledge : fact/  
rule/assertion; at any point of time, every  
node is in one of two conditions.

①

②

③

④

IN → currently believed to be T

OUT → " " " " F

(There is no possible cond' that would rule



if T / the conditions required to note if T are  
correctly IN)

• belief set.  
each inference

= E & TMS,  
it has node  
beliefs &  
a consistent

is called  
generates a  
belief  
required to  
tain consistency.

age : fact/  
time, every  
itions

be T

• F

that would note

(support by)

### SL justifications

→ Associated with each node → justif^n for  
node's truth value ; assume, 1 justif^n for  
each node

→ For each node, that is IN, TMS records a  
well founded support → proof of the  
validity of the node

structure [SL (in-nodes) (out-nodes)]

→ In-nodes → list of all nodes that must  
be IN for this node to be T

→ Out-nodes → OUT - - - T  
                        <sup>fact true</sup>      <sup>should be</sup>      <sup>IN (true)</sup>      <sup>should be</sup>  
                        (1)              (2)              (3)              (4)

① It is sunny 1

② It is daytime 2

③ It is raining 3

④ It is warm 4

SL (2)(3)

SL (1)()

SL ()(1)

SL (1)(3)

There start having  
no dependency or  
②

So ② is an  
absolute stmb.

### SL justification

- ~~Premise~~ Premise: always valid; in-list, out-list always empty
- Normal deduction: It is formed in normal sense of a monotonic system; out-list always empty
- Assumption: a belief supported by lack of contrary info. Out-list never empty

→ Prism

is

→ Human

w/o

→

0

S

### CP Justification

- Used to support hypothetical reasoning
- $[CP \langle \text{consequent} \rangle (\text{in-hypothesis})]$
- CP also includes out-hypothesis, always empty
- A CP justification is valid iff the consequent node is IN whenever all of the nodes on in-hypothesis are IN.

Purpose

Defn

## NeuroComputing : an Intro

→ Primary task of all biological neural systems.

is to control various functions (mainly behaviour)

→ Human being can do it almost instantaneously &

w/o much effort eg recognizing a score of music

→ Artificial Neural Network (ANN):

or Neural Network (NN) models try to simulate the biological neural n/w with electronic circuitry

→ Also known as Connectionist Model / Parallel Distributed Processing (PDP)

Purpose: To achieve human like performance  
(particularly in pattern recognition & image processing)

## Definition

Def'n: Massively parallel interconnected network of simple processing elements which are intended to interact with the objects of the real world in the same way as biological systems do.



→ NN models are extreme simplifications of human neural systems

→ Computational elements (neurons/nodes/processors) are analogous to Ne.

→ An

→ Act

r/w

hum

→

b

### Similarities betw BNN & ANN

→ Gets i/p via synoptic connection.

→ Accumulated i/p is transformed to a single o/p

→ O/p is transmitted through axon

→ Firing of neuron

Ge

Proc

### An artificial neuron

diag.

#### Artif. / electronic neuron

→ Gets i/p through resistors

→ Total i/p is converted to a single o/p by OP-AMP

O/P

→ --- transmitted via resistors.

### Neural network

one simplifications of

neurons / nodes / processors)

& ANN

connection.

formed to a single o/p  
via 1 axon

a single o/p

by OP-AMP

o/p.

### Summary

- An electronic neuron emulates a biological neuron
- Actf. neurons are then connected to form a n/w to mimic (!) the topology of human nervous system
- Func<sup>y</sup> performed by a NN is determined by the n/w Topology, conn<sup>y</sup> strength, processing performed at computing elements / nodes, & status updating rule

### General framework of neural n/w

#### Processing unit

- Receives i/p from connected neurons, compute an o/p value & sends it to other connected neurons

→ Three types of units - i/p, o/p, hidden

$$\underline{\text{o/p value}} \quad o_i(t) = f(I_i(t))$$

→ Total i/p for  $i^{\text{th}}$  neuron is  $I_i$

→  $f$  is a threshold or squashing func<sup>y</sup>.

## → Unidirectional Connections ( $w_{ij}$ )

→  $w_{ij} < 0 \rightarrow$  unit  $U_j$  inhibits unit  $U_i$

→  $w_{ij} = 0 \rightarrow$  unit  $U_j$  has no direct effect on unit  $U_i$

→  $w_{ij} > 0 \rightarrow$  unit  $U_j$  excites unit  $U_i$

rugged  
optimal

## Characteristics of neural networks

Associ

Train  
Learn from example : shown a set of i/p's,  $t_k$ ,  
self-adjust to produce consistent response

Test  
Generalize from prev eg to new ones once trained  
a n/w's response is mostly insensitive to variation  
in i/p

→ out  
→ hate

Abstract essential chars from i/p : find the ideal  
(prototype) from imperfect i/p's.

Regu  
→

Unsupervised learning

## Major advantages

adaptivity - adjusting the connection strengths to  
new data/information

speed - due to massively parallel architectures

robustness - to missing, confusing, ill-defined/  
noisy data

Sor



)

bits unit  $u_i$

o direct effect  
on unit  $u_i$

bits unit  $u_i$

wires

of i/p's, they  
produce consistent  
response

once trained,  
tire to variations  
in i/p  
: find the ideals

ruggedness - to failure of components

optimality - as regards error rates in performance.

## Learning (parameter updating)

### Associative (supervised) learning

Learning pattern pair association

$$\text{Input} = X = \{x_1, \dots, x_n\}$$

$$\text{Output} = T = \{t_1, t_2, \dots, t_n\}$$

Learn ( $X, T$ )

→ auto-associator ( $T \cong X$ )

→ hetero-associator (any arbitrary combination  
of  $X, T$ )  
(classification)

### Regularity detection (unsupervised)

→ System discovers statistically salient  
features of i/p population (clustering)

n strengths to  
formation  
architectures

ill-defined/  
noisy data

Popularly used NN models

Some common feature are there; but differ in  
fine details

→ Multi-layer perceptron

→ Hopfield's model

→

→

→

Learning =  $p_a$

$w_i(t)$

$\Delta_i$

$S_i$

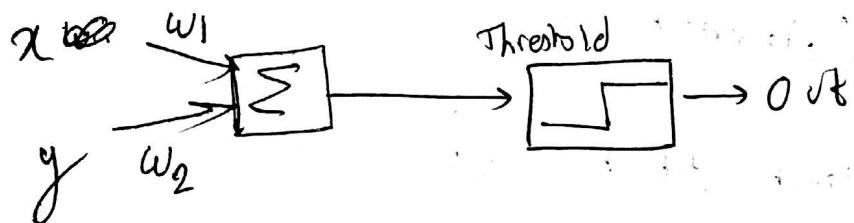
~~Applicability~~

→ ~~What human intell~~

## Two input perception

→ If he  
he si

Perception : A single neuron connected by  $w_1, w_2$  to a set of inputs



→ Let  $x$  &  $y$  be two inputs &  $w_1, w_2$  be weights

→ If  $w_1x + w_2y > 0$ , then the output is 1  
else 0, where 0 = Threshold

→  $w_1x + w_2y = 0 \rightarrow$  separating line



## Learning rule

Learning : Present a set of input patterns, adjust the weights until no desired o/p occurs for each of them

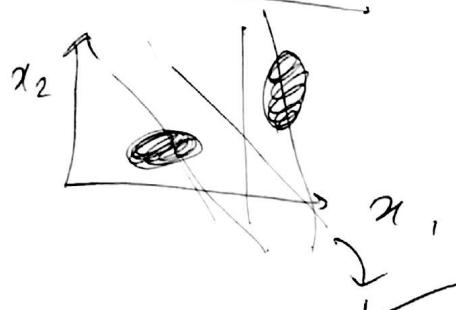
$$w_i(t+1) = w_i(t) + \Delta_i ;$$

$$\Delta_i = \eta \delta x_i ;$$

$$\delta = T - A \text{ (i.e. target - actual)}$$

→ If the sets of patterns are linearly separable, the single layer perceptron algo is guaranteed to find a separating hyperplane in a finite no. of steps.

## Chng of weights



output is /

line

-n